
Algorithm *Preconditioned BiCGStab*

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1:  $\mathbf{r}_0 = \mathbf{b} - \mathbf{A}\mathbf{x}_0$ 
2: for  $i = 1, 2, \dots$  until convergence do
3:   if  $i == 1$  then
4:      $\mathbf{p}_i = \mathbf{r}_{i-1}$ 
5:   else
6:     
$$\beta = \frac{\overbrace{(\bar{\mathbf{r}}_0, \mathbf{r}_{i-1})}^{\delta_i}}{\underbrace{(\bar{\mathbf{r}}_0, \mathbf{r}_{i-2})}_{\delta_{i-1}}} \cdot \frac{\alpha_{i-1}}{\omega_{i-1}}$$

7:     
$$\mathbf{p}_i = \mathbf{r}_{i-1} + \beta(\mathbf{p}_{i-1} - \omega_{i-1} \underbrace{\mathbf{A}\tilde{\mathbf{p}}_{i-1}}_{\mathbf{v}_{i-1}}) \quad \triangleright \mathbf{p}_i \neq 0$$

8:   end if
9:    $\tilde{\mathbf{p}}_i = \mathbf{M}^{-1}\mathbf{p}_i = \mathbf{M}_U^{-1}\mathbf{M}_L^{-1}\mathbf{p}_i$ 
10:  
$$\alpha_i = \frac{\overbrace{(\bar{\mathbf{r}}_0, \mathbf{r}_{i-1})}^{\delta_i}}{\underbrace{(\bar{\mathbf{r}}_0, \mathbf{A}\tilde{\mathbf{p}}_i)}_{\mathbf{v}_i}}$$

11:   $\mathbf{x}_i = \mathbf{x}_{i-1} + \alpha_i \tilde{\mathbf{p}}_i$ 
12:   $\mathbf{s} = \mathbf{r}_{i-1} - \alpha_i \underbrace{\mathbf{A}\tilde{\mathbf{p}}_i}_{\mathbf{v}_i}$ 
13:  check the convergence of  $\mathbf{s}$ . If converge, return
14:   $\tilde{\mathbf{s}} = \mathbf{M}_U^{-1}\mathbf{M}_L^{-1}\mathbf{s}$ 
15:  
$$\omega_i = \frac{(\mathbf{A}\tilde{\mathbf{s}}, \mathbf{s})}{\underbrace{(\mathbf{A}\tilde{\mathbf{s}}, \mathbf{A}\tilde{\mathbf{s}})}_t} \quad \triangleright \omega_i \neq 0$$

16:   $\mathbf{x}_i = \mathbf{x}_i + \omega_i \tilde{\mathbf{s}}$ 
17:   $\mathbf{r}_i = \mathbf{s} - \omega_i \underbrace{\mathbf{A}\tilde{\mathbf{s}}}_t$ 
18:  check the convergence of  $\mathbf{r}_i$ . If converge, return
19: end for

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