

# Formulas: Sum of Natural, Odd, Even & Consecutive Numbers

## 1 ■■■ Sum of First n Natural Numbers

Numbers: 1, 2, 3, 4, 5, ..., n

Formula:  $S = n(n + 1) / 2$

Example:  $1 + 2 + 3 + 4 + 5 = 15$

## 2 ■■■ Sum of First n Odd Numbers

Numbers: 1, 3, 5, 7, 9, ...

Formula:  $S = n^2$

Example:  $1 + 3 + 5 + 7 + 9 = 25$

## 3 ■■■ Sum of First n Even Numbers

Numbers: 2, 4, 6, 8, 10, ...

Formula:  $S = n(n + 1)$

Example:  $2 + 4 + 6 + 8 + 10 = 30$

## 4 ■■■ Sum of n Consecutive Numbers starting from x

Numbers: x, x+1, x+2, ..., x+(n-1)

Formula:  $S = nx + [n(n-1)]/2$

Example: Starting from 7 → 7, 8, 9, 10, 11

$S = 5 \times 7 + (5 \times 4)/2 = 45$

## 5 ■■■ Sum of n Consecutive Even Numbers starting from x

Numbers: x, x+2, x+4, ..., x+2(n-1)

Formula:  $S = nx + n(n-1)$

Example: Starting from 6 → 6, 8, 10, 12, 14

$S = 5 \times 6 + 5 \times 4 = 50$

## 6 ■■■ Sum of n Consecutive Odd Numbers starting from x

Numbers: x, x+2, x+4, ..., x+2(n-1)

Formula:  $S = nx + n(n-1)$

Example: Starting from 5 → 5, 7, 9, 11, 13

$S = 5 \times 5 + 5 \times 4 = 45$

## ■ Quick Shortcut:

Sum = Average × Number of terms

(For consecutive numbers, the average = middle number)

## ■ Summary Table

Type	Numbers	Formula
First n natural numbers	1, 2, 3, ..., n	$n(n+1)/2$
First n odd numbers	1, 3, 5, ...	$n^2$
First n even numbers	2, 4, 6, ...	$n(n+1)$
n consecutive from x	x, x+1, ...	$nx + [n(n-1)]/2$
n consecutive even from x	x, x+2, ...	$nx + n(n-1)$
n consecutive odd from x	x, x+2, ...	$nx + n(n-1)$