

Average and Sum Formulas (For Quick Exam Revision)

1■■ Natural Numbers

- Sum of first n natural numbers: $n(n + 1) / 2$
- Average of first n natural numbers: $(n + 1) / 2$

Example: For first 40 natural numbers → Sum = $40 \times 41 / 2 = 820$, Average = 20.5

2■■ Even Numbers

- Sum of first n even numbers: $n(n + 1)$
- Average of first n even numbers: $n + 1$

Example: First 10 even numbers → Sum = $10 \times 11 = 110$, Average = 11

3■■ Odd Numbers

- Sum of first n odd numbers: n^2
- Average of first n odd numbers: n

Example: First 10 odd numbers → Sum = $10^2 = 100$, Average = 10

4■■ Arithmetic Progression (A.P.)

If a series has a common difference 'd':

- Sum: $n/2 \times (2a + (n - 1)d)$
- Average: $(\text{First term} + \text{Last term}) / 2$

Example: 3, 8, 13, 18, 23 → Average = $(3 + 23)/2 = 13$

5■■ Prime Numbers

No fixed formula — use divisibility rules to find primes, then apply normal average formula:
Average = (Sum of all primes) / (Number of primes)

Example: Primes between 30 and 50 → 31, 37, 41, 43, 47 → Average = 39.8

6■■ Key Tricks

- For consecutive numbers → (First + Last)/2
- For 1 to n → $(n + 1)/2$
- For even numbers → $n + 1$
- For odd numbers → n