

Average and Sum Formulas (For Quick Exam Revision)

1■■■ Natural Numbers

- Sum of first n natural numbers: $n(n + 1) / 2$
- Average of first n natural numbers: $(n + 1) / 2$

Example: For first 40 natural numbers \rightarrow Sum = $40 \times 41 / 2 = 820$, Average = 20.5

2■■■ Even Numbers

- Sum of first n even numbers: $n(n + 1)$
- Average of first n even numbers: $n + 1$

Example: First 10 even numbers \rightarrow Sum = $10 \times 11 = 110$, Average = 11

3■■■ Odd Numbers

- Sum of first n odd numbers: n^2
- Average of first n odd numbers: n

Example: First 10 odd numbers \rightarrow Sum = $10^2 = 100$, Average = 10

4■■■ Arithmetic Progression (A.P.)

If a series has a common difference 'd':

- Sum: $n/2 \times (2a + (n - 1)d)$
- Average: $(\text{First term} + \text{Last term}) / 2$

Example: 3, 8, 13, 18, 23 \rightarrow Average = $(3 + 23) / 2 = 13$

5■■■ Prime Numbers

No fixed formula — use divisibility rules to find primes, then apply normal average formula:

Average = (Sum of all primes) / (Number of primes)

Example: Primes between 30 and 50 \rightarrow 31, 37, 41, 43, 47 \rightarrow Average = 39.8

6■■■ Key Tricks

- For consecutive numbers $\rightarrow (First + Last) / 2$
- For 1 to $n \rightarrow (n + 1) / 2$
- For even numbers $\rightarrow n + 1$
- For odd numbers $\rightarrow n$