



# Vehicle Dynamics in Ride and Handling Stability

## Homework #1

### Question #1

- Describe mechanics of *rolling resistance* of a pneumatic tire with an appropriate sketch.
- Discuss two factors that have the most influence on rolling resistance of a tire.
- Laboratory tests on a tire (nominal diameter = 70 cm) under a 4000N load show that at a speed of 7 m/s, the normal pressure acts 1 cm ahead of vertical central axis when there is 6% slip. Similarly at 20 m/s, the normal pressure acts 1.8 cm ahead and when there is 10% slip.

Determine  $\alpha_1$  and  $\alpha_2$  for the rolling resistance model, expressed as:

$$f_1 = \alpha_1 + \alpha_2 V^2 \text{ for } V \text{ in km/h}$$

### Question #2

A 20 kN vehicle with 4 identical tires is known to support 12 kN on its front axle. For the vehicle, compute and plot the power required to overcome the rolling resistance in the speed range 0 to 100 km/h. (Use rolling resistance model in Question #1).

### Question #3

A truck tire (Uniroyal Fleet Master) with vertical load 25 kN has longitudinal stiffness of 195 kN/unit slip in traction and 240 kN/unit skid in braking. Using simplified approximate approach; obtain plots for the following on dry concrete ( $\mu_p=0.74$ ;  $\mu_s=0.55$ ) and wet concrete ( $\mu_p=0.51$ ;  $\mu_s=0.38$ ) pavement.

- Plot tractive effort vs. slip considering slip up to 30%
- Plot braking effort vs. skid considering skid up to 30%

### Question #4

The above tire is subjected to simultaneous cornering and braking. Given that the cornering stiffness of the tire is 180 kN/rad and it experiences a skid of 5%, estimate the available cornering force corresponding to a side slip angle of  $3^\circ$ .

### Question #5

Using the 'Magic Tire formula', determine the cornering force properties of a car tire for a normal load of 6 kN in the 0 to 8 degrees side-slip range, assuming negligible camber and absence of tire skid. Repeat the problem for normal load of 4 kN. Use following relationships:

$$D = a_1 F_z^2 + a_2 F_z; a_1 = -22.1, a_2 = 1011 \text{ (} F_z \text{ in kN)}$$

$$C=1.30$$

$$BCD = a_3 \sin \left[ a_4 \tan^{-1} (a_5 F_z) \right]; \quad a_3 = 1078, \quad a_4 = 1.82, \quad a_5 = 0.208$$

$$E = a_7 F_z + a_8; \quad a_7 = -0.354, \quad a_8 = 0.707$$

$$S_h = -0.126 \text{ for } F_z = 6 \text{ kN and } -0.049 \text{ for } F_z = 4 \text{ kN}$$

$$S_v = -77.34 - 20.33 F_z$$

Briefly discuss the influence of normal load on the cornering force developed by the tire.