# R for Data Science (IV): Essential Statistics with R

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#### Outline: Essential Statistics with R\*

- Descriptive Statistics
  - Numerical summaries
  - Graphical exploration
- Statistical test
  - Continous variables
  - Discrete variables
- BONUS: ANOVA and Linear Models

<sup>\*</sup>Based on this Course.\* [BIMS 8382, University of Virginia School of Medicine (USA)] (https://bioconnector.github.io/workshops/index.html).

#### What this class is *not*

- This is not a statistics course. Not covering:
  - Underlying mathematical motivation
  - How to choose the correct statistical procedure
  - Model assumptions
  - Interpreting every aspect of model output

#### What packages we will use today?

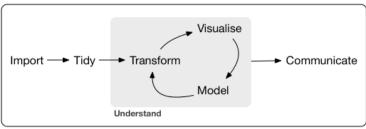
Please be sure yo have the following packages installed:

- dplyr subsetting, sorting, transforming variables, grouping
- **ggplot2** system for creating graphics
- readxl reading .xls files

```
# install.packages("dplyr", dependencies = TRUE)
# install.packages("ggplot2", dependencies = TRUE)
# install.packages("readxl", dependencies = TRUE)

library(dplyr)
library(ggplot2)
library(readxl)
```

#### The Data Science Approach in R



Program

#### **Getting started**

### **Getting started (I)**

Load dataset: today we will continue working with diabetes dataset:

```
diab <- read_excel("datasets/diabetes_mod.xls")</pre>
```

2 Check if we have loaded it correctly:

```
diab[1:4, 1:8]
  # A tibble: 4 x 8
    numpacie mort tempsviu edat bmi edatdiag tabac
##
                                                              sbp
##
       <dhl> <chr>
                      <dbl> <dbl> <dbl>
                                           <dhl> <chr>>
                                                            <dh1>
                       12.4
                               44 34.2
## 1
           1 Vivo
                                              41 No fumador
                                                             132
                       12.4 49 32.6
                                                             130
## 2
           2 Vivo
                                             48 Fumador
           3 Vivo
                        9.6 49 22
                                             35 Fumador
                                                             108
           4 Vivo
                        7.2
                                   37.9
                                             45 No fumador
## 4
                                                             128
```

#### Getting started (II)

Some useful functions in R to check a dataframe:

- Content
  - head(name of dataframe): shows the first few rows
  - tail(): shows the last few rows
- Size
  - dim(): returns the number of rows and the number of
  - nrow(): returns the number of rows
  - ncol(): returns the number of columns
- Summary
  - colnames() or names(): returns the column names

#### Getting started

Descriptive Statistics: Numerical summaries
Descriptive Statistics: Graphical summaries
Statistics test. Continuos Variables
Statistics test. Discrete Variables
Bonus: ANOVA and Linear Regression
Your turn

## Getting started (III)

head(diab)

```
## # A tibble: 6 x 11
     numpacie mort tempsviu
                               edat
                                      bmi edatdiag tabac
                                                            sbp
                                                                  dbp ecg
        <dbl> <chr>
                        <db1> <db1> <db1>
                                             <dbl> <chr> <dbl> <dbl> <chr>
##
## 1
            1 Vivo
                        12.4
                                     34.2
                                                41 No f~
                                                            132
                                                                   96 Norm~
                        12.4
## 2
            2 Vivo
                                     32.6
                                                48 Filma~
                                                            130
                                                                   72 Norm~
## 3
            3 Vivo
                          9.6
                                     22
                                                35 Fuma~
                                                            108
                                                                   58 Norm~
## 4
            4 Vivo
                         7.2
                                     37.9
                                                45 No f~
                                                            128
                                                                   76 Fron~
## 5
            5 Vivo
                        14.1
                                 43 42.2
                                                42 Fuma~
                                                            142
                                                                   80 Norm~
## 6
            6 Vivo
                        14.1
                                 47 33.1
                                                44 No f~
                                                            156
                                                                   94 Norm~
     ... with 1 more variable: chd <chr>
```

#### Getting started

Descriptive Statistics: Numerical summaries Descriptive Statistics: Graphical summaries Statistics test. Continuos Variables Statistics test. Discrete Variables Bonus: ANOVA and Linear Regression Your turn

#### **Getting started (IV)**

##

```
dim(diab)
## [1] 149 11
nrow(diab)
## [1] 149
colnames (diab)
                                                        "bmi"
                                                                    "edatdia
##
        "numpacie" "mort"
                                "tempsviu" "edat"
        "tabac"
                                            "ecg"
                                                        "chd"
```

"dbp"

"sbp"

#### Getting started

Descriptive Statistics: Numerical summaries
Descriptive Statistics: Graphical summaries
Statistics test. Continuos Variables
Statistics test. Discrete Variables
Bonus: ANOVA and Linear Regression
Your turn

#### Getting started (IV)

glimpse(diab)

```
## Observations: 149
## Variables: 11
## $ numpacie <dbl> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16...
                                            <chr> "Vivo", 
## $ mort
## $ tempsviu <dbl> 12.4, 12.4, 9.6, 7.2, 14.1, 14.1, 12.4, 14.2, 12.4, 1...
## $ edat.
                                              <dbl> 44, 49, 49, 47, 43, 47, 50, 36, 50, 49, 50, 54, 42, 4...
                                              <dbl> 34.2, 32.6, 22.0, 37.9, 42.2, 33.1, 36.5, 38.5, 41.5,...
## $ bmi
## $ edatdiag <dbl> 41, 48, 35, 45, 42, 44, 48, NA, 47, 45, 48, 43, 36, 4...
                                              <chr> "No fumador". "Fumador". "Fumador". "No fumador". "Fu...
## $ tabac
## $ sbp
                                              <dbl> 132, 130, 108, 128, 142, 156, 140, 144, 134, 102, 142...
## $ dbp
                                              <dbl> 96, 72, 58, 76, 80, 94, 86, 88, 78, 68, 84, 74, 86, 5...
## $ ecg
                                              <chr> "Normal", "Normal", "Frontera", "Normal", "...
## $ chd
                                            <chr> "No", "No", "Si", "Si", "No", "No", "Si", "No", "Si", ...
```

diab <- diab %>% mutate if(is.character, as.factor)

#### Changing characters (chr) to factors (Factor)

Use dplyr function mutate\_if can do it easily:

```
glimpse(diab)
## Observations: 149
## Variables: 11
## $ numpacie <dbl> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16...
## $ mort
            <fct> Vivo, ...
## $ tempsviu <dbl> 12.4, 12.4, 9.6, 7.2, 14.1, 14.1, 12.4, 14.2, 12.4, 1...
           <dbl> 44, 49, 49, 47, 43, 47, 50, 36, 50, 49, 50, 54, 42, 4...
## $ edat
            <dbl> 34.2. 32.6. 22.0. 37.9. 42.2. 33.1. 36.5. 38.5. 41.5....
## $ bmi
## $ edatdiag <dbl> 41, 48, 35, 45, 42, 44, 48, NA, 47, 45, 48, 43, 36, 4...
## $ tabac
            <fct> No fumador, Fumador, Fumador, No fumador, Fumador, No...
## $ sbp
            <dbl> 132, 130, 108, 128, 142, 156, 140, 144, 134, 102, 142...
## $ dbp
           <dbl> 96, 72, 58, 76, 80, 94, 86, 88, 78, 68, 84, 74, 86, 5...
## $ ecg
           <fct> Normal, Normal, Frontera, Normal, Fro...
## $ chd
```

#### Check the levels of a factor

Usually when humans fill the database...a plenty of errors are encountered :(

```
- An answer like "SI", could be entered like:
"SI", "Si", "si", "SI ", "SÍ", .....
```

All this possible answers will be differents levels for the same variable

#### How to correct it?

We can use: recode\_factor:

```
diab$mort <- recode_factor(diab$mort, "Muerto" = "muerto")
levels(diab$mort)

## [1] "muerto" "Vivo"</pre>
```

Return to the original version:

```
diab$mort <- recode_factor(diab$mort, "muerto" = "Muerto")
levels(diab$mort)</pre>
```

```
## [1] "Muerto" "Vivo"
```

# Descriptive Statistics: Numerical summaries

## **Numerical Summaries (I)**

We can access individual variables within a data frame using the \$ operator. Let's print out all the *edat* values in the data. Let's then see what are unique values of each. Then let's calculate the mean , median and range for the *edad* variable:

```
## [1] 44 49 49 47 43 47 50 36 50 49 50 54 42 44 40 48 50 47 38 35 51 40 54
## [24] 53 45 41 34 38 43 45 40 44 48 51 36 52 41 49 44 37 51 47 45 38 35 50
## [47] 53 48 40 43 54 52 69 38 50 64 44 38 62 47 78 49 63 71 51 59 50 66 42
## [70] 40 67 86 52 42 60 75 81 60 60 63 62 57 71 58 42 45 66 61 48 82 35 57
## [93] 56 49 50 53 71 55 69 59 47 75 80 57 52 48 57 58 51 33 52 52 64 31 69
## [116] 59 38 49 49 68 40 36 60 74 61 54 35 46 40 53 66 61 41 41 41 46 80 63
## [13] 72 41 52 53 61 53 75 40 61 62 49
```

### Numerical Summaries (II)

```
## [1] 44 49 47 43 50 36 54 42 40 48 38 35 51 53 45 41 34 52 37 69 64 62 78
## [24] 63 71 59 66 67 86 60 75 81 57 58 61 82 56 55 80 33 31 68 74 46 72

diab$edat %>% unique() %>% length()

## [1] 45
```

### Numerical Summaries (III)

```
#Mean, median and rang
mean(diab$edat)
## [1] 52.16779
median(diabsedat)
## [1] 50
sd(diabsedat)
## [1] 11.77285
var(diab$edat)
## [1] 138.6
range(diab$edat)
```

## [1] 31 86

```
Getting started

Descriptive Statistics: Numerical summaries

Descriptive Statistics: Graphical summaries

Statistics test. Continuos Variables

Statistics test. Discrete Variables

Bonus: ANOVA and Linear Regression

Your turn
```

### Numerical Summaries (IV)

If we want to group the descriptive summaries by other variables we can use group\_by function:

```
diab %>%
  group by(tabac, ecg) %>%
  summarize(mean(edat))
## # A tibble: 9 x 3
  # Groups:
               tabac [?]
     tabac
                          `mean(edat)`
                ecg
     <fct>
                <fct>
                                 <dh1>
## 1 Ex filmador Anormal
                                  68.5
  2 Ex fumador Frontera
                                  59.8
## 3 Ex filmador Normal
                                  51.1
## 4 Fumador
                Anormal
                                  58
## 5 Fumador
                Frontera
                                  44.8
## 6 Fumador
                Normal
                                  44.7
## 7 No fumador Anormal
                                  66.5
## 8 No fumador Frontera
                                  53.8
## 9 No fumador Normal
                                  56.0
```

# Numerical Summaries (V) A general summary of all variables:

```
summary(diab[, 2:11])
##
        mort
                     tempsviu
                                        edat
                                                         bmi
    Muerto: 25
                         . 0.00
                                          .31.00
                                                           .18.20
                  Min
                                   Min.
                                                    Min
    Vivo :124
                  1st Qu.: 7.30
                                   1st Qu.:43.00
                                                    1st Qu.:26.60
##
                  Median :11.60
                                   Median :50.00
                                                    Median :31.20
##
                  Mean
                         :10.52
                                          :52.17
                                                    Mean
                                                           :31.78
                                   Mean
                  3rd Qu.:13.90
                                   3rd Qu.:60.00
                                                    3rd Qu.:35.20
##
##
                  Max.
                         :16.90
                                   Max.
                                          :86.00
                                                    Max.
                                                           :59.70
##
##
       edatdiag
                            tabac
                                           sbp
                                                            dbp
           :26.00
                                                              : 58.00
    Min.
                     Ex fumador:41
                                      Min.
                                           : 98.0
                                                       Min.
    1st Qu.:38.00
                     Fumador
                                .51
                                      1st Qu.:124.5
                                                       1st Qu.: 74.00
    Median :45.00
                     No fumador:57
                                      Median :138.0
                                                       Median: 80.00
           :46.01
                                             :139.3
                                                              : 90.04
    Mean
                                      Mean
                                                       Mean
    3rd Qu.:53.25
                                      3rd Qu.:152.0
                                                       3rd Qu.: 88.00
    Max
           :81.00
                                      Max.
                                             :222.0
                                                       Max.
                                                              :862.00
           :5
                                      NA's
                                             :3
    NA's
##
                    chd
          ecg
    Anormal: 11
                    No:99
    Frontera: 27
                    Si:50
##
    Normal :111
##
```

Numerical Summaries (VI)
What happens if we have missing data in our dataset?

```
mean(diab$sbp)
## [1] NA
```

**NA** indicates *missing data* in the variable Let's look the sbp variable:

```
diab$sbp
     [1] 132 130 108 128 142 156 140 144 134 102 142 128 156 102 146 120 142
    [18] 144 NA 134 130 122 132 150 134 142 124 102 134 118 192 122 122 112
    [35] 142 152 112 118 152 136 134 130 108 126 132 144 126 128 NA 128 142
    [52] 132 148 170 140 138 112 140 138 130 178 158 168 146 128 132 154 154
    [69] 122 144 178 162 142 120 124 174 142 160 122 162 132 116 152 144
    [86] 138 138 184 158 176 118 172 182 144 142 154 122 222 150 142 128 122
  [103] 162 172 132 112 138 128 132 120 140 140 172 136 152 126 104 142 128
  [120] 122 122 122 122 168 162 NA 126 180 132 150 106 154 122 120 120 144
## [137] 134 148 170 160 154 124 130 156 162 132 120 160 146
```

# Numerical Summaries (VII) How to work with missing data:

```
?mean
mean(diab$sbp, na.rm = TRUE)
## [1] 139.2603
is.na(diab$sbp)
    [1] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
##
   [12] FALSE FALSE FALSE FALSE FALSE FALSE FALSE TRUE FALSE FALSE FALSE
   [23] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
   [34] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
   [45] FALSE FALSE FALSE TRUE FALSE FALSE FALSE FALSE FALSE FALSE
   [56] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
   [67] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
   [78] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
   [89] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
  [100] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
  [111] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
  [122] FALSE FALSE FALSE FALSE TRUE FALSE FALSE FALSE FALSE FALSE
  [133] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [144] FALSE FALSE FALSE FALSE FALSE
```

#### Numerical Summaries (VIII)

How to work with missing data:

```
sum(is.na(diab$sbp))
## [1] 3
sum(is.na(diab$dbp))
## [1] 0
```

#### **EXERCISE**

- With the diab dataset
  - Show only the rows from 35 to 98 and columns 5, 7, and from 9 to 11
  - Change the level of the variable tabac, from No Fumador to No\_Fumador
  - Display the unique values for the variable bmi. Count how many exist.
  - Display the mean of edatdiag, grouped by ecg

# Descriptive Statistics: Graphical summaries

#### **Exploratory Data Analysis (EDA)**

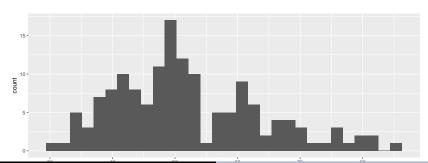
We could dedicate half of the course only to EDA. Here we will only see the most common approaches to visualize data:

- Histograms
- Scatterplots
- Boxplots

#### **Histograms**

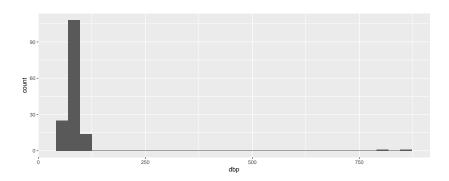
We will use histograms to plot the frequencies of each level of variables. This is the way to see the data distribution of particulars variables.

```
ggplot(diab, aes(edat)) +
geom_histogram(bins = 30)
```



# Histograms (II)

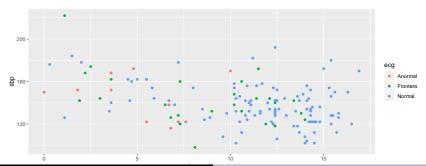
```
ggplot(diab, aes(dbp)) +
geom_histogram(bins = 30)
```



#### Scatterplots. Two continous variables

This is the graphical way to check the relation between two variables:

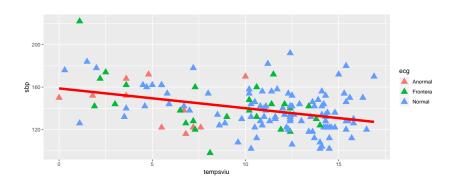
```
ggplot(diab, aes(tempsviu, sbp, col = ecg)) +
  geom_point()
```



# Scatterplots (II)

```
ggplot(diab, aes(tempsviu, sbp, col = ecg)) +
geom_point(size = 4, pch = 17) +
geom_smooth(lwd=2, se=FALSE, method="lm", col="red")
```

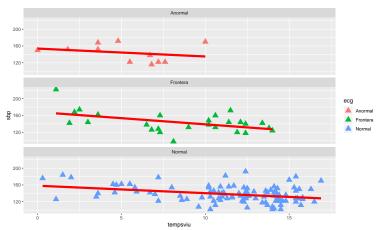
# Scatterplots (II)



#### **Faceting**

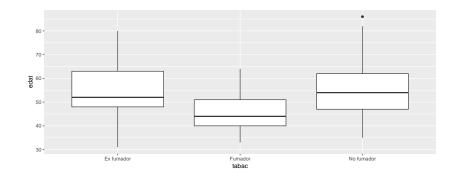
```
ggplot(diab, aes(tempsviu, sbp, col = ecg)) +
  geom_point(size = 4, pch = 17) +
  geom_smooth(lwd = 2, se=FALSE, method="lm", col="red") +
  facet_wrap(~ ecg, ncol = 1)
```

### **Faceting**



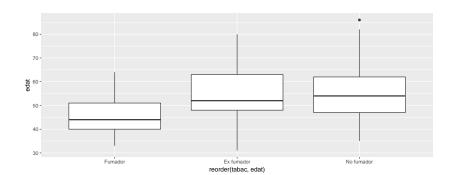
#### Boxplot. Continous versus categorical

```
ggplot(diab, aes(tabac, edat)) +
  geom_boxplot()
```



# Boxplot (II)

```
ggplot(diab, aes(x= reorder(tabac, edat), y = edat)) +
geom_boxplot()
```



#### **EXERCISE**

- With the diab dataset
  - Use the best graphic type to plot the relation between sbp and dbp
  - Show graphically the relation between edat and ecg
  - Plot the sbp frequencies
  - Improve the first graphic (add linear regression, avoid strange data in dbp, ...)

#### Statistics test. Continuos Variables

### Two-sample t-test

- Two-sample t-test will assess the differences in means between two groups
- The function for a t-test is t.test()
- The usage is t.test(response~group, data=myDataFrame)

#### Recode levels of tabac variable

Let's recode the levels of the variable to gain more opportunities of "playing" with the dataset

```
levels(diab$tabac)

## [1] "Ex fumador" "Fumador" "No fumador"

diab$tabac <- recode_factor(diab$tabac, "Ex fumador" = "Fumador")
levels(diab$tabac)

## [1] "Fumador" "No fumador"</pre>
```

## Two-sample t-test (II)

Are there differences in coronary heart disease (*chd*) depending of body mass index (*bmi*) in this dataset?

## Two-sample t-test (II)

t.test(bmi ~ chd, data = diab)

```
##
##
    Welch Two Sample t-test
##
## data: bmi by chd
## t = 2.3387, df = 102.14, p-value = 0.0213
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.4072447 4.9543310
## sample estimates:
## mean in group No mean in group Si
           32 67879
                            29.99800
##
```

## Two-sample t-test (III)

Are there differences in *chd* depending of *tabac* in this dataset?

t.test(edat ~ tabac, data = diab)

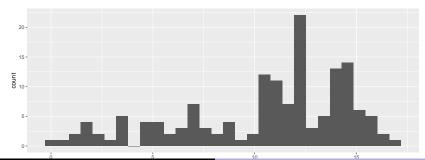
## Two-sample t-test (III)

```
##
##
    Welch Two Sample t-test
##
## data: edat by tabac
## t = -3.3969, df = 111.3, p-value = 0.0009461
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -10.501812 -2.763635
## sample estimates:
##
      mean in group Fumador mean in group No fumador
##
                   49 63043
                                            56.26316
```

## Wilcoxon rank-sum test (a.k.a. Mann-Whitney *U* test)

When the continous variable i not uniformly distributed.

```
ggplot(diab, aes(tempsviu)) +
  geom_histogram(bins = 30)
```



# Wilcoxon rank-sum test (a.k.a. Mann-Whitney *U* test) II

```
##
## Wilcoxon rank sum test with continuity correction
##
## data: tempsviu by chd
## W = 3711, p-value = 6.738e-07
## alternative hypothesis: true location shift is not equal to 0
```

#### Statistics test. Discrete Variables

## **Contingency tables**

```
xtabs(~ chd + tabac, data = diab)
##
       tabac
        Fumador No fumador
  chd
##
     Nο
              61
                         38
              31
##
     Si
                         19
addmargins(xtabs(~ chd + tabac, data = diab))
##
        tabac
## chd
         Fumador No fumador Sum
##
     Nο
               61
                          38
                              99
##
     Si
               31
                           19
                               50
                          57 149
##
     Sum
               92
```

## Chi-square test

Chi-square test is used top assess the independence of these two factors. That is, if the null hypothesis that smoking habits and coronary heart disease history are independent is true, then we would expect a proportionally equal number of smokers across each coronary heart disease history level. Smokers seem to be slightly higher risk than non-smokers, but the difference is just short of statistically significant.

### Chi-square test

```
chisq.test(xtabs(~ chd + tabac, data = diab))

##

## Pearson's Chi-squared test with Yates' continuity correction
##

## data: xtabs(~chd + tabac, data = diab)
## X-squared = 5.3975e-31, df = 1, p-value = 1
```

#### Fisher's exact test

Useful when n < 5 in some of the groups.

```
fisher.test(xtabs(~ chd + tabac, data = diab))
##
##
    Fisher's Exact Test for Count Data
##
## data: xtabs(~chd + tabac, data = diab)
## p-value = 1
## alternative hypothesis: true odds ratio is not equal to 1
## 95 percent confidence interval:
   0.4569698 2.0900449
## sample estimates:
## odds ratio
## 0.9839764
```

mosaicplot(xtabs(~ chd + tabac, data = diab))

#### Plot the results

Mosaic plot is a useful way to visualize contingency table data

chd

#### **EXERCISE**

- With the diab dataset
  - Are there any differences in sbp values between chd groups
  - Show graphically the relation between sbp and chd
  - Create a contingency table between mort and tabac. Plot the table
  - Test if smoking habits is related with mort variable.

**Bonus: ANOVA and Linear Regression** 

#### **ANOVA**

Remember that t-tests are for assessing the differences in means between two groups. A t-test is a specific case of ANOVA, which is a specific case of a linear model.

```
t.test(edat ~ ecg, data = diab)

Error in t.test.formula(edat ~ ecg, data = diab) :
   grouping factor must have exactly 2 levels
```

fit <- lm(edat ~ ecg, data = diab)

## ANOVA (II)

Let's look the relationship between edat and ecg with ANOVA:

## ANOVA (II)

ANOVA only says if there exists differences among the levels (in general), but does not say anything about differences within the levels. We have to draw on **Tukey's test** 

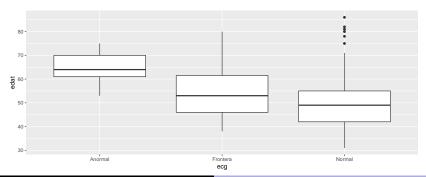
```
TukeyHSD(aov(fit))

## Tukey multiple comparisons of means
## 95% family-wise confidence level
##
## Fit: aov(formula = fit)
##
## Secg
## Giff lwr upr p adj
## Frontera-Anormal -11.09428 -20.588782 -1.599771 0.0174729
## Normal-Anormal -14.40459 -22.794951 -6.014221 0.0002297
## Normal-Frontera -3.31031 -9.006113 2.385493 0.3560430
```

## ANOVA (III)

It is very useful to plot the comparison

```
ggplot(diab, aes(ecg, edat)) +
geom_boxplot()
```



#### **Linear Models**

Linear model seeks to explain the relationship between a variable of interest, our Y, outcome, response, or dependent variable, and one or more X, predictor, or independent variables.

$$Y = beta0 + beta1 \cdot X + error$$

#### where

Y is the response X is the predictor variable beta0 is the intercept beta1 is the coefficient error is the random error

## Linear Models (II)

Let's look the relationship between sbp and dbp

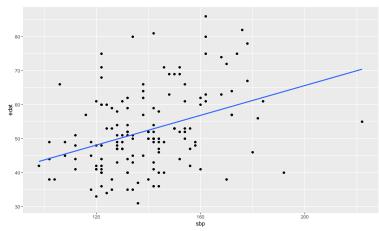
```
fit <- lm(edat ~ sbp, data = diab)
summary(fit)
##
## Call:
## lm(formula = edat ~ sbp, data = diab)
##
## Residuals:
      Min
              1Q Median
                                     Max
## -23 882 -7 012 -1 498 5 624 28 816
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 21.84633 6.30134 3.467 0.000694 ***
               0.21894 0.04478 4.889 2.67e-06 ***
## sbp
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.96 on 144 degrees of freedom
     (3 observations deleted due to missingness)
## Multiple R-squared: 0.1424, Adjusted R-squared: 0.1364
## F-statistic: 23.91 on 1 and 144 DF, p-value: 2.668e-06
```

## Linear Models (III)

#### Let's plot the relationship

```
ggplot(diab, aes(sbp, edat)) +
geom_point() +
geom_smooth(method = "lm", se = FALSE)
```

## Linear Models (III)



#### Your turn

#### **EXERCISE**

Using the osteoporosis.csv dataset