



$$\begin{aligned}
 \frac{\partial o}{\partial w} &= \frac{\partial o}{\partial p} \cdot \frac{\partial p}{\partial w} + \frac{\partial o}{\partial q} \cdot \frac{\partial q}{\partial w} \quad [\text{Multivariable Chain Rule}] \\
 &= \frac{\partial o}{\partial p} \cdot \frac{\partial p}{\partial y} \cdot \frac{\partial y}{\partial w} + \frac{\partial o}{\partial q} \cdot \frac{\partial q}{\partial z} \cdot \frac{\partial z}{\partial w} \quad [\text{Univariate Chain Rule}] \\
 &= \underbrace{\frac{\partial K(p, q)}{\partial p} \cdot g'(y) \cdot f'(w)}_{\text{First path}} + \underbrace{\frac{\partial K(p, q)}{\partial q} \cdot h'(z) \cdot f'(w)}_{\text{Second path}}
 \end{aligned}$$

Figure 1.13: **Illustration of chain rule in computational graphs:** The products of node-specific partial derivatives along paths from weight w to output o are aggregated. The resulting value yields the derivative of output o with respect to weight w . Only two paths between input and output exist in this simplified example.