

LU_SNR_db

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Function:

- `char ch = toupper('z');` or, `ch=('z' ^ 32);` \Rightarrow `ch='Z';`
- `char ch = tolower('B');` or, `ch=('B' | 32);` \Rightarrow `ch='b';`
- `abs(x) = abs(-x) = x;`
- `sqrt(x) = \sqrt{x} ; [sqrtl(x) return long double;]`
- `pow(x, y) = x^y ; [powl(x, y) return long double;]` \Rightarrow `round(pow(x, y));`
- `log10(3) = 0.4771212;` `log2(3) = 1.584962501;`
- `round(x.y) \Rightarrow if $y \geq 5$ then ans = x+1;`
- `ceil(x.y) \Rightarrow if $y \geq 01$ then ans = x+1; or, ans=(a+b-1)/b; [ceil symbol \Rightarrow [x.y] = x+1;]`
- `floor(x.y) \Rightarrow if $x.y$ positive then ans=x; if $x.y$ negative then ans=x-1;
ex: floor(-2.3) = -3; floor(3.8) = 3;`
- `trunc(x.y) \Rightarrow if $x.y$ positive / negative then ans = x; if ex: floor(-2.3) = -2; floor(3.8) = 3;`
- `stoi(s) \Rightarrow convert string to integer;` [`stoll(s)` \rightarrow for long long int value.]
- `to_string(num) \Rightarrow convert integer to string;`
- `getline(cin, name) \Rightarrow input a line. [ignore buffer_use \Rightarrow fflush(stdin); or, cin.ignore();]`
- `s2.substr(s1_pos, s2_len) \Rightarrow This function generates a new string with its value initialized to a copy of a sub-string of this object. [if string s1="abcdef"; then, string s2=s1.substr(1,3); \rightarrow s2 = "bcd"; string s2 = s1.substr(1); \rightarrow s2 = "bcdef";]`
- `next_permutation()`: It is used to rearrange the elements in the range [first, last) into the next lexicographically greater permutation. { {1,2,3}, {1,3,2}, {2,1,3}, {2,3,1}, {3,1,2}, {3,2,1} };
`int arr[] = {1, 2, 3};` \Rightarrow `O(n*n!)`
`do{`
`//Add any conditions;`
`cout << arr[0] << " " << arr[1] << " " << arr[2] << "\n";`
`} while (next_permutation(arr, arr + 3));`

STL Function:

- `size()` – Returns the number of elements in the vector. [`v.size(); mp.size(); st.size();`]
- `empty()` – Returns whether the container is empty. If `empty` return `true(1)`, if not `empty` return `false(0)`. [`v.empty(); mp.empty (); st.empty ();`]
- `front()` – Returns a reference to the first element in the vector. [`v.front();`]
- `back()` – Returns a reference to the last element in the vector. [`v.back();`]
- `push_back()` – It push the elements into a vector from the back.
- `pop_back()` – It is used to pop or remove elements from a vector from the back.
- `insert()` – It inserts new elements before the element at the specified position.
[`v.insert(v.begin(), value); mp.insert({key, value}); st.insert(key);`]

- **erase()** – It is used to remove elements from a container from the specified position or range. [**v.erase(v.begin() + position); mp.erase(value); st.erase(value); str.erase(v.begin() + position);**]
- **clear()** – It is used to remove all the elements. [**name.clear();**]
- **mp.count(K)** - The function returns the number of times the key K is present in the map/set container. [**st.count(K);**] $\Rightarrow O(\log n)$;
- **max_size()** - Returns the maximum number of elements a set container can hold. [**v.max_size(); mp.max_size(); st.max_size();**]
- **find()** - An iterator to the first element in the range that compares equal to val. If no elements match, the function returns last(v.end()). [**find (v.begin(), v.end(), val);**] $\Rightarrow O(n)$; [**mp.find(val); st.find(val);**] $\Rightarrow O(\log(n))$
- **lower_bound()** – Let $v=\{1,5,7\}$; if we search **1** return **0's** index address, if we search **2** return **1's** index address, if we search **0** return **0's** index address, if we search **7 < value** then return **v.end()** address. (**must be sorted**) $\Rightarrow O(\log n)$
[**auto x=lower_bound(v.begin(), v.end(), val);**] [**auto x = mp.lower_bound(val); auto x = st.lower_bound(val);**] $\rightarrow \{x \rightarrow \text{first}; x \rightarrow \text{second};\}$
- **upper_bound()** - Let $v=\{1,5,7\}$; if we search **1** return **1's** index address, if we search **2** return **1's** index address, if we search **0** return **0's** index address, if we search **7 < value** then return **v.end()** address. (**must be sorted**) $\Rightarrow O(\log n)$
- **rand()**: The rand() function is used in C++ to generate random numbers in the range [0, RAND_MAX]. Ex: **a=rand(); a=(rand()%10)+1** [$\Rightarrow a \geq 1 \ \&\& \ a \leq 10$]; if **lb=20** and **ub=40** Then, **a=(rand() % (ub - lb + 1)) + lb** [$\Rightarrow a \geq 20 \ \&\& \ a \leq 40$];
- **Ordered Set**: The complexity of the **insert** and **erase** functions is $O(\log n)$.
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template <typename T> using ordered_set = tree<T, null_type, less<T>, rb_tree_tag, tree_order_statistics_node_update>;

// *s.find_by_order(k): K-th element in a set (counting from zero).
// s.order_of_key(k): Number of items strictly smaller than k. (same as, lower_bound of k)
ordered_set<int> s; // we can change the data type.

Stack & Queue & Deque & Priority Queue :

- **push()**: Adds the element 'x'. [**s.push(x); q.push(x); pd.push(x);**]
 - In Deque, you can push both side [**dq.push_back(x); dq.push_front(x);**]
- **pop()**: Deletes the element. [**name.pop();**]
 - In Deque, you can pop both side [**dq.pop_back(x); dq.pop_front(x);**]
- **top()**: Returns a reference to the top most element of the stack. [**s.top(); pq.top();**]
- **front()**: Returns a reference to the first element of the queue. [**q.front(); dq.front();**]

- **back()**: Returns a reference to the last element of the queue. [**q.back()**; **dq.back()**;
- **empty()**: Returns whether the stack/queue is empty. It return **true** if the stack/queue is empty otherwise returns false. [**name.empty()**];
- **dq.at(x)**: Returns a reference to the element at position **x** in the deque container object.
Ex: `dq = {10,3,15,20}`; `ans= dq.at(2);` \Rightarrow `ans=15`
- **priority_queue<int>max_heapPQ;** \Rightarrow In this queue elements are in non-increasing. [same as **multiset <int, greater<int> > s;**]
- **priority_queue<int, vector<int>, greater<int>>min_heapPQ;** \Rightarrow In this queue elements are in non-decreasing order. [similar to **multiset**]

Others:

- **binary_search()**: Return true(1) or false(0). If found return **1**. Else return **0**.
[**binary_search(start_address, end_address, value_to_find);**]
- **max_element()**: Return the maximum value's address of the vector.
[**int max= *max_element(v.begin(),v.end());**] \Rightarrow $O(n)$
- **min_element()**: Return minimum value's address of the vector.
[**int min= *min_element(v.begin(),v.end());**] \Rightarrow $O(n)$
- **accumulate()**: Return summation of the vector.
[**int sum= accumulate(v.begin(),v.end(), 0);**] \Rightarrow $O(n)$
- **count()**: Return count of the 'val' element.
[**int c = count(v.begin(), v.end(), val);**] \Rightarrow $O(n)$
- **all of()/any_of()/none of()**: Are **all of/at least one/none of** the elements **greater than 0?** (you can change this condition) \Rightarrow **return true(1) or, false(0).**
 - **all_of(v.begin(), v.end(), [](int x){return x>0; });**
 - **any_of(v.begin(), v.end(), [](int x){return x>0; });**
 - **none_of(v.begin(), v.end(), [](int x){return x>0; });**
- **iota()**: The algorithm **iota()** creates a range of sequentially increasing values.
[**iota(a, a+5, 10);** \Rightarrow `a[5]={10,11,12,13,14};`]
- **is_sorted()**: Return bool value. If, vector are sorted return 1. Else return 0.
[**bool x= is_sorted(v.begin(), v.end());**] \Rightarrow $O(n)$
- **gcd()**: Return a and b gcd(**Greatest Common Divisor**) value.
[**int gcd= __gcd(a,b);**] \Rightarrow $O(\log n)$
- **lcm()**: Return a and b lcm(**Least Common Multiple**) value.
[**int lcm= (a*b)/ __gcd(a,b);**] \Rightarrow $O(\log n)$
- **memset()**: Initialize a **1D** vector with **-1**(or, **0**): \Rightarrow $O(n)$
memset(vec_name, -1, sizeof(vec_name)); \rightarrow use any time.
- Initialize a **1D** vector with **1**(or, any number): \Rightarrow $O(n)$
vector<int> vec(n, 1); [n=row, m=col] \rightarrow use only initialize time.

- Initialize a **2D** vector with 1(or, any number): $\Rightarrow 0(n)$
vector<vector<int>> vec(n , vector<int> (m, 1)); [n=row, m=col]

Math:

- $p+(p+1)+\dots+(q-1)+q = \frac{(q+p)(q-p+1)}{2}$; [Ex: $7+8+9+10+11 = \frac{(11+7)(11-7+1)}{2} = 45$]
- $1+2+3+\dots+(n-1)+n = \frac{(n * (n+1))}{2}$; [Ex: $1+2+3+4+5 = \frac{(5*(5+1))}{2} = 15$]
- $1+3+5+\dots+(2n-3)+(2n-1) = N^2$; [**N-> number of size**] [Ex: $1+3+5 = 3^2 = 9$]
- $2+4+6+\dots+(2n-2)+2n = N * (N+1)$; [**N-> number of size**] [Ex: $2+4+6 = 3*(3+1) = 12$]
- $1^2+2^2+3^2+\dots+(n-1)^2+n^2 = \frac{n(n+1)(2n+1)}{6}$; [Ex: $1+4+9 = \frac{3(3+1)(2*3+1)}{6} = 14$]
- $1^3+2^3+3^3+\dots+(n-1)^3+n^3 = \frac{(n(n+1))^2}{4}$; [Ex: $1+8+27 = \frac{(3(3+1))^2}{4} = 36$]
- $1^2+3^2+5^2+\dots+(2n-3)^2+(2n-1)^2 = \frac{N*(4N^2-1)}{3}$; [Ex: $1+9+25 = \frac{3*(4*3^2-1)}{3} = 35$]
- $1^3+3^3+5^3+\dots+(2n-3)^3+(2n-1)^3 = \frac{N^2(2N^2-1)}{3}$; [Ex: $1+27+125 = \frac{3^2(2*3^2-1)}{3} = 153$]
- $1^4+2^4+3^4+\dots+(n-1)^4+n^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30}$;
[Ex: $1+16+81+256 = \frac{4(4+1)(2*4+1)(3*4^2+3*4-1)}{30} = 354$]
- $c^a + c^{a+1} + \dots + c^b = \frac{(c^{b+1} - c^a)}{(c - 1)}$; [$c \neq 1$]
- $2^0 + 2^1 + 2^2 + 2^3 + \dots + 2^{(k-1)} = 2^k - 1$; [Ex: $1+2+4+8+16+32 = 2^6 - 1 = 63$]
- If $F(n) = -1 + 2 - 3 + \dots + (-1)^n * n$
 - If **N even** number, **ans = N/2;**
 - If **N odd** number, **ans = ((N + 1) / 2) * (-1);**
- N-th **Odd** number = **(2 * N)-1;**
- N-th **Even** number = **2*N;**
- $a + a*k + a*k^2 + \dots + b = \frac{(b * k) - a}{(k - 1)}$. [ex: $3 + 6 + 12 + 24 = \frac{(24 * 2) - 3}{(2-1)} = 45$]
- $a + (a+4) + (a+2*4) + \dots + b = \frac{(n * (a + b))}{2}$. [n-> number of size]
[ex: $3 + 7 + 11 + 15 = \frac{(4 * (3 + 15))}{2} = 36$.]
- even \pm even = **even**; even \pm odd = **odd**; odd \pm odd = **even**;
- even \times even = **even**; even \times odd = **even**; odd \times odd = **odd**;
- Number of digits in N = **floor(log10(N)) + 1;**
- Number of trailing **zeros** in **N!** \Rightarrow **while(N) sum+=N/5, N/=5;** [Ex: $10! = 3628800$;
- For a grid of size **(N x N)** the total number of **squares** formed: **((n*(n+1)) * (2n+1)) / 6;**
- 5 minutes** Clock Angular Value is **30°**. [**1 min = 6°**]
- Angle between clock minute and hour, **ans = abs ((0.5 * 11 * m) - (30 * h));**
 - For smaller angle, **if (ans > 180) ans = 360 - ans;**
- The number of ways of selecting one or more things from N different things is given by $2^N - 1$. (combination)
- Number of possible of N bits = 2^N . [4bits, $2^4 = 16 \Rightarrow$ 0 to 15 number possible with using 4 bits] $(2^n - 1) \rightarrow$ highest value.
- $N = 2^x \Rightarrow x = \log_2(N)$. Ex: $64 = 2^6$ [$\log_2(64) = 6$].

- $\log_u(x) = \frac{\log_k(x)}{\log_k(u)}$ [k-> any base (2,10)]; $\log_a(k) = \frac{1}{\log_k(a)}$; $a^x = b \Rightarrow x = \log_a b$;
- $(A * B) = ((A \% \text{Mod}) * (B \% \text{Mod})) \% \text{Mod}$; \leq [Same As +,- Operator]
- $(A / B) = ((A \% \text{Mod}) * (\text{BinExp}(A, \text{Mod}-2) \% \text{Mod})) \% \text{Mod}$;

Bits:

- Bitwise AND(&): $(1 \& 1) = 1$;
- Bitwise OR(|): $(0 | 1) = 1$; $(1 | 0) = 1$; $(1 | 1) = 1$;
- Bitwise EXOR(^): $(0 \wedge 1) = 1$; $(1 \wedge 0) = 1$;
- Bitwise NOT(~): inverts all bits of it. [$a = 1001_2 \rightarrow (\sim a) = 0110$]
- Right Shift(>>): right shifting an integer “x” with an integer “y” denoted as ‘(x>>y)’ is equivalent to **dividing** x with 2^y . Ex: let’s take $N=32$; which is 100000 in Binary Form. Now, if $N=(N>>2)$ then N will become $N=N / (2^2)$. Thus, $N=32 / (2^2) = 8$ which can be written as 1000. [$18 = (10010)_2 \rightarrow (18>>1) = 01001$; $(18>>2) = 00100$;]
- Left Shift(<<): left shifting an integer “x” with an integer “y” denoted as ‘(x<<y)’ is equivalent to **multiplying** x with 2^y . Ex: let’s take $N=22$; which is 00010110 in Binary Form. Now, if $N=(N<<2)$ then N will become $N=N * (2^2)$. Thus, $N=22 * (2^2) = 88$ which can be written as 01011000. [$3 = (11)_2 \Rightarrow (3<<1) = 110$; $(3<<2) = 1100$;]
- $(N\&1) == 1 \rightarrow N$ **odd** number; $(N\&1) == 0 \rightarrow N$ **even** number;
- $(N / 2) == (N >> 1)$; $(N * 2) == (N << 1)$;
- $(2^N) == (1LL << N)$; $\Rightarrow N = (1LL << (\text{long long})\log_2(N))$;
- A quick way to **swap** a and b $\Rightarrow [a \wedge b, b \wedge a, a \wedge b]$;
- CheckBit(x, k) $\Rightarrow (x \& (1LL << k))$;
- SetBit(x, k) $\Rightarrow (x |= (1LL << k))$;
- ClearBit(x, k) $\Rightarrow (x \&= \sim(1LL << k))$;
- FlipBit(x, k) $\Rightarrow (x \wedge= \sim(1LL << k))$;
- MSB(mask) $\Rightarrow 63 - \text{__builtin_clzll}(\text{mask})$; [Most Significant Bit position]
- LSB(mask) $\Rightarrow \text{__builtin_ctzll}(\text{mask})$; [Least Significant Bit position]
- **__builtin_popcount(x)**: This function is used to count the number of one’s(set bits) in an integer(32 bits). Similarly you can use **__builtin_popcountll(x)** for **long long** data types (64 bits). Ex: $x = 5$ (101) $\Rightarrow \text{ans}=2$;
- **__builtin_clz(x)**: It counts number of zeros before the first occurrence of one(set bit) of the integer(32 bit). (**clz = count leading zero’s.**)
Ex: $x = 16$ (00000000 00000000 00000000 00010000) $\Rightarrow \text{ans} = 27$
- **__builtin_parity(x)**: This function returns true(1) if the number has **odd** parity else it returns false(0) for **even** parity. (**parity= count the number of one’s**)
Ex: $x = 7$ (111) $\Rightarrow \text{ans} = 1$; $x = 6$ (110) $\Rightarrow \text{ans} = 0$;
- **__builtin_ctz(x)**: Count number of zeros from **last to first** occurrence of one(set bit) of the given integer. (**ctz = count trailing zeros;**) Ex: $x = 16$ (00010000) $\Rightarrow \text{ans} = 4$;

Bitset Function:

bitset< highest_Bit_number > name(data);

- **bitset<64> b1(val);** or, **bitset<4>b2("1011");** => auto-convert to binary;
- **to_ulong():** Converts the contents of the **bitset** to an **unsigned long integer**; [Ex: b1 = 1001, int val = b1.to_ulong(); => val = 9;]
- **to_string():** Converts the contents of the **bitset** to a **string**; [Ex: b1 = 1001, s1 = b1.to_string(); => s1= "1001";]
- **flip(position):** flip function flips all bits (**1 to 0** and **0 to 1**). [Ex: b1 = 1001; b1.flip(1); =>b1 = 1011; b1.flip(1); =>b1=1001;]
- **count():** returns the total number of **set bits(1)**; [Ex: b1=1001; bit= b1.count(); => bit =2;]
- **any():** function to check if **any of its bits are set or not**; [Ex: b1=1001, any_set = b1.any(); => any_set = 1; b2=0000; any_set = b1.any(); => any_set = 0;]
- **set():** b1.set(**pos**) makes bset[pos] = 1;(i.e. default is 1). b1.set(**pos, value**) makes bset[pos] = 0 or, 1; [Ex: b1=1001; b1.set() =>b1 = 1111; b1.set(1)> b1= 1011; b1.set(0)> b1=1001; b1.set(3, 0);=> b1=0001; b1.set(2,1)> b1= 1101;]
- **reset():** reset function makes all bits 0; [Ex: b1 = 1001; b1.reset()=> b1 = 0000; b1.reset(3)> b1 = 0001;]

Combination And Permutation:

$$\diamond nC_r = \frac{nPr}{r!} \quad \text{Or, } nPr = nCr * r!$$

Combination(C):

- If, **Order Doesn't Matter** and **Repetition Allowed** then,

$$\text{Possibilities, } nC_r = \frac{n!}{r!(n-r)!}$$

- If, **Order Doesn't Matter** and **Repetition Not Allowed** then,

$$\text{Possibilities, } nC_r = \frac{(n+r-1)!}{r!(n-1)!}$$

- **Properties:** $nCr = nC(n-r)$, $nC_0 = nC_n = 1$, $nC_1 = nC(n-1) = n$, $nCr + nC(r-1) = (n+1)Cr$,
 $nCx = nCy \Rightarrow x = y$ or, $x + y = n$.
- **nCr has maximum value if:**
 - **r = n/2 ;** when n is **Even**.
 - **r = (n+1)/2;** when n is **Odd**.

- **Short Technique:**
$$nC_r = \frac{n*(n-1)*(n-2)*... r' th\ times}{r*(r-1)*(r-2)*... r' th\ times}$$

Ex: ${}^{20}C_3 = \frac{20 * 19 * 18}{3 * 2 * 1} = 1140$, ${}^{10}C_8 = {}^{10}C_{10-8} = {}^{10}C_2 = \frac{10 * 9}{2 * 1} = 45$, ${}^{20}C_{15} = {}^{20}C_{20-15} = {}^{20}C_5 = \frac{20 * 19 * 18 * 17 * 16}{5 * 4 * 3 * 2 * 1} = 15504$.

Permutation(P):

- If, **Order Matter** and **Repetition Allowed** then, Possibilities = n^r
- If, **Order Matter** and **Repetition Not Allowed** then, Possibilities = $\frac{n!}{(n-r)!}$
- **Properties:** $nP_0 = 1$, $nP_1 = n$, $nP(n-1) = n!$, $nPr/nP(r-1) = n - r + 1$.
- **Short Technique:** $nPr = n*(n-1)*(n-2)*... r' th\ times$.

Ex: ${}^{10}P_3 = 10 * (10-1) * (10-2) = 720$, ${}^{15}P_4 = 15 * 14 * 13 * 12 = 32760$.

Find Combination(nCr):

$\Rightarrow O(r*\log(n))$

Ex: $5C2 = 10$, $13C5 = 1287$;

```
void nCr( ll n, ll r)
{
    ll p= 1, k=1, m;
    if (n - r < r) r = n - r;
    if (r != 0)
    {
        while(r)
        {
            p*=n, k*=r;
            m=__gcd(p, k);
            p/=m, k/=m;
            n--, r--;
        }
    }
    else p=1;
    cout<<p<<endl;
}
```

Find Permutation (nPr):

$\Rightarrow O(n)$

Ex: $5P2 = 20$, $6P3 = 120$;


```
ll fact(ll n)
{
    if(n <= 1) return 1;
    return n * fact(n - 1);
}
ll nPr(ll n, ll r)
{
    return fact(n) / fact(n - r);
}
int main()
{
    ll n, r;
    cin>>n>>r;
    cout<<nPr(n, r);
}
```

Geometry:

GEOMETRY QUICK GUIDE 2: 2D SHAPES (UK)

TRIANGLES	QUADRILATERALS	REGULAR POLYGONS
Equilateral triangle All sides equal; interior angles 60°	Square All sides equal; all angles 90°	Equilateral triangle 3 sides; angle 60°
Isosceles triangle 2 sides equal; 2 congruent angles	Rectangle Opposite sides equal, all angles 90°	Square 4 sides; angle 90°
Scalene triangle No sides or angles equal	Rhombus All sides equal; 2 pairs of parallel lines; opposite angles equal	Regular Pentagon 5 sides; angle 108°
Right triangle 1 right angle	Parallelogram Opposite sides equal, 2 pairs of parallel lines	Regular Hexagon 6 sides; angle 120°
Acute triangle All angles acute	Kite Adjacent sides equal; 2 congruent angles	Regular Octagon 8 sides; angle 135°
Obtuse triangle 1 obtuse angle	Trapezium 1 pair of parallel sides	Regular Decagon 10 sides; angle 144°
	Trapezoid No pairs of parallel sides	

Law of sines

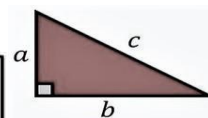
$$\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c}$$

Law of Cosines

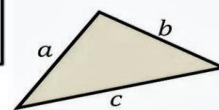
$$c^2 = a^2 + b^2 - 2ab \cos(C)$$

$$a^2 = b^2 + c^2 - 2bc \cos(A)$$

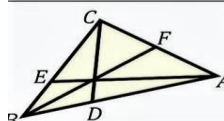
$$b^2 = a^2 + c^2 - 2ac \cos(B)$$



Pythagoras' Theorem
 $a^2 + b^2 = c^2$



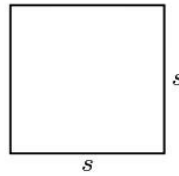
Heron's Formula
 $\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$
Semiperimeter, $s = \frac{a+b+c}{2}$



Ceva's Theorem
Given AE, BF & CD concurrent,
 $\frac{AD}{BD} \times \frac{BE}{CE} \times \frac{CF}{AF} = 1$

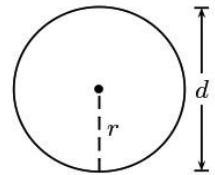
SQUARE

s = side
Area: $A = s^2$
Perimeter: $P = 4s$



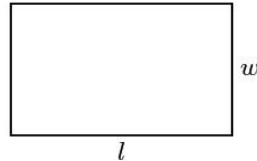
CIRCLE

r = radius, d = diameter
Diameter: $d = 2r$
Area: $A = \pi r^2$
Circumference: $C = 2\pi r = \pi d$



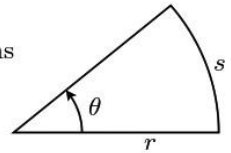
RECTANGLE

l = length, w = width
Area: $A = lw$
Perimeter: $P = 2l + 2w$



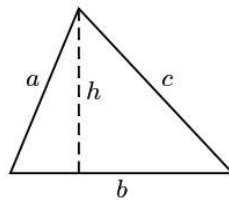
SECTOR OF CIRCLE

r = radius, θ = angle in radians
Area: $A = \frac{1}{2}\theta r^2$
Arc Length: $s = \theta r$



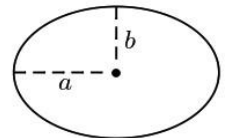
TRIANGLE

b = base, h = height
Area: $A = \frac{1}{2}bh$
Perimeter: $P = a + b + c$



ELLIPSE

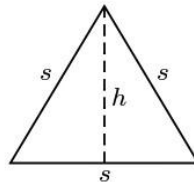
a = semimajor axis
 b = semiminor axis
Area: $A = \pi ab$



Circumference:
 $C \approx \pi \left(3(a+b) - \sqrt{(a+3b)(b+3a)} \right)$

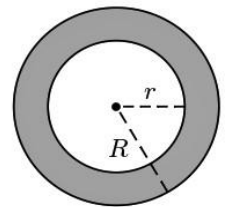
EQUILATERAL TRIANGLE

s = side
Height: $h = \frac{\sqrt{3}}{2}s$
Area: $A = \frac{\sqrt{3}}{4}s^2$



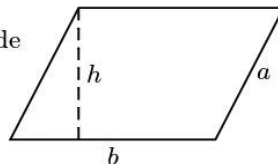
ANNULUS

r = inner radius,
 R = outer radius
Average Radius: $\rho = \frac{1}{2}(r + R)$
Width: $w = R - r$
Area: $A = \pi(R^2 - r^2)$
or $A = 2\pi\rho w$



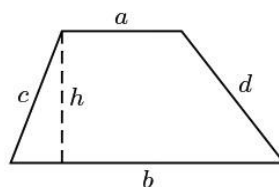
PARALLELOGRAM

b = base, h = height, a = side
Area: $A = bh$
Perimeter: $P = 2a + 2b$



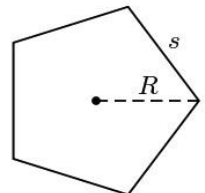
TRAPEZOID

a, b = bases; h = height;
 c, d = sides
Area: $A = \frac{1}{2}(a+b)h$
Perimeter:
 $P = a + b + c + d$



REGULAR POLYGON

s = side length,
 n = number of sides
Circumradius: $R = \frac{1}{2}s \csc\left(\frac{\pi}{n}\right)$
Area: $A = \frac{1}{4}ns^2 \cot\left(\frac{\pi}{n}\right)$
or $A = \frac{1}{2}nR^2 \sin\left(\frac{2\pi}{n}\right)$



Rhombus: Area = $(d_1 * d_2) / 2 = s^2 * \sin(C)$;

Perimeter = $4*s$;

Kite: Area = $(d_1 * d_2) / 2$;

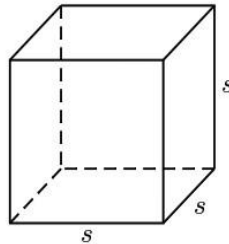
Perimeter = $2(s_1 + s_2)$;

[d_1 and d_2 = lengths of the diagonals, $s = s_1 = s_2$ = length of side, C = interior angle;]

3D GEOMETRY FORMULAS

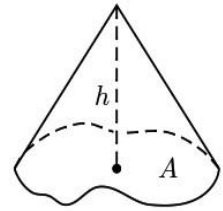
CUBE

s = side
Volume: $V = s^3$
Surface Area: $S = 6s^2$



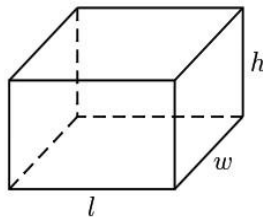
GENERAL CONE OR PYRAMID

A = area of base, h = height
Volume: $V = \frac{1}{3}Ah$



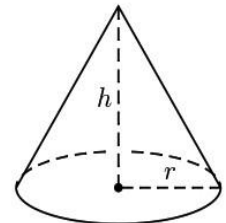
RECTANGULAR SOLID

l = length, w = width,
 h = height
Volume: $V = lwh$
Surface Area:
 $S = 2lw + 2lh + 2wh$



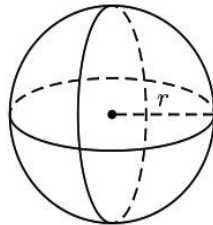
RIGHT CIRCULAR CONE

r = radius, h = height
Volume: $V = \frac{1}{3}\pi r^2 h$
Surface Area:
 $S = \pi r \sqrt{r^2 + h^2} + \pi r^2$



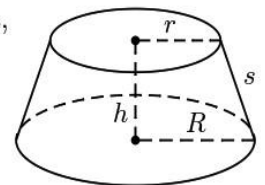
SPHERE

r = radius
Volume: $V = \frac{4}{3}\pi r^3$
Surface Area: $S = 4\pi r^2$



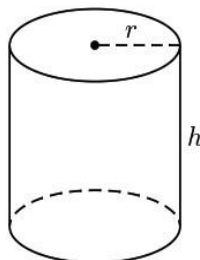
FRUSTUM OF A CONE

r = top radius, R = base radius,
 h = height, s = slant height
Volume: $V = \frac{\pi}{3}(r^2 + rR + R^2)h$
Surface Area:
 $S = \pi s(R + r) + \pi r^2 + \pi R^2$



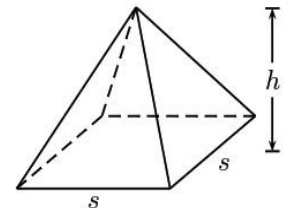
RIGHT CIRCULAR CYLINDER

r = radius, h = height
Volume: $V = \pi r^2 h$
Surface Area: $S = 2\pi r h + 2\pi r^2$



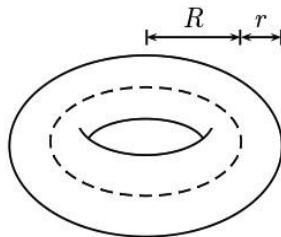
SQUARE PYRAMID

s = side, h = height
Volume: $V = \frac{1}{3}s^2 h$
Surface Area:
 $S = s(s + \sqrt{s^2 + 4h^2})$



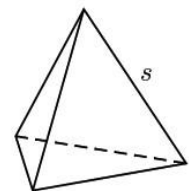
TORUS

r = tube radius,
 R = torus radius
Volume: $V = 2\pi^2 r^2 R$
Surface Area: $S = 4\pi^2 r R$



REGULAR TETRAHEDRON

s = side
Volume: $V = \frac{1}{12}\sqrt{2}s^3$
Surface Area: $S = \sqrt{3}s^2$



Algorithm

Binary Search:

=> $O(\log(n))$

```
void BinarySearch(vector<ll> &v, int n, int target)
{
    int low = 0, high = v.size() - 1, c = 0, mid = 0;
    while (high - low > 1) // or, low <= right
    {
        c++;
        mid = (low + high) >> 1; // or, mid = low + (high - low) / 2; or, (low + high) / 2;
        if (v[mid] < target) low = mid + 1;
        else high = mid;
    }
    if (v[low] == target) cout << low << "Found\n";
    else if (v[high] == target) cout << high << "Found\n";
    else cout << "Not Found\n";
}
```

Sieve Algorithm (find prime number):

=> $O(n \log \log n)$

```
const int N = 1e7 + 10; // N = 10^7
vector<bool> isPrime(N, 1);
void sieve()
{
    isPrime[0] = isPrime[1] = false;
    for (int i = 2; i < N; i++)
    {
        if (isPrime[i] == true)
        {
            for (int j = 2 * i; j < N; j += i)
            {
                isPrime[j] = false;
            }
        }
    }
}
```

Prime Factorization (Integer factorization):

=> $O(\sqrt{n})$

Ex: 36 => 2 2 3 3

```
int main()
{
    int n;
    cin >> n;
    vector<int> prime_factors;
    for (int i = 2; i * i <= n; i++)
    {
        while (n % i == 0)
        {
```

```
        prime_factors.push_back(i);
        n /= i;
    }
}
if (n > 1) prime_factors.push_back(n);
for (auto &prime : prime_factors)
    cout << prime << " ";
}
```

Prime Factorization using Sieve algorithm:

=> $O(\log(n))$

Ex: 50 => 2 5 5

```
vector<int> spf(N); // SPF : smallest prime factor
void sieve()      // =>  $O(n \log \log n)$ 
{
    for (int i = 1; i < N; i++) spf[i] = i;
    for (int i = 2; i * i < N; i++)
    {
        if (spf[i] == i)
        {
            for (int j = i * i; j < N; j += i)
                if (spf[j] == j) spf[j] = i;
        }
    }
}
int main()
{
    sieve();
    int n;
    cin >> n;
    while (n != 1)
    {
        cout << spf[n] << " ";
        n /= spf[n];
    }
}
```

Find N'th Fibonacci number using Binet's Formula:

=> $O(1)$

```
int fib(int n){
    double phi = (sqrt(5) + 1) / 2;
    return round(pow(phi, n) / sqrt(5));
}
```

Binary Exponentiation using Iterative method:

=> $O(\log(b))$.

Ex: $3^{13} \Rightarrow 3^{(8+4+0+1)} \Rightarrow 3^8 * 3^4 * 3^0 * 3^1 \Rightarrow 1594323; \rightarrow (a^b)$

const int Mod = 1e9 + 7;

long long BinExpIter(long long a, long long b)

```
{
    long long ans = 1;
    while (b)
    {
        if (b & 1)
        {
            ans = ans * a;
            // ans=(ans*a) % Mod;
        }
        a = a * a;
        // a=(a*a) % Mod;
        b >>= 1;
    }
    return ans;
}
```

Binary Exponentiation for $N^{1/x}$:

=> $O(x * \log(N * 10^d))$

$3^{1/5} = 1.2457312346;$

double **eps** = 1e-6; // eps=1e-**d**; =>with **d** decimal accuracy

double **BinExpPow** (double n, int x)

```
{
    double l = 0, r = n, m = (l + r) / 2;
    while (r - l > eps)
    {
        if (pow(m, x) > n) r = m;
        else l = m;
        m = (l + r) / 2;
    }
    return m;
}
```

Sum and Count of Divisor:

=> $O(\sqrt{n})$

Ex(sum): 20 => 22 (1+2+4+5+10+20). Ex(count): 20 => 6 (1,2,4,5,10,20).

int main()

```
{
    ll n, sum = 0, i, c = 0;
    cin >> n;
    for (i = 1; i * i <= n; i++)
    {
        if (n % i == 0)
        {
```

```
        sum += i, ++c;
        if (i != n / i) sum += n / i, ++c;
    }
}
cout << "Sum = " << sum << " Count = " << c << endl;
}
```

Number of divisors:

=> $O(n \log(n))$

Ex: 32 => 2 4 8 16 32

```
const int N = 1e5 + 10;
vector<int> divisor[N];
int main()
{
    for (int i = 2; i < N; i++)
    {
        for (int j = i; j < N; j += i)
            divisor[j].push_back(i);
    }
    int n; cin >> n;
    for (auto &it : divisor[n]) cout << it << " ";
    cout << endl;
}
```

Graph:

```
const int fx[] = {+0,+0,+1,-1,-1,+1,-1,+1}; // king's move (0 to 3 index => Side Moves)
const int fy[] = {-1,+1,+0,+0,+1,+1,-1,-1}; // king's move (4 to 7 index => Diagonal Moves)

const int kx[] = {-2,-2,-1,-1,+1,+1,+2,+2}; // knight's move
const int ky[] = {-1,+1,-2,+2,-2,+2,-1,+1}; // knight's move
```

Depth First Search(DFS):

=> $O(V+E)$

```
const ll N = 1e5 + 10;
vector<ll> g[N], height(N), depth(N);
bool vis[N];
int Par[N];

void dfs(ll vertex, ll par = -1)
{
    /** Take action on vertex after entering the vertex. ***/
    vis[vertex] = true;
    // bool isLoopExists = false;    //<= Use For Finding Cycle
    Par[vertex] = par;
    for (auto &child : g[vertex])
    {
        /** Take action on child before entering the child node. **/
        if (vis[child]) continue;
        dfs(child, vertex);
    }
}
```



```

/* => Use for Finding Cycle:
    if(vis[child] && child == par) continue;
    if(vis[child]) return true;
    isLoopExists |= dfs(child, vertex);
*/
/* => Use for Tree (No need Visited array):
    if(child == par) continue;
    depth[child] = depth[vertex]+1;
    dfs(child, vertex);
    height[vertex] = max(height[vertex], height[child]+1);
*/
/**/ Take action on child after exiting child node. ***/
}
/**/ Take action on vertex before exiting the vertex. ***/
}

```

Breadth-first search (BFS) And 0/1 BFS:

=> $O(V+E)$

```

const int N=1e5+10;
vector<int>g[N];          //vector<pair<int, int>> g[N]; =>For 0/1 BFS
bool vis[N];             // No need vis array for 0/1 BFS.
vector<int> level(N);     //vector<int> level(N, INT_MAX); =>For 0/1 BFS

```

```

void bfs(int source)
{
    queue<int>q;          //deque<int>q; =>For 0/1 BFS
    q.push(source);      //q.push_fornt(source); =>For 0/1 BFS
    vis[source]=1;       //level[source] = 0; =>For 0/1 BFS
    while(!q.empty())
    {
        int par=q.front();
        q.pop();          //q.pop_front(); =>For 0/1 BFS
        for(auto &child: g[par])
        {
            if(vis[child]) continue;
            q.push(child);
            vis[child]=1;
            level[child]=level[par]+1;

            /*=> For 0/1 BFS:
            int u = child.first, w = child.second ;
            if(level[par] + w < level[u])
            {
                level[u] = level[par] + w;
                if(w==0) q.push_front(u);
                else q.push_back(u);
            }
            */
        }
    }
}

```

```

    /*
    }
}
}

```

Dijkstra's Shortest Path Algorithm(Single Source Shortest Path):

```

const int N = 1e5 + 10, INF = 1e9 + 7;                                     => O((V+ E)*log(V))
vector<pair<int, int>> g[N]; //g[u].pb({v,w});
vector<int> dist(N, INF); //store minimum distance;
vector<bool> vis(N);

```

```

void dijkstra(int s)
{
    multiset<pair<int, int>> st;
    st.insert({0, s});
    dist[s] = 0;
    while (st.size())
    {
        int u = (st.begin())->second;
        // int u_w=(st.begin())->first;
        st.erase(st.begin());
        if (vis[u]) continue;
        vis[u] = 1;
        for (auto &child : g[u])
        {
            int v = child.first;
            int v_w = child.second;
            if (dist[u] + v_w < dist[v])
            {
                dist[v] = dist[u] + v_w;
                st.insert({dist[v], v});
            }
        }
    }
}

```

Floyd-Warshall Algorithm(All Pair Shortest Path):

=>O(n³)

=> finding the shortest paths in a weighted graph with positive or negative edge weights (but with **no negative cycles**);

```

const int N=510, INF=1e9+10;
int dp[N][N];
int n, m;
void floyd_warshall()
{
    for (int k = 1; k <= n; ++k)
    {

```

```

    for (int i = 1; i <= n; ++i)
    {
        for (int j = 1; j <= n; ++j)
        {
            if (dp[i][k] < INF && dp[k][j] < INF)
                dp[i][j] = min(dp[i][j], dp[i][k] + dp[k][j]);
        }
    }
}
int main()
{
    cin >> n >> m;
    for (int i = 1; i <= n; ++i)
    {
        for (int j = 1; j <= n; ++j)
        {
            if (i == j) dp[i][j] = 0;
            else dp[i][j] = INF;
        }
    }
    for (int i = 0; i < m; i++)
    {
        int x, y, wt; cin >> x >> y >> wt;
        dp[x][y] = wt;
    }
    floyd_warshall();
    return 0;
}

```

Others:

Sorting pair Using Compare Function:

=> $O(n \log(n))$

If `vector<pair<ll, ll>> vec` = {{3, 4}, {1, 2}, {3, 5}, {3, 2}, {6, 1}};

bool **cmp**(pair<ll, ll> a, pair<ll, ll> b)

```

{
    if (a.first != b.first) return a.first < b.first;    // => first value increasing order;
    return a.second > b.second;                        // => second value descending order;
}

```

sort(vec.begin(), vec.end(), **cmp**); // => **vec** = {{1,2}, {3,5}, {3,4}, {3,2}, {6,1}};

Minimum fraction:

If $a/b = c/d$ => ex: $12/18 = 2/3$

$c = a / _gcd(a,b); \quad d = b / _gcd(a,b);$

Count words in a string using stringstream:

```
#include<sstream>
#include<string>
int countWords(string str)
{
    stringstream sf(str);
    string word;
    int count = 0;
    while (sf >> word)
        count++;    // <= u can change statement
    return count;
}
```

Find SubString of a string:

=> $O(n^2)$

str = "abcd" => a, ab, abc, abcd, b, bc, bcd, c, cd, d.

```
for (int i = 0; i < str.length(); i++)
{
    string subStr;
    for (int j = i; j < str.length(); j++)
    {
        subStr += str[j];
        cout << subStr << endl;
    }
}
```

Find SubSequences / SubSet using Iterative:

=> $O(n * 2^n)$

{1, 2, 3} => {1}, {2}, {1, 2}, {3}, {2, 3}, {1, 2, 3}, {4}, {1, 4}, {2, 4}, ...

```
vector<vector<int>> subsets(vector<int> &nums)
{
    vector<vector<int>> allSubSets;
    int n = nums.size();
    ///=> In Bits SubSets, the nums array is which Bit position you want for SubSets;
    for (int i = 0; i < (1 << n); i++)    //for  $2^n$  possible solution
    {
        vector<int> subset;
        ///int tempA=a, tempB=b; ///=> for Bits SubSets
        for (int j = 0; j < n; j++)    //for nums array
        {
            if (i & (1 << j))
            {
                subset.push_back(nums[j]);
                ///tempA |= (1LL << nums[j]);    ///ON the nums[j] position Bit in tempA
            }
            ///else tempB |= (1LL << nums[j]);    ///ON the nums[j] position Bit in tempB
        }
        allSubSets.push_back(subset);
    }
}
```

```
    ///ans=max(ans, temA*tempB); //qn needed operation
}
return allSubSets;
}
```

Find SubSequences / SubSet using Recursion:

=> $O(n \cdot 2^n)$

s="abc" => **subsequences** = { "a", "b", "c", "ab", "bc", "ac", "abc"};

```
vector<string> subsequences;
void AllSubsequences(string &s, string subseq="", int index=0)
{
    if (index == s.length())
    {
        subsequences.push_back(subseq);
        return;
    }
    AllSubsequences(s, subseq, index + 1);
    AllSubsequences(s, subseq + s[index], index + 1);
}
```

Extended Euclid:

//=> $O(\log(\min(a, b)))$

For this Eq. **$(a \cdot x) + (b \cdot y) = \gcd(a, b)$** ;

```
ll extended_euclid(ll a, ll b, ll &x, ll &y)
{
    if (b == 0)
    {
        x = 1, y = 0;
        return a;
    }
    ll x1, y1;
    ll gcd = extended_euclid(b, a % b, x1, y1);
    x = y1;
    y = x1 - y1 * (a / b);
    return gcd;
}
```

- ◆ **Subarrays/Substring:** A subarray is a contiguous part of array and maintains relative ordering of elements. For an array/string of size n , there are $n*(n+1)/2$ non-empty subarrays/substrings. ["1234" => {1,2}, {1,2,3}, {2,3,4} etc.]
- ◆ **Subsequence:** A subsequence maintain relative ordering of elements but may or may not be a contiguous part of an array. For a sequence of size n , we can have $(2^n)-1$ non-empty subsequences in total. ["1234" => {1,2,4}, {2,4} etc.]
- ◆ **Subset:** A subset **MAY NOT** maintain relative ordering of elements and can or cannot be a contiguous part of an array. For a set of size n , we can have (2^n) sub-sets in total. ["1234" => {1,3,2}, {4,2,3} etc.]
- ◆ **Co-Prime:** That means a pair of numbers are said to be co-prime when they have their highest common factor as 1. [i.e: $\text{gcd}(A, B)=1$;]
- ◆ **Lexicographic or Lexicographically:** means sorting in the natural order / dictionary order. [Ex: "a" < "b"; "aa" < "ab"; "aaab" < "ab"; "abcd" < "baa";]
- ◆ **Parity:** is a term used to refer to the property of being even or odd.
- ◆ **Permutations:** are often used to count the **number of ways to arrange** a certain number of objects. The number of permutations of a set of n objects is given by $n!$.
- ◆ **MEX:** usually refers to the "minimum excluded value" of a set. Given a set of non-negative integers, the MEX is the smallest non-negative integer that is not present in the set. Ex: {0, 1, 3, 4, 7} => MEX is 2;