## DSA HW3 Report

Zhongze Tang (zt67)

Q1

In Line 7, you can change the number of random input. Then you will see the output of in-order traversal of this tree.

Q2

The experiment is based on the tree written in Q1.

The result is shown in the table:

N	Ave path len(ordered)	Ave path len(random)
1	1.0	1.0
2	1.5	1.5
4	2.5	2.225
8	4.5	3.165
16	8.5	4.188125
32	16.5	5.3846875
64	32.5	6.496875
128	64.5	8.089921875
256	128.5	9.2400390625
512	256.5	10.5942578125
1024	512.5	12.00736328125
2048	1024.5	13.3846533203125
4096	2048.5	14.75482177734375
8192	4096.5	16.236561279296875

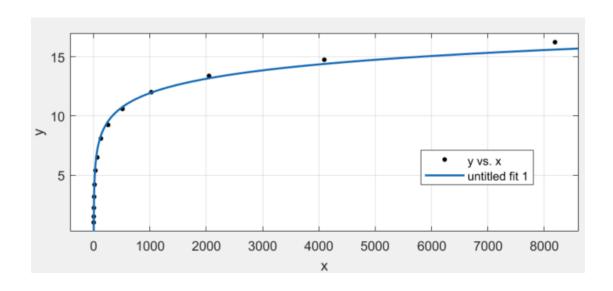
Adding the depths of all nodes, we get a quantity known as the internal path length of the tree. So, I use this formula to calculate the internal path length  $P_N$ :

$$P_N = N + P_L + P_R$$

where N is the size of Node P, and  $P_L$  and  $P_R$  are its two subtrees.

I use Curve Fitting Tool in MATLAB to fit the number and the average length (with random input), and the result is:

$$f(x) = 1.212*log2(x) - 0.1438$$



As for the ordered input,

the average path Length = (N / 2 + 0.5).

The curve fitting file is Q2/Q2curvefit.sfit.

## Q3

The results are:

Result of 10000 is: 0.25411100000000003

Result of 100000 is: 0.2539944

Result of 1000000 is: 0.25390362999999994

We can safely conclude that the average percentage of red nodes in a random-input red-black tree is 25.4%.

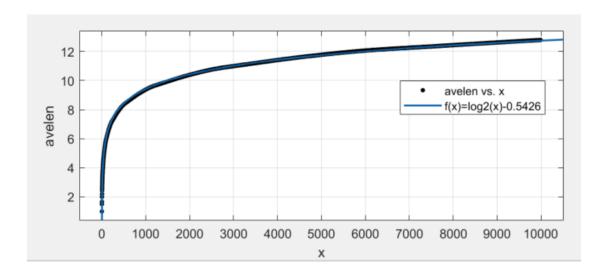
The code of Red-Black BST is from Algorithms book website.

## Q4

The calculation method of internal path length is the same in Q1.

I use Curve Fitting Tool in MATLAB to fit the number and the average length, and the result is:

$$f(x) = \log 2(x) - 0.5426$$



At the same time, the standard deviation is quite small, and its average value is 0.077.

All the results are stored in Q4/result.csv, and the curve fitting file is Q4/curvefit.sfit. The code of Red-Black BST is from *Algorithms* book website.

Note that it took almost 3 hours on my computer (i7-4710MQ, 8G RAM) to work out all the results.

## Q5

- (i) The value of select(7) is 8.
- (ii) The value of rank(7) is 6.