Professor Khan

Stock Simulation Final Report

Due: 4/29/2024

Introduction:

In this project, our original goal was to gain a deeper understanding of the factors that influence stock prices. Then, use that knowledge to develop a simulation in R that simulates/predicts the stock market through statistical analysis and techniques. Through the development and creation of our simulation, we hoped to both gain insight into the stock market and further our knowledge of simulation in R.

By analyzing the impact factors such as company performance, industry trends, and interest rate, we want to understand how these factors can influence shaping the a stock's price over time. A crucial aspect of our project is identifying and understanding the variables that affect stock prices, like volatility, drift, and interest rates. In order to accurately simulate the market we would have to develop a deep understanding of how each of these variables affects a stock's price. We would then have to both extract/calculate their values from historical data and recreate their effect through statistical techniques to predict future prices. To this end, we'd have to learn how to use packages and datasets to make our simulation realistic and be able to predict prices with a degree of accuracy. Finally, we would have to learn how to then use our simulated stock price data as a resource to make investment decisions.

Model and Simulation:

Our model has two primary components/functions, one goes back in time "n" trading days and simulates the prices of a specified stock throughout said days, comparing the simulated prices to the actual prices. The other function starts from the current date and predicts the stock for "n" days in the future. The parameters for both functions are; symbol (the symbol of the stock that they want to simulate ex. Amazon = "AMZN"), days (the number of trading days the simulation will run for, defaults to 30), paths (the number of times the stock will be simulated, defaults to 10), and interest_rate (allows the user to input a hypothetical market interest rate, defaults to last recorded market interest rate).

The base for both of our models uses a geometric Brownian motion function for predicting and simulating stock prices based on the drift and volatility of the stock. To get the data required, our model downloads historical data of a given stock. It then uses the historical data to find the daily returns and the initial price for the stock at the start of the simulation period, based on the daily closing prices. Next, it uses the returns to calculate the drift and volatility of the stock. The drift, volatility, and initial price are then run through the geometric Brownian motion function to get the predicted stock prices.

In total, our model has four functions and uses one package. The package we use is called "quantmod", and it is what allows us to download historical data of both stocks and interest rates, along with helping perform some of the analysis with its dailyReturns() and volatility() methods. The first two functions our model uses are the components mentioned earlier, Stock.Simulator() which compares our predicted stock prices to the real prices for "n" trading days in the past to

the present and Future.Stock.Simulator() which simulates future stock prices for "n" trading days in the future. Both these functions download and extract the needed data but then use the other two functions, gbm.f() and Simulated.Prices(), to actually predict/simulate the stock.

The gbm.f() function, takes an initial price, drift and volatility of a stock, and using geometric Brownian motion, it generates predicted stock prices for "n" trading days from the initial price. The second function Simulated.Prices() creates and returns a matrix, with each column of the matrix holding a separate realization for the stock prices over the "n" trading days. It takes a "paths" parameter which determines how many columns or different realizations for the stock it will simulate. It then loops through code "paths" times using the gbm.f() function to generate a single path/realization for the stock and finally appends said path to the matrix

Features and Assumptions:

Some other feature that our model has that makes it stand out from other models are how it calculates the volatility, the incorporation of interest rates on drift, and the random chance that volatility will double. In the process of making and testing our model, we noticed that when compared to the path the actual stocks were taking, our simulated stock paths appeared to have a lower volatility. At the time we were calculating the volatility as the standard deviation of the returns. We decided to do some research and experiment with different ways of calculating the volatility, during which we found the built-in volatility function in "quantmod". The problem with this function is that after testing it extensively it kept returning a value that appeared to be larger than the actual volatility. Seeing this we decided to find the mean or average of these two values and use that as the volatility, and though this solution seemed quite simple, it worked surprisingly well and when tested returned the best results.

Another feature our model has is its incorporation of interest rates. Our model downloads historical data of the interest rates leading up to the starting date of the simulation and compares the average interest rate over the entire period leading up to the start date to the interest rate on the start date. This difference will represent how the interest rates are currently changing and we then use said difference to adjust the drift of our stock accordingly. If the interest rates are currently dropping then the difference will be positive, if the interest rates are rising the difference will be negative. To use this number to adjust the drift we divide it by a thousand to mediate its impact as the drift is already a very small number, and then add it to the drift. If the user enters a custom interest rate then the model will use that interest rate at the current or latest interest rate.

The final feature of our model is the random one-in-a-thousand-chance that the volatility will double for a realization of the stock. This feature is implemented inside of the Simulated.Prices() function right before a realization/path of stock is created there is a 0.1% chance that the volatility double for that path. This simulates the true randomness of the stock market as an event could occur at any time that drastically affects either a particular stock or the entire stock market. Events like natural disasters, war, recession, or good events like breakthroughs, all of these events can have a drastic impact on stock prices over a short period of time. With this in consideration and the fact that the stock market tends to be a very volatile and

hard to predict place, having a small chance of the stock volatility going up is more realistic than not.

The main assumption that our model makes is that the historical data of the market leading up to the start of the simulation is a good representation of how the market will play out during the simulated time period. In addition to this, it assumes that what we are getting for the calculated drift and volatility of the stock is accurate to the actual drift and volatility. Though our numbers have appeared to be relatively what the real drift and volatility are, they are still just predicted calculations made based on the historical data of the stock.

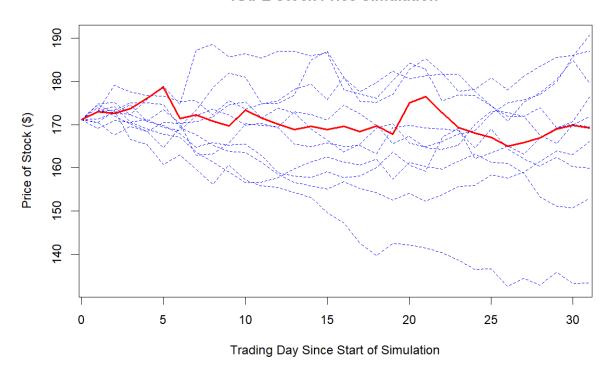
Analysis and Discussion:

Our model takes in historical stock price and interest rate data from a relevant time frame for the period our simulation is running. It then extracts the daily closing prices of the stock from said data, taking the last closing price as the initial price of the stock. Then, our model calculates the daily returns of the stock from the closing prices using quantmod's dailyReturn() function. The daily returns are the percentage change of the stock on a given day and are what we use to calculate the volatility and drift of the stock. We have already discussed how to find volatility, as for the drift it is as simple as finding the average daily returns using the mean() function. The drift is then adjusted according to the interest rate as stated before.

After our model gets the drift, volatility, and initial price of a stock, it then makes use of our geometric Brownian motion function to simulate future stock prices. This function works by first creating a sequence/vector of "n + 1" time steps, n being the number of trading days our simulation runs and a time step being one trading day. This sequence represents the time points at which the stock price will be simulated. Then, the function calculates "dt" or the change in time/size of a time step, which will be one trading day divided by the total length of our simulation. Next, the function generates a vector of Brownian motion random variables, which is essentially a random positive or negative number that simulates the random fluctuation of a stock's price over time. It generates the vector using rnorm() to generate "n + 1" random normally distributed numbers with a standard deviation of one and a mean of zero. It then takes the cumulative sum of these values as the change in the stock's price will carry over to the next day. The vector is then multiplied by the square root of "dt" to scale the values appropriately. Finally, the function uses the geometric Brownian motion formula to generate future stock prices. This formula incorporates the drift (mu), volatility (sigma), initial price (s0), time sequence (t.s), and the Brownian motion variable (Bt) in order to model the stock's price motion over time.

When running our Stock.Simulator() component of our model on default settings (days = 30, paths = 10, interest_rate = NULL) and passing Appl's symbol or "AAPL". Using historical data from before to the last thirty days to simulate the stock's price over the last thirty days and then compare that to the actual price trajectory. The simulated prices are represented by the dotted blue lines and the real stock is represented by the solid red line. In addition to making this graph, it returns a table of all the simulated prices and the real closing prices over the simulated time period.

AAPL Stock Price Simulation

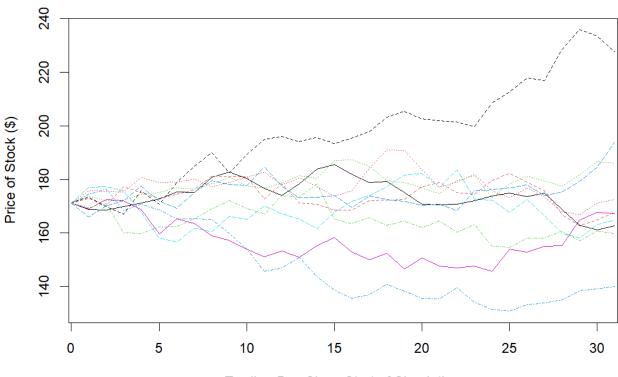


| ^ | sim_prices | sim_prices.1 | sim_prices.2 | sim_prices.3 | sim_prices.4 | sim_prices.5 | sim_prices.6 | sim_prices.7 | sim_prices.8 | sim_prices.9 | AAPL.Close |
|------------|------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|------------|
| 2024-03-13 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.13 |
| 2024-03-14 | 169.0652 | 173.9376 | 172.9571 | 173.0913 | 170.4814 | 173.1625 | 174.5780 | 174.8340 | 171.2765 | 170.5188 | 173.00 |
| 2024-03-15 | 170.8739 | 172.0221 | 173.3671 | 179.2056 | 173.1979 | 174.2305 | 172.6288 | 175.1232 | 172.7449 | 167.6036 | 172.62 |
| 2024-03-18 | 170.5781 | 170.1768 | 175.0848 | 177.5837 | 166.5897 | 170.5659 | 172.4444 | 172.3017 | 174.5439 | 169.6149 | 173.72 |
| 2024-03-19 | 171.2141 | 168.4379 | 175.0554 | 176.7984 | 165.3839 | 168.9396 | 175.8420 | 170.8440 | 170.6786 | 168.3825 | 176.08 |
| 2024-03-20 | 169.3911 | 170.4982 | 174.6237 | 176.6235 | 160.7588 | 167.7498 | 178.9047 | 173.4593 | 169.7896 | 164.5867 | 178.67 |
| 2024-03-21 | 168.6318 | 170.3362 | 169.5872 | 175.3828 | 162.9166 | 167.0735 | 174.7393 | 170.3859 | 167.9232 | 169.3449 | 171.37 |
| 2024-03-22 | 171.9621 | 170.7450 | 173.3014 | 175.5730 | 159.6416 | 163.7093 | 187.2083 | 162.9868 | 164.7680 | 167.6380 | 172.28 |
| 2024-03-25 | 173.5894 | 171.7694 | 178.5243 | 172.2740 | 156.1775 | 161.3992 | 188.6436 | 163.1890 | 165.8513 | 165.2336 | 170.85 |
| 2024-03-26 | 172.3021 | 174.6175 | 181.9731 | 175.5270 | 160.6213 | 159.0315 | 185.7235 | 165.7330 | 165.2869 | 163.8005 | 169.71 |
| 2024-03-27 | 169.8025 | 175.2463 | 181.0089 | 173.5639 | 157.1400 | 156.5925 | 186.4322 | 170.2404 | 165.4835 | 163.5682 | 173.31 |
| 2024-03-28 | 170.2725 | 171.4900 | 174.9659 | 174.8293 | 155.8247 | 156.6365 | 185.4247 | 169.8370 | 162.7834 | 161.2585 | 171.48 |
| 2024-04-01 | 169.2106 | 173.8071 | 174.9148 | 175.4883 | 155.4487 | 157.8057 | 187.0302 | 169.4329 | 158.7922 | 158.4477 | 170.03 |
| 2024-04-02 | 165.5357 | 172.7608 | 176.9099 | 178.1529 | 154.1875 | 159.7451 | 187.0482 | 173.0002 | 158.1563 | 156.6671 | 168.84 |
| 2024-04-03 | 164.8536 | 169.0576 | 184.9595 | 179.4449 | 153.1351 | 161.3909 | 185.8801 | 172.4286 | 157.8058 | 155.7692 | 169.65 |
| 2024-04-04 | 165.7674 | 166.4864 | 187.0302 | 175.7454 | 149.5842 | 162.4801 | 186.6904 | 171.0637 | 159.0277 | 155.1469 | 168.82 |
| 2024-04-05 | 165.0527 | 163.6479 | 180.9591 | 180.9364 | 147.1944 | 161.3319 | 178.0220 | 174.5600 | 157.7144 | 156.8127 | 169.58 |
| 2024-04-08 | 165.1257 | 165.4342 | 177.5829 | 175.4437 | 142.4673 | 160.5982 | 177.0577 | 172.5286 | 158.1247 | 155.2098 | 168.45 |
| 2024-04-09 | 163.3421 | 169.2821 | 179.7049 | 175.1174 | 139.5623 | 161.9433 | 176.1118 | 169.8797 | 160.0225 | 154.2515 | 169.67 |
| 2024-04-10 | 169.3178 | 170.1535 | 182.4088 | 176.9750 | 142.5376 | 157.4424 | 180.2988 | 165.5625 | 163.6936 | 152.5502 | 167.78 |
| 2024-04-11 | 169.8763 | 165.6973 | 180.6330 | 182.8467 | 142.1490 | 161.2473 | 184.2338 | 167.3588 | 160.6789 | 154.1304 | 175.04 |
| 2024-04-12 | 169.1970 | 164.8298 | 181.3741 | 185.3121 | 141.4730 | 160.2599 | 182.8682 | 164.6513 | 159.2390 | 152.3398 | 176.55 |
| 2024-04-15 | 168.9663 | 166.0558 | 181.6704 | 181.9817 | 140.3744 | 159.7180 | 175.5492 | 164.2752 | 167.0102 | 153.7360 | 172.69 |
| 2024-04-16 | 168.6387 | 167.8463 | 181.7526 | 177.7146 | 138.6974 | 161.5533 | 176.8534 | 165.2705 | 169.0924 | 155.7054 | 169.38 |
| 2024-04-17 | 164.6348 | 168.6340 | 177.7563 | 178.2452 | 136.3998 | 163.2212 | 176.7585 | 170.1070 | 162.1447 | 155.9127 | 168.00 |
| 2024-04-18 | 168.9405 | 172.4874 | 174.4242 | 180.7975 | 136.5934 | 161.2898 | 174.2887 | 173.0619 | 163.4644 | 158.3172 | 167.04 |
| 2024-04-19 | 164.4243 | 175.0217 | 170.7666 | 178.0321 | 132.4290 | 161.0720 | 171.9123 | 172.8635 | 164.9635 | 157.6102 | 165.00 |
| 2024-04-22 | 162.1225 | 175.7779 | 175.1854 | 181.2151 | 134.3634 | 158.6746 | 171.9317 | 171.9534 | 163.2396 | 158.9011 | 165.84 |
| 2024-04-23 | 160.4366 | 176.9963 | 177.3082 | 183.4834 | 132.8369 | 153.2504 | 173.9620 | 167.5220 | 166.9553 | 161.4631 | 166.90 |
| 2024-04-24 | 162.4914 | 179.8988 | 180.4889 | 185.6197 | 135.8553 | 151.1267 | 169.2881 | 165.5747 | 169.1908 | 163.9744 | 169.02 |
| 2024-04-25 | 160.2369 | 185.6746 | 184.9446 | 186.1068 | 133.2228 | 150.7341 | 170.0411 | 169.9242 | 170.6686 | 163.0675 | 169.89 |
| 2024-04-26 | 159.9656 | 190.7864 | 179.6347 | 187.0335 | 133.3494 | 152.8544 | 169.5184 | 171.8321 | 176.4188 | 166.1007 | 169.30 |

From this data, we can get an idea of the accuracy of our prediction model. In the process of making our project, creating this component of our model was an instrument for fine-tuning our model to be more accurate. For example, it is what allowed us to see that our volatility wasn't very accurate and make adjustments to how we went about calculating it. Overall it was an essential step in creating an effective model and if we were to continue this project and try to make our predictions even more accurate it would continue to assist us.

When running our other component Future.Stock.Simulator() on default settings (days = 30, paths = 10, interest_rate = NULL) and passing Appl's symbol or "AAPL". Using historical data from the previous thirty days to simulate the stock's price over the next thirty days. In this graph, each line represents a simulated stock price, and in each column of the corresponding table is the prices of a simulated path over the simulation period.

AAPL Stock Price Simulation



Trading Day Since Start of Simulation

| • | V1 [‡] | V2 [‡] | V3 [‡] | V4 [‡] | V5 [‡] | V6 [‡] | V7 [‡] | V8 [‡] | V9 [‡] | V10 [‡] |
|----|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|------------------|
| 1 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 | 171.1300 |
| 2 | 168.8558 | 173.0021 | 173.8398 | 174.3944 | 177.1684 | 168.9499 | 173.3688 | 175.8895 | 169.4640 | 166.0909 |
| 3 | 168.6548 | 170.2672 | 171.9971 | 176.3586 | 177.3373 | 172.5360 | 169.9910 | 175.5674 | 171.0636 | 170.1674 |
| 4 | 169.8118 | 177.2517 | 172.3375 | 168.2971 | 175.7983 | 172.0229 | 166.9715 | 175.4618 | 160.0638 | 172.0431 |
| 5 | 171.2043 | 175.2464 | 174.5069 | 170.8763 | 167.6288 | 168.8070 | 175.7599 | 180.8063 | 159.8495 | 177.5572 |
| 6 | 172.7946 | 173.0708 | 175.1274 | 168.6127 | 158.1191 | 159.7146 | 170.8572 | 178.9071 | 162.3478 | 171.9156 |
| 7 | 175.4338 | 174.4684 | 176.8841 | 165.4376 | 156.6686 | 165.4302 | 178.7904 | 179.0288 | 162.5057 | 169.3024 |
| 8 | 175.1076 | 176.3271 | 176.3908 | 165.2953 | 161.9353 | 163.6015 | 184.9655 | 180.1897 | 165.3443 | 175.0344 |
| 9 | 180.7673 | 181.1538 | 178.3109 | 165.1929 | 160.5886 | 158.9047 | 189.8695 | 177.3534 | 169.1240 | 179.5814 |
| 10 | 182.7623 | 180.9848 | 180.9018 | 159.8757 | 166.2066 | 157.2302 | 182.5488 | 178.8075 | 172.1353 | 178.2949 |
| 11 | 180.3326 | 180.9785 | 177.4591 | 153.9786 | 165.0895 | 154.0709 | 189.2357 | 181.0464 | 169.2712 | 177.7554 |
| 12 | 176.6663 | 172.7320 | 176.8573 | 145.7602 | 170.1657 | 151.1173 | 195.0085 | 182.6908 | 167.0932 | 184.8072 |
| 13 | 174.0511 | 178.4121 | 178.7040 | 147.0262 | 167.3157 | 153.4421 | 196.0958 | 177.8850 | 174.1008 | 177.5880 |
| 14 | 178.3604 | 171.2170 | 181.5382 | 150.8872 | 165.2277 | 151.0502 | 194.0187 | 180.5840 | 173.3436 | 173.1472 |
| 15 | 183.9687 | 170.7386 | 180.3166 | 143.8607 | 161.7180 | 155.2209 | 195.6510 | 177.2683 | 178.5199 | 173.4040 |
| 16 | 185.6689 | 168.6398 | 187.0647 | 138.6360 | 167.8131 | 158.4109 | 193.4662 | 173.8204 | 165.1689 | 173.9521 |
| 17 | 181.8944 | 168.6617 | 187.2550 | 135.6801 | 171.9663 | 152.8930 | 195.4831 | 175.7262 | 163.5140 | 169.3803 |
| 18 | 178.9182 | 172.1424 | 185.0218 | 137.0835 | 174.0022 | 150.0581 | 197.9125 | 184.3221 | 165.6722 | 173.9052 |
| 19 | 179.3281 | 172.3464 | 179.5444 | 140.9471 | 177.3565 | 152.3834 | 203.2474 | 191.1092 | 162.9393 | 172.6265 |
| 20 | 175.2152 | 172.4221 | 178.8485 | 138.3332 | 181.7575 | 146.5327 | 205.3408 | 190.9064 | 164.3844 | 171.8981 |
| 21 | 170.8315 | 177.3576 | 176.9892 | 135.7574 | 182.3453 | 150.7851 | 202.6145 | 183.7193 | 162.0604 | 170.2413 |
| 22 | 170.5837 | 178.7514 | 174.7312 | 135.3947 | 177.0906 | 147.6347 | 201.8566 | 177.1278 | 164.3998 | 170.8840 |
| 23 | 170.8416 | 175.0382 | 179.8109 | 139.5736 | 183.5584 | 147.1117 | 201.6137 | 178.9639 | 160.3048 | 168.3360 |
| 24 | 172.0925 | 174.5314 | 181.4851 | 134.2645 | 172.8361 | 147.6758 | 199.8302 | 181.9963 | 163.1270 | 175.7731 |
| 25 | 173.8543 | 179.5807 | 173.2315 | 131.4668 | 172.4103 | 145.6995 | 208.4967 | 175.8526 | 155.0744 | 176.1441 |
| 26 | 174.8937 | 182.2947 | 178.4663 | 130.8210 | 167.8293 | 154.0263 | 212.6877 | 173.2350 | 154.6040 | 176.8507 |
| 27 | 173.6444 | 179.1429 | 181.2885 | 133.3189 | 172.4928 | 152.8887 | 217.8503 | 176.9141 | 158.2442 | 178.0295 |
| 28 | 174.9016 | 175.8433 | 179.5939 | 133.8484 | 166.3779 | 155.0746 | 217.0933 | 173.3950 | 158.0898 | 173.9886 |
| 29 | 168.9174 | 166.8920 | 177.4594 | 135.0128 | 159.9736 | 155.2412 | 228.4824 | 167.9595 | 160.8419 | 175.2739 |
| 30 | 162.8374 | 162.8075 | 181.6688 | 138.4431 | 158.1762 | 164.9839 | 235.9862 | 166.8570 | 156.9555 | 179.2914 |
| 31 | 161.2420 | 164.9318 | 186.5953 | 139.0851 | 163.1401 | 167.6498 | 233.6671 | 171.3226 | 160.7493 | 184.5347 |
| 32 | 162.7513 | 167.7293 | 186.0311 | 139.9539 | 164.9311 | 167.1887 | 227.6469 | 172.6248 | 159.8634 | 193.8667 |

Based on these simulated prices, we can look at the average ending price to determine if we think the stock is going to go up or down. The level of accuracy of this prediction can be obtained from our other function from before. In this case, I would conclude that the stock price of Apple will go down slightly over the next thirty days.

Questions and Answers:

When coming into this project neither of us had any real idea about how the stock market functioned other than that prices go up-and-down over time. We didn't know the factors that influenced a stock's price and we wanted to both learn about these factors and how we could then use them to predict future prices. We wanted to learn about various trading strategies, and based on our simulation what we would think to work the best, effectively using our simulation to make investment decisions. We ultimately wanted to gain a deeper understanding of the stock market and be able to predict future stock prices with some level of confidence. In addition to learning about the stock market, we wanted to learn and develop our simulation skills, which would have to in order to be able to accurately simulate a stock's price.

Through the completion of this project, I would say we answered all these questions and more. We now have extensive knowledge about factors that influence a stock's price, like company performance and interest rates. We also know the variables that are used to quantify a stock's trajectory, volatility and drift. Along with how to both calculate them based on past stock performance and then use them to predict future prices. During the extensive tests that we performed on our simulation using a multitude of different stocks, we concluded that in most cases making your investment choices based on the overall current drift of a stock while taking into account the current interest rate is usually the best choice when investing. In contrast to trying to day trade and make a profit off of a stock's volatility which is too random to try and account for. In addition to gaining a deeper understanding of the stock market and its movement, we also learned quite a bit about simulation and statistical analysis. We learned about geometric Brownian motion and how to build a function to simulate it in R. We how to use packages(quatmod) and online datasets(stock data) in R and how to then extract what we need from said datasets using said packages. In addition to this, we had to learn more about graphing in R by constructing and plotting matrices. Overall, through the project's development, we were able to address our initial questions while also uncovering additional questions that emerged throughout the process.

Conclusion:

In conclusion, our research aimed to deepen our understanding of the stock market and develop a simulation in R for predicting stock behavior. We analyzed factors such as company performance, industry trends, and interest rates to comprehend their impact on stock prices and figure out a way to simulate them. We developed functions to simulate past and future stock prices using historical data of the stock and the geometric Brownian motion formula. Throughout the project, we refined our model using our Stock.Simulator() function that compared our

simulated prices to the real price of a stock. This allowed us to fine-tune aspects of our model like our volatility calculations and the incorporation of interest rates on drift.

Initially, we were unfamiliar with the stock market mechanisms, but despite that, we were able to gain extensive knowledge about factors affecting stock prices and simulation techniques. Ultimately, we were able to learn extensively about how the stock market functions and learned applicable knowledge like that buying-and-holding onto a stock that has a positive long-term drift is much safer and wiser than trying to buy and sell when a stock randomly fluctuates. This research not only addressed your initial inquiries but also expanded our understanding of the stock market and simulation methodologies.

In addition, throughout the creation of this project, we ended up running into some limitations. This included having more ideas for our model that we were unable to implement/ more questions that we were unable to answer in the given time frame for the project. One thing that we would be interested in implementing, if we were to continue the development of this project, is having an average path or endpoint of all simulated paths to give an overall idea of if it would be wise to invest in the stock. Another implementation that we think could have been useful would be to quantify or compute the accuracy of our predictions when we compare our simulated paths to the real path of a stock. In addition to these implementations, we also would like to have answered questions like what drift/ volatility would make a stock considered a worthy investment. This question would combine aspects like the stock's current trajectory versus the entire market. Overall, though there were some questions that we might be leaving unanswered and implementations not implemented, we are quite satisfied with our final product and can confidently say that we exceeded what we initially sought to do. This is especially prevalent when looking back at our first meeting where we had no clue on how we would even start this project or what it would entail.

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Appendix: R Code
install.packages('quantmod')
library(quantmod)
# Simulate stock prices, then plots and returns said simulates prices against the real prices
# symbol - symbol of stock
# days - trading days of simulation
# paths - number of simulated realizations of stock
# interest rate - Allows user to enter custom interest rate.
            defaults to true interest rate at start of simulation
Stock.Simulator <- function(symbol, days = 30, paths = 10, interest_rate = NULL) {
 # downloads historical prices for double the amount of trading days we're
 # simulating + 10(min amount of data for training), takes double since
 # it'll be split for training data
 getSymbols(symbol, from = Sys.Date() - 2.91*(days) - 10)
 # Gets closing values for stock
 closings <- Cl(get(symbol))
 # separates test and training data based on # of simulation days
 closing_train <- closings[1:(length(closings) - days)]</pre>
 closing_test <- closings[(length(closings) - days - 1):length(closings)]</pre>
 # Calculates daily returns
 returns <- dailyReturn(closing train)
 # Calculates volatility based on last 30 days(tested for a while and this way gave best results)
 vol <- mean(c((as.numeric(tail(volatility(closing_train, n = days), 1))), sd(returns)))
 # Calculates drift
 drift <- mean(returns)</pre>
```

```
# downloads historical treasury interest rate data,
 interest_rates <- getSymbols("DGS10", src = "FRED",
                    from = Sys.Date() - 6*(days) - 10, auto.assign = FALSE)
 # sections off the interest rate data so we are only using data from before start of simulation
 interest rates <- interest rates[1:(length(interest rates) - days)]
 # checks if user inputted custom interest rate
 if (is.null(interest_rate)) {
  # Calculates last interest rate
  latest interest rate <- as.numeric(tail(interest rates, 1))
 } else {
  latest interest rate <- interest rate
 }
 # Calculates mean of past interest rates
 mean_interest_rate <- mean(interest_rates, na.rm = TRUE)
 # finds difference for avg interest rate vs current rate
 cur rate diff <- mean interest rate - latest interest rate
 # adjusts drift to account for current interest rate
 drift <- drift + (cur_rate_diff/1000)
 # gets last price of stock
 init_price <- as.numeric(closings[(length(closings) - days - 1)])</pre>
 # gets simulated prices
 sim_prices <- Simulated.Prices(drift, vol, init_price, days, paths)</pre>
 # adds real prices to matrix
 sim_prices_and_real <- cbind(sim_prices, closing_test)</pre>
 # plots simulated stock prices(dotted blue) vs real prices(bold red)
 matplot(c(0:(days + 1)), sim_prices_and_real, type = "I",
      xlab = "Trading Day Since Start of Simulation",
      ylab = "Price of Stock ($)",
      xlim = c(1, days),
      main = paste(symbol, "Stock Price Simulation"),
      col = c(rep("blue", paths), "red"),
      Ity = c(rep(2, paths), 1),
      lwd = c(rep(1, paths), 2))
 return (sim prices and real)
}
#test
apple table <- Stock.Simulator("MSFT", days = 20, paths = 30)
```

```
# Simulates and plots/returns future stock prices
# symbol - symbol of stock
# days - trading days of simulation
# paths - number of simulated realizations of stock
# interest rate - Allows user to enter custom interest rate.
            defaults to true interest rate at start of simulation
Future.Stock.Simulator <- function(symbol, days = 30, paths = 10, interest_rate = NULL) {
 # downloads historical prices based on the amount of trading days we're
 # simulating + 10(min amount of data for training)
 getSymbols(symbol, from = Sys.Date() - 1.45*(days) - 10)
 # Gets closing values for stock
 closings <- Cl(get(symbol))
 # Calculates daily returns
 returns <- dailyReturn(closings)
 # Calculates volatility based on last 30 days(tested for a while and this way gave best results)
 vol <- mean(c((as.numeric(tail(volatility(closings, n = days), 1))), sd(returns)))
 # Calculates mean return (drift)
 drift <- mean(returns)</pre>
 # downloads historical treasury interest rate data
 interest_rates <- getSymbols("DGS10", src = "FRED",
                    from = Sys.Date() - 3*(days) - 10, auto.assign = FALSE)
 # checks if user inputted custom interest rate
 if (is.null(interest rate)) {
  # Calculates last interest rate
  latest_interest_rate <- as.numeric(tail(interest_rates, 1))
 } else {
  latest interest rate <- interest rate
 }
 # Calculates mean of past interest rates
 mean interest rate <- mean(interest rates, na.rm = TRUE)
 # finds difference for avg interest rate vs current rate
 cur_rate_diff <- mean_interest_rate - latest_interest_rate
 # adjusts drift to account for current interest rate
 drift <- drift + (cur rate diff/1000)
 # gets last price of stock
 init_price <- as.numeric(closings[(length(closings) - days - 1)])</pre>
 # gets simulated prices
 sim_prices <- Simulated.Prices(drift, vol, init_price, days, paths)
```

```
# plots simulated stock prices
 matplot(c(0:(days + 1)), sim_prices, type = "I",
      xlab = "Trading Day Since Start of Simulation",
      ylab = "Price of Stock ($)",
      xlim = c(1, days),
      main = paste(symbol, "Stock Price Simulation"))
 return (sim prices)
}
#test
future_apple_table <- Future.Stock.Simulator("AAPL")</pre>
# Simulates multiple price paths and store them in a matrix and returns said matrix
# drift - drift of the stock
# vol - volatility of the stock
# init_price - initial price of the stock
# days - trading days of simulation
# paths - number of simulated realizations of stock
Simulated.Prices <- function(drift, vol, init_price, days = 30, paths = 10) {
 # creates matrix to hold all possible realizations
 sim_price_matrix <- matrix(0, nrow = days + 2, ncol = paths)
 for (i in 0:paths) {
  # Unexpected event(1 in a 1000) making volatility double
  if (runif(1) < .001) {
   vol <- vol*2
  }
  # Uses GBM function to generate new stock prices
  sim_price <- c(init_price ,gbm.f(n = days, s0 = init_price, mu = drift, sigma = vol))
  # appends matrix to hold new path stock could take
  sim price matrix[,i] <- sim price
 return (sim_price_matrix)
# Source: Stat Legend - https://www.youtube.com/watch?v=ZIRxkD6SOLQ
# Geometric Brownian Motion Stock Price Simulator
# n - end time
# s0 - init price
# mu - drift
# sigma - volatility
gbm.f <- function(n, s0, mu, sigma) {
 #Get a time horizon, 1 day
```

```
t <- 1

# time step, makes sequence from 0 to end time by time horizon
t.s <- seq(0,t,length=n+1)

# change in time
dt <- t/n

# generating Brownian random variable
Bt <- sqrt(dt)*cumsum(rnorm((n+1),0,1))

# Uses GBM formula to generate future stock prices
St <- s0*exp((mu-sigma^2/2)*t.s+sigma*Bt)

return (St)
}</pre>
```