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```

1 Basic

1.1 .vimrc

1.2 IncreaseStackSize

```
//stack resize
asm( "mov %0,%%esp\n" ::"g"(mem+10000000) );
//change esp to rsp if 64-bit system

//stack resize (linux)
#include <sys/resource.h>
void increase_stack_size() {
   const rlim_t ks = 64*1024*1024;
   struct rlimit rl;
   int res=getrlimit(RLIMIT_STACK, &rl);
   if(res==0) {
      if(rl.rlim_cur<ks) {
        rl.rlim_cur=ks;
        res=setrlimit(RLIMIT_STACK, &rl);
   }
   }
}</pre>
```

1.3 Default Code

```
#include<bits/stdc++.h>
#include<unistd.h>
using namespace std;
#define FZ(n) memset((n),0,sizeof(n))
#define FMO(n) memset((n),-1,sizeof(n))
#define F first
#define S second
#define PB push_back
#define ALL(x) begin(x),end(x)
#define SZ(x) ((int)(x).size())
#define IOS ios_base::sync_with_stdio(0); cin.tie(0)
template<typename A, typename B>
ostream& operator <<(ostream &s, const pair<A,B> &p) {
  return s<<"("<<p.first<<","<<p.second<<")";</pre>
template<typename T>
ostream& operator <<(ostream &s, const vector<T> &c) {
  for (auto it : c) s << it << " ";</pre>
  s<<"]";
  return s;
// Let's Fight!
int main() {
    return 0:
}
```

2 Data Structure

2.1 Bigint

```
struct Bigint{
 static const int LEN = 60;
 static const int BIGMOD = 10000;
  int s;
 int vl, v[LEN];
  // vector<int> v;
 Bigint() : s(1) { vl = 0; }
 Bigint(long long a) {
   s = 1; vl = 0;
   if (a < 0) { s = -1; a = -a; }
   while (a) {
      push_back(a % BIGMOD);
      a /= BIGMOD;
 Bigint(string str) {
   s = 1; vl = 0;
   int stPos = 0, num = 0;
    if (!str.empty() && str[0] == '-') {
      stPos = 1;
      s = -1;
   for (int i=SZ(str)-1, q=1; i>=stPos; i--) {
  num += (str[i] - '0') * q;
      if ((q *= 10) >= BIGMOD) {
        push_back(num);
        num = 0; q = 1;
    if (num) push_back(num);
 7
  int len() const {
   return vl:
         return SZ(v);
 bool empty() const { return len() == 0; }
  void push_back(int x) {
   v[vl++] = x;
         v.PB(x);
 void pop_back() {
   vl--;
        v.pop_back();
  int back() const {
   return v[vl-1];
         return v.back();
 void n() {
   while (!empty() && !back()) pop_back();
 void resize(int nl) {
   vl = nl;
   fill(v, v+vl, 0);
   //
         v.resize(nl):
          fill(ALL(v), 0);
 void print() const {
   if (empty()) { putchar('0'); return; }
   if (s == -1) putchar('-');
   printf("%d", back());
    for (int i=len()-2; i>=0; i--) printf("%.4d",v[i]);
 friend std::ostream& operator << (std::ostream& out,</pre>
     const Bigint &a) {
    if (a.empty()) { out << "0"; return out; }</pre>
   if (a.s == -1) out << "-";</pre>
    out << a.back();
    for (int i=a.len()-2; i>=0; i--) {
     char str[10];
      snprintf(str, 5, "%.4d", a.v[i]);
      out << str:
```

```
return out:
int cp3(const Bigint &b)const {
  if (s != b.s) return s > b.s;
  if (s == -1) return -(-*this).cp3(-b);
  if (len() != b.len()) return len()>b.len()?1:-1;
  for (int i=len()-1; i>=0; i--)
   if (v[i]!=b.v[i]) return v[i]>b.v[i]?1:-1;
  return 0;
bool operator < (const Bigint &b)const{ return cp3(b)</pre>
    ==-1; }
bool operator == (const Bigint &b)const{ return cp3(b
    )==0; }
bool operator > (const Bigint &b)const{ return cp3(b)
Bigint operator - () const {
  Bigint r = (*this);
  r.s = -r.s;
  return r;
Bigint operator + (const Bigint &b) const {
  if (s == -1) return -(-(*this)+(-b));
  if (b.s == -1) return (*this)-(-b);
  Bigint r;
  int nl = max(len(), b.len());
  r.resize(nl + 1);
  for (int i=0; i<nl; i++) {</pre>
    if (i < len()) r.v[i] += v[i];</pre>
    if (i < b.len()) r.v[i] += b.v[i];</pre>
    if(r.v[i] >= BIGMOD) {
     r.v[i+1] += r.v[i] / BIGMOD;
      r.v[i] %= BIGMOD;
    }
  r.n();
  return r;
Bigint operator - (const Bigint &b) const {
  if (s == -1) return -(-(*this)-(-b));
  if (b.s == -1) return (*this)+(-b);
  if ((*this) < b) return -(b-(*this));</pre>
  Bigint r;
  r.resize(len());
  for (int i=0; i<len(); i++) {</pre>
    r.v[i] += v[i];
    if (i < b.len()) r.v[i] -= b.v[i];</pre>
    if (r.v[i] < 0) {
     r.v[i] += BIGMOD;
      r.v[i+1]--;
   }
  r.n();
  return r;
Bigint operator * (const Bigint &b) {
  Bigint r;
  r.resize(len() + b.len() + 1);
  r.s = s * b.s;
  for (int i=0; i<len(); i++) {</pre>
    for (int j=0; j<b.len(); j++) {</pre>
      r.v[i+j] += v[i] * b.v[j];
      if(r.v[i+j] >= BIGMOD) {
        r.v[i+j+1] += r.v[i+j] / BIGMOD;
        r.v[i+j] %= BIGMOD;
      }
   }
  r.n();
  return r;
Bigint operator / (const Bigint &b) {
  r.resize(max(1, len()-b.len()+1));
  int oriS = s;
  Bigint b2 = b; // b2 = abs(b)
  s = b2.s = r.s = 1;
  for (int i=r.len()-1; i>=0; i--) {
    int d=0, u=BIGMOD-1;
    while(d<u) {</pre>
```

```
int m = (d+u+1)>>1;
    r.v[i] = m;
    if((r*b2) > (*this)) u = m-1;
    else d = m;
}
    r.v[i] = d;
}
s = oriS;
r.s = s * b.s;
r.n();
return r;
}
Bigint operator % (const Bigint &b) {
    return (*this)-(*this)/b*b;
}
};
```

2.2 unordered_map

```
struct Key {
  int first, second;
  Key () {}
  Key (int _x, int _y) : first(_x), second(_y) {}
 bool operator == (const Key &b) const {
   return tie(F,S) == tie(b.F,b.S);
 }
};
struct KeyHasher {
 size_t operator()(const Key& k) const {
   return k.first + k.second*100000;
 }
typedef unordered_map<Key,int,KeyHasher> map_t;
int main(int argc, char** argv){
  map_t mp;
 for (int i=0; i<10; i++)</pre>
   mp[Key(i,0)] = i+1;
  for (int i=0; i<10; i++)</pre>
   printf("%d \ n", mp[Key(i,0)]);
  return 0;
}
```

2.3 extc balance tree

```
#include <bits/extc++.h>
using namespace __gnu_pbds;
typedef tree<int,null_type,less<int>,rb_tree_tag,
    tree_order_statistics_node_update> set_t;
int main()
{
  // Insert some entries into s.
  set_t s;
  s.insert(12);
 s.insert(505);
  // The order of the keys should be: 12, 505.
  assert(*s.find_by_order(0) == 12);
  assert(*s.find_by_order(3) == 505);
  // The order of the keys should be: 12, 505.
  assert(s.order_of_key(12) == 0);
 assert(s.order_of_key(505) == 1);
  // Erase an entry.
  s.erase(12);
 // The order of the keys should be: 505.
  assert(*s.find_by_order(0) == 505);
  // The order of the keys should be: 505.
  assert(s.order_of_key(505) == 0);
}
```

2.4 Disjoint Set

```
struct DisjointSet {
  // save() is like recursive
  // undo() is like return
  int n, fa[MXN], sz[MXN];
  vector<pair<int*,int>> h;
  vector<int> sp;
  void init(int tn) {
    n=tn;
    for (int i=0; i<n; i++) {</pre>
      fa[i]=i;
      sz[i]=1;
    sp.clear(); h.clear();
  void assign(int *k, int v) {
    h.PB({k, *k});
    *k=v;
  void save() { sp.PB(SZ(h)) };
  void undo() {
    assert(!sp.empty());
    int last=sp.back(); sp.pop_back();
    while (SZ(h)!=last) {
      auto x=h.back(); h.pop_back();
      *x.F=x.S;
    }
  int f(int x) {
    while (fa[x]!=x) x=fa[x];
    return x;
  void uni(int x, int y) {
    x=f(x); y=f(y);
    if (x==y) return ;
    if (sz[x] < sz[y]) swap(x, y);
    assign(\&sz[x], sz[x]+sz[y]);
    assign(&fa[y], x);
}djs;
```

2.5 Treap

```
const int MEM = 16000004;
struct Treap {
  static Treap nil, mem[MEM], *pmem;
  Treap *l, *r;
  char val;
  int size;
  Treap () : l(&nil), r(&nil), size(0) {}
  Treap (char _val) :
    l(&nil), r(&nil), val(_val), size(1) {}
} Treap::nil, Treap::mem[MEM], *Treap::pmem = Treap::
    mem;
int size(const Treap *t) { return t->size; }
void pull(Treap *t) {
  if (!size(t)) return;
  t\rightarrow size = size(t\rightarrow l) + size(t\rightarrow r) + 1;
Treap* merge(Treap *a, Treap *b) {
  if (!size(a)) return b;
  if (!size(b)) return a;
  Treap *t
  if (rand() % (size(a) + size(b)) < size(a)) {</pre>
    t = new (Treap::pmem++) Treap(*a);
    t->r = merge(a->r, b);
  } else {
    t = new (Treap::pmem++) Treap(*b);
    t->l = merge(a, b->l);
  pull(t);
  return t;
void split(Treap *t, int k, Treap *&a, Treap *&b) {
  if (!size(t)) a = b = &Treap::nil;
  else if (size(t->l) + 1 <= k) {
    a = new (Treap::pmem++) Treap(*t);
```

```
split(t->r, k - size(t->l) - 1, a->r, b);
    pull(a);
  } else {
    b = new (Treap::pmem++) Treap(*t);
    split(t->l, k, a, b->l);
    pull(b);
  }
}
int nv;
Treap *rt[50005];
void print(const Treap *t) {
 if (!size(t)) return;
  print(t->l);
  cout << t->val;
  print(t->r);
int main(int argc, char** argv) {
  IOS;
  rt[nv=0] = &Treap::nil;
  Treap::pmem = Treap::mem;
  int Q, cmd, p, c, v;
  string s;
  cin >> Q;
  while (Q--) {
    cin >> cmd;
    if (cmd == 1) {
      // insert string s after position p
      cin >> p >> s;
      Treap *tl, *tr;
      split(rt[nv], p, tl, tr);
for (int i=0; i<SZ(s); i++)</pre>
        tl = merge(tl, new (Treap::pmem++) Treap(s[i]))
      rt[++nv] = merge(tl, tr);
    } else if (cmd == 2) {
      // remove c characters starting at position
      Treap *tl, *tm, *tr;
      cin >> p >> c;
      split(rt[nv], p-1, tl, tm);
      split(tm, c, tm, tr);
      rt[++nv] = merge(tl, tr);
    } else if (cmd == 3) {
      // print c characters starting at position p, in
          version v
      Treap *tl, *tm, *tr;
      cin >> v >> p >> c;
      split(rt[v], p-1, tl, tm);
      split(tm, c, tm, tr);
      print(tm);
      cout << "\n":
    }
  7
  return 0;
}
```

2.6 Heavy Light Decomposition

```
// only one segment tree / no 0/1 base issue
// getPathSeg return the segment in order u->v
// fa[root] = root
typedef pair<int,int> pii;
int N, fa[MXN], belong[MXN], dep[MXN], sz[MXN], que[MXN];
int step,line[MXN],stPt[MXN],edPt[MXN];
vector<int> E[MXN], chain[MXN];
void DFS(int u){
 vector<int> &c = chain[belong[u]];
  for (int i=c.size()-1; i>=0; i--){
    int v = c[i];
    stPt[v] = step;
    line[step++] = v;
 for (int i=0; i<(int)c.size(); i++){</pre>
   u = c[i];
    for (auto v : E[u]){
      if (fa[u] == v || (i && v == c[i-1])) continue;
```

```
DFS(v);
    edPt[u] = step-1;
  }
void build_chain(int st){
  int fr,bk;
  fr=bk=0; que[bk++] = 1; fa[st]=st; dep[st]=0;
  while (fr < bk){</pre>
    int u=que[fr++]
    for (auto v : E[u]){
      if (v == fa[u]) continue;
      que[bk++] = v;
      dep[v] = dep[u]+1;
      fa[v] = u;
  for (int i=bk-1,u,pos; i>=0; i--){
    u = que[i]; sz[u] = 1; pos = -1;
    for (auto v : E[u]){
      if (v == fa[u]) continue;
      sz[u] += sz[v];
      if (pos==-1 || sz[v]>sz[pos]) pos=v;
    if (pos == -1) belong[u] = u;
    else belong[u] = belong[pos];
    chain[belong[u]].PB(u);
  step = 0;
  DFS(st);
int getLCA(int u, int v){
  while (belong[u] != belong[v]){
    int a = chain[belong[u]].back();
    int b = chain[belong[v]].back();
    if (dep[a] > dep[b]) u = fa[a];
    else v = fa[b];
  return sz[u] >= sz[v] ? u : v;
vector<pii> getPathSeg(int u, int v){
  vector<pii> ret1,ret2;
  while (belong[u] != belong[v]){
    int a = chain[belong[u]].back();
    int b = chain[belong[v]].back();
    if (dep[a] > dep[b]){
      ret1.PB({stPt[a],stPt[u]});
      u = fa[a];
    } else {
      ret2.PB({stPt[b],stPt[v]});
      v = fa[b];
    }
  if (dep[u] > dep[v]) swap(u,v);
  ret1.PB({stPt[u],stPt[v]});
  reverse(ret2.begin(), ret2.end());
  ret1.insert(ret1.end(),ret2.begin(),ret2.end());
  return ret1;
// Usage
void build(){
  build_chain(1); //change root
init(0,step,0); //init segment tree
int get_answer(int u, int v){
  int ret = -2147483647;
  vector<pii> vec = getPathSeg(u,v);
  for (auto it : vec)
    ; // check answer with segment [it.F, it.S]
  return ret;
}
```

2.7 Link-Cut Tree

```
const int MXN = 100005;
const int MEM = 100005;
struct Treap {
    static Treap nil, mem[MEM], *pmem;
    Treap *l, *r, *p, *lctp;
    int val;
```

```
int rev, size;
  Treap ():
    l(&nil), r(&nil), p(&nil), lctp(&nil), val(-1), rev
        (0), size(0) {}
  Treap (int _val) :
    l(&nil), r(&nil), p(&nil), lctp(&nil), val(_val),
        rev(0), size(1) {}
} Treap::nil,Treap::mem[MEM],*Treap::pmem=Treap::mem;
int size(const Treap *t) { return t->size; }
void push(Treap *t) {
  if (!size(t)) return;
  if (t->rev) {
    swap(t->l, t->r);
    if (size(t->l)) t->l->rev^=1;
    if (size(t->r)) t->r->rev^=1;
  t->rev=0;
void pull(Treap *t) {
 if (!size(t)) return;
  t->size = size(t->l)+size(t->r)+1;
  if (size(t->l)) t->l->p=t;
  if (size(t->r)) t->r->p=t;
Treap* merge(Treap *a, Treap *b) {
  if (!size(a)) return b;
 if (!size(b)) return a;
  push(a); push(b);
  if (rand() % (size(a) + size(b)) < size(a)) {
    a->r = merge(a->r, b);
    pull(a);
    return a:
  } else {
    b->l = merge(a, b->l);
    pull(b);
    return b;
 }
void split(Treap *t, int k, Treap *&a, Treap *&b) {
 push(t):
  if (!size(t)) a=b=&Treap::nil;
  else if (size(t->l) + 1 <= k) {
    split(t->r, k - size(t->l) - 1, a->r, b);
    pull(a);
  } else {
   b=t;
    split(t->l, k, a, b->l);
    pull(b);
 }
Treap* getRoot(Treap *t) {
 while (size(t->p)) t=t->p;
  return t;
Treap* head(Treap *t) {
  push( t=getRoot(t) );
  while (size(t->l)) push( t=t->l );
  return t;
Treap* tail(Treap *t) {
  push( t=getRoot(t) );
  while (size(t->r)) push( t=t->r );
  return t;
int get_rank(Treap *t) {
 vector<Treap*> path;
  for (; size(t); t=t->p) path.push_back(t);
  reverse(begin(path), end(path));
  for (auto it:path) push(it);
 int k=0;
 t=path.back();
 Treap *last=t->r;
 while (size(t)) {
    if (last == t->r) k+=size(t->l)+1;
    last=t; t=t->p;
 return k;
void lct_split(Treap *t, Treap *&a, Treap *&b, int flg)
     {
```

```
// if fla==1. Treap a should include node t:
  int k=get_rank(t);
  if (!flg) k--
  split(getRoot(t), k, a, b);
  a->p=b->p=&Treap::nil;
  if (size(b)) head(b)->lctp=tail(a);
Treap* expose(Treap *t) {
  Treap *tr:
  vector<Treap*> vec;
  while (size(t)) {
    lct_split(t, t, tr, 1);
    vec.push_back(t);
    t=head(t)->lctp;
  for (auto v:vec) t=merge(v, t);
  t->p=head(t)->lctp=&Treap::nil;
  return t;
Treap* evert(Treap *t) {
  t=expose(t);
  t->rev^=1:
  t->p=head(t)->lctp=&Treap::nil;
  return t;
void cut(Treap *x, Treap *y) {
  // cut node y when root is x.
  x=evert(x);
  if (head(y) != y) lct_split(y, x, y, 0);
  head(y)->lctp=&Treap::nil;
void link(Treap *x, Treap *y) {
// head(y)->lctp = x;
// return;
 y=evert(y);
  y=expose(y);
  head(y)->lctp=x;
int N, Q, jmp[MXN];
Treap *vt[MXN];
int flg;
int getNxt(int v) {
  v += jmp[v];
  if (v>N) v=0;
  return v;
int main(int argc, char** argv) {
  vt[0] = new (Treap::pmem++) Treap(0);
  scanf("%d%d", &N, &Q);
  for (int i=1; i<=N; i++) {</pre>
    RI(jmp[i]);
    vt[i] = new (Treap::pmem++) Treap(i);
  for (int i=N; i>=1; i--) link(vt[getNxt(i)],vt[i]);
  int cmd, a, b;
  while (Q--) {
    scanf("%d", &cmd);
    if (cmd == 0) {
      scanf("%d%d", &a, &b);
      cut(vt[0], vt[a]);
      imp[a]=b:
      link(vt[getNxt(a)], vt[a]);
    } else {
      scanf("%d", &a);
      evert(vt[0]);
      Treap *rt=expose(vt[a]);
      int v=head(rt)->p->val, sz = size(rt)-1;
      rt=head(rt);
      if (size(rt->r)) {
        rt=rt->r:
        while (size(rt->l)) rt=rt->l;
        v=rt->val;
      printf("%d %d \n", v, sz);
    }
  return 0;
```

3 Graph

3.1 Tarjan

```
const int MAXV = 101000;
int V, E;
vector<int> el[MAXV];
int dfn[MAXV], low[MAXV], did;
bool ins[MAXV];
stack<int> st;
int scc[MAXV], scn;
void tarjan(int u){
  cout << u << endl;</pre>
  dfn[u] = low[u] = ++did;
  st.push(u); ins[u] = true;
  for(int i=0; i<(int)el[u].size(); i++){</pre>
    int v = el[u][i];
    if(!dfn[v]){
      tarjan(v);
      low[u] = min(low[u], low[v]);
    }else if(ins[v]){
      low[u] = min(low[u], dfn[v]);
  }
  if(dfn[u] == low[u]){
    int v;
    do{
      v = st.top();
      st.pop();
      scc[v] = scn;
      ins[v] = false;
    }while(v != u);
    scn ++;
  }
}
void calcscc(){
  did = scn = 0;
  for(int i=0; i<V; i++){</pre>
    if(!dfn[i]) tarjan(i);
}
```

3.2 Strongly Connected Components

```
struct Scc{
 int n, nScc, vst[MXN], bln[MXN];
  vector<int> E[MXN], rE[MXN], vec;
 void init(int _n){
   n = _n;
    for (int i=0; i<MXN; i++){</pre>
      E[i].clear();
      rE[i].clear();
   }
 7
 void add_edge(int u, int v){
   E[u].PB(v):
    rE[v].PB(u);
 void DFS(int u){
   vst[u]=1;
    for (auto v : E[u])
      if (!vst[v]) DFS(v);
   vec.PB(u);
 }
 void rDFS(int u){
    vst[u] = 1;
   bln[u] = nScc;
    for (auto v : rE[u])
      if (!vst[v]) rDFS(v);
  void solve(){
   nScc = 0;
   vec.clear();
```

```
FZ(vst);
    for (int i=0; i<n; i++)
        if (!vst[i]) DFS(i);
    reverse(vec.begin(),vec.end());
    FZ(vst);
    for (auto v : vec){
        if (!vst[v]){
            rDFS(v);
            nScc++;
        }
    }
}</pre>
```

3.3 DMST_with_sol

```
const int INF = 1029384756;
struct edge_t{
 int u,v,w;
  set< pair<int,int> > add, sub;
  edge_t() : u(-1), v(-1), w(0) {}
  edge_t(int _u, int _v, int _w) {
    u = _u; v = _v; w = _w;
    add.insert({u, v});
  edge_t& operator += (const edge_t& obj) {
    w += obj.w;
    FOR (it, obj.add) {
      if (!sub.count(*it)) add.insert(*it);
      else sub.erase(*it);
    FOR (it, obj.sub) {
      if (!add.count(*it)) sub.insert(*it);
      else add.erase(*it);
    return *this;
  edge_t& operator -= (const edge_t& obj) {
    w -= obj.w;
    FOR (it, obj.sub) {
      if (!sub.count(*it)) add.insert(*it);
      else sub.erase(*it);
    for (auto it : obj.add) {
      if (!add.count(it)) sub.insert(it);
      else add.erase(it);
    return *this;
  }
}eg[MXN*MXN],prv[MXN],EDGE_INF(-1,-1,INF);
int N,M;
int cid,incyc[MXN],contracted[MXN];
vector<int> E[MXN];
edge_t dmst(int rt){
  edge_t cost;
  for (int i=0; i<N; i++){</pre>
    contracted[i] = incyc[i] = 0;
    prv[i] = EDGE_INF;
  cid = 0;
  int u,v;
  while (true){
    for (v=0; v<N; v++){
      if (v != rt && !contracted[v] && prv[v].w == INF)
           break;
    if (v >= N) break; // end
    for (int i=0; i<M; i++){</pre>
      if (eg[i].v == v && eg[i].w < prv[v].w)</pre>
        prv[v] = eg[i];
    if (prv[v].w == INF) // not connected
      return EDGE_INF;
    cost += prv[v];
    for (u=prv[v].u; u!=v && u!=-1; u=prv[u].u);
    if (u == -1) continue;
    incyc[v] = ++cid;
    for (u=prv[v].u; u!=v; u=prv[u].u){
```

```
contracted[u] = 1:
      incyc[u] = cid;
    for (int i=0; i<M; i++){</pre>
      if (incyc[eg[i].u] != cid && incyc[eg[i].v] ==
          cid){
        eg[i] -= prv[eg[i].v];
      }
    for (int i=0; i<M; i++){</pre>
      if (incyc[eg[i].u] == cid) eg[i].u = v;
      if (incyc[eg[i].v] == cid) eg[i].v = v;
      if (eg[i].u == eg[i].v) eg[i--] = eg[--M];
    for (int i=0; i<N; i++){</pre>
      if (contracted[i]) continue;
      if (prv[i].u>=0 && incyc[prv[i].u] == cid)
        prv[i].u = v;
    prv[v] = EDGE_INF;
  return cost;
}
void solve(){
  edge_t cost = dmst(0);
  for (auto it : cost.add){ // find a solution
    E[it.F].PB(it.S);
    prv[it.S] = edge_t(it.F,it.S,0);
}
```

3.4 Maximum Clique

```
class MaxClique {
public:
    static const int MV = 210;
    int el[MV][MV/30+1];
    int dp[MV];
    int ans:
    int s[MV][MV/30+1];
    vector<int> sol;
    void init(int v) {
        V = v; ans = 0;
        FZ(el); FZ(dp);
    /* Zero Base */
    void addEdge(int u, int v) {
        if(u > v) swap(u, v);
        if(u == v) return;
        el[u][v/32] |= (1<<(v%32));
    }
    bool dfs(int v, int k) {
        int c = 0, d = 0;
        for(int i=0; i<(V+31)/32; i++) {
    s[k][i] = el[v][i];</pre>
             if(k != 1) s[k][i] &= s[k-1][i];
             c += __builtin_popcount(s[k][i]);
        if(c == 0) {
             if(k > ans) {
                 ans = k;
                 sol.clear();
                 sol.push_back(v);
                 return 1;
             }
             return 0;
        for(int i=0; i<(V+31)/32; i++) {</pre>
             for(int a = s[k][i]; a; d++) {
                 if(k + (c-d) <= ans) return 0;</pre>
                 int lb = a&(-a), lg = 0;
                 a ^= lb;
                 while(lb!=1) {
                     lb = (unsigned int)(lb) >> 1;
```

```
lg ++:
                  int u = i*32 + lg;
                  if(k + dp[u] <= ans) return 0;</pre>
                  if(dfs(u, k+1)) {
                      sol.push_back(v);
                      return 1;
             }
         }
         return 0:
    }
    int solve() {
         for(int i=V-1; i>=0; i--) {
             dfs(i, 1);
             dp[i] = ans;
         return ans;
    }
};
```

3.5 MinimumMeanCycle

```
/* minimum mean cycle */
const int MAXE = 1805;
const int MAXN = 35;
const double inf = 1029384756;
const double eps = 1e-6;
struct Edge {
  int v,u;
  double c;
int n,m,prv[MAXN][MAXN], prve[MAXN][MAXN], vst[MAXN];
Edge e[MAXE];
vector<int> edgeID, cycle, rho;
double d[MAXN][MAXN];
inline void bellman_ford() {
  for(int i=0; i<n; i++) d[0][i]=0;</pre>
  for(int i=0; i<n; i++) {</pre>
    fill(d[i+1], d[i+1]+n, inf);
    for(int j=0; j<m; j++) {</pre>
      int v = e[j].v, u = e[j].u;
      if(d[i][v]<inf && d[i+1][u]>d[i][v]+e[j].c) {
        d[i+1][u] = d[i][v]+e[j].c;
        prv[i+1][u] = v;
        prve[i+1][u] = j;
      }
    }
  }
double karp_mmc() {
  // returns inf if no cycle, mmc otherwise
  double mmc=inf;
  int st = -1;
  bellman_ford();
  for(int i=0; i<n; i++) {</pre>
    double avg=-inf;
    for(int k=0; k<n; k++) {</pre>
      if(d[n][i]<inf-eps) avg=max(avg,(d[n][i]-d[k][i])</pre>
           /(n-k));
      else avg=max(avg,inf);
    if (avg < mmc) tie(mmc, st) = tie(avg, i);</pre>
  FZ(vst); edgeID.clear(); cycle.clear(); rho.clear();
  for (int i=n; !vst[st]; st=prv[i--][st]) {
    vst[st]++;
    edgeID.PB(prve[i][st]);
    rho.PB(st);
  while (vst[st] != 2) {
    int v = rho.back(); rho.pop_back();
    cycle.PB(v);
    vst[v]++;
  reverse(ALL(edgeID));
  edgeID.resize(SZ(cycle));
  return mmc;
```

Flow 4

4.1 ISAP

```
struct Isap{
  static const int MXN = 10000;
  struct Edge{ int v,f,re; };
  int n,s,t,h[MXN],gap[MXN];
  vector<Edge> E[MXN];
  void init(int _n, int _s, int _t){
  n = _n;  s = _s;  t = _t;
    for (int i=0; i<n; i++) E[i].clear();</pre>
  void add_edge(int u, int v, int f){
    E[u].PB({v,f,SZ(E[v])});
    E[v].PB({u,0,SZ(E[u])-1});
  int DFS(int u, int nf, int res=0){
    if (u == t) return nf;
    for (auto &it : E[u]){
      if (h[u] == h[it.v] + 1 && it.f > 0) {
        int tf = DFS(it.v,min(nf,it.f));
        res += tf; nf -= tf; it.f -= tf;
        E[it.v][it.re].f += tf;
        if (nf == 0) return res;
      }
    if (nf){
      if (--gap[h[u]] == 0) h[s]=n;
      gap[++h[u]]++;
    return res;
  int flow(int res=0){
    FZ(h); FZ(gap);
    gap[0] = n;
    while (h[s] < n) res += DFS(s,2147483647);
    return res;
}flow;
```

4.2 Dinic

```
struct Dinic{
 static const int MXN = 10000;
struct Edge{ int v,f,re; };
  int n,s,t,level[MXN];
  vector<Edge> E[MXN];
 for (int i=0; i<n; i++) E[i].clear();</pre>
  void add_edge(int u, int v, int f){
   E[u].PB({v,f,SZ(E[v])});
    E[v].PB({u,0,SZ(E[u])-1});
 bool BFS(){
    FMO(level);
    queue<int> que;
    que.push(s);
    level[s] = 0;
    while (!que.empty()){
      int u = que.front(); que.pop();
      for (auto it : E[u]){
        if (it.f > 0 && level[it.v] == -1){
          level[it.v] = level[u]+1;
          que.push(it.v);
     }
    return level[t] != -1;
  int DFS(int u, int nf){
    if (u == t) return nf;
    int res = 0:
    for (auto &it : E[u]){
      if (it.f > 0 && level[it.v] == level[u]+1){
        int tf = DFS(it.v, min(nf,it.f));
```

```
res += tf; nf -= tf; it.f -= tf;
        E[it.v][it.re].f += tf;
        if (nf == 0) return res;
    if (!res) level[u] = -1;
    return res;
  int flow(int res=0){
    while ( BFS() )
      res += DFS(s,2147483647);
    return res;
}flow;
4.3
    Cost Flow
typedef pair<long long, long long> pll;
struct CostFlow {
  static const int MXN = 205;
  static const long long INF = 102938475610293847LL;
  struct Edge {
    int v, r;
    long long f, c;
  int n, s, t, prv[MXN], prvL[MXN], inq[MXN];
  long long dis[MXN], fl, cost;
  vector<Edge> E[MXN];
  void init(int _n, int _s, int _t) {
    n = _n; s = _s; t = _t;
for (int i=0; i<n; i++) E[i].clear();</pre>
    fl = cost = 0;
  void add_edge(int u, int v, long long f, long long c)
    E[u].PB(\{v, SZ(E[v]), f, c\});
    E[v].PB({u, SZ(E[u])-1, 0, -c});
  pll flow() {
    while (true) {
      for (int i=0; i<n; i++) {</pre>
        dis[i] = INF;
        inq[i] = 0;
      dis[s] = 0;
      queue<int> que;
      que.push(s);
      while (!que.empty()) {
        int u = que.front(); que.pop();
        inq[u] = 0;
        for (int i=0; i<SZ(E[u]); i++) {</pre>
          int v = E[u][i].v;
          long long w = E[u][i].c;
          if (E[u][i].f > 0 && dis[v] > dis[u] + w) {
            prv[v] = u; prvL[v] = i;
             dis[v] = dis[u] + w;
             if (!inq[v]) {
               inq[v] = 1;
               que.push(v);
            }
          }
        }
      if (dis[t] == INF) break;
      long long tf = INF;
      for (int v=t, u, l; v!=s; v=u) {
        u=prv[v]; l=prvL[v];
        tf = min(tf, E[u][l].f);
      for (int v=t, u, l; v!=s; v=u) {
        u=prv[v]; l=prvL[v];
        E[u][l].f -= tf;
        E[v][E[u][l].r].f += tf;
      cost += tf * dis[t];
      fl += tf;
    return {fl, cost};
```

}flow;

4.4 Bipartite Matching (Augmenting Path)

```
bool DFS(int u){
  for (auto v : E[u]){
    if (!vst[v]){
      vst[v]=1:
      if (match[v] == -1 || DFS(match[v])){
        match[v] = u; match[u] = v;
        return true;
      }
   }
 }
  return false;
int DoMatch(int res=0){
 memset(match,-1,sizeof(match));
  for (int i=1; i<=N; i++){</pre>
    if (match[i] == -1){
      memset(vst,0,sizeof(vst));
      DFS(i);
  for (int i=1; i<=N; i++)</pre>
   if (match[i] != -1) res++;
  return res;
```

4.5 Kuhn Munkres

struct KM{

```
// Maximum Bipartite Weighted Matching (Perfect Match)
 static const int MXN = 650;
  static const int INF = 2147483647; // long long
  int n,match[MXN],vx[MXN],vy[MXN];
 int edge[MXN][MXN],lx[MXN],ly[MXN],slack[MXN];
  // ^^^ long long
 void init(int _n){
   n = _n;
    for (int i=0; i<n; i++)</pre>
      for (int j=0; j<n; j++)</pre>
        edge[i][j] = 0;
  void add_edge(int x, int y, int w){ // long long
    edge[x][y] = w;
 bool DFS(int x){
    vx[x] = 1;
    for (int y=0; y<n; y++){</pre>
      if (vy[y]) continue;
      if (lx[x]+ly[y] > edge[x][y]){
        slack[y] = min(slack[y], lx[x]+ly[y]-edge[x][y
             ]);
      } else {
        vy[y] = 1;
        if (match[y] == -1 \mid | DFS(match[y])){
          match[y] = x;
          return true;
        }
      }
    7
    return false;
  int solve(){
    fill(match, match+n, -1);
    fill(lx,lx+n,-INF);
    fill(ly,ly+n,0);
    for (int i=0; i<n; i++)</pre>
      for (int j=0; j<n; j++)</pre>
        lx[i] = max(lx[i], edge[i][j]);
    for (int i=0; i<n; i++){</pre>
      fill(slack,slack+n,INF);
      while (true){
        fill(vx,vx+n,0);
        fill(vy,vy+n,0);
        if ( DFS(i) ) break;
int d = INF; // long long
        for (int j=0; j<n; j++)</pre>
          if (!vy[j]) d = min(d, slack[j]);
        for (int j=0; j<n; j++){</pre>
```

```
if (vx[j]) lx[j] -= d;
    if (vy[j]) ly[j] += d;
    else slack[j] -= d;
    }
    }
    int res=0;
    for (int i=0; i<n; i++)
        res += edge[match[i]][i];
    return res;
}
}graph;</pre>
```

4.6 SW-Mincut

```
struct SW{ // O(V^3)
  static const int MXN = 514;
  int n,vst[MXN],del[MXN];
  int edge[MXN][MXN],wei[MXN];
  void init(int _n){
    n = _n;
    FZ(edge);
    FZ(del);
  void add_edge(int u, int v, int w){
    edge[u][v] += w;
    edge[v][u] += w;
  void search(int &s, int &t){
    FZ(vst); FZ(wei);
s = t = -1;
    while (true){
      int mx=-1, cur=0;
      for (int i=0; i<n; i++)</pre>
         if (!del[i] && !vst[i] && mx<wei[i])</pre>
           cur = i, mx = wei[i];
      if (mx == -1) break;
      vst[cur] = 1;
      s = t:
      t = cur;
      for (int i=0; i<n; i++)</pre>
         if (!vst[i] && !del[i]) wei[i] += edge[cur][i];
    }
  int solve(){
    int res = 2147483647;
    for (int i=0,x,y; i<n-1; i++){</pre>
      search(x,y);
      res = min(res,wei[y]);
      del[y] = 1;
      for (int j=0; j<n; j++)</pre>
        edge[x][j] = (edge[j][x] += edge[y][j]);
    return res;
  }
}graph;
```

4.7 Maximum Simple Graph Matching

```
struct GenMatch { // 1-base
  static const int MAXN = 250;
  int V;
  bool el[MAXN][MAXN];
  int pr[MAXN];
  bool inq[MAXN],inp[MAXN],inb[MAXN];
  queue<int> qe;
  int st,ed;
  int nb;
  int bk[MAXN],djs[MAXN];
  int ans;
  void init(int _V) {
    V = _V;
    FZ(el); FZ(pr);
    FZ(inq); FZ(inp); FZ(inb);
FZ(bk); FZ(djs);
    ans = 0;
  void add_edge(int u, int v) {
```

```
el[u][v] = el[v][u] = 1;
int lca(int u,int v) {
 memset(inp,0,sizeof(inp));
  while(1) {
    u = djs[u];
    inp[u] = true;
    if(u == st) break;
    u = bk[pr[u]];
  while(1) {
    v = djs[v];
    if(inp[v]) return v;
    v = bk[pr[v]];
  }
  return v;
void upd(int u) {
  int v:
  while(djs[u] != nb) {
    v = pr[u];
    inb[djs[u]] = inb[djs[v]] = true;
    u = bk[v];
    if(djs[u] != nb) bk[u] = v;
 }
}
void blo(int u,int v) {
 nb = lca(u,v);
  memset(inb,0,sizeof(inb));
  upd(u); upd(v);
  if(djs[u] != nb) bk[u] = v;
  if(djs[v] != nb) bk[v] = u;
  for(int tu = 1; tu <= V; tu++)</pre>
    if(inb[djs[tu]]) {
      djs[tu] = nb;
      if(!inq[tu]){
        qe.push(tu);
        inq[tu] = 1;
      }
    }
}
void flow() {
  memset(inq, false, sizeof(inq));
  memset(bk,0,sizeof(bk));
  for(int i = 1; i <= V;i++)</pre>
    djs[i] = i;
  while(qe.size()) qe.pop();
  qe.push(st);
  inq[st] = 1;
  ed = 0;
  while(qe.size()) {
    int u = qe.front(); qe.pop();
    for(int v = 1; v <= V; v++)</pre>
      if(el[u][v] && (djs[u] != djs[v]) && (pr[u] !=
          v)) {
        if((v == st) || ((pr[v] > 0) && bk[pr[v]] >
            0))
          blo(u,v);
        else if(bk[v] == 0) {
          bk[v] = u;
          if(pr[v] > 0) {
            if(!inq[pr[v]]) qe.push(pr[v]);
          } else {
            ed = v;
            return;
          }
        }
      }
 }
7
void aug() {
  int u,v,w;
  u = ed;
  while(u > 0) {
    v = bk[u];
    w = pr[v];
    pr[v] = u;
    pr[u] = v;
    u = w;
}
```

```
int solve() {
    memset(pr,0,sizeof(pr));
    for(int u = 1; u <= V; u++)</pre>
       if(pr[u] == 0) {
         st = u;
         flow();
         if(ed > 0) {
           aug();
           ans ++:
         }
    return ans;
  }
};
int main() {
  gp.init(V);
  for(int i=0; i<E; i++) {</pre>
    int u, v;
    cin >> u >> v;
    gp.edge(u, v);
  cout << gp.solve() << endl;</pre>
}
```

4.8 Minimum Weight Matching (Clique version)

```
struct Graph {
  // Minimum General Weighted Matching (Perfect Match)
  static const int MXN = 105;
  int n, edge[MXN][MXN];
  int match[MXN],dis[MXN],onstk[MXN];
  vector<int> stk;
  void init(int _n) {
    n = _n;
    FZ(edge);
  void add_edge(int u, int v, int w) {
    edge[u][v] = edge[v][u] = w;
  bool SPFA(int u){
    if (onstk[u]) return true;
    stk.PB(u);
    onstk[u] = 1;
    for (int v=0; v<n; v++){</pre>
      if (u != v && match[u] != v && !onstk[v]){
        int m = match[v];
        if (dis[m] > dis[u] - edge[v][m] + edge[u][v]){
          dis[m] = dis[u] - edge[v][m] + edge[u][v];
          onstk[v] = 1;
          stk.PB(v);
          if (SPFA(m)) return true;
          stk.pop_back();
          onstk[v] = 0;
      }
    onstk[u] = 0;
    stk.pop_back();
    return false;
  int solve() {
    // find a match
    for (int i=0; i<n; i+=2){</pre>
      match[i] = i+1;
      match[i+1] = i;
    while (true){
      int found = 0;
      FZ(dis); FZ(onstk);
      for (int i=0; i<n; i++){</pre>
        stk.clear();
        if (!onstk[i] && SPFA(i)){
          found = 1:
          while (SZ(stk)>=2){
            int u = stk.back(); stk.pop_back();
            int v = stk.back(); stk.pop_back();
```

```
match[u] = v;
             match[v] = u;
        }
      if (!found) break;
    int ret = 0;
    for (int i=0; i<n; i++)</pre>
      ret += edge[i][match[i]];
    ret /= 2;
    return ret;
  }
}graph;
```

4.9 2-Commodity Flow

```
const int MAXN = 64;
const int INF = 1029384756;
int N;
int s1, s2, t1, t2, d1, d2, S, T;
int edge[MAXN][MAXN];
int cap[MAXN][MAXN];
int h[MAXN], gap[MAXN];
bool vis[MAXN];
int isap(int v, int f)
{
    if(v == T)return f;
    if(vis[v])return 0;
    vis[v] = true;
    for(int i=0; i<N+2; i++)</pre>
        if(cap[v][i] <= 0)continue;</pre>
        if(h[i] != h[v] - 1)continue;
        int res = isap(i, min(cap[v][i], f));
        if(res > 0)
             cap[v][i] -= res;
             cap[i][v] += res;
             return res;
        }
    }
    gap[h[v]]--;
    if(gap[h[v]] <= 0)h[S] = N + 4;
    h[v]++;
    gap[h[v]]++;
    return 0;
}
int get_flow()
    for(int i=0; i<MAXN; i++)</pre>
    {
        h[i] = gap[i] = 0;
    gap[0] = N + 2;
    int flow = 0;
    while(h[S] \le N + 3)
        for(int i=0; i<N+2; i++)</pre>
        {
             vis[i] = false;
        int df = isap(S, INF);
        flow += df;
    }
    return flow;
}
```

```
int main()
    ios_base::sync_with_stdio(0);
    int TT;
    cin>>TT;
    while(TT--)
        cin>>N:
        cin>>s1>>t1>>d1>>s2>>t2>>d2;
         for(int i=0; i<MAXN; i++)</pre>
             for(int j=0; j<MAXN; j++)</pre>
                 edge[i][j] = 0;
             }
        }
         for(int i=0; i<N; i++)</pre>
             string s;
             cin>>s;
             for(int j=0; j<N; j++)</pre>
                 if(s[j] == 'X')edge[i][j] = 0;
                 else if(s[j] == '0')edge[i][j] = 1;
                 else if(s[j] == 'N')edge[i][j] = INF;
        }
        int ans = 0;
        S = N;
        T = N + 1;
         //first
         for(int i=0; i<MAXN; i++)</pre>
             for(int j=0; j<MAXN; j++)</pre>
                 cap[i][j] = edge[i][j];
         }
        cap[S][s1] = cap[t1][T] = d1;
        cap[S][s2] = cap[t2][T] = d2;
        ans = get_flow();
         //second
         for(int i=0; i<MAXN; i++)</pre>
             for(int j=0; j<MAXN; j++)</pre>
                 cap[i][j] = edge[i][j];
        }
        cap[S][s1] = cap[t1][T] = d1;
        cap[S][t2] = cap[s2][T] = d2;
        ans = min(ans, get_flow());
        cout<<(ans == d1 + d2 ? "Yes" : "No")<<endl;</pre>
    }
    return 0;
}
       (+1) SW-mincut O(NM)
// {{{ StoerWagner
const int inf=10000000000;
// should be larger than max.possible mincut
class StoerWagner {
  public:
    int n,mc; // node id in [0,n-1]
    vector<int> adj[MAXN];
    int cost[MAXN][MAXN];
```

```
int cs[MAXN];
                                                                 return cut:
bool merged[MAXN],sel[MAXN];
// --8<-- include only if cut is explicitly needed
  DisjointSet djs;
                                                         };
vector<int> cut;
                                                        1// }}}
//--8<---
  StoerWagner(int _n):n(_n),mc(inf),djs(_n) {
    for(int i=0;i<n;i++)</pre>
                                                              Math
                                                         5
     merged[i]=0;
    for(int i=0;i<n;i++)</pre>
      for(int j=0;j<n;j++)</pre>
                                                              ax+by=gcd
                                                         5.1
        cost[i][j]=cost[j][i]=0;
void append(int v,int u,int c) {
                                                         typedef pair<int, int> pii;
  if(v==u) return;
  if(!cost[v][u]&&c) {
                                                         pii gcd(int a, int b){
    adj[v].PB(u);
    adj[u].PB(v);
                                                             int p = a / b;
  cost[v][u]+=c;
                                                             pii q = gcd(b, a % b);
  cost[u][v]+=c;
void merge(int v,int u) {
                                                         }
  merged[u]=1;
  for(int i=0;i<n;i++)</pre>
    append(v,i,cost[u][i]);
                                                              Chinese Remainder
                                                         5.2
  // --8<-- include only if cut is explicitly
      needed
    djs.merge(v,u);
                                                         int pm[MAXNUM];
                                                         inline void generate_primes() {
void phase() {
                                                           int i,j;
  priority_queue<pii> pq;
                                                           pnum=1;
  for(int v=0;v<n;v++) {</pre>
                                                           prime[0]=2;
    if(merged[v]) continue;
                                                           for(i=3;i<MAXVAL;i+=2) {</pre>
    cs[v]=0;
                                                             if(nprime[i]) continue;
    sel[v]=0:
                                                             prime[pnum++]=i;
    pq.push({0,v});
                                                           }
  int v,s,pv;
  while(pq.size()) {
    if(cs[pq.top().S]>pq.top().F) {
                                                           int q,tmp,a=x,b=p;
      pq.pop();
                                                           int a0=1,a1=0,b0=0,b1=1;
      continue;
                                                           while(b) {
    }
    pv=v;
                                                             tmp=b0; b0=a0-b0*q; a0=tmp;
    v=pq.top().S;
                                                             tmp=b1; b1=a1-b1*q; a1=tmp;
    s=pq.top().F;
    pq.pop();
                                                           return a0;
    sel[v]=1;
    for(int i=0;i<adj[v].size();i++) {</pre>
                                                         inline void decompose_mod() {
      int u=adj[v][i];
                                                           int i,p,t=mod;
      if(merged[u]||sel[u]) continue;
                                                           pfn=0;
      cs[u]+=cost[v][u];
      pq.push({cs[u],u});
                                                             p=prime[i];
    }
                                                             if(t%p==0) {
                                                               pf[pfn]=1;
  if(s<mc) {</pre>
                                                               while(t%p==0) {
                                                                 t/=p;
    // --8<-- include only if cut is explicitly
                                                                 pf[pfn]*=p;
    needed ---
                                                               }
      cut.clear();
                                                               pfn++;
    for(int i=0;i<n;i++)</pre>
                                                             }
      if(djs.getrep(i)==djs.getrep(v)) cut.PB(i);
                                                           if(t>1) pf[pfn++]=t;
  }
  merge(v,pv);
                                                           int i,m,s=0;
int mincut() {
                                                           for(i=0;i<pfn;i++) {</pre>
  if(mc==inf) {
                                                             m=mod/pf[i];
    for(int t=0;t<n-1;t++)</pre>
      phase();
  return mc;
                                                           return s;
}
// --8<-- include only if cut is explicitly needed
  vector<int> getcut() { // return one side of the
      cut
    mincut();
```

```
if(b == 0) return make_pair(1, 0);
  return make_pair(q.second, q.first - q.second * p);
```

```
int pfn; // number of distinct prime factors
int pf[MAXNUM]; // prime factor powers
int rem[MAXNUM]; // corresponding remainder
    for(j=i*i;j<MAXVAL;j+=i) nprime[j]=1;</pre>
inline int inverse(int x,int p) {
    q=a/b; tmp=b; b=a-b*q; a=tmp;
  for(i=0;i<pnum&&prime[i]<=t;i++) {</pre>
inline int chinese_remainder() {
    pm[i]=(long long)m*inverse(m,pf[i])%mod;
    s=(s+(long long)pm[i]*rem[i])%mod;
```

5.3 Fast Fourier Transform

```
// const int MAXN = 262144;
// (must be 2^k)
typedef long double ld;
typedef complex<ld> cplx;
const ld PI = acosl(-1);
const cplx I(0, 1);
cplx omega[MAXN+1];
void pre_fft()
  for(int i=0; i<=MAXN; i++)</pre>
    omega[i] = exp(i * 2 * PI / MAXN * I);
void fft(int n, cplx a[], bool inv=false)
  int basic = MAXN / n;
  int theta = basic;
  for (int m = n; m >= 2; m >>= 1) {
    int mh = m >> 1;
    for (int i = 0; i < mh; i++) {</pre>
      cplx w = omega[inv ? MAXN-(i*theta%MAXN) : i*
          theta%MAXN];
      for (int j = i; j < n; j += m) {</pre>
        int k = j + mh;
        cplx x = a[j] - a[k];
        a[j] += a[k];
        a[k] = w * x;
      }
    theta = (theta * 2) % MAXN;
  int i = 0:
  for (int j = 1; j < n - 1; j++) {
    for (int k = n >> 1; k > (i ^= k); k >>= 1);
    if (j < i) swap(a[i], a[j]);</pre>
  if (inv)
    for (i = 0; i < n; i++)
      a[i] /= n;
```

5.4 (+1) ntt

```
int P=605028353,root=3,MAXNUM=262144;
// Remember coefficient are mod P
/*
p=a*2^n+1
   2^n
                                        root
n
                                 а
                 97
    32
5
                                 .3
                                        5
6
                 193
                                 3
                                        5
    64
                 257
                                 2
    128
                                        3
8
    256
                 257
                                 1
                                        3
9
                  7681
    512
                                 15
                                        17
10
    1024
                 12289
                                 12
                                        11
11
    2048
                 12289
                                 6
                                        11
12
    4096
                 12289
                                 3
                                        11
1.3
   8192
                 40961
                                 5
                                        .3
   16384
                  65537
                                 4
14
                                        3
15
    32768
                 65537
                                 2
                                        3
16
    65536
                 65537
                                 1
                                        .3
17
   131072
                  786433
                                 6
                                        10
                                           (605028353,
                  786433
                                 3
18
    262144
                                        10
    2308, 3)
   524288
                 5767169
                                 11
    1048576
                  7340033
                                        3
                                 7
20
21
    2097152
                 23068673
                                 11
                                        3
    4194304
                 104857601
                                 25
22
                                        3
23
    8388608
                 167772161
                                 20
                                        3
24
    16777216
                 167772161
                                 10
25
    33554432
                 167772161
                                 5
                                        3 (1107296257, 33,
    10)
26
    67108864
                  469762049
27
                 2013265921
                                 15
    134217728
                                        31
int bigmod(long long a,int b){
  if(b==0)return 1;
```

```
return (bigmod((a*a)%P,b/2)*(b%2?a:1ll))%P;
int inv(int a,int b){
   if(a==1)return 1;
   return (((long long)(a-inv(b%a,a))*b+1)/a)%b;
std::vector<long long> ps(MAXNUM);
std::vector<int> rev(MAXNUM);
struct poly{
   std::vector<unsigned int> co;
   int n;//polynomial degree = n
   poly(int d){n=d;co.resize(n+1,0);}
   void trans2(int NN){
     int r=0,st,N;
     unsigned int a,b;
     while((1<<r)<(NN>>1))++r;
     for (N=2;N<=NN;N<<=1,--r) {</pre>
       for(st=0;st<NN;st+=N){</pre>
         int i,ss=st+(N>>1);
         for(i=(N>>1)-1;i>=0;--i){
           a=co[st+i]; b=(ps[i<<r]*co[ss+i])%P;
           co[st+i]=a+b; if(co[st+i]>=P)co[st+i]-=P;
           co[ss+i]=a+P-b; if(co[ss+i]>=P)co[ss+i]-=P;
       }
     }
   void trans1(int NN){
     int r=0,st,N;
     unsigned int a,b;
     for(N=NN;N>1;N>>=1,++r){
       for(st=0;st<NN;st+=N){</pre>
         int i,ss=st+(N>>1);
         for(i=(N>>1)-1;i>=0;--i){
           a=co[st+i]; b=co[ss+i];
           co[st+i]=a+b; if(co[st+i]>=P)co[st+i]-=P;
            co[ss+i]=((a+P-b)*ps[i<< r])%P;
         }
       }
     }
   }
   poly operator*(const poly& _b)const{
     poly a=*this,b=_b;
     int k=n+b.n,i,N=1;
     while(N<=k)N*=2;</pre>
     a.co.resize(N,0); b.co.resize(N,0);
     int r=bigmod(root, (P-1)/N), Ni=inv(N,P);
     ps[0]=1;
     for(i=1;i<N;++i)ps[i]=(ps[i-1]*r)%P;</pre>
     a.trans1(N);b.trans1(N);
     for(i=0;i<N;++i)a.co[i]=((long long)a.co[i]*b.co[i</pre>
         ])%P
     r=inv(r,P);
     for(i=1;i<N/2;++i)std::swap(ps[i],ps[N-i]);</pre>
     a.trans2(N);
     for(i=0;i<N;++i)a.co[i]=((long long)a.co[i]*Ni)%P;</pre>
     a.n=n+_b.n; return a;
};
      Mod
5.5
/// _fd(a,b) floor(a/b).
/// _rd(a,m) a-floor(a/m)*m.
/// _pv(a,m,r) largest x s.t x<=a && x%m == r.
///_nx(a,m,r) smallest x s.t x>=a && x%m == r.
///_ct(a,b,m,r) |A| , A = { x : a<=x<=b && x%m == r }.
int _fd(int a,int b){ return a<0?(-~a/b-1):a/b; }</pre>
int _rd(int a,int m){ return a-_fd(a,m)*m; }
int _pv(int a,int m,int r)
     r = (r\%m + m)\%m:
     return _fd(a-r,m)*m+r;
```

int _nt(int a,int m,int r)

m=abs(m);

r = (r%m + m)%m;

{

```
return _fd(a-r-1,m)*m+r+m;
}
int _ct(int a,int b,int m,int r)
{
    m=abs(m);
    a=_nt(a,m,r);
    b=_pv(b,m,r);
    return (a>b)?0:((b-a+m)/m);
}
```

5.6 (+1) Miller Rabin

```
3: 2, 7, 61
// n < 4,759,123,141
// n < 1,122,004,669,633
                             4 : 2, 13, 23, 1662803
// n < 3,474,749,660,383
                                   6 : pirmes <= 13
// n < 2^64
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
long long power(long long x,long long p,long long mod){
  long long s=1,m=x;
 while(p) {
    if(p&1) s=mult(s,m,mod);
   m=mult(m,m,mod);
  7
  return s;
bool witness(long long a,long long n,long long u,int t)
  long long x=power(a,u,n);
  for(int i=0;i<t;i++) {</pre>
    long long nx=mult(x,x,n);
    if(nx==1&&x!=1&&x!=n-1) return 1;
    x=nx;
  }
  return x!=1;
bool miller_rabin(long long n,int s=100) {
 // iterate s times of witness on n
    return 1 if prime, 0 otherwise
 if(n<2) return 0;</pre>
  if(!(n&1)) return n==2;
  long long u=n-1;
  int t=0;
  // n-1 = u*2^t
 while(u&1) {
   u>>=1;
    t++;
 while(s--) {
    long long a=randll()%(n-1)+1;
    if(witness(a,n,u,t)) return 0;
  return 1;
```

5.7 Pollard Rho

```
// does not work when n is prime
long long modit(long long x,long long mod) {
 if(x>=mod) x-=mod;
  //if(x<0) x+=mod;
  return x;
long long mult(long long x,long long y,long long mod) {
 long long s=0, m=x%mod;
 while(y) {
   if(y&1) s=modit(s+m,mod);
   y>>=1;
   m=modit(m+m,mod);
 return s;
long long f(long long x,long long mod) {
 return modit(mult(x,x,mod)+1,mod);
long long pollard_rho(long long n) {
 if(!(n&1)) return 2;
 while (true) {
```

```
long long y=2, x=rand()%(n-1)+1, res=1;
for (int sz=2; res==1; sz*=2) {
    for (int i=0; i<sz && res<=1; i++) {
        x = f(x, n);
        res = __gcd(abs(x-y), n);
    }
    y = x;
}
if (res!=0 && res!=n) return res;
}
</pre>
```

5.8 Algorithms about Primes

```
* 12721
 * 13331
 * 14341
 * 75577
 * 123457
 * 222557
 * 556679
 * 999983
 * 1097774749
 * 1076767633
 * 100102021
 * 999997771
 * 1001010013
 * 1000512343
 * 987654361
 * 999991231
 * 999888733
 * 98789101
 * 987777733
 * 999991921
 * 1010101333
 * 1010102101
 * 1000000000039
 * 10000000000000037
 * 2305843009213693951
 * 4611686018427387847
 * 9223372036854775783
 * 18446744073709551557
int mu[MX],p_tbl[MX];
vector<int> primes;
void sieve() {
  mu[1] = p_tbl[1] = 1;
  for (int i=2; i<MX; i++) {</pre>
    if (!p_tbl[i]) {
      p_tbl[i] = i;
      primes.PB(i);
      mu[i] = -1;
    for (auto p : primes) {
      int x = i*p;
      if (x >= M) break;
      p_{tbl}[x] = p;
      mu[x] = -mu[i];
      if (i%p==0) {
        mu[x] = 0;
        break;
      }
    }
  }
}
vector<int> factor(int x) {
  vector<int> fac{1};
  while (x > 1) {
    int fn=SZ(fac), p=p_tbl[x], pos=0;
    while (x%p == 0) {
      x /= p;
      for (int i=0; i<fn; i++)</pre>
        fac.PB(fac[pos++]*p);
    }
  return fac;
```

5.9 (+1) PolynomialGenerator

```
class PolynomialGenerator {
  /* for a nth-order polynomial f(x), *
   * given f(0), f(1), ..., f(n) *
   * express f(x) as sigma_i\{c_i*C(x,i)\} */
  public:
    int n;
    vector<long long> coef;
    // initialize and calculate f(x), vector _fx should
    // filled with f(0) to f(n)
      PolynomialGenerator(int _n,vector<long long> _fx)
           ),coef(_fx) {
        for(int i=0;i<n;i++)</pre>
          for(int j=n;j>i;j--)
            coef[j]-=coef[j-1];
    // evaluate f(x), runs in O(n)
    long long eval(int x) {
      long long m=1,ret=0;
      for(int i=0;i<=n;i++) {</pre>
        ret+=coef[i]*m;
        m=m*(x-i)/(i+1);
      }
      return ret;
|};
```

5.10 Gauss Elimination

```
const int MAX = 300;
const double EPS = 1e-8;
double mat[MAX][MAX];
void Gauss(int n) {
  for(int i=0; i<n; i++) {</pre>
     bool ok = 0;
     for(int j=i; j<n; j++) {</pre>
       if(fabs(mat[j][i]) > EPS) {
         swap(mat[j], mat[i]);
         ok = 1;
         break;
       }
     if(!ok) continue;
     double fs = mat[i][i];
     for(int j=i+1; j<n; j++) {
  double r = mat[j][i] / fs;</pre>
       for(int k=i; k<n; k++) {</pre>
         mat[j][k] -= mat[i][k] * r;
    }
  }
}
```

5.11 Simplex

```
const int maxn = 111;
const int maxm = 111;
const double eps = 1E-10;
double a[maxn][maxm], b[maxn], c[maxm], d[maxn][maxm];
double x[maxm];
int ix[maxn + maxm]; // !!! array all indexed from 0
// max{cx} subject to {Ax<=b,x>=0}
// n: constraints, m: vars !!!
// x[] is the optimal solution vector
//
// usage :
// value = simplex(a, b, c, N, M);
double simplex(double a[maxn][maxm], double b[maxn],
     double c[maxm], int n, int m) {
     ++m;
     int r = n, s = m - 1;
     memset(d, 0, sizeof(d));
for (int i = 0; i < n + m; ++i) ix[i] = i;</pre>
     for (int i = 0; i < n; ++i) {</pre>
         for (int j = 0; j < m - 1; ++j) d[i][j] = -a[i</pre>
              ][j];
         d[i][m-1] = 1;
         d[i][m] = b[i];
          if (d[r][m] > d[i][m]) r = i;
     for (int j = 0; j < m - 1; ++j) d[n][j] = c[j];
d[n + 1][m - 1] = -1;</pre>
     for (double dd;; ) {
         if (r < n) {
              int t = ix[s]; ix[s] = ix[r + m]; ix[r + m]
              d[r][s] = 1.0 / d[r][s];
              for (int j = 0; j <= m; ++j) if (j != s) d[</pre>
                  r][j] *= -d[r][s];
              for (int i = 0; i <= n + 1; ++i) if (i != r
                   ) {
                   for (int j = 0; j <= m; ++j) if (j != s
                       ) d[i][j] += d[r][j] * d[i][s];
                  d[i][s] *= d[r][s];
              }
         }
         r = -1; s = -1;
          for (int j = 0; j < m; ++j) if (s < 0 || ix[s]</pre>
              > ix[j]) {
              if (d[n + 1][j] > eps || (d[n + 1][j] > -
                   eps && d[n][j] > eps)) s = j;
         if (s < 0) break;</pre>
          for (int i = 0; i < n; ++i) if (d[i][s] < -eps)</pre>
              if (r < 0 || (dd = d[r][m] / d[r][s] - d[i</pre>
                  ][m] / d[i][s]) < -eps || (dd < eps &&
ix[r + m] > ix[i + m])) r = i;
          if (r < 0) return -1; // not bounded</pre>
     if (d[n + 1][m] < -eps) return -1; // not</pre>
          executable
     double ans = 0;
     for(int i=0; i<m; i++) x[i] = 0;</pre>
     for (int i = m; i < n + m; ++i) { // the missing</pre>
          enumerated x[i] = 0
          if (ix[i] < m - 1)</pre>
              ans += d[i - m][m] * c[ix[i]];
              x[ix[i]] = d[i-m][m];
          }
     return ans;
}
```

5.12 Theorom

5.12.1 Lucas' Theorem

For non-negative integer n, m and prime p, $\binom{m}{n} \equiv \prod_{i=0}^k \binom{m_i}{n_i} \pmod{p}$ where m_i is the i-th digit of m in base p.

5.12.2 Sum of Two Squares Thm (Legendre)

For a given positive integer n, let $D_1=(\# \text{ of positive integers } d \text{ dividing } N \text{ that } 1\equiv d \pmod 4)$) $D_3=(\# \text{ of positive integers } d \text{ dividing } N \text{ that } 3\equiv d \pmod 4)$) then n can be written as a sum of two squares in exactly $R(n)=4(D_1-D_3)$ ways.

5.12.3 Difference of D1-D3 Thm

```
\begin{array}{l} \mathrm{let}\,n=2^t\cdot(p_1^{e_1}\cdot\ldots\cdot p_r^{e_r})\cdots(q_1^{f_1}\cdot\ldots\cdot q_s^{f_s})\\ \mathrm{where}\,p_i,\,q_i \;\mathrm{are}\,\mathrm{primes}\;\mathrm{and}\;1\equiv p_i \pmod 4, 3\equiv q_i \pmod 4\\ \mathrm{then}\;D_1-D_3=\begin{cases} (\mathbf{e}_1+1)(e_2+1)...(e_r+1), & \mathrm{if}\;(\mathbf{f}_i)\mathrm{s}\;\mathrm{all}\;\mathrm{even}\\ 0, & \mathrm{if}\;\mathrm{any}\;\mathbf{f}_i\;\mathrm{is}\;\mathrm{odd} \end{cases}
```

5.12.4 Krush-Kuhn-Tucker Conditions

Stationarity

```
For maximizing f(x): \nabla f(x^*) = \sum_{i=1}^m \mu_i \nabla g_i(x^*) + \sum_{j=1}^l \lambda_j \nabla h_j(x^*)
For minimizing f(x): -\nabla f(x^*) = \sum_{i=1}^m \mu_i \nabla g_i(x^*) + \sum_{j=1}^l \lambda_j \nabla h_j(x^*)
```

Primal feasibility

```
g_i(x^*) \leq 0, for all i = 1, ..., m
h_j(x^*) = 0, for all j = 1, ..., l
```

Dual feasibility

 $\mu_i \geq 0, \text{ for all } i=1,\dots,m$

Complementary slackness

 $\mu_i g_i(x^*) = 0$, for all i = 1, ..., m

6 Geometry

6.1 Point operators

```
#include<bits/stdc++.h>
using namespace std;
#define _x first
#define _y second
typedef pair<double, double> pdd;
pdd operator + (const pdd p1, const pdd p2){
 return pdd(p1._x + p2._x, p1._y + p2._y);
pdd operator - (const pdd p1, const pdd p2){
  return pdd(p1._x - p2._x, p1._y - p2._y);
pdd operator * (const double c, const pdd p){
 return pdd(p._x * c, p._y * c);
pdd operator - (const pdd p){
  return (-1.0) * p;
double operator * (const pdd p1, const pdd p2){
 return p1._x * p2._x + p1._y * p2._y;
double operator % (const pdd p1, const pdd p2){
  return p1._x * p2._y - p2._x * p1._y;
```

6.2 Intersection of two circles

```
Let {f O}_1=(x_1,y_1), {f O}_2=(x_2,y_2) be two centers of circles, r_1,r_2 be the radius. If: d=|{f O}_1-{f O}_2| {f u}=\frac{1}{2}({f O}_1+{f O}_2)+\frac{(r_2^2-r_1^2)}{2d^2}({f O}_1-{f O}_2) {f v}=\frac{\sqrt{(r_1+r_2+d)(r_1-r_2+d)(r_1+r_2-d)(-r_1+r_2+d)}}{2d^2}(y_1-y_2,-x_1+x_2) then {f u}+{f v},{f u}-{f v} are the two intersections of the circles, provided that d< r_1+r_2.
```

6.3 Intersection of two lines

```
#include < bits / stdc++.h>
using namespace std;
const double EPS = 1e-9;

pdd interPnt(pdd p1, pdd p2, pdd q1, pdd q2) {
    double f1 = (p2 - p1) % (q1 - p1);
    double f2 = (p2 - p1) % (p1 - q2);
    double f = (f1 + f2);

if(fabs(f) < EPS) return pdd(nan(""), nan(""));

return (f2 / f) * q1 + (f1 / f) * q2;
}</pre>
```

6.4 Half Plane Intersection

#include<bits/stdc++.h>

```
using namespace std;
#define PB push_back
#define SZ(x) ((int)(x).size())
#define ALL(x) begin(x), end(x)
#define F first
#define S second
#define x first
#define y second
#define IOS ios::sync_with_stdio(0);cin.tie(0)
const double EPS = 1E-9;
struct point : public pair<double, double> {
    point() {}
    point(double _x, double _y) : pair<double, double>(
        _x, _y) {
    point operator + (const point he) const {
        return {x+he.x, y+he.y};
    }
    point operator - (const point he) const {
        return {x-he.x, y-he.y};
    friend point operator * (const double c, const
        point &p) {
        return {c*p.x, c*p.y};
    point operator * (const double c) const {
        return {c*x, c*y};
    double operator * (const point he) const {
        return x*he.x + y*he.y;
    double cross (const point &he) const {
        return x*he.y - y*he.x;
    friend ostream& operator << (ostream& o, const</pre>
        point &p) {
        cout << "(" << p.x << ", " << p.y << ")";
        return o;
    }
```

```
typedef pair<point, point> Line;
point interPnt(Line l1, Line l2, bool &res){
    point p1, p2, q1, q2;
    tie(p1, p2) = l1;
    tie(q1, q2) = l2;
  double f1 = (p2 - p1).cross(q1 - p1);
 double f2 = (p2 - p1).cross(p1 - q2);
 double f = (f1 + f2);
    if(fabs(f) < EPS) {</pre>
        res = false;
        return {0, 0};
   }
   res = true:
 return (f2 / f) * q1 + (f1 / f) * q2;
bool isin(Line l0, Line l1, Line l2) {
   // Check inter(l1, l2) in l0
   bool res;
    point p = interPnt(l1, l2, res);
    return (l0.S - l0.F).cross(p - l0.F) > 1e-9;
}
/* If no solution, check: 1. ret.size() < 3</pre>
* Or more precisely, 2. interPnt(ret[0], ret[1])
* in all the lines. (use (l.S - l.F).cross(p - l.F) >
*/
vector<Line> halfPlaneInter(vector<Line> lines) {
   int sz = lines.size();
    vector<double> ata(sz), ord(sz);
    for (int i=0; i<sz; i++) {</pre>
        ord[i] = i;
        point d = lines[i].S - lines[i].F;
        ata[i] = atan2(d.y, d.x);
    sort(ALL(ord), [&](int i, int j) {
        return ata[i] < ata[j];</pre>
    });
    vector<Line> fin;
    for (int i=0; i<sz; i++) {</pre>
        if (i and fabs(ata[ord[i]] - ata[ord[i-1]]) <</pre>
            EPS) {
            Line li = lines[ord[i]];
            Line lj = lines[ord[i-1]];
            if ((li.S - li.F).cross(lj.S - li.F) >= 0)
                continue;
            else
                fin.back() = li;
        } else {
            fin.PB(lines[ord[i]]);
   }
    deque<Line> dq;
    for (int i=0; i<SZ(fin); i++) {</pre>
        while(SZ(dq) >= 2 and
              not isin(fin[i], dq[SZ(dq)-2], dq[SZ(dq)
                  -1])) {
            dq.pop_back();
        while(SZ(dq) >= 2 and
              not isin(fin[i], dq[0], dq[1])) {
            dq.pop_front();
        dq.push_back(fin[i]);
    }
    while (SZ(dq) >= 3 and
           not isin(dq[0], dq[SZ(dq)-2], dq[SZ(dq)-1]))
        dq.pop_back();
    }
    while (SZ(dq) >= 3 and
           not isin(dq[SZ(dq)-1], dq[0], dq[1])) {
        dq.pop_front();
    }
```

```
vector<Line> res(SZ(dq));
copy(ALL(dq), res.begin());
return res;
```

6.5 Convex Hull

}

```
double cross(pdd o, pdd a, pdd b){
  return (a-o) % (b-o);
vector<pdd> convex_hull(vector<pdd> pt){
  sort(pt.begin(),pt.end());
  int top=0;
  vector<pdd> stk(2*pt.size());
  for (int i=0; i<(int)pt.size(); i++){</pre>
    while (top >= 2 && cross(stk[top-2],stk[top-1],pt[i
        ]) <= 0)
      top--;
    stk[top++] = pt[i];
  for (int i=pt.size()-2, t=top+1; i>=0; i--){
    while (top >= t && cross(stk[top-2],stk[top-1],pt[i
        ]) <= 0)
      top--:
    stk[top++] = pt[i];
  stk.resize(top-1);
  return stk;
```

6.6 Minimum Covering Circle

```
struct Mcc{
  // return pair of center and r^2
  static const int MAXN = 1000100;
  int n:
  pdd p[MAXN],cen;
  double r2;
  void init(int _n, pdd _p[]){
    n = _n;
    memcpy(p,_p,sizeof(pdd)*n);
  double sqr(double a){ return a*a; }
  double abs2(pdd a){ return a*a; ]
  pdd center(pdd p0, pdd p1, pdd p2) {
    pdd a = p1-p0;
    pdd b = p2-p0;
    double c1=abs2(a)*0.5;
    double c2=abs2(b)*0.5;
    double d = a % b;
    double x = p0.x + (c1 * b.y - c2 * a.y) / d;
double y = p0.y + (a.x * c2 - b.x * c1) / d;
    return pdd(x,y);
  }
  pair<pdd,double> solve(){
    random_shuffle(p,p+n);
    for (int i=0; i<n; i++){</pre>
      if (abs2(cen-p[i]) <= r2) continue;</pre>
      cen = p[i];
      r2 = 0;
       for (int j=0; j<i; j++){</pre>
         if (abs2(cen-p[j]) <= r2) continue;</pre>
         cen = 0.5 * (p[i]+p[j]);
         r2 = abs2(cen-p[j]);
         for (int k=0; k<j; k++){</pre>
           if (abs2(cen-p[k]) <= r2) continue;</pre>
           cen = center(p[i],p[j],p[k]);
           r2 = abs2(cen-p[k]);
    }
    return {cen,r2};
}mcc;
```

(+1) KDTreeAndNearestPoint

```
const INF = 11000000000:
class NODE{ public:
  int x,y,x1,x2,y1,y2;
  int i,f;
 NODE *L,*R;
inline long long dis(NODE& a,NODE& b){
  long long dx=a.x-b.x;
  long long dy=a.y-b.y;
  return dx*dx+dy*dy;
NODE node[100000];
bool cmpx(const NODE& a,const NODE& b){ return a.x<b.x;</pre>
bool cmpy(const NODE& a,const NODE& b){ return a.y<b.y;</pre>
     }
NODE* KDTree(int L,int R,int dep){
 if(L>R) return 0;
  int M=(L+R)/2;
  if(dep%2==0){
    nth_element(node+L,node+M,node+R+1,cmpx);
    node[M].f=0;
 }else{
   nth_element(node+L,node+M,node+R+1,cmpy);
    node[M].f=1;
 node[M].x1=node[M].x2=node[M].x;
 node[M].y1=node[M].y2=node[M].y;
  node[M].L=KDTree(L,M-1,dep+1);
  if(node[M].L){
    node[M].x1=min(node[M].x1,node[M].L->x1);
    node[M].x2=max(node[M].x2,node[M].L->x2);
    node[M].y1=min(node[M].y1,node[M].L->y1);
    node[M].y2=max(node[M].y2,node[M].L->y2);
 node[M].R=KDTree(M+1,R,dep+1);
 if(node[M].R){
    node[M].x1=min(node[M].x1,node[M].R->x1);
    node[M].x2=max(node[M].x2,node[M].R->x2);
    node[M].y1=min(node[M].y1,node[M].R->y1);
    node[M].y2=max(node[M].y2,node[M].R->y2);
  }
  return node+M;
inline int touch(NODE* r, int x, int y, long long d){
  long long d2;
  d2 = (long long)(sqrt(d)+1);
  if(x<r->x1-d2 || x>r->x2+d2 || y<r->y1-d2 || y>r->y2+
      d2)
    return 0;
  return 1;
void nearest(NODE* r, int z, long long &md) {
  if(!r || !touch(r,node[z].x,node[z].y,md)) return;
  long long d;
  if(node[z].i!=r->i){
    d=dis(*r,node[z]);
    if(d<md) md=d;</pre>
  if(r->f==0){
    if(node[z].x<r->x){
      nearest(r->L,z,md);
      nearest(r->R,z,md);
    }else{
      nearest(r->R,z,md);
      nearest(r->L,z,md);
  }else{
    if(node[z].y<r->y){
      nearest(r->L,z,md);
      nearest(r->R,z,md);
    }else{
      nearest(r->R,z,md);
      nearest(r->L,z,md);
  }
int main(){
```

```
int TT,n,i;
long long d;
NODE* root;
scanf("%d",&TT);
while(TT--){
  scanf("%d",&n);
  for(i=0;i<n;i++){</pre>
    scanf("%d %d",&node[i].x,&node[i].y);
    node[i].i=i;
  root=KDTree(0,n-1,0);
  for(i=0;i<n;i++){</pre>
    d=90000000000000000000LL;
    nearest(root,i,d);
    ans[node[i].i]=d;
}
```

(+1) MinkowskiSum

```
/* convex hull Minkowski Sum*/
#define INF 1000000000000000LL
class PT{ public:
  long long x,y;
  int POS(){
    if(y==0) return x>0?0:1;
    return y>0?0:1;
PT pt[300000],qt[300000],rt[300000];
long long Lx,Rx;
int dn,un;
inline bool cmp(PT a,PT b){
  int pa=a.POS(),pb=b.POS();
  if(pa==pb) return (a^b)>0;
  return pa<pb;</pre>
int minkowskiSum(int n,int m){
  int i,j,r,p,q,fi,fj;
  for(i=1,p=0;i<n;i++){</pre>
    if(pt[i].y<pt[p].y || (pt[i].y==pt[p].y && pt[i].x<</pre>
          pt[p].x)) p=i; }
  for(i=1,q=0;i<m;i++){</pre>
    if(qt[i].y<qt[q].y || (qt[i].y==qt[q].y && qt[i].x<</pre>
           qt[q].x)) q=i; }
  rt[0]=pt[p]+qt[q];
  r=1; i=p; j=q; fi=fj=0;
  while(1){
    if((fj&&j==q) || ((!fi||i!=p) && cmp(pt[(p+1)%n]-pt
             p],qt[(q+1)%m]-qt[q]))){
      rt[r]=rt[r-1]+pt[(p+1)%n]-pt[p];
      p=(p+1)%n;
      fi=1;
    }else{
      rt[r]=rt[r-1]+qt[(q+1)%m]-qt[q];
      q = (q+1)\%m;
      fj=1;
    if(r<=1 || ((rt[r]-rt[r-1])^(rt[r-1]-rt[r-2]))!=0)
      ++;
    else rt[r-1]=rt[r];
    if(i==p && j==q) break;
  return r-1;
void initInConvex(int n){
  int i,p,q;
  long long Ly,Ry;
  Lx=INF; Rx=-INF;
  for(i=0;i<n;i++){</pre>
    if(pt[i].x<Lx) Lx=pt[i].x;</pre>
    if(pt[i].x>Rx) Rx=pt[i].x;
  Lv=Rv=INF:
  for(i=0;i<n;i++){</pre>
    if(pt[i].x==Lx && pt[i].y<Ly){ Ly=pt[i].y; p=i; }</pre>
    if(pt[i].x==Rx && pt[i].y<Ry){ Ry=pt[i].y; q=i; }</pre>
```

```
for(dn=0,i=p;i!=q;i=(i+1)%n){ qt[dn++]=pt[i]; }
  qt[dn]=pt[q]; Ly=Ry=-INF;
  for(i=0;i<n;i++){</pre>
    if(pt[i].x==Lx && pt[i].y>Ly){ Ly=pt[i].y; p=i; }
    if(pt[i].x==Rx && pt[i].y>Ry){ Ry=pt[i].y; q=i; }
  for(un=0,i=p;i!=q;i=(i+n-1)%n){ rt[un++]=pt[i]; }
  rt[un]=pt[q];
inline int inConvex(PT p){
  int L,R,M;
  if(p.x<Lx || p.x>Rx) return 0;
  L=0; R=dn;
  while(L<R-1){ M=(L+R)/2;</pre>
    if(p.x<qt[M].x) R=M; else L=M; }</pre>
    if(tri(qt[L],qt[R],p)<0) return 0;</pre>
    L=0;R=un;
    while(L<R-1){ M=(L+R)/2;
      if(p.x<rt[M].x) R=M; else L=M; }</pre>
       if(tri(rt[L],rt[R],p)>0) return 0;
int main(){
  int n,m,i;
  PT p;
  scanf("%d",&n);
  for(i=0;i<n;i++) scanf("%I64d %I64d",&pt[i].x,&pt[i].</pre>
  scanf("%d",&m);
  for(i=0;i<m;i++) scanf("%I64d %I64d",&qt[i].x,&qt[i].</pre>
       y);
  n=minkowskiSum(n,m);
  for(i=0;i<n;i++) pt[i]=rt[i];</pre>
  scanf("%d",&m);
  for(i=0;i<m;i++) scanf("%I64d %I64d",&qt[i].x,&qt[i].</pre>
  n=minkowskiSum(n,m);
  for(i=0;i<n;i++) pt[i]=rt[i];</pre>
  initInConvex(n);
  scanf("%d",&m);
  for(i=0;i<m;i++){</pre>
    scanf("%I64d %I64d",&p.x,&p.y);
    p.x*=3; p.y*=3;
    puts(inConvex(p)?"YES":"NO");
}
```

7 Stringology

7.1 Suffix Array

```
const int MAX = 1020304;
int ct[MAX], he[MAX], rk[MAX], sa[MAX], tsa[MAX], tp[
     MAX][2];
void suffix_array(char *ip){
   int len = strlen(ip);
   int alp = 256;
   memset(ct, 0, sizeof(ct));
   for(int i=0;i<len;i++) ct[ip[i]+1]++;</pre>
   for(int i=1;i<alp;i++) ct[i]+=ct[i-1];</pre>
   for(int i=0;i<len;i++) rk[i]=ct[ip[i]];</pre>
   for(int i=1;i<len;i*=2){</pre>
     for(int j=0;j<len;j++){</pre>
       if(j+i>=len) tp[j][1]=0;
       else tp[j][1]=rk[j+i]+1;
       tp[j][0]=rk[j];
     }
     memset(ct, 0, sizeof(ct));
     for(int j=0;j<len;j++) ct[tp[j][1]+1]++;</pre>
     for(int j=1;j<len+2;j++) ct[j]+=ct[j-1];</pre>
     for(int j=0;j<len;j++) tsa[ct[tp[j][1]]++]=j;</pre>
     memset(ct, 0, sizeof(ct));
     for(int j=0;j<len;j++) ct[tp[j][0]+1]++;
for(int j=1;j<len+1;j++) ct[j]+=ct[j-1];</pre>
     for(int j=0;j<len;j++) sa[ct[tp[tsa[j]][0]]++]=tsa[</pre>
          il:
     rk[sa[0]]=0;
     for(int j=1;j<len;j++){</pre>
       if( tp[sa[j]][0] == tp[sa[j-1]][0] &&
          tp[sa[j]][1] == tp[sa[j-1]][1] )
         rk[sa[j]] = rk[sa[j-1]];
       else
         rk[sa[j]] = j;
     }
   for(int i=0,h=0;i<len;i++){</pre>
     if(rk[i]==0) h=0;
     else{
       int j=sa[rk[i]-1];
       h=max(0,h-1);
       for(;ip[i+h]==ip[j+h];h++);
     he[rk[i]]=h;
   }
}
```

7.2 Suffix Array (SAIS TWT514)

```
struct SA{
#define REP(i,n) for ( int i=0; i<int(n); i++ )</pre>
#define REP1(i,a,b) for ( int i=(a); i<=int(b); i++ )
    static const int MXN = 300010;
    bool _t[MXN*2];
    int _s[MXN*2], _sa[MXN*2], _c[MXN*2], x[MXN], _p[
        MXN], _q[MXN*2], hei[MXN], r[MXN];
    int operator [] (int i){ return _sa[i]; }
    void build(int *s, int n, int m){
        memcpy(_s, s, sizeof(int) * n);
        sais(_s, _sa, _p, _q, _t, _c, n, m);
        mkhei(n);
    void mkhei(int n){
        REP(i,n) r[\_sa[i]] = i;
        hei[0] = 0;
        REP(i,n) if(r[i]) {
             int ans = i>0 ? max(hei[r[i-1]] - 1, 0) :
             while(_s[i+ans] == _s[_sa[r[i]-1]+ans]) ans
                 ++;
             hei[r[i]] = ans;
        }
    void sais(int *s, int *sa, int *p, int *q, bool *t,
         int *c, int n, int z){
        bool uniq = t[n-1] = true, neq;
        int nn = 0, nmxz = -1, *nsa = sa + n, *ns = s +
             n, lst = -1;
#define MSO(x,n) memset((x),0,n*sizeof(*(x)))
#define MAGIC(XD) MS0(sa, n); \
        memcpy(x, c, sizeof(int) * z); \
        memcpy(x + 1, c, sizeof(int) * (z - 1)); \setminus
        REP(i,n) if(sa[i] \&\& !t[sa[i]-1]) sa[x[s[sa[i]-1]]
             ]-1]]++] = sa[i]-1; \
        memcpy(x, c, sizeof(int) * z); \
for(int i = n - 1; i >= 0; i--) if(sa[i] && t[
             sa[i]-1]) sa[--x[s[sa[i]-1]]] = sa[i]-1;
        MSO(c, z);
        REP(i,n) uniq &= ++c[s[i]] < 2;
        REP(i,z-1) c[i+1] += c[i];
        if (uniq) { REP(i,n) sa[--c[s[i]]] = i; return;
        for(int i = n - 2; i >= 0; i--) t[i] = (s[i]==s
             [i+1] ? t[i+1] : s[i] < s[i+1]);
        MAGIC(REP1(i,1,n-1) if(t[i] && !t[i-1]) sa[--x[
             s[i]]]=p[q[i]=nn++]=i);
        REP(i, n) if (sa[i] && t[sa[i]] && !t[sa[i]-1])
             {
             neq=lst<0||memcmp(s+sa[i],s+lst,(p[q[sa[i</pre>
                 ]]+1]-sa[i])*sizeof(int));
             ns[q[lst=sa[i]]]=nmxz+=neq;
        sais(ns, nsa, p + nn, q + n, t + n, c + z, nn,
             nmxz + 1);
        MAGIC(for(int i = nn - 1; i >= 0; i--) sa[--x[s]]
             [p[nsa[i]]]] = p[nsa[i]]);
    }
}sa;
void suffix_array(int* ip, int len) {
    // should padding a zero in the back
    // s is int array, n is array length
    // s[0..n-1] != 0, and s[n] = 0
    // resulting SA will be length n+1
    ip[len++] = 0;
    sa.build(ip, len, 128);
    // original 1-base
    for (int i=0; i<l; i++) {</pre>
        hei[i] = sa.hei[i + 1];
        sa[i] = sa.\_sa[i + 1];
    }
}
```

7.3 Aho-Corasick Algorithm

```
struct ACautomata{
  struct Node{
    int cnt,dp;
     Node *go[26], *fail;
     Node (){
       cnt = 0;
       dp = -1;
      memset(go,0,sizeof(go));
       fail = 0;
    }
  };
  Node *root, pool[1048576];
  int nMem;
  Node* new_Node(){
     pool[nMem] = Node();
     return &pool[nMem++];
  void init(){
    nMem = 0;
     root = new_Node();
  void add(const string &str){
     insert(root,str,0);
  void insert(Node *cur, const string &str, int pos){
     if (pos >= (int)str.size()){
       cur->cnt++;
       return;
     int c = str[pos]-'a';
     if (cur->go[c] == 0){
      cur->go[c] = new_Node();
     insert(cur->go[c],str,pos+1);
  void make_fail(){
     queue<Node*> que;
     que.push(root);
     while (!que.empty()){
       Node* fr=que.front();
       que.pop();
       for (int i=0; i<26; i++){</pre>
         if (fr->go[i]){
           Node *ptr = fr->fail;
           while (ptr && !ptr->go[i]) ptr = ptr->fail;
           if (!ptr) fr->go[i]->fail = root;
           else fr->go[i]->fail = ptr->go[i];
           que.push(fr->go[i]);
    }
};
7.4 Z value
void Z_value(char *s, int *z, int len) {
  int i,j,left,right;
  left=right=0; z[0]=len;
  for(i=1;i<len;i++)</pre>
     j=max(min(z[i-left],right-i),0);
     for(;i+j<len&&s[i+j]==s[j];j++);</pre>
     z[i]=j;
     if(i+z[i]>right) {
       right=i+z[i];
```

left=i;

}

}

}

7.5 Z value (palindrome ver.)

```
const int MAX = 1000;
int len;
char ip[MAX];
char op[MAX*2];
int zv[MAX*2];
int main(){
  cin >> ip;
  len = strlen(ip);
  int l2 = len*2 - 1;
 for(int i=0; i<l2; i++){
  if(i&1) op[i] = '@';</pre>
    else op[i] = ip[i/2];
 int l=0, r=0;
 zv[0] = 1;
  for(int i=1; i<l2; i++){</pre>
    if( i > r ){
      l = r = i;
      while( l>0 && r<l2-1 && op[l-1] == op[r+1] ){</pre>
        l --;
        r ++;
      zv[i] = (r-l+1);
    }else{
      int md = (l+r)/2;
      int j = md + md - i;
      zv[i] = zv[j];
      int q = zv[i] / 2;
      int nr = i + q;
      if( nr == r ){
        l = i + i - r;
        while( l>0 && r<l2-1 && op[l-1] == op[r+1] ){</pre>
          l --;
        zv[i] = r - l + 1;
      }else if( nr > r ){
        zv[i] = (r - i) * 2 + 1;
    }
 }
  return 0;
```

7.6 Lexicographically Smallest Rotation

```
string mcp(string s){
  int n = s.length();
  s += s;
  int i=0, j=1, k=0;
  while (j<n && k<n){
    if (s[i+k] == s[j+k]) k++;
    else {
      if (s[i+k] < s[j+k]) {
        j += k + 1;
      } else {
        i = j;
        j = max(j+1, j+k);
      k = 0;
    }
  }
  return s.substr(i, n);
}
```

7.7 Suffix Automaton

```
/// par : fail link
// val : a topological order ( useful for DP )
```

```
// go[x] : automata edge ( x is integer in [0,26) )
struct SAM{
  struct State{
    int par, go[26], val;
State () : par(0), val(0){ FZ(go); }
    State (int _val) : par(0), val(_val){ FZ(go); }
  vector<State> vec:
  int root, tail;
  void init(int arr[], int len){
    vec.resize(2);
    vec[0] = vec[1] = State(0);
    root = tail = 1;
    for (int i=0; i<len; i++)</pre>
      extend(arr[i]);
  void extend(int w){
    int p = tail, np = vec.size();
    vec.PB(State(vec[p].val+1));
    for ( ; p && vec[p].go[w]==0; p=vec[p].par)
      vec[p].go[w] = np;
    if (p == 0){
      vec[np].par = root;
    } else {
      if (vec[vec[p].go[w]].val == vec[p].val+1){
        vec[np].par = vec[p].go[w];
      } else {
         int q = vec[p].go[w], r = vec.size();
         vec.PB(vec[q]);
        vec[r].val = vec[p].val+1;
        vec[q].par = vec[np].par = r;
        for ( ; p && vec[p].go[w] == q; p=vec[p].par)
           vec[p].go[w] = r;
      }
    }
    tail = np;
  }
};
```

8 Problems

8.1 Find the maximun tangent (x,y is increasing)

```
typedef long long LL;
const int MAXN = 100010;
struct Coord{
  LL x, y;
  Coord operator - (Coord ag) const{
    Coord res;
    res.x = x - ag.x;
    res.y = y - ag.y;
    return res;
 }
}sum[MAXN], pnt[MAXN], ans, calc;
inline bool cross(Coord a, Coord b, Coord c){
  return (c.y - a.y) * (c.x - b.x) > (c.x - a.x) * (c.y)
        - b.y);
}
int main(){
  int n, l, np, st, ed, now;
scanf("%d %d\n", &n, &l);
  sum[0].x = sum[0].y = np = st = ed = 0;
  for (int i = 1, v; i <= n; i++){</pre>
    scanf("%d", &v);
    sum[i].y = sum[i - 1].y + v;
    sum[i].x = i;
  ans.x = now = 1;
  ans.y = -1;
  for (int i = 0; i <= n - l; i++){
  while (np > 1 && cross(pnt[np - 2], pnt[np - 1],
         sum[i]))
      np--;
    if (np < now && np != 0) now = np;
```

8.2 Orange Protection

```
* Given a Tree and the power of every node.
 * Each Node can protect the nodes whose distance <=
     cover[i] with it
* output the number of each node that it can protect.
const int MXN = 100005;
int cover[MXN], ans[MXN];
int N, ok[MXN];
int fr,bk,que[MXN],vst[MXN],dis[MXN],fa[MXN],sz[MXN];
vector<int> E[MXN];
int bit[MXN];
int lb(int a){ return a & -a; }
void reset_bit(int st){
  for (int i = st+1; i < MXN; i+=lb(i))</pre>
   bit[i] = 0;
void update(int st){
  for (int i = st+1; i < MXN; i+=lb(i))</pre>
   bit[i]++;
int query(int st, int ret = 0){
 for (int i = st+1; i > 0; i-=lb(i))
   ret += bit[i];
  return ret;
void BFS(int st){
 fr = bk = 0;
  que[bk++] = st;
 vst[st] = 1;
 dis[st] = 0;
 while (fr < bk){</pre>
    int u = que[fr++];
    for (auto v : E[u]){
      if (!ok[v] || vst[v]) continue;
      vst[v] = 1;
      dis[v] = dis[u] + 1;
      fa[v] = u;
      que[bk++] = v;
   }
  for (int i=0; i<bk; i++)</pre>
   vst[que[i]] = 0;
int find_centroid(int st){
  int ret=-1, cnt=MXN+100;
  BFS(st);
  for (int i = bk-1; i>=0; i--){
   int u = que[i], mx = 0;
    sz[u] = 1;
    for (auto v : E[u]){
      if (!ok[v] || v == fa[u]) continue;
      sz[u] += sz[v];
      mx = max(mx, sz[v]);
    mx = max(mx, bk-sz[u]);
    if (mx < cnt){</pre>
      ret = u;
```

```
cnt = mx:
    }
  }
  return ret:
}
void solve(int u){
  int root = find_centroid(u);
  ok[root] = 0;
  for (auto v : E[root])
    if (ok[v]) solve(v);
  for (auto v : E[root]){
    if (!ok[v]) continue;
    BFS(v);
    for (int i=0; i<bk; i++){</pre>
      dis[que[i]]++;
      update(dis[que[i]]);
    for (int i=0; i<bk; i++){</pre>
      int it = que[i];
      ans[it] -= query(cover[it] - dis[it]);
    for (int i=0; i<bk; i++)</pre>
      reset_bit(dis[que[i]]);
  BFS(root);
  for (int i=0; i<bk; i++) update(dis[que[i]]);</pre>
  for (int i=0; i<bk; i++){</pre>
    int v = que[i];
    ans[v] += query(cover[v] - dis[v]);
  for (int i=0; i<bk ;i++) reset_bit(dis[que[i]]);</pre>
  ok[root] = 1;
}
int main(int argc, char** argv){
  scanf("%d", &N);
  for (int i=0; i<N; i++){</pre>
    scanf("%d", &cover[i]);
    cover[i] = min(cover[i], N);
  for (int i=0,u,v; i<N-1; i++){</pre>
    scanf("%d%d", &u, &v);
    E[u].PB(v);
    E[v].PB(u);
  fill(ok,ok+N,1);
  FZ(vst); FZ(ans); FZ(bit);
  solve(0);
  for (int i=0; i<N; i++)</pre>
   printf("%d \ n", ans[i]);
  return 0;
```