# Machine Learning for Economists and Business Analysts

Anthony Strittmatter

## Lecturer

## **Anthony Strittmatter**

**Research Interests:** Business, Labour, and Health Economics, Program Evaluation, Computational Data Analytics

#### Positions:

Since 2020	Assistant Professor at the Institut Polytechnique in Paris,
	Center for Research in Economics and Statistics (CREST)
2014-2020	University of St. Gallen, with research visits at UC Berke-
	ley, Stanford University, and Ludwig Maximilian University
	of Munich
2009-2016	Albert-Ludwig University of Freiburg

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## **Course Outline**

- ► Lecture 1: Introduction to Statistical Learning
  - Out-of-Sample Prediction
  - Prediction vs. Causal Analysis
- ► Lecture 2: Regularized Regression
  - Lasso, Ridge, Elastic Net
- ► **Lecture 3:** Non-parametric Supervised Machine Learning
  - ► Classification and Regression Trees
  - Forests
- Lecture 4: High-Dimensional Confounding
  - Double Selection Procedure
  - Double Machine Learning

## **Schedule**

	Wednesday	Thursday	Friday
	June 23	June 24	June 25
#1	9:15-10:45	9:15-10:45	9:15-10:45
#2	11:00-12:30	11:00-12:30	11:00-12:30
#3	14:15-15:45	14:15-15:45	14:15-15:45

## **PC Labs**

- PC labs are integral part of the course.
- ► I will provide the entire course material on my GitHub repository: https://github.com/AStrittmatter/RTG-2484-Mini-Course
- ▶ I will use interactive Jupyter notebooks during the PC labs: https://mybinder.org/v2/gh/AStrittmatter/RTG-2484-Mini-Course/HEAD
- ► The advantage of the notebooks is that you do not need to install anything and the data is in the correct folder.
- ▶ However, in case the connection to the server is weak I also provide an R-file for download on my GitHub repository. To use it, you need to install R and RStudio on your PC. This are both open source softwares.

## **Participation Certificate**

- ► Home assignment after the course.
- ▶ Deadline for submission: Friday, July 25, 2021

## **General**

- ▶ Feel free to interrupt me at any time when you have questions.
- ► Tell me when I'm too slow or too fast. Ask me to repeat material in case something was not clear.
- You can also send me an email with questions: anthony.strittmatter@ensae.fr
- Proposals to improve the course are also welcome.
- ▶ Please try to interact as much as possible with your fellow students. Build learning groups.

## References

- Mullainathan and Spiess (2017): "Machine Learning: An Applied Econometric Approach", Journal of Economic Perspectives, 31 (2), pp. 87-106, download.
- ► Athey (2017): "Beyond Prediction: Using Big Data for Policy Problems", Science, 355 (6324), pp. 483-485, download.

# What is Machine Learning (ML)?

- ▶ ML (or statistical learning) methods exist already since decades.
- Currently "Machine Learning" is a buzz word
- Probably most people think of ML as some computational intensive methods that make data-driven modelling decisions and/or can deal with large data amounts.
- However, relevant textbooks consider even OLS/Logit as a statistical learning tool.

# **Purpose of Machine Learning**

Consider the structural model

$$Y = f(X) + \epsilon = X\beta + \epsilon,$$

with  $E[\epsilon] = 0$ .

- Causal analysis has the purpose to estimate  $\hat{\beta}$ , with  $plim(\hat{\beta}) = \beta$ .
- ▶ Machine learning has the purpose to predict *Y*.
- There is a clear link between causal analysis and machine learning, because

$$\widehat{Y} = \widehat{f}(X) = X\widehat{\beta}$$

is a potential predictor for Y.

▶ Parameter consistency has not the highest priority when it comes to predictions.

# Potential Advantages and Disadvantages of ML

- ▶ ML methods can be very powerful to predict Y, even when  $\hat{\beta}$  is biased.
- ► ML methods can incorporate many (or even high-dimensional) covariates *X* in a convenient way.
- lacktriangle ML methods can model  $\hat{f}(\cdot)$  in a very flexible and data-driven way.
- ▶ Main disadvantage: ML is a black-box approach and we loose the interpretability of  $\hat{f}(\cdot)$  or  $\hat{\beta}$ .

# **Prediction vs. Causality**



## Causal vs. Predictive Questions

#### **Predictive Questions:**

- ► How will the oil price change tomorrow (forecasting)?
- How high is the current unemployment rate (nowcasting)?
- Which adolescents have a high probability of becoming addicted to drugs (policy prediction)?

#### **Causal Questions:**

- What is the effect of a tweet by president Donald Trump on oil prices?
- How does inflation affect the unemployment rate?
- Can prevention programs reduce the probability of drug addiction among high risk youths?

# **Assessing the Model Accuracy**

## Causal Analysis:

- ightharpoonup True  $\beta$  is unobservable.
- ► Assess the model with asymptotic properties

$$\sqrt{N}(\hat{\beta}-\beta) \stackrel{d}{\rightarrow} N(0,\sigma^2).$$

Finite sample biases are mostly neglected.

# **Assessing the Model Accuracy**

#### **Prediction:**

- ▶ We observe *Y* for each unit (e.g. individual).
- We can assess the model accuracy directly in the sample of our analysis, for example, using the mean-squared-error (MSE)

$$\frac{1}{N}\sum_{i=1}^{N}(Y_i-\hat{Y}_i)^2.$$

MSE accounts for finite sample biases.

## **Example: Prediction of Used Car Prices**

- ▶ We have access to web-scraped data from the online advertisement platform *myLemons*.
- We want to predict asking prices of used cars based on observable characteristics.
- ► We observe around 40 covariates about car brand, mileage, age, emissions, maintenance certificate, seller type, guarantee, etc. (including several non-linear and interaction terms)

# In-Sample MSE

- Partition data into training and test sample
- ▶ In the training sample, we estimate the empirical model

$$Y_{tr} = \hat{f}_{tr}(X_{tr}) + \hat{\epsilon}_{tr} = X_{tr}\hat{\beta}_{tr} + \hat{\epsilon}_{tr}$$

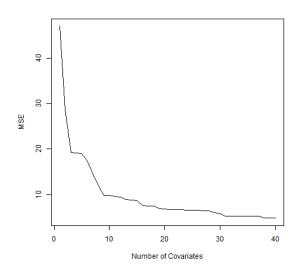
In the training sample, we predict the fitted values

$$\widehat{Y}_{tr} = \widehat{f}_{tr}(X_{tr}) = X_{tr}\widehat{\beta}_{tr}$$

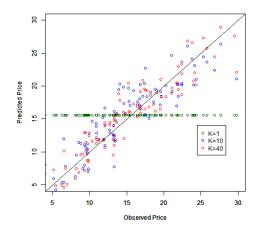
and calculate the MSE

$$\widehat{MSE}_{tr} = \frac{1}{N_{tr}} \sum_{i=1}^{N_{tr}} (Y_{i,tr} - \widehat{Y}_{i,tr})^2.$$

# **MSE** in Training Sample



## **Predicted Car Prices in Training Sample**



Number of Covariates	1	10	40
MSE	46.948	9.819	4.866

# **Out-of-Sample MSE**

In the training sample, we estimate the empirical model

$$Y_{tr} = \hat{f}_{tr}(X_{tr}) + \hat{\epsilon}_{tr} = X_{tr}\hat{\beta}_{tr} + \hat{\epsilon}_{tr}$$

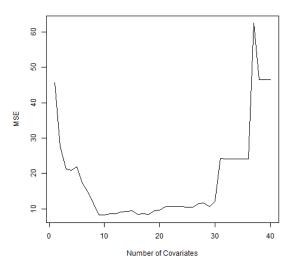
In the test sample, we predict the fitted values

$$\widehat{Y}_{te} = \widehat{f}_{tr}(X_{te}) = X_{te}\widehat{\beta}_{tr}$$

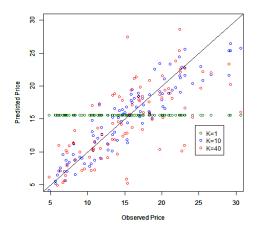
and calculate the MSE

$$\widehat{\mathit{MSE}}_{te} = \frac{1}{\mathit{N}_{te}} \sum_{i=1}^{\mathit{N}_{te}} (Y_{i,te} - \widehat{Y}_{i,te})^2.$$

# **MSE** in Test Sample



# **Predicted Car Prices in Test Sample**



Number of Covariates	1	10	40
MSE	45.742	8.222	46.499

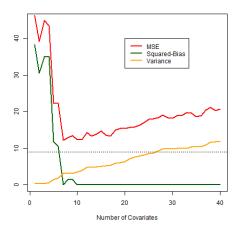
## **Bias-Variance Trade-Off**

▶ When we assess the model for one randomly drawn individual from the test sample with fixed characteristics x<sub>te</sub>, then we can decompose the MSE to

$$\begin{split} MSE_{te} = & E[(Y_{te} - \hat{Y}_{te})^2] \\ = & E[(f(x_{te}) + \epsilon_{te} - \hat{f}_{tr}(x_{te}))^2] \\ = & \underbrace{E[(f(x_{te}) - \hat{f}_{tr}(x_{te}))^2]}_{\text{Reducible}} + \underbrace{Var(\epsilon_{te})}_{\text{Irreducible}} \\ = & \underbrace{E[f(x_{te}) - \hat{f}_{tr}(x_{te})]^2}_{\text{Squared-Bias}} + \underbrace{Var(\hat{f}_{tr}(x_{te}))}_{\text{Variance}} + Var(\epsilon_{te}) \end{split}$$

▶ For i.i.d. data,  $\hat{f}_{tr}(\cdot)$  and  $\epsilon_{te}$  are independent of each other.

## Simulation of Bias-Variance Trade-Off



- Only the first ten covariate have an impact on car prices in the simulation.
- ▶ Horizontal dashed line is the simulated noise  $Var(\epsilon_{te})$ .

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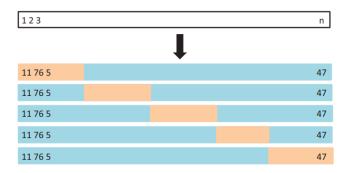
## Lasso Example

$$\arg\min_{\beta} \left\{ \sum_{i=1}^{N} \left( Y_i - \beta_0 - \sum_{j=1}^{p} X_{ij} \beta_j \right)^2 + \lambda \sum_{j=1}^{p} |\beta_j| \right\}$$

	OLS	Lasso
Intercept	21.246	22.776
diesel	2.075	
other_car_owner	0.730	
pm_green	1.635	
private_seller	6.100	0.076
guarantee	-2.440	-0.437
inspection	-0.813	
maintenance_cert	1.481	
mileage	-0.049	-0.031
age_car_years	-1.291	-1.012
$R^2$ training	0.655	0.543
$R^2$ test	0.606	0.611

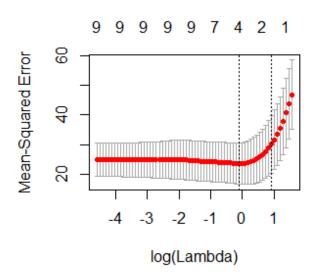
## **Selection of Optimal Penalty Parameter**

## k-fold Cross-Validation (CV) Algorithm



Source: James et al. (2013), p. 181

## **Cross-Validated MSE**



# Stability of the Lasso Model

	Lasso 1	Lasso 2	Lasso 3	Lasso 4	Lasso 5
Intercept	22.776	25.947	24.937	27.309	25.116
diesel			2.387		0.886
other_car_owner		-1.257	0.393		•
pm_green	•	2.871		•	
private_seller	0.076	5.094	•	-1.037	
guarantee	-0.437	1.677	15.939	•	•
inspection	•	-0.666	-0.374	•	•
maintenance_cert	•	-2.579	-0.868	•	•
mileage	-0.031	-0.037	-0.041	-0.069	-0.062
age_car_years	-1.012	-1.347	-1.416	-0.874	-1.115

 $\rightarrow$  ML is a black-box approach

<sup>→</sup> We do not learn the "true" structural model from ML

## **Stability of the Lasso Predictions**

## Correlation of Predicted Car Prices in Test Sample:

Lasso 2 0.94 Lasso 3 0.85 0.81 Lasso 4 0.97 0.91 0.85 Lasso 5 0.99 0.94 0.87 0.99		Lasso 1	Lasso 2	Lasso 3	Lasso 4
Lasso 4 0.97 0.91 0.85	Lasso 2	0.94			
	Lasso 3	0.85	0.81		
Lasso 5 0.99 0.94 0.87 0.99	Lasso 4	0.97	0.91	0.85	
24350 5 0.55 0.54 0.07 0.95	Lasso 5	0.99	0.94	0.87	0.99

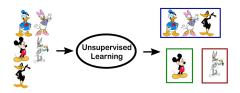
# Supervised vs. Unsupervised Machine Learning

## **Supervised Machine Learning:**

- We observe data on Y and X and want to learn the mapping  $\widehat{Y} = \widehat{f}(X)$
- lacktriangle Classification when  $\widehat{Y}$  is discrete, regression when  $\widehat{Y}$  is continuous

## **Unsupervised Machine Learning:**

- We observe only data on X and want to learn something about its structure
- Clustering: Partition data into homogeneous groups based on X



Principal component analysis

## **Examples of Business and Economic Studies**

#### **Prediction Tasks:**

- ► <u>Chandler, Levitt, and List (2011)</u> predict shootings among high-risk youth to target mentoring interventions.
- ► <u>Kleinberg, et al. (2018)</u> predict the crime probability of defendants released from investigative custody to improve judge decisions.

## **Pre-Processing Unstructured Data:**

- ► Glaeser et al. (2016) use images from Google Street View to measure block-level income in New York City and Boston.
- ► Kang et al. (2013) use restaurant reviews on Yelp.com to predict the outcome of hygiene inspections.
- ► Kogan et al. (2009) predict volatility of firms from market-risk disclosure texts (annual 10-K forms).

## Predictions vs. Causal Inference

- ► Outcome (e.g., earnings): Y
- ▶ Binary Treatment (e.g., participation in training program):  $D \in \{0,1\}$
- Potential Outcome:
  - $\triangleright$  Y(1) potential earnings under participation
  - $\triangleright$  Y(0) potential earnings under non-participation
  - ightarrow Only one potential earnings can be observed
- ▶ Causal effect:  $\delta = Y(1) Y(0)$
- ightarrow Predictions have the observable estimation target  $\widehat{Y}$
- ightarrow Causal inference has the (partly) unobservable estimation target  $\widehat{\delta}$

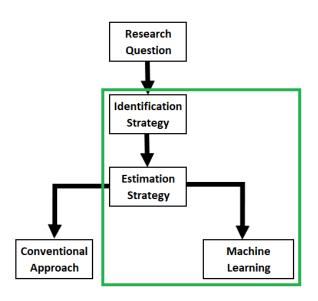
## **Training of ML Algorithms**

Out-of-Sample Mean-Squared-Error (MSE):

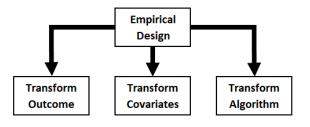
$$MSE_{\hat{\delta}} = E\left[(\hat{\delta} - \delta)^2\right] = \underbrace{E\left[(\hat{\delta} - E[\hat{\delta}])^2\right]}_{\text{Variance}} + \underbrace{E[\hat{\delta} - \delta]^2}_{\text{Squared Bias}}$$

 $\rightarrow \delta$  is unobservable

## Research Design



# Causal Machine Learning (CML) Designs



 $\Rightarrow$  Knaus, Lechner, Strittmatter (2018) provide a comparison of all designs.

## Four potential applications of CML:

- 1. Account for (very) many instruments in IV or Heckit approach (prediction problem, issues with inference).

  References:
  - ▶ Belloni, Chen, Chernozhukov, and Hansen (2012)
  - ► Hansen and Kozbur (2014)
- 2. Account for confounders, e.g., in matching, IV, or difference-in-difference approaches:
  - ► ML enables the incorporation of (very) many covariates which can make the exclusion restriction more credible
  - ► Some ML approaches make little functional form assumptions.

#### Reference:

► Chernozhukov et al. (2017)

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- 3. Heterogeneous effects:
  - Principled approach makes it less likely to overlook important heterogeneity.
  - Problems: Issues with interpretability and works only for the low-dimensional case.

#### References:

- ► Wager and Athey (2018)
- ► Chernozhukov, Demirer, Duflo, and Fernéndez-Val (2018)
- 4. Optimal policy rules (e.g. Bandits):
  - ► Focus on the (discrete) treatment decision instead on the effect size.

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## **Limitations of Causal Machine Learning (CML)**

- ML algorithms cannot distinguish between causation and correlation.
  - ightarrow CML will not select the relevant causal parameters automatically.
  - $\rightarrow$  We have to provide some structure to the CML algorithm.
- ► CML can estimate causal effects only for a few (usually only one) endogenous variables.
  - $\rightarrow$  We will not obtain the (complete) structural model.
- Identifying assumptions do not change, no matter if we use ML or conventional methods.
- We should resist the temptation to interpret prediction models in a causal way.

## **Applications of CML Methods**

- ▶ Davis and Heller (2017) investigate the effects of summer jobs on the probability to commit a violent crime.
- ► Taddy et al. (2016) investigate the heterogeneous effects of A/B-experiments in online-auctions (EBay) on customer responses (experimental study).
- ▶ Bertrand et al. (2017) and Knaus, Lechner, and Strittmatter (2020) estimate heterogeneous employment effects of training programmes for unemployed persons.