



## 4 Beyond Libraries

- Fast development (no compile-link-run cycle)
- Interactive development
- High level (no need to worry about pointers)

# Python

- Powerful builtins
- Object oriented
- Rich libraries
- Dynamic typing

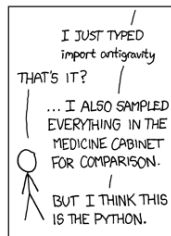
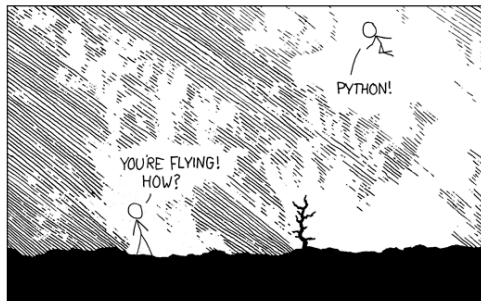
## Official Tutorial and Manual

<https://docs.python.org/2/tutorial/index.html>

There are two slightly inconsistent versions of python in the wild, python 2.x and python 3.x

Within the 2.x series (currently 2.7.8) features were added from time to time. If you're very concerned about portability you may want to avoid newer constructions (e.g. `<x> if <logical> else <y>`, `with`) Eventually we'll all have to move to python 3 (currently at 3.4), but I'm not in a hurry. Neither is google.

# XKCD



```
print "Hello world"
```

u can run python

```
$ cat hello.py
```

```
print "Hello world"
```

```
$ python
```

On `nobel.princeton.edu` you can use `python 2.7` and `ipython 2.2.0` by saying `module load anaconda` (maybe in your **.bashrc** file). If you find other Princeton machines where this doesn't work please let CSES know (and notify us).

## Primitive types

- `None`
- `bool` (`True`, `False`)
- `int`
- `long` (arbitrary precision)
- `float`



- **set**: a list with each element appearing only once.

# Strings

Python strings can be delimited with `"`, `'`, `"""`, or `'''`

```
>>> s = "Hello world"
>>> s2 = 'Goodbye, sweet life'
>>> s3 = """I really like
to split greetings over multiple lines"""
```

(there's no difference between " and ', unlike the unix shells). I recommend **not** randomly switching between " and ' strings (as it makes it hard to find them in your editor). I personally follow the C convention: "Hello world" but 'H'. Sometimes.

Strings have several useful methods:

```
>>> print s.upper()
HELLO WORLD

>>> s.find('w')
6

>>> print s[s.find('w'):]
world

>>> s.split()
['Hello', 'world']
```

You can't interpolate variable ("**\$a \$b \$c**"), but you can say

```
>>> a, b, c = "A", "B", "C"
>>> print "%S %S %S" % (a, b, c)
A B C
```

# Dictionaries

```
>>> di = {"cwright" : "Clancy", "jstone" : "Jim", "rhl" : "Robert"}
>>> print di['rhl']
Robert
>>> print di.keys(), di.values()
['cwright', 'rhl', 'jstone'] ['Clancy', 'Robert', 'Jim']
>>> di = dict(president = "Obama")
>>> di["president"] = "Eisgruber"
>>> di["provost"] = "Lee"
```

*N.b.* python supports *garbage collection*; when we said `di = dict(president = "Obama")` the memory for our email dictionary was returned to the system.

You can use dictionaries in conjunction with `%` formatting:

```
>>> foods = dict(a="Apple", b="Banana", c="Carrot")
>>> print "%(a)s %(b)s %(c)s" % foods
Apple Banana Carrot
```

This style `%` formatting is actually deprecated in python `>= 2.6`; you're supposed to say things like

```
"{0} {1} {c}".format("Apple", "Banana", c="Carrot")
```

but this seems pretty clunky to me. It seems unlikely that `%` formatting will ever go away.

```
>>> addressBook = {}
```

You can't use a **list** as a key in a **dict** (as you might modify the list)

"Orphan" `.pyc` files can be very confusing. If you move **foo.py** to a directory later in `$PYTHONPATH`, but leave **foo.pyc** behind, python will happily import the `.pyc` file for you; this may not be what you intended. Examining `foo. file` can help diagnose the problem.

### Discussion

Dealing with the *g* factor

A . . . . .

## Changing program logic

In C I can write

```
if (x == 1) {
    printf("One\n");
} else {
    printf("Not one\n");
}
```

If I need to change the indentation level I can modify this to

```
if (y == 10) {
if (x == 1) {
    printf("One\n");
} else {
    printf("Not one\n");
}
}
```

and get my editor to reindent to make it look pretty.

In python, things aren't so nice.

```
if y == 10:
    if x == 1:
        print("One")
    else:
        print("Not one")
```

I cannot tell whether the `else` belongs to the `x` or `y` test. My only hope is to rigidly reindent the block (use `^C>` in emacs)

Note that `range(n)` counts from 0 to  $n-1$ , not up to  $n$ .

`continue` is also available. But `goto` isn't.

```
>>> for c in ("abc",): print c
abc

>>> for c in ("abc"): print c
a
b
c
```

That comma is essential. It isn't really the loop's fault, it's just that a string is treated as a list of characters.



# Functions

```
def my_range(n):  
    """Return (0..n)"""  
    i = 0  
    out = list()  
    while i < n:  
        out.append(i)  
        i += 1  
    return out  
  
for i in my_range(10):  
    print i
```

Simple variables (**int**, **float**) are passed by *value*; everything else is passed by *reference*.

This means that if you modify a list or dictionary passed to a function it'll be modified in the calling routine too; you may need to make a copy:

```
li = li[:]  
di = di.copy()
```

It'd be nice if **list** also supported **copy**, the closest is **list(xxx)**. You can always use **import copy; copy.copy(xxx)** (but it's slower). This is a *shallow copy*, but **copy.deepcopy** is also available.

(`__name__` is `"__main__"` when run from the shell, and `"hello"` when imported).

## Default arguments

You can also specify default values for arguments (as well as variable numbers of arguments):

```
def my_range(n, end=None, dn=1):
    """Return a list of numbers
    Details ...
    """
    if end is None:
        i, end = 0, n
    else:
        i = n

    out = []
    while i < end:
        out.append(i)
        i += dn

    return out

>>> my_range(3)
(0, 1, 2)
>>> my_range(2, 4)
(2, 3)
>>> my_range(2, 10, 2)
(2, 4, 6, 8)
>>> my_range(10, dn=2)
(0, 2, 4, 6, 8)
```



```
def fibonacci(n):
    prev = 0
    cur = 1
    for j in range(n):
        yield cur
        (cur, prev) = (cur + prev, cur)

>>> [x for x in fibonacci(10)]
[1, 1, 2, 3, 5, 8, 13, 21, 34, 55]
```

`fibonacci` returns a *generator* which has a method `next`. The first call to `next` calls `fibonacci` and returns the value of the `yield` statement. When you call `next` again it miraculously resumes just after the `yield` and continues until it reaches `yield` again; when it `returns` (either explicitly or implicitly) a `StopIteration` exception is raised:

```
>>> f = fibonacci(1)
>>> f.next()
1
>>> f.next()
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
StopIteration
```



There are also more complicated and powerful forms of this `try except` pattern.

That **self** closes the mouth of God's **this** test



```
>>> print addressBook["Clancy"]
(cwrowley, Rowley)
```

1. **Introduction**

Let's return to another old friend<sup>1</sup>, `max`

```
def max(a, b):
    if a > b:
        return a
    else:
        return b
```

That's it. *N.b.* templates provide exactly this sort of 'duck typing' for C++ (the code's valid if `a` and `b` support `>`)

```
>>> print max(1, 2)
2
>>> print max("a", "b")
'b'
>>> print max(["a", "b"], ["a", "c"])
['a', 'c']

>>> import people
>>> Clancy = people.Person("cwrowley", "Rowley")
>>> Robert = people.Person("rhl", "Lupton")
>>> print max(Clancy, Robert)
(cwrowley, Rowley)
```

The comparison is consistent-but-undefined. If we want to sort by the email address:

```
def __cmp__(self, rhs):
    return cmp(self.email, rhs.email)
```

and now `max` works as expected.

<sup>1</sup>actually, `max` is a builtin, but builtin names are not protected

you can install `matplotlib` and `numpy` (and more) using `anaconda`; `re` and `argparse` are part of python's standard library.

Python's `re` module provides two searching methods. I've been using `search`, but there is also `match`. I recommend that you **never** use `match` (because `re.match(r"RE", ...) == re.search(r"RE", ...)`).

- `getopt` Deprecated since python 2.3
- `optparse` Deprecated in python 2.7
- `argparse` The new kid on the block; only in python 2.7 (and 3.?) but back-ported to 2.6

```
#!/usr/bin/env python
import argparse

parser = argparse.ArgumentParser(description='Say hello')

parser.add_argument('who', metavar='who', type=str, nargs='*',
                    help='List of people to greet', default=["world"])

parser.add_argument("-w", "--who",
                    dest="speaker", help="name of speaker", default="Robert")
parser.add_argument("-s", "--silent", action='store_true', default=False,
                    help="Refuse to say anything")

args = parser.parse_args()

if args.silent:
    print "I plead the fifth"
else:
    print "%s says \"Hello %s\" " % (args.speaker, " ".join(args.who))

$ hello.py
Robert says "Hello world"
$ hello.py -s TAs and the class
I plead the fifth
$ hello.py --who Clancy TAs and the class
Clancy says "Hello TAs and the class"
```

There's quite a nice tutorial from the EuroScipy 2012 conference at <http://webloria.loria.fr/~rougier/teaching/matplotlib>

The `interactive: True` means that `matplotlib` should *not* enter its wait-for-the-user interactive loop.



# Plotting using `matplotlib`

There are two-and-a-half ways to use `matplotlib`

- Interactive:
  - uses `matplotlib.pyplot` package (or `matplotlib.pylab`)
  - good for quickly making single plots, hiding all the object-oriented aspects.
  - looks very similar to matlab
- Object-oriented (more *pythonic*), using `pyplot.figure` and `axes`
- Using the low-level objects directly:
  - Renderers which provide an abstract interface to drawing primitives (e.g. `draw_path`)
  - Backend objects which take care of how to actually draw the object (e.g. `Qt4Agg` to use `Qt`)
  - A `FigureCanvas` to draw on
  - An `Artist` that knows how to use *renderers* to draw on *canvases*.

If you need fine control over your plots you need to know the classes and their methods, but you may not need to go far down that path.

```
from matplotlib.pyplot import *
from numpy import *

# make data
x = linspace(0, 9)
model = sin(x)
dy = random.uniform(0.75, 1, len(x))
y = model + random.normal(scale=dy)

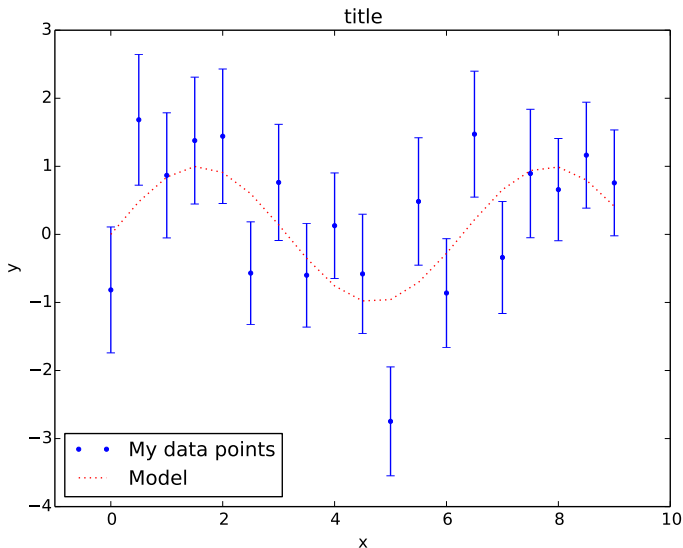
# plot the data
plot(x, y, "b.", label="My data points")
errorbar(x, y, yerr=dy, fmt="none", color='b')
plot(x, model, "r:", label="Model")

# axis limits
xlim(-1, 10)

# labels
xlabel("x")
ylabel("y")
title("title")

# add a legend using the labels you gave to plot()
legend()
```

## plot\_sin.pdf



# Using matplotlib.pyplot

```
import matplotlib.pyplot as plt
import numpy as np

# make data
x = np.linspace(0.0, 9.0, 19)
model = np.sin(x)
dy = np.random.uniform(0.75, 1, len(x))
y = model + np.random.normal(scale=dy)

# plot the data
plt.plot(x, y, "b.", label="My data points")
plt.errorbar(x, y, xerr=None, yerr=dy, fmt=None, color='b')
plt.plot(x, model, "r:", label="Model")

# axis limits
plt.xlim(-1, 10)

# labels
plt.xlabel("x")
plt.ylabel("y")
plt.title("title")

# add a legend using the labels you gave to plot()
plt.legend(loc="best", ncol=1).dragable()

# Show the figure (should pop up a new window)
plt.show()

# Save the plot to a file
plt.savefig("figures/plot_sin.pdf")

# Clear the figure (so we can make a new one)
plt.clf()
```

# Format characters

The format string is of the form CM (ColourMarker)

---

b	blue	-	solid line	.	point
g	green	--	dashed line	,	pixel
r	red	:	dotted line	o	circle
c	cyan	-.	dot-dash line	v	triangle (down)
m	magenta			^	triangle (up)
y	yellow			<	triangle (left)
k	black			>	triangle (right)
w	white				

---

There are more colours, but it's better to use the `color` keyword.  
For markers, it's really better to use the `marker` and `linestyle`  
(abbreviation: `ls`) keywords

# Semi-OO plotting with matplotlib

We can do the same thing using a **figure**:

```
fig = plt.figure()
axes = fig.add_axes((0.1, 0.1, 0.85, 0.80))

# plot the data
axes.plot(x, y, "b.", label="My data points")
axes.errorbar(x, y, xerr=None, yerr=dy, fmt=None, color='b')
axes.plot(x, model, "r:", label="Model")

# axis limits
axes.set_xlim(-1, 10)

# labels
axes.set_xlabel("x")
axes.set_ylabel("y")
axes.set_title("Clever Title")

# add a legend using the labels you gave to plot()
fontProps = dict(size = "small")
axes.legend(loc="best", prop=fontProps, ncol=1).draggable()
```



# Multi-panel plots

Once again, I need a [figure](#), and then the command to select the third sub-window out of a [2x2](#) set is

```
figure.add_subplot(2, 2, 3)
```

so I could say

```
axes = figure.add_subplot(2, 2, 1)
# make a plot
axes = figure.add_subplot(2, 2, 2)
# make another plot
axes = figure.add_subplot(2, 2, 3)
# keep plotting
axes = figure.add_subplot(2, 2, 4)
# plot plot plot
```

But I'm lazy and I don't like duplicating [2, 2](#)

Instead, I'll use a generator:

```
def makeSubplots(figure, nx=2, ny=2):
    """Return a generator of a set of subplots"""
    for window in range(nx*ny):
        yield figure.add_subplot(nx, ny, window + 1) # 1-indexed

subplots = makeSubplots(fig)
# Initialize
axes = subplots.next()
```

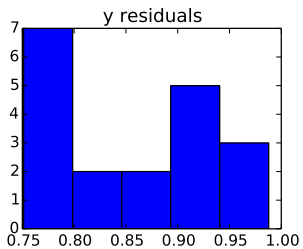


```
fig = plt.figure()

def makeSubplots(figure, nx=2, ny=2):
    """Return a generator of a set of subplots"""
    for window in range(nx*ny):
        yield figure.add_subplot(nx, ny, window + 1) # 1-indexed

subplots = makeSubplots(fig)
# Initialize
axes = subplots.next()

#make a histogram of residuals, returns bin delimiters and number/bin
myhist = axes.hist(dy, bins=5)
axes.set_title("y residuals")
```



Hmm. Not a good choice for the axis limits.

# Panel I: Histogram

Let's fix those limits:

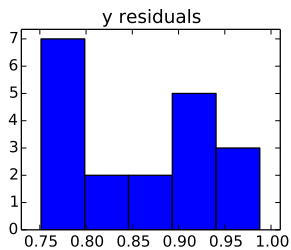
```
fig = plt.figure()

def makeSubplots(figure, nx=2, ny=2):
    """Return a generator of a set of subplots"""
    for window in range(nx*ny):
        yield figure.add_subplot(nx, ny, window + 1) # 1-indexed

subplots = makeSubplots(fig)
# Initialize
axes = subplots.next()

#make a histogram of residuals, returns bin delimiters and number/bin
myhist = axes.hist(dy, bins=5)
axes.set_title("y residuals")

axes.set_xlim(0.73, 1.01)
ymin, ymax = axes.get_ylim()
axes.set_ylim(ymin, 1.05*ymax)
```



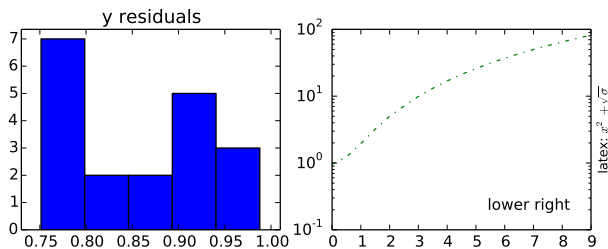
## Panel II: Log-linear

```
# Initialize and make a log plot
z = x**2 + np.sqrt(dy)

axes = subplots.next()
axes.semilogy(x, z, "g-.")

# Move the axis label to the right hand size
axes.yaxis.set_label_position("right")
axes.set_ylabel(r"latex:  $x^2 + \sqrt{\sigma}$ ", size="small")

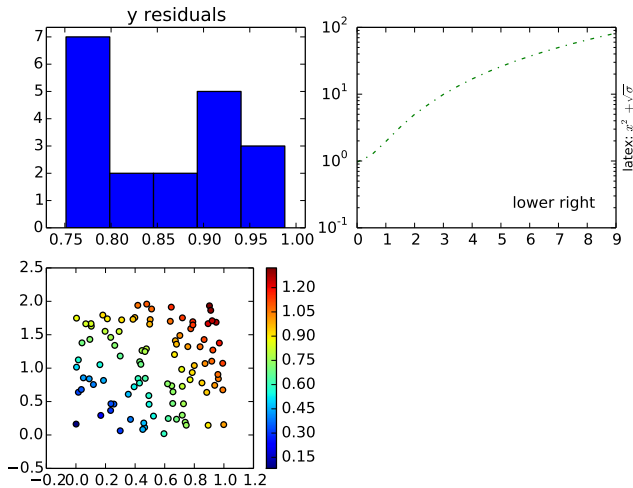
# can work in pixel, figure, or axes or plotting coordinates
# in this case put the text in 60%, 10% of the axes
axes.text(0.6, 0.1, "lower right", transform=axes.transAxes)
```



## Panel III: Scatter Plot

```
# Initialize and calculate points
axes = subplots.next()
xs = np.random.random(100)
ys = np.random.random(100)*2
zs = np.sqrt(xs**2 + ys**2/4.0)

# Make plot
sc = axes.scatter(xs, ys, c=zs)
fig.colorbar(sc)
```





## Panel IV: Contours

```
# Initialize and calculate data
axes = subplots.next()
axis = np.linspace(-2.5, 2.5, 100)
X, Y = np.meshgrid(axis, axis)

sigma_x, sigma_y, f = 0.5, 1.0, 3
Z = 1/(2*np.pi*sigma_x*sigma_y)*np.exp(-0.5*((X/sigma_x)**2 + (Y/sigma_y)**2)) + \
    2/(2*np.pi*(f*sigma_x)**2)*np.exp(-0.5*(X**2 + Y**2)/(f*sigma_x)**2)

# Make a contour plot
CS = axes.contour(X,Y,Z)

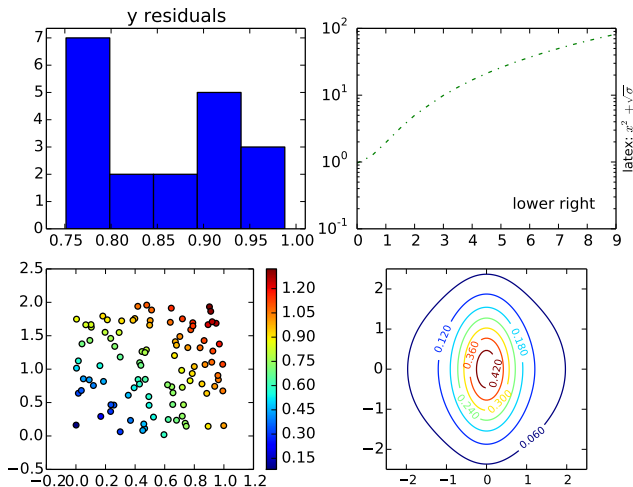
# put labels on the contours
axes.clabel(CS, inline=1, fontsize=8)

# make circles circular
axes.set_aspect('equal')

# Change the ticklabel size
axes.tick_params(axis="x", labelsize="small")

# Save the plot to a file
fig.savefig("figures/plot_multi.pdf")
```

# plot\_multi.pdf



# Non-interactive plotting

What if you just want to make a plot, and not worry about [interactive](#) and [Qt](#)? One way is to use a [canvas](#):

We needn't `import pyplot`: and the command to make the [figure](#) is a little different:

```
fig = matplotlib.figure.Figure()
```

The rest of the plotting is identical:

```
axes = fig.add_axes((0.1, 0.1, 0.85, 0.80))

# plot the data
axes.plot(x, y, "b.", label="My data points")
axes.errorbar(x, y, xerr=None, yerr=dy, fmt=None, color='b')
axes.plot(x, model, "r:", label="Model")

# axis limits
axes.set_xlim(-1, 10)

# labels
axes.set_xlabel("x")
axes.set_ylabel("y")
axes.set_title("Clever Title")
```

And finally we use that [canvas](#):

```
from matplotlib.backends.backend_pdf import FigureCanvasPdf as FigCanvas

canvas = FigCanvas(fig)
canvas.print_figure("foo.png")          # a PNG file this time
```

# Array operations, `numpy`

While the array library, `numpy`, is not part of the python standard library it is widely available.

NumPy home (but it's easier to get it from *anaconda*)

<http://numpy.scipy.org>

We used a few pieces of `numpy` in the `matplotlib` examples:

```
import numpy as np
x = np.linspace(0.0, 9.0, 19)
model = np.sin(x)

yerr = np.abs(y - model)
zs = np.sqrt(xs**2 + ys**2/4.0)

np.random.seed(666)
xs = np.random.random(100)
y = np.random.normal(loc=model, scale=0.2)

axis = np.linspace(-2.0, 2.0, 100)
X, Y = np.meshgrid(axis, axis)
```

The `import numpy as np` is common enough that it's what the `numpy` documentation assumes.

```
>>> x = np.linspace(0.0, 5.0, 11); print x
[ 0.  0.5  1.  1.5  2.  2.5  3.  3.5  4.  4.5  5.]
```

We could have used `arange` (analogous to python's `range`):

```
>>> print np.arange(0.0, 5.1, 0.5)
[ 0.  0.5  1.  1.5  2.  2.5  3.  3.5  4.  4.5  5.]
```

There's also

```
>>> print np.zeros(4), np.ones(4), np.empty(4, dtype='i')
[0.  0.  0.  0.] [1.  1.  1.  1.] [9 0 18402543 1]
```

```
>>> x = np.arange(5); print np.multiply.outer(x, x)
[[ 0  0  0  0  0]
 [ 0  1  2  3  4]
 [ 0  2  4  6  8]
 [ 0  3  6  9 12]
 [ 0  4  8 12 16]]
```

# numpy Mathematical functions

```
>>> x = np.arange(5)
>>> y = np.sin(x); print y
[ 0.          0.84147098  0.90929743  0.14112001 -0.7568025 ]
```

There are lots of other mathematical builtins (`sin`, `cos`, `tan`, `arcsin`, `arctan2`, `abs`, `sqrt`, ...)

```
>>> print zip(x, y)
[(0, 0.0), (1, 0.8414709848078965), (2, 0.90929742682568171),
 (3, 0.14112000805986721), (4, -0.7568024953079282)]

>>> print "\n".join("%d %6.3f" % z for z in zip(x, y))
0  0.000
1  0.841
2  0.909
3  0.141
4 -0.757
```

(OK, so that's a python, not `numpy`, trick)

# numpy Random Numbers

```
>>> np.random.seed(666)
>>> np.random.random(10)
array([ 0.70043712,  0.84418664,  0.67651434,  0.72785806,  0.95145796,
        0.0127032 ,  0.4135877 ,  0.04881279,  0.09992856,  0.50806631])
```

(*n.b.* I didn't say **print**, so I got the **repr** not the **str** value of the result)

```
>>> print np.random.normal(loc=np.arange(5), scale=0.2)
[-0.2177586  0.88484585  1.66341985  3.04583705  3.64867496]
>>> print np.random.normal(np.arange(5), 0.2)
[ 0.16892652  1.05544397  2.17058031  3.03891992  4.26212754]
```

The two calls are identical, but the random numbers are (of course) different.

# numpy in n-D

```
>>> axis = np.linspace(-2.0, 2.0, 5)
>>> X, Y = np.meshgrid(axis, axis)
>>> print X
[[-2. -1.  0.  1.  2.]
 [-2. -1.  0.  1.  2.]
 [-2. -1.  0.  1.  2.]
 [-2. -1.  0.  1.  2.]
 [-2. -1.  0.  1.  2.]]
>>> print Y
[[-2. -2. -2. -2. -2.]
 [-1. -1. -1. -1. -1.]
 [ 0.  0.  0.  0.  0.]
 [ 1.  1.  1.  1.  1.]
 [ 2.  2.  2.  2.  2.]]

>>> print np.cos(X)*np.sin(Y)
[[ 0.37840125 -0.4912955 -0.90929743 -0.4912955  0.37840125]
 [ 0.35017549 -0.45464871 -0.84147098 -0.45464871  0.35017549]
 [-0.          0.          0.          0.          -0.          ]
 [-0.35017549  0.45464871  0.84147098  0.45464871 -0.35017549]
 [-0.37840125  0.4912955  0.90929743  0.4912955 -0.37840125]]

>>> print np.fft.fft(X)*np.sin(Y)
[[-0.00000000+0.j          2.27324357-3.12885135j  2.27324357-0.73862161j
  2.27324357+0.73862161j  2.27324357+3.12885135j]
 [-0.00000000+0.j          2.10367746-2.89546363j  2.10367746-0.68352624j
  2.10367746+0.68352624j  2.10367746+2.89546363j]
 [ 0.00000000+0.j         -0.00000000+0.j         -0.00000000+0.j
  0.00000000-0.j         0.00000000-0.j        ]
...

```



# numpy extended indexing

You aren't restricted to using scalars as array indexes:

```
>>> x = np.arange(-4, 5); print x
[-4 -3 -2 -1  0  1  2  3  4]
>>> i = x**2 > 4
>>> print i
[ True  True False False False False  True  True]
>>> print x[i]
[-4 -3  3  4]

>>> x[i] = 10 + np.abs(x[i])
>>> print x
[14 13 -2 -1  0  1  2 13 14]

>>> I = np.array([2, 7])
>>> print x[I]
[-2 13]
```

# Plotting and Extended Indexing

Here's another example

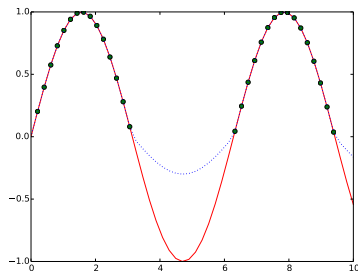
```
import numpy as np
import matplotlib.pyplot as plt

x = np.linspace(0, 10, 50); y = np.sin(x)

plt.plot(x, y, '-', color="red")
l = y > 0
plt.plot(x[l], y[l], 'o', color="green")

plt.plot(x, np.where(l, y, 0.3*y), color="blue", ls=':')
```

The `np.where` is like C/C++'s `?:` operator.



# numpy Linear Algebra

```
>>> n = 3; i = np.arange(n); M = np.zeros((n,n))
>>> M[(i,i)] = i + 1; print M
[[ 1.  0.  0.]
 [ 0.  2.  0.]
 [ 0.  0.  3.]]
>>> np.linalg.inv(M)
array([[ 1.          ,  0.          ,  0.          ],
       [ 0.          ,  0.5         ,  0.          ],
       [ 0.          ,  0.          ,  0.33333333]])

>>> M = np.matrix(M)
>>> U, s, Vt = np.linalg.svd(M)
>>> U * np.diag(s) * Vt                                     # should == M
matrix([[ 1.,  0.,  0.],
        [ 0.,  2.,  0.],
        [ 0.,  0.,  3.]])
```

Traps await the unwary:

```
>>> M = np.zeros((n,n)); M[(i,i)] = i + 1
>>> U, s, Vt = np.linalg.svd(M)
>>> U * np.diag(s) * Vt
array([[ 0.,  0.,  0.],
       [ 0.,  2.,  0.],
       [ 0.,  0.,  0.]])
```

Uh oh; that's an element-by-element product. An **array** is not a **matrix**; you have to say

```
>>> U.dot(np.diag(s)).dot(Vt)
```

# numpy Linear Algebra

Beware: vectors are treated differently from matrices. The vector `x` is the same as the vector `x.T`:

```
>>> x = np.array((1, 2))
>>> x
array([1, 2])
>>> x.T
array([1, 2])
>>> np.dot(x, x.T)
5
>>> np.dot(x.T, x)
5
```

If you want to distinguish between row vectors and column vectors, need to use a  $1 \times n$  or  $n \times 1$  matrix:

```
>>> x.resize(1,2)
>>> x
array([[1, 2]])
>>> x.T
array([[1],
       [2]])
>>> np.dot(x, x.T)
array([[5]])
>>> np.dot(x.T, x)
array([[1, 2],
       [2, 4]])
```

# numpy Linear Algebra

If you use a **matrix**, you don't need to use **dot**:

```
>>> v = np.matrix((1, 2))
>>> v * v.T
matrix([[5]])
>>> v.T * v
matrix([[1, 2],
        [2, 4]])
```

A future version of python will support **U @ np.diag(s) @ Vt** with **@** meaning, "matrix multiply". This does not remove the confusion between vectors and matrices, however: it is merely a shorthand for **U.dot(np.diag(s)).dot(Vt)**.

- N-dimensional image convolution
- Interpolation
- Sparse linear algebra (e.g. 3M x 5k least-squares problems)
- Optimization
- *etc.*

One extremely powerful technique is to wrap your own code in python, a topic that we'll cover later in the course. To whet your appetite, here's some analysis code that I wrote four years ago last week:

Every operation in **red** is written in C++.