

$$S = \{1, 2, 3, 4\}$$

$$T = \{12, 3, 4\}$$

$$g: S \rightarrow T$$

$$g(1) = g(2) = 12$$

$$g(3) = 3 \quad g(4) = 4$$

1.97) 15 partitions of a set with 4 elements.

1, 2, 3, 4

1, 2, 34

12, 34

1, 23, 4

There are
Fifteen
of these

$$c: S \rightarrow P$$

$$g!(c) = 12, 3, 4$$

12, 34

12, 34

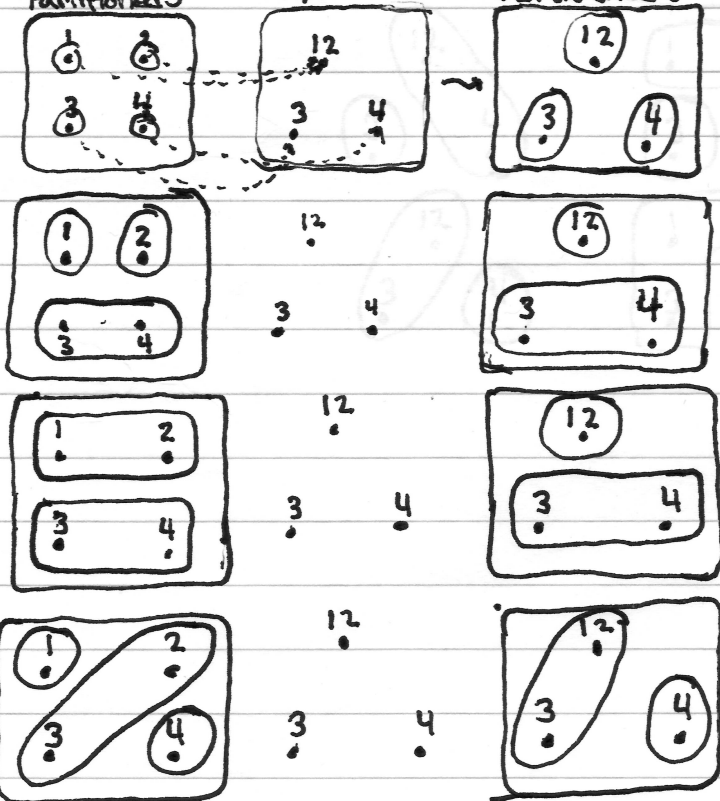
123, 4

There are
Five
of these

Partitioned S

T

Partitioned T



In each case $g!$
has the effect of
identifying (treating
as equivalent)
points 1 and 2

This is a sum (colimit)

The S-part
that 1 is in
merges (union)
with the one
that 2 is in.

$$[12] \sim [1] \cup [2]$$

$$s \leq g!(s)$$

1 2 3
12 3
1 2 3
123

1.44) Five partitions on a set of 3 elements $\{1, 2, 3, 4\}$

1, 2, 3, 4

1, 2, 3, 4

1, 2, 3, 4

1, 2, 3, 4

1, 2, 3, 4

There are exactly five of these.

But there are fifteen of these.



τ

$g^*(\tau)$

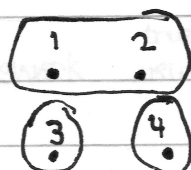
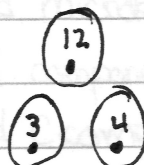
S

Partitioned T

Partitioned S

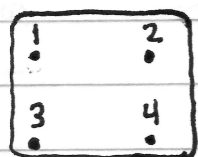
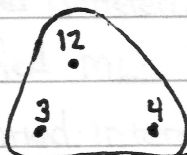
1, 2, 3, 4

1 2
3 4



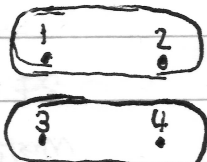
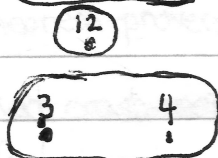
1, 2, 3, 4

1 2
3 4



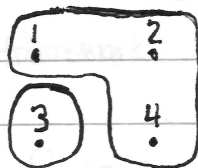
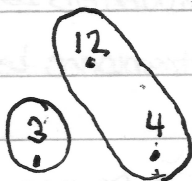
1, 2, 3, 4

1 2
3 4



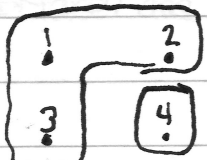
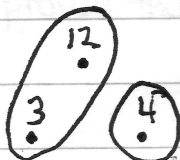
1, 2, 3, 4

1 2
3 4



1, 2, 3, 4

1 2
3 4



g^* has the effect of spreading out single point 1, 2 into two points 1, 2 that are always in the same part (equivalent)