



Semester One Examination, 2017

Question/Answer booklet

**MATHEMATICS  
METHODS  
UNIT 1**

**Section One:  
Calculator-free**

Your name \_\_\_\_\_

**Time allowed for this section**

Reading time before commencing work: five minutes  
Working time: fifty minutes

**Materials required/recommended for this section**

***To be provided by the supervisor***

This Question/Answer booklet  
Formula sheet

***To be provided by the candidate***

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

**Important note to candidates**

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

**Structure of this paper**

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
<b>Total</b>					100

**Instructions to candidates**

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.
5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you do not use pencil, except in diagrams.
7. The Formula sheet is not to be handed in with your Question/Answer booklet.

**Section One: Calculator-free**

**35% (52 Marks)**

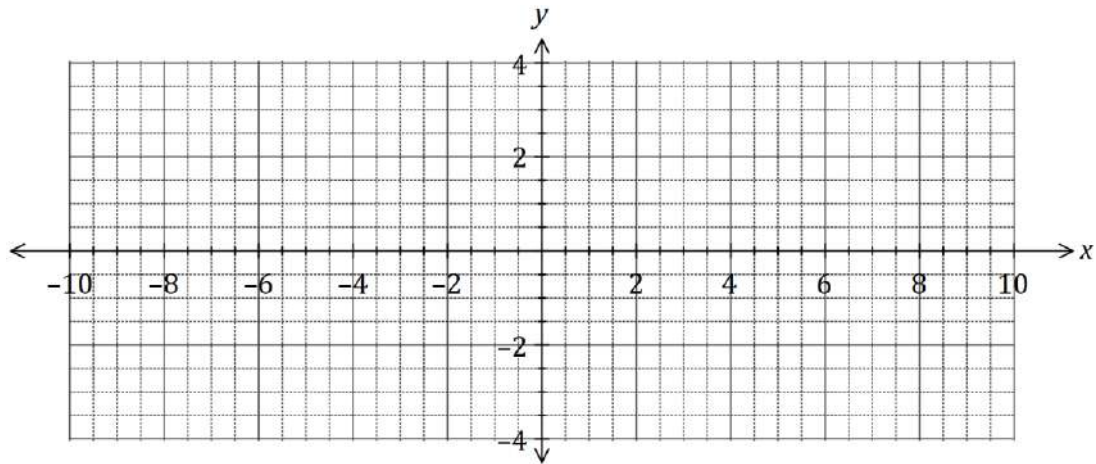
This section has **seven (7)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

**Question 1**

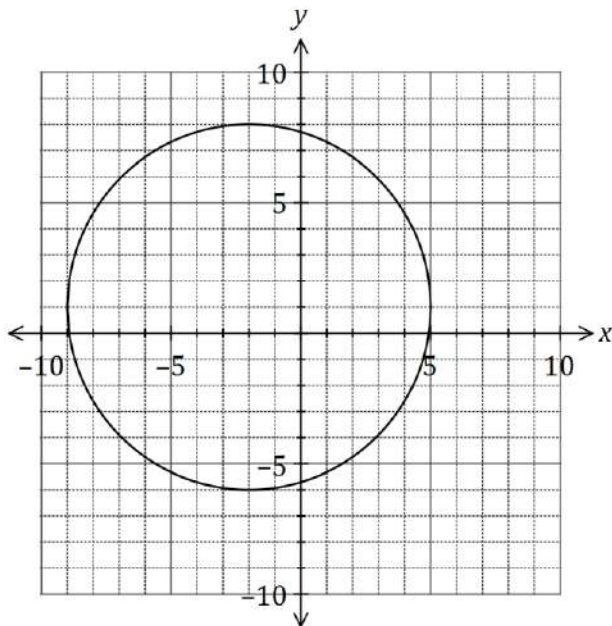
**(6 marks)**

- (a) On the axes below, sketch the graph of the relation  $y^2 = x$ , labelling all key features with their coordinates or equations. (3 marks)



- (b) Determine the equation of the circle shown below.

(3 marks)



**Question 2****(9 marks)**

- (a) The point  $M(8, 1)$  is the midpoint of  $A$  and  $B(20, 7)$ . Determine the coordinates of  $A$ .

**(2 marks)**

- (b) A relationship between  $x$  and  $y$  is given by  $x = 2y - 3$ .

- (i) Determine  $y$  when  $x = 25$ .

**(1 mark)**

- (ii) State, with justification, whether  $x$  is a function of  $y$ .

**(2 marks)**

- (c) A straight line passes through points  $C(2, -5)$  and  $D(-2, 2)$ . Determine the equation of the straight line that is perpendicular to this line and passes through  $C$ , expressing your answer in the form  $ax + by + c = 0$ , where  $a$ ,  $b$  and  $c$  are integers. (4 marks)

**Question 3****(7 marks)**

Solve each of the following equations for the variable  $x$ .

(a)  $3(1 - x) + 4 = 2(2x - 7)$ .

**(2 marks)**

(b)  $\frac{x}{2} = 1 + \frac{2x}{5}$ .

**(2 marks)**

(c)  $\frac{4}{x} = 3 + x$ .

**(3 marks)**

**Question 4**

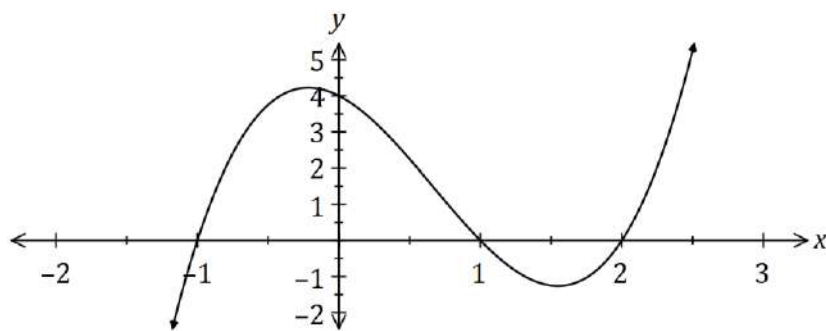
**(8 marks)**

(a) Solve the equation  $x^3 = 7x^2 + 30x$ .

(4 marks)

(b) The graph of  $y = ax^3 + bx^2 + cx + d$  is shown below. Determine the values of the constants  $a$ ,  $b$ ,  $c$  and  $d$ .

(4 marks)



**Question 5****(6 marks)**

A function is defined as  $f(x) = x^3 - 5x^2 - 12x + 36$ .

(a) Evaluate  $f(2)$ . (1 mark)

(b) Factorise  $f(x)$ . (3 marks)

(c) Hence, or otherwise, solve  $f(x) = (x - 2)(x - 3)(x - 6)$  (2 marks)



**Question 6**

**(8 marks)**

(a) For the graph with equation  $y = (x + 1)(x - 3)$ , determine the coordinates of

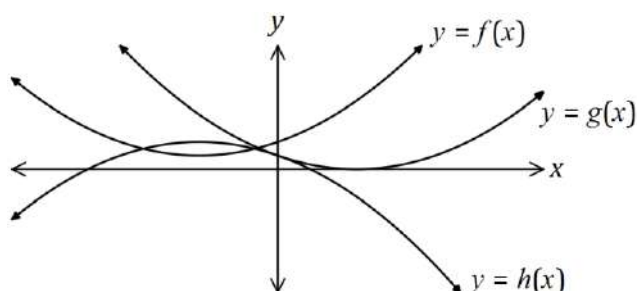
(i) all axes intercepts.

(2 marks)

(ii) the turning point.

(2 marks)

(b) The graphs of three quadratic functions with discriminants of 0, 1 and -2 are shown below.



(i) Underneath each function in this table, write the value of it's discriminant.

(2 marks)

Function	$f(x)$	$g(x)$	$h(x)$
Discriminant			

(ii) Clearly explain your choices in part (i).

(2 marks)

**Question 7****(8 marks)**

- (a) If  $\alpha$  and  $\beta$  are acute angles such that  $\cos \alpha = \frac{2}{3}$  and  $\sin \beta = \frac{3}{5}$ , determine the value of  $\cos(\alpha - \beta)$  as a single fraction. (4 marks)

- (b) Solve the following equations.

(i)  $\sqrt{2} \sin x = -1$  where  $0 \leq x \leq 2\pi$ . (2 marks)

(ii)  $\tan(2x) = 0.4$  where  $0 \leq x \leq 180^\circ$  and given that  $\tan 22^\circ = 0.4$ . (2 marks)

Additional working space

Question number: \_\_\_\_\_

