# Variational Inference with Normalizing Flows

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# Introduction

- ► Calculating the true posterior distribution of inference tasks is in most cases an intractable problem.
- ► Lots of research on approaches for efficient approximation of the posterior, however the resulting classes prove to be of limited expressiveness.
- ► The authors in [1] introduce the notion of normalizing flows, sequences of invertible transformations applied to a simple initial density, to efficiently create more expressive families of candidate posteriors to be used for variational inference.
- ► We compare the performance of different types of normalizing flows on the MNIST dataset.

#### Our Work

- ► Reproduced experiment on MNIST using Linear Normalizing Flows
- Reproduced experiment on MNIST using NICE
- ► Extended the ideas of the paper and experimented with Invertible Convolutional Flows
- ► Created open-source Github repository with code and results: github.com/ATML-Group-12/normalising\_flows

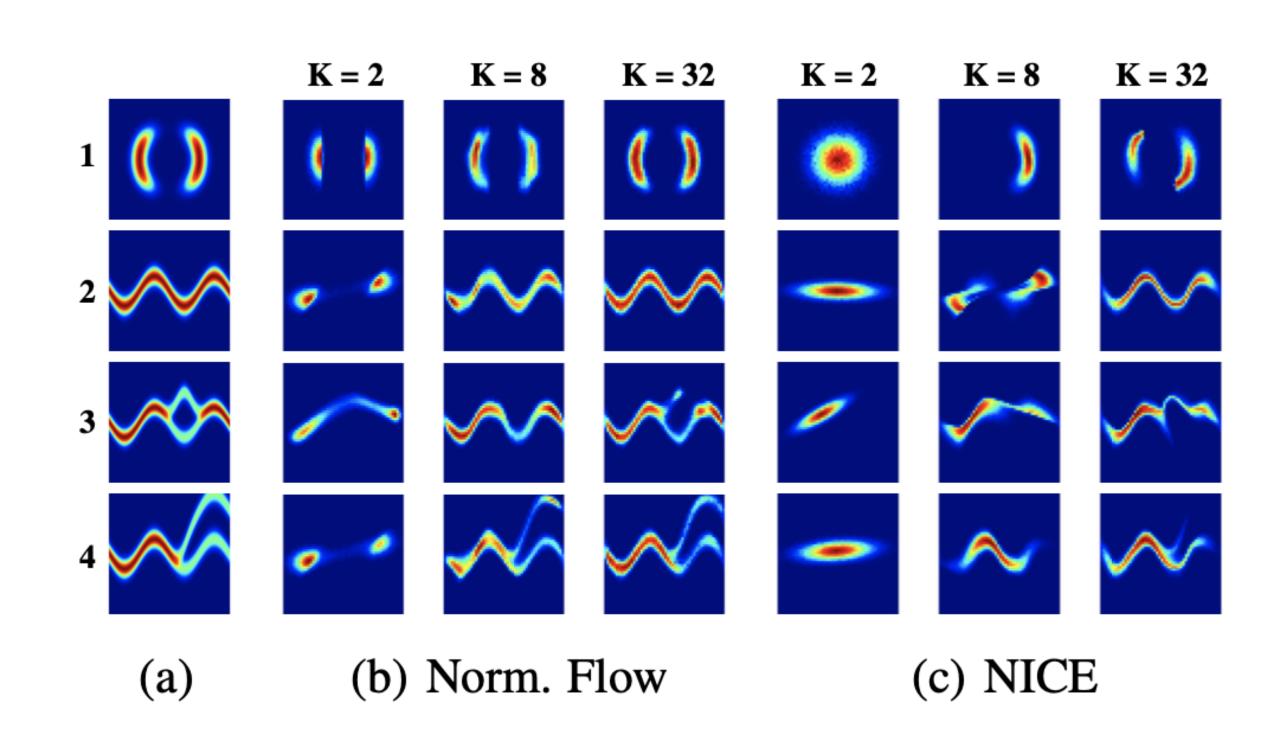
### **Theoretical Background**

- **►** TODO!!!
- ► Focus on theory between NFs here, specifically Linear NFs and NICE
- ► ELBO
- Stochastic Backpropagation
- Deep Latent Gaussian Models
- ► Flows
- ► Non-Linear Independent Components Estimation

# **Theoretical Background**

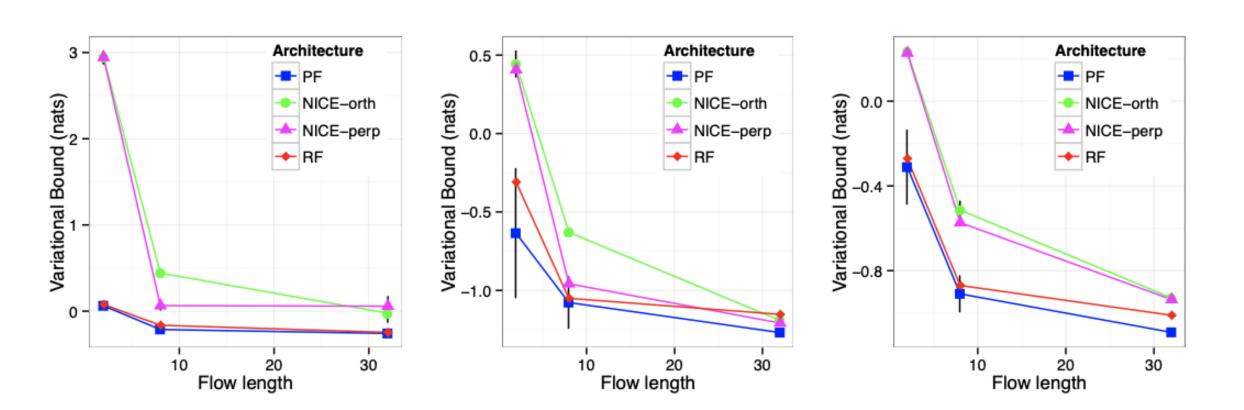
**TODO** We formulate...  $S = \{s_1, s_2, s_3, s_4, s_5, s_6\}$ 

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#### **Experiments**

- ► DLGM + NF
- ▶ DLGM + NICE



(d) Comparison of KL-divergences.

#### Results

# TODO!!! Results...

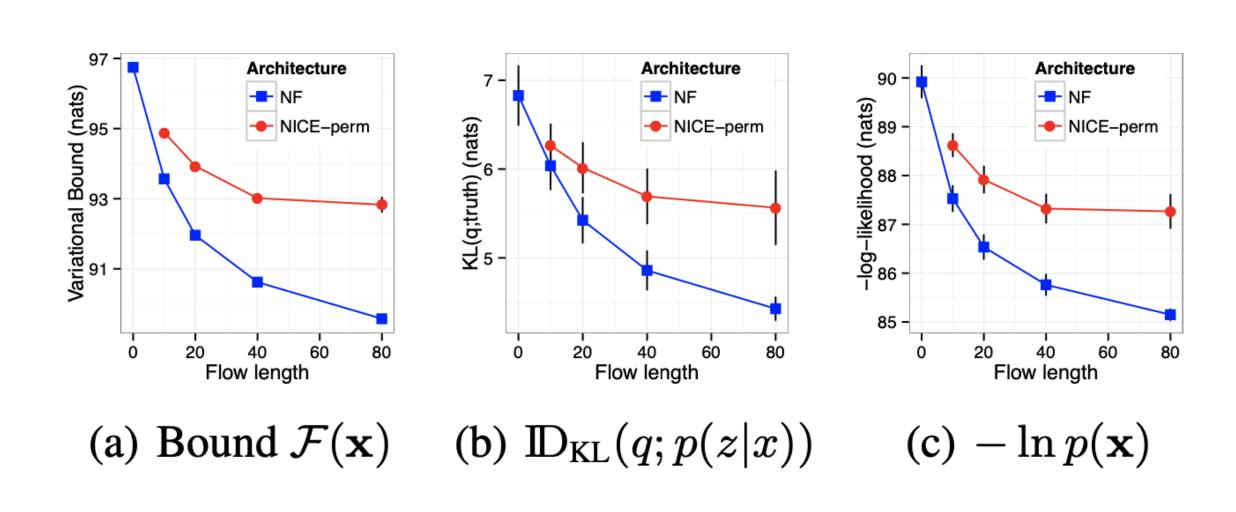


Figure 4. Effect of the flow-length on MNIST.

# Our Improvements and Extensions

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#### References

- [1] Danilo Jimenez Rezende and Shakir Mohamed. Variational inference with normalizing flows, 2015.
- [2] Laurent Dinh, David Krueger, and Yoshua Bengio. Nice: Non-linear independent components estimation, 2014.