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Hyperparameter tuning

Tuning process

Hyperparameters

$\rightarrow \boxed{\alpha}$

$\boxed{\beta}$ ~ 0.9

$\beta_1, \beta_2, \varepsilon$

$0.9 \quad 0.999 \quad 10^{-8}$

$\boxed{\text{\# layers}}$

$\boxed{\text{\# hidden units}}$

$\boxed{\text{learning rate decay}}$

$\boxed{\text{mini-batch size}}$

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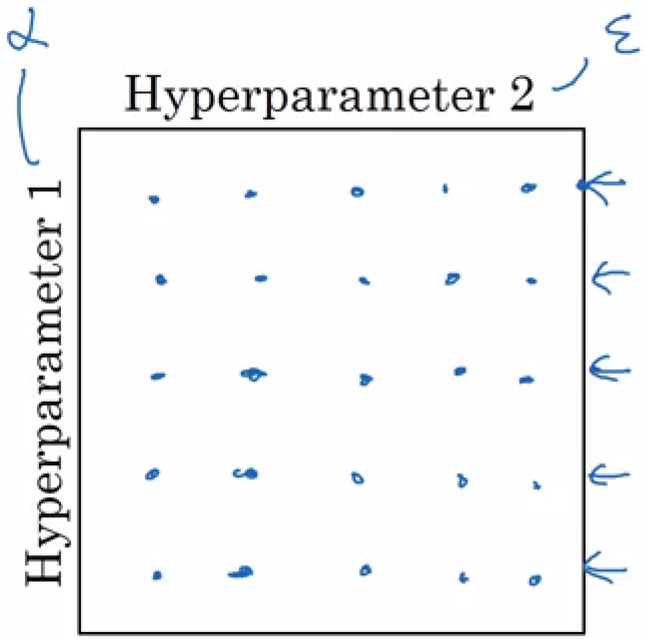
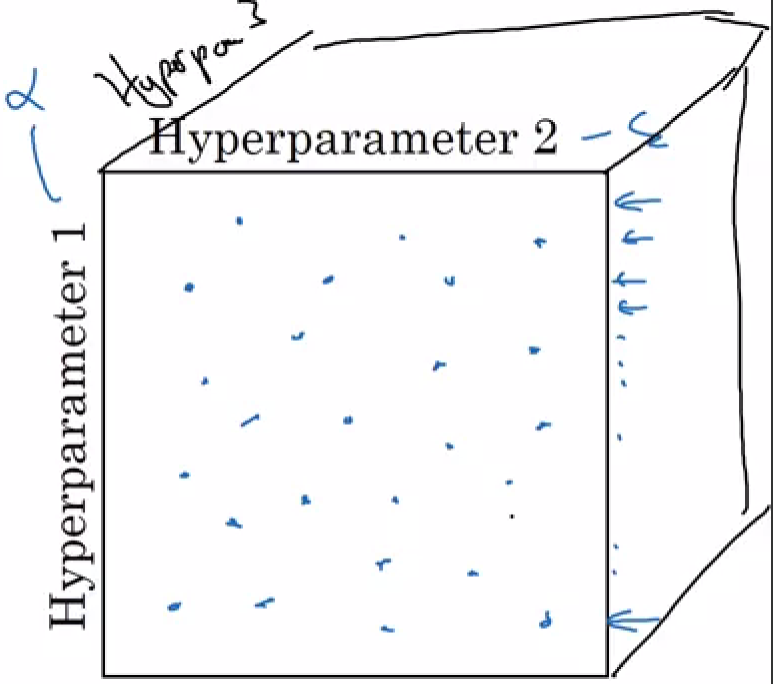
Try random values: Don't use a grid





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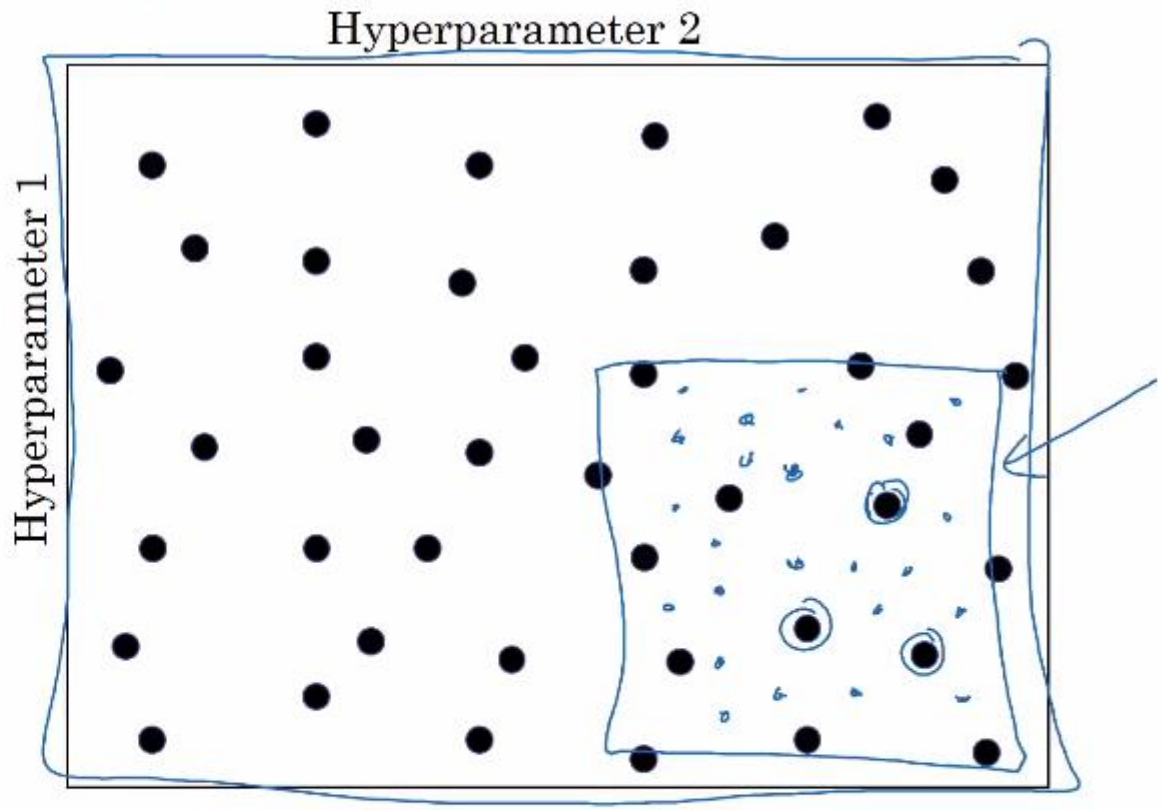
Coarse to fine



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Hyperparameter tuning

Using an appropriate scale to pick hyperparameters

Picking hyperparameters at random

$\rightarrow n^{[l]} = 50, \dots, 100$

$\rightarrow$ #layers $L: \; 2 - 4$

$2, \; 3, \; 4$

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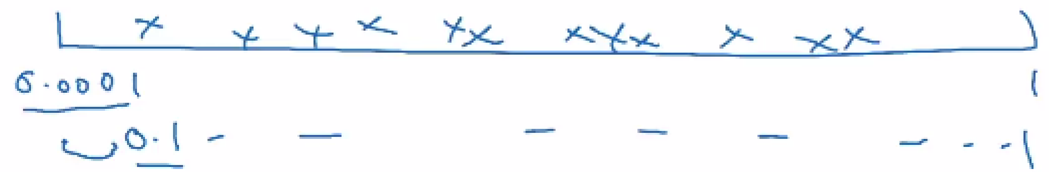
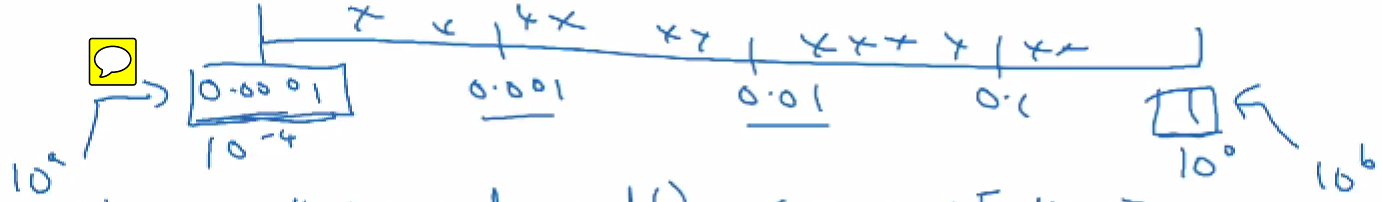
Appropriate scale for hyperparameters

$\alpha = 0.0001, \ldots, 1$





$a = \log_{10} 0.0001 = -4$

$b = \log_{10} 1 = 0$

$r = -4 * \text{np.random.rand()} \leftarrow r \in [-4, 0]$

$\alpha = 10^{r} \leftarrow 10^{-4} \ldots 10^{0}$

$10^{a} \ldots 10^{b}$ $\quad r \in [a, b]$ $\quad [-4, 0]$ $\quad \alpha = 10^{r}$

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Hyperparameters for exponentially weighted averages

$\beta = 0.9 \quad \ldots \quad 0.999$

$10 \qquad 1000$

$1-\beta = 0.1 \quad \ldots \quad 0.001$

$\beta: 0.9000 \rightarrow 0.9005 \Big\} \sim 10$

$\beta: \underset{\sim 1000}{0.999} \rightarrow \underset{\sim 2000}{0.9995}$

$\frac{1}{1-\beta}$

$0.9 \qquad 0.999$

$0.9 \qquad 0.99 \qquad 0.999$

$0.1 \qquad 0.01 \qquad 0.001$

$10^{-1} \qquad 10^{-3}$

$r \in [-3, -1]$

$1-\beta = 10^r$

$\beta = 1 - 10^r$

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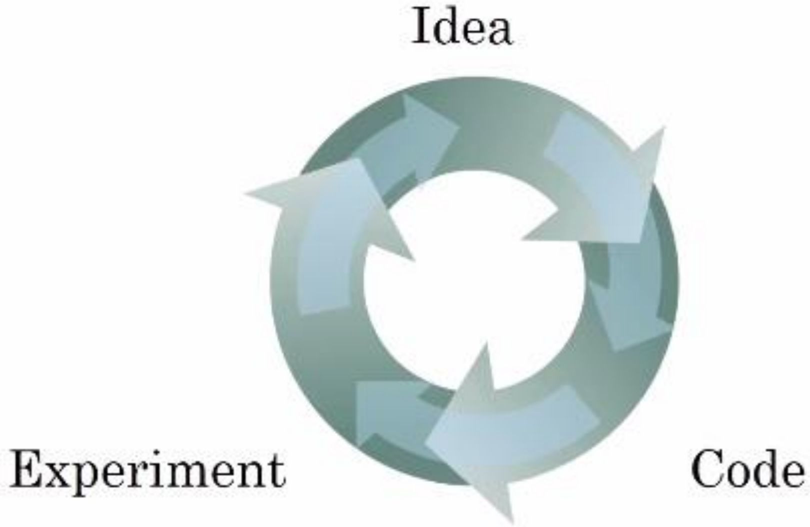
Hyperparameters tuning

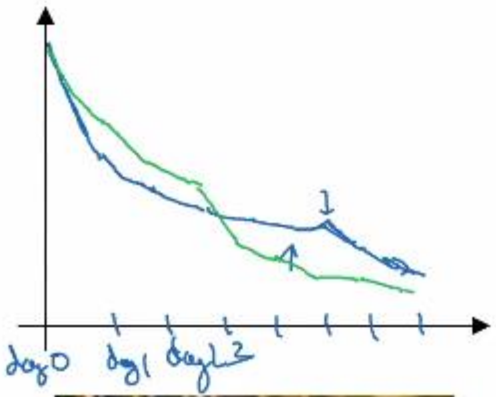
Hyperparameters tuning in practice: Pandas vs. Caviar

Re-test hyperparameters occasionally



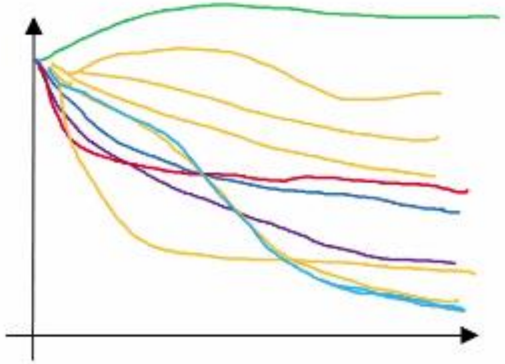
- NLP, Vision, Speech, Ads, logistics, ….
- Intuitions do get stale. Re-evaluate occasionally.

Babysitting one model



Panda

Training many models in parallel



Caviar

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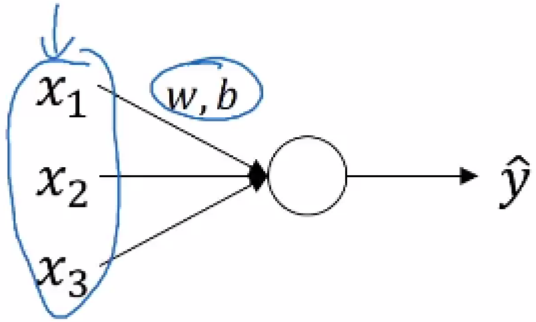
Batch Normalization

Normalizing activations in a network

Normalizing inputs to speed up learning

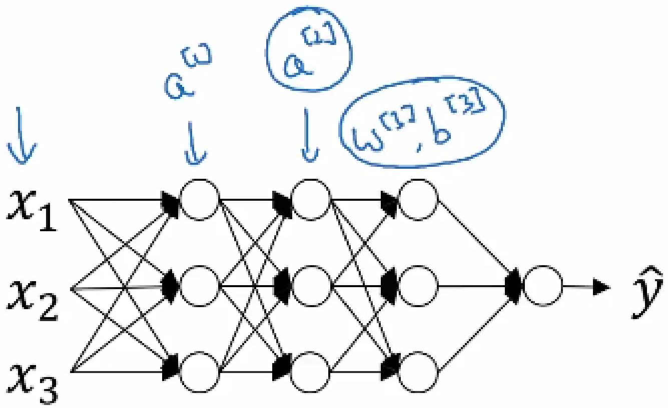


$\mu = \frac{1}{m} \sum_i x^{(i)}$

$X = X - \mu$ ← element-wise

$\sigma^2 = \frac{1}{m} \sum_i x^{(i)2}$

$X = X / \sigma^2$



Can we normalize $a^{[2]}$ so as to train $W^{[3]}, b^{[3]}$ faster

Normalize $z^{[2]}$

Andrew Ng

Implementing Batch Norm

Given some intermediate values in NN $\underbrace{z^{(1)}, \ldots, z^{(m)}}_{z^{[l](i)}}$

$$\mu = \frac{1}{m} \sum_i z^{(i)}$$

$$\sigma^2 = \frac{1}{m} \sum_i (z_i - \mu)^2$$

$$z^{(i)}_{norm} = \frac{z^{(i)} - \boxed{\mu}}{\boxed{\sqrt{\sigma^2 + \varepsilon}}}$$

$$\tilde{z}^{(i)} = \gamma z^{(i)}_{norm} + \beta$$

learnable parameters of model.

If

$$\gamma = \boxed{\sqrt{\sigma^2 + \varepsilon}}$$

$$\beta = \boxed{\mu}$$

then $\tilde{z}^{(i)} = z^{(i)}$

X

$z^{(i)}$

Use $\tilde{z}^{[l](i)}$ instead of $z^{[l](i)}$.

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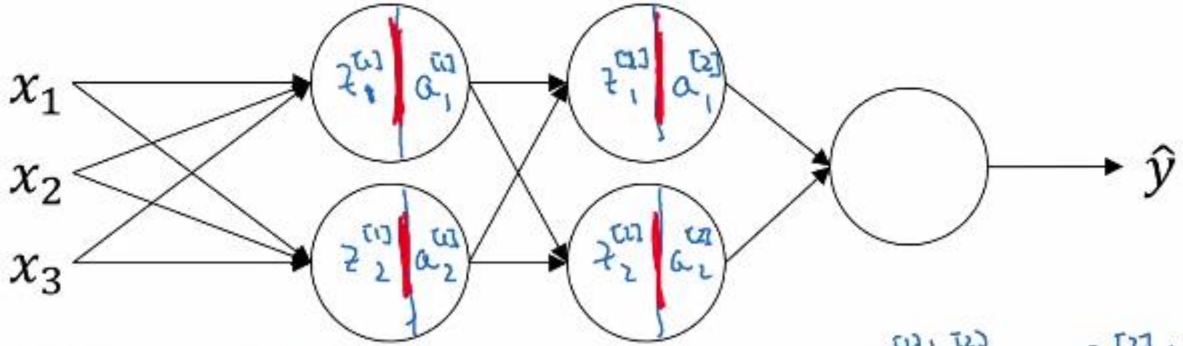
Batch Normalization

Fitting Batch Norm into a neural network

Adding Batch Norm to a network



$$X \xrightarrow{W^{[1]}, b^{[1]}} z^{[1]} \xrightarrow[\text{Batch Norm (BN)}]{\beta^{[1]}, \gamma^{[1]}} \tilde{z}^{[1]} \to a^{[1]} = g^{[1]}(\tilde{z}^{[1]}) \xrightarrow{W^{[2]}, b^{[2]}} z^{[2]} \xrightarrow[\text{BN}]{\beta^{[2]}, \gamma^{[2]}} \tilde{z}^{[2]} \to a^{[2]} \to \cdots$$

Parameters: $W^{[1]}, b^{[1]}, W^{[2]}, b^{[2]}, \ldots, W^{[L]}, b^{[L]},$
$\to \beta^{[1]}, \gamma^{[1]}, \beta^{[2]}, \gamma^{[2]}, \ldots, \beta^{[L]}, \gamma^{[L]}$

$d\beta^{[l]}$ $\quad \beta^{[l]} = \beta^{[l]} - \alpha \, d\beta^{[l]}$

tf.nn.batch_normalization $\Leftarrow$

$\to \beta$

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Working with mini-batches

$$X^{\{1\}} \xrightarrow{W^{[1]}, b^{[1]}} \underline{z^{[1]}} \xrightarrow[BN]{\beta^{[1]}, \gamma^{[1]}} \tilde{z}^{[1]} \rightarrow g^{[1]}(\tilde{z}^{[1]}) = a^{[1]} \xrightarrow{W^{[2]}, b^{[2]}} z^{[2]} \rightarrow \dots$$

$$\boxed{X^{\{2\}}} \longrightarrow \underline{z^{[1]}} \xrightarrow[BN]{\beta^{[1]}, \gamma^{[1]}} \tilde{z}^{[1]} \rightarrow \dots$$

$$X^{\{3\}} \longrightarrow \dots$$

Parameters: $W^{[l]}, \cancel{b^{[l]}}, \beta^{[l]}, \gamma^{[l]}$.

$(n^{[l]}, 1)$ $(n^{[l]}, 1)$ $(n^{[l]}, 1)$

$z^{[l]}$
$(n^{[l]}, 1)$

$$\underline{z^{[l]}} = W^{[l]} a^{[l-1]} + \boxed{\cancel{b^{[l]}}}$$

$$z^{[l]} = W^{[l]} a^{[l-1]}$$

$$z^{[l]}_{norm}$$

$$\tilde{z}^{[l]} = \gamma^{[l]} z^{[l]}_{norm} + \boxed{\beta^{[l]}}$$

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Implementing gradient descent

for $t = 1 \ldots$ numMiniBatches

Compute forward prop on $X^{\{t\}}$.

In each hidden layer, use BN to replace $\underline{z^{[l]}}$ with $\underline{\tilde{z}^{[l]}}$.

Use backprop to compute $\underline{dW^{[l]}}$, $\cancel{db^{[l]}}$, $\underline{d\beta^{[l]}}$, $\underline{d\gamma^{[l]}}$

Update params
$$\left.\begin{aligned} W^{[l]} &:= W^{[l]} - \alpha\, dW^{[l]} \\ \beta^{[l]} &:= \beta^{[l]} - \alpha\, d\beta^{[l]} \\ \gamma^{[l]} &:= \ldots \end{aligned}\right\} \leftarrow$$

Works w/ momentum, RMSprop, Adam.

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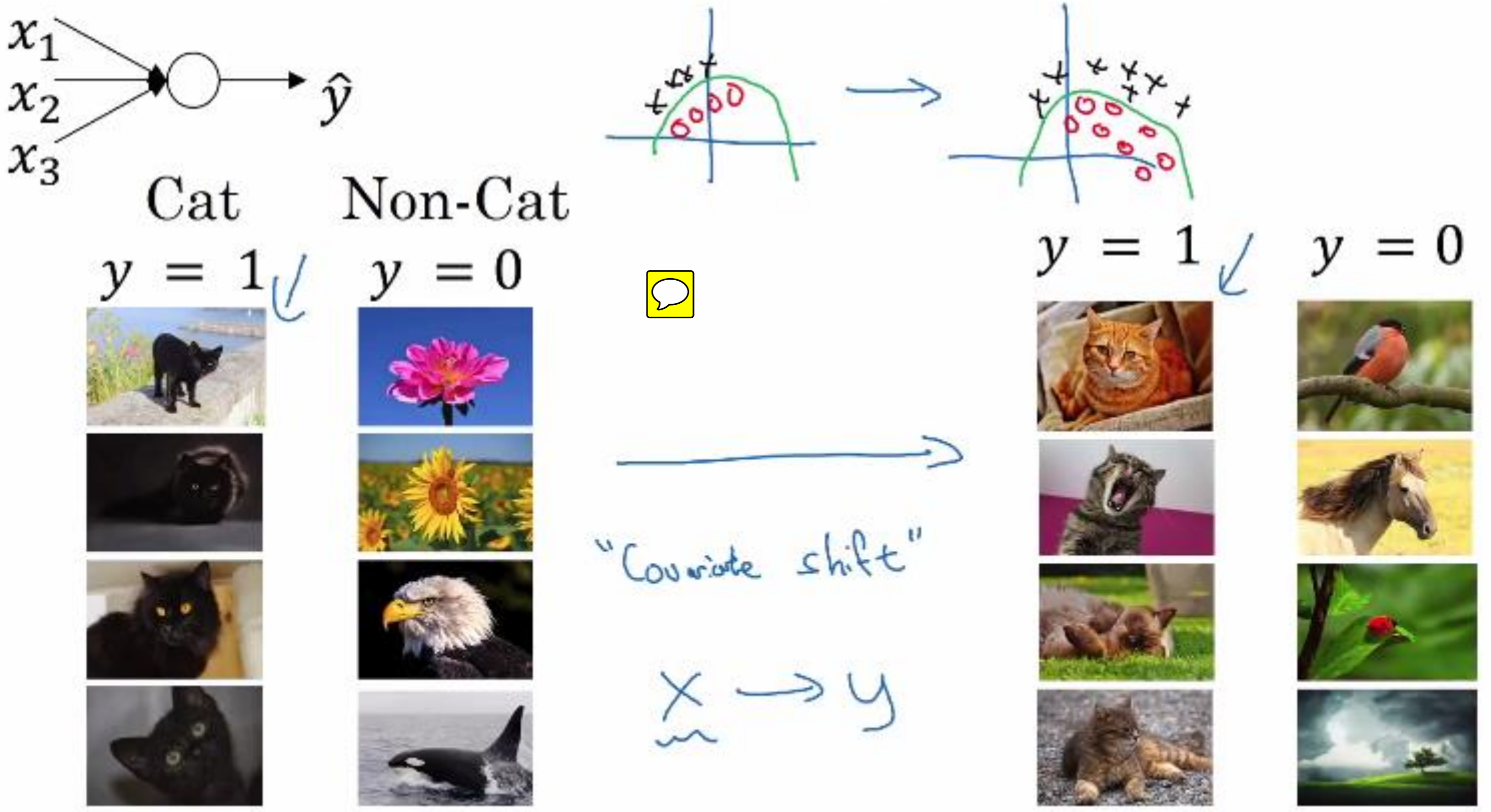
Batch Normalization

Why does Batch Norm work?

Learning on shifting input distribution



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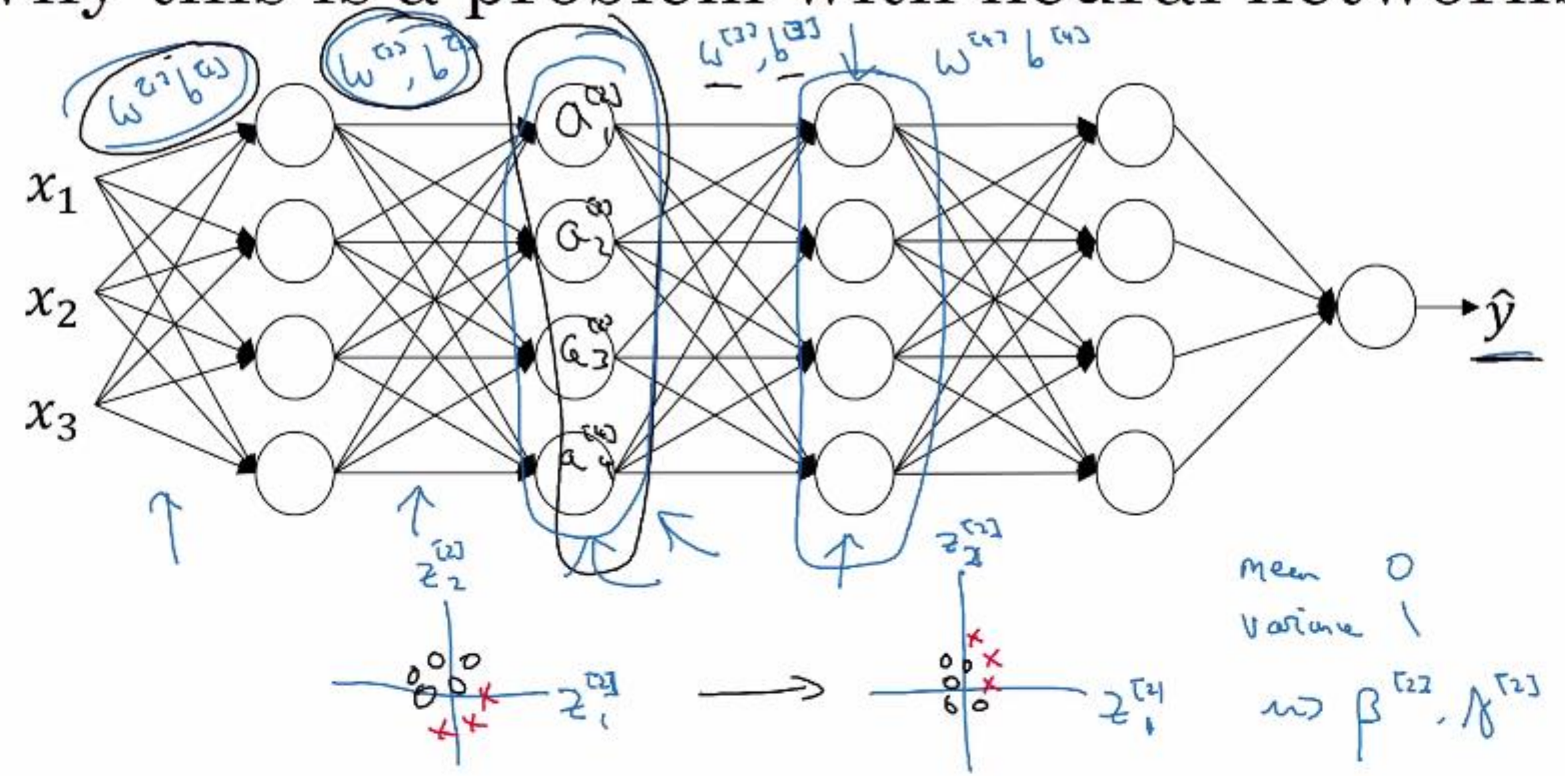
Why this is a problem with neural networks?



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Batch Norm as regularization

X

- Each mini-batch is scaled by the mean/variance computed on just that mini-batch.

$X^{\{t\}}$

$\tilde{z}^{[l]}$ 64, 128 $z^{[l]}$

- This adds some noise to the values $z^{[l]}$ within that minibatch. So similar to dropout, it adds some noise to each hidden layer's activations.

μ, σ^2

- This has a slight regularization effect.

Mini-batch : 64 $\longrightarrow$ 512

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Batch Normalization

Batch Norm at test time

Batch Norm at test time

$$\mu = \frac{1}{m}\sum_i z^{(i)}$$

$$\sigma^2 = \frac{1}{m}\sum_i (z^{(i)} - \mu)^2$$

$$z_{\text{norm}}^{(i)} = \frac{z^{(i)} - \mu}{\sqrt{\sigma^2 + \varepsilon}}$$

$$\tilde{z}^{(i)} = \gamma z_{\text{norm}}^{(i)} + \beta$$

μ, σ^2: estimate using exponentially weighted average (across mini-batches).

$X^{\{1\}}, X^{\{2\}}, X^{\{3\}}, \ldots$

$\mu^{\{1\}[l]}$, $\mu^{\{2\}[l]}$, $\mu^{\{3\}[l]}$ $\longrightarrow$ μ

θ_1, θ_2, θ_3 σ^2

$\sigma^{2\{1\}[l]}$, $\sigma^{2\{2\}[l]}$, $\ldots$

$$z_{\text{norm}} = \frac{z - \mu}{\sqrt{\sigma^2 + \varepsilon}}$$

$$\tilde{z} = \gamma z_{\text{norm}} + \beta$$

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Multi-class classification

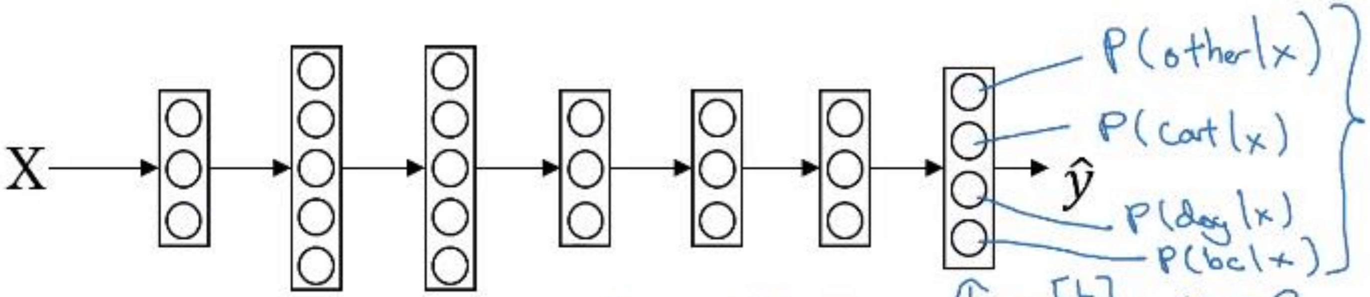
Softmax regression

Recognizing cats, dogs, and baby chicks, other

cats: 1, dogs: 2, baby chicks: 3, other: 0

3 1 2 0 3 2 0 1

C = #classes = 4 $(0, \dots, 3)$



$\hat{y}$ is $(4,1)$

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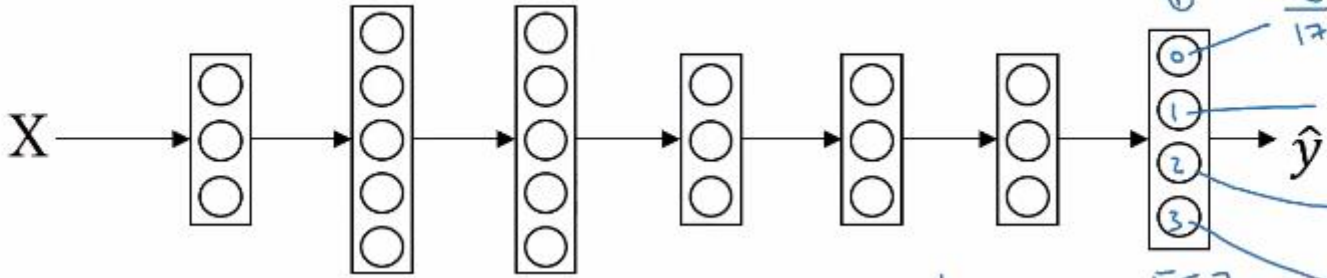
Softmax layer



layer L

$$\frac{e^5}{176.3} = 0.842$$

$$\frac{e^2}{176.3} = 0.042$$

$$\frac{e^{-1}}{176.3} = 0.002$$

$$\frac{e^3}{176.3} = 0.114$$

$$z^{[L]} = w^{[L]} a^{[L-1]} + b^{[L]} \qquad (4,1)$$

Activation function:

$$t = e^{(z^{[L]})} \qquad (4,1)$$

$$\boxed{a^{[L]}} = \frac{e^{z^{[L]}}}{\sum_{j=1}^{4} t_i}, \qquad a_i^{[L]} = \frac{t_i}{\sum_{j=1}^{4} t_i}$$

$\boxed{(4,1)}$ $\hat{y}$

$$\underset{(4,1)}{a^{[L]}} = g^{[L]}(\underset{(4,1)}{z^{[L]}})$$

$$z^{[L]} = \begin{bmatrix} 5 \\ 2 \\ -1 \\ 3 \end{bmatrix}$$

$$t = \begin{bmatrix} e^5 \\ e^2 \\ e^{-1} \\ e^3 \end{bmatrix} = \begin{bmatrix} 148.4 \\ 7.4 \\ 0.4 \\ 20.1 \end{bmatrix}. \qquad \sum_{j=1}^{4} t_j = 176.3$$

$$a^{[L]} = \frac{t}{176.3}$$

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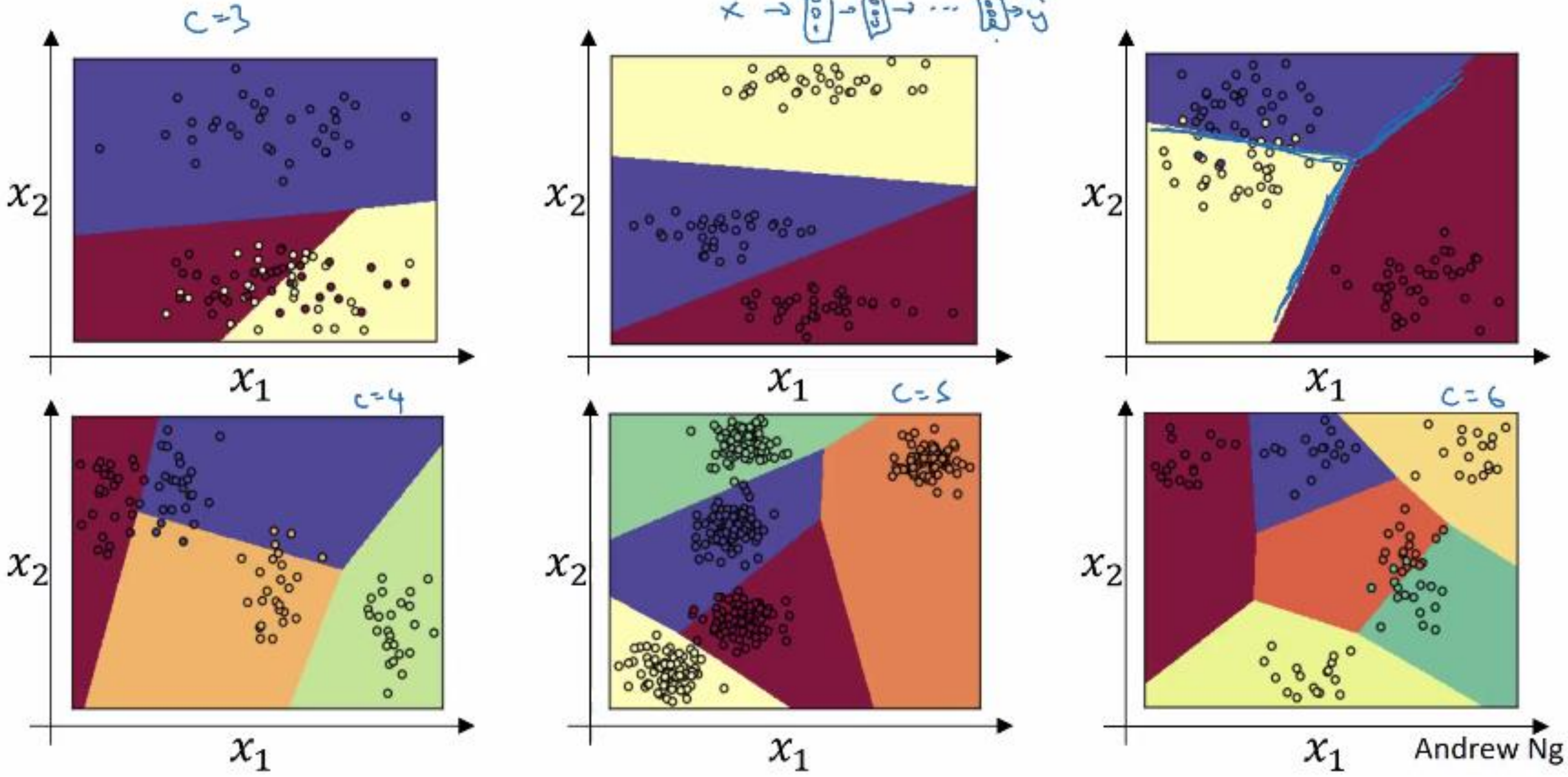
Softmax examples

$x_1, x_2 \rightarrow \boxed{\circ\,\circ\,\circ} \rightarrow \hat{y}$

$z^{[l]} = w^{[l]} x + b^{[l]}$

$a^{[l]} = \hat{y} = g(z^{[l]})$

$x \rightarrow \boxed{\ } \rightarrow \boxed{\ } \rightarrow \cdots \boxed{\ } \rightarrow \hat{y}$



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Multi-class classification

Training a softmax classifier

Understanding softmax

(4,1)

$$z^{[L]} = \begin{bmatrix} 5 \\ 2 \\ -1 \\ 3 \end{bmatrix} \qquad t = \begin{bmatrix} e^5 \\ e^2 \\ e^{-1} \\ e^3 \end{bmatrix}$$

$C = 4$ $\qquad g^{[L]}(\cdot)$

"soft max"

$$a^{[L]} = g^{[L]}(z^{[L]}) = \begin{bmatrix} e^5/(e^5+e^2+e^{-1}+e^3) \\ e^2/(e^5+e^2+e^{-1}+e^3) \\ e^{-1}/(e^5+e^2+e^{-1}+e^3) \\ e^3/(e^5+e^2+e^{-1}+e^3) \end{bmatrix} = \begin{bmatrix} 0.842 \\ 0.042 \\ 0.002 \\ 0.114 \end{bmatrix}$$

"hard max"

$$\begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Softmax regression generalizes logistic regression to C classes.

If $\underline{C=2}$, softmax reduces to logistic regression. $a^{[L]} = \begin{bmatrix} 0.842 \\ \cancel{0.158} \end{bmatrix}$

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Loss function

$(4,1)$

$y^{(i)} = \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \end{bmatrix}$ — cat

$\underline{y_2 = 1}$

$y_1 = y_3 = y_4 = 0$

$(4,1)$

$a^{[L](i)} \approx \hat{y}^{(i)} = \begin{bmatrix} 0.3 \\ 0.2 \\ 0.1 \\ 0.4 \end{bmatrix}$

$C = 4$

$$\underbrace{\mathcal{L}(\hat{y}, y)}_{\text{small}} = \underbrace{-\sum_{j=1}^{4} y_j \log \hat{y}_j}$$

$$J(w^{[1]}, b^{[1]}, \dots) = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(\hat{y}^{(i)}, y^{(i)})$$

$$-y_2 \log \hat{y}_2 = \underline{-\log \hat{y}_2}.$$

Make $\hat{y}_2$ big.

$$Y = [y^{(1)} \; y^{(2)} \dots, y^{(m)}]$$

$$= \begin{bmatrix} 0 & 0 & 1 & \dots \\ 1 & 0 & 0 & \\ 0 & 1 & 0 & \\ 0 & 0 & 0 & \end{bmatrix}$$

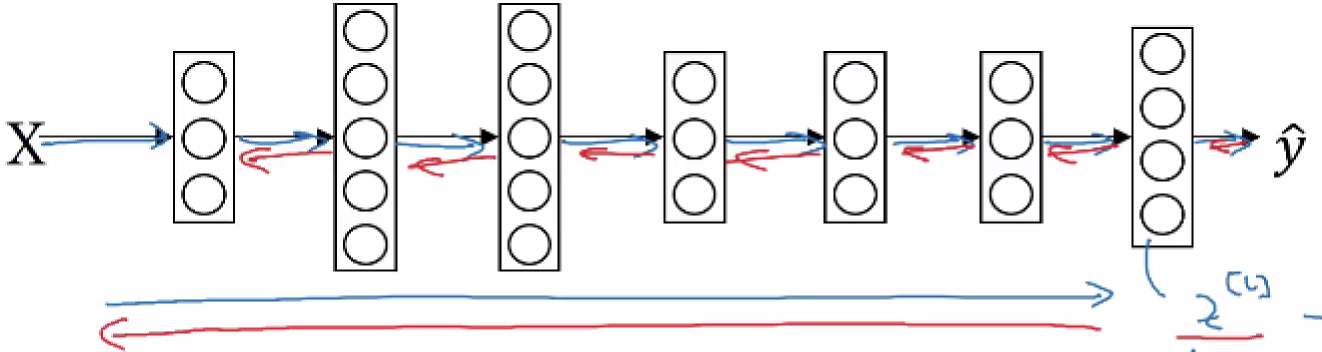
$(4, m)$

$$\hat{Y} = [\hat{y}^{(1)}, \dots, \hat{y}^{(m)}]$$

$$= \begin{bmatrix} 0.3 & \dots \\ 0.2 & \\ 0.1 & \\ 0.4 & \end{bmatrix}$$

$(4, m)$

Gradient descent with softmax



$\underset{(4,1)}{z^{[L]}} \rightarrow a^{[L]} = \hat{y} \rightarrow \mathcal{L}(\hat{y}, y)$

Backprop: $\underset{(4,1)}{dz^{[L]}} = \hat{y} - y$

$\frac{\partial J}{\partial z^{[L]}}$

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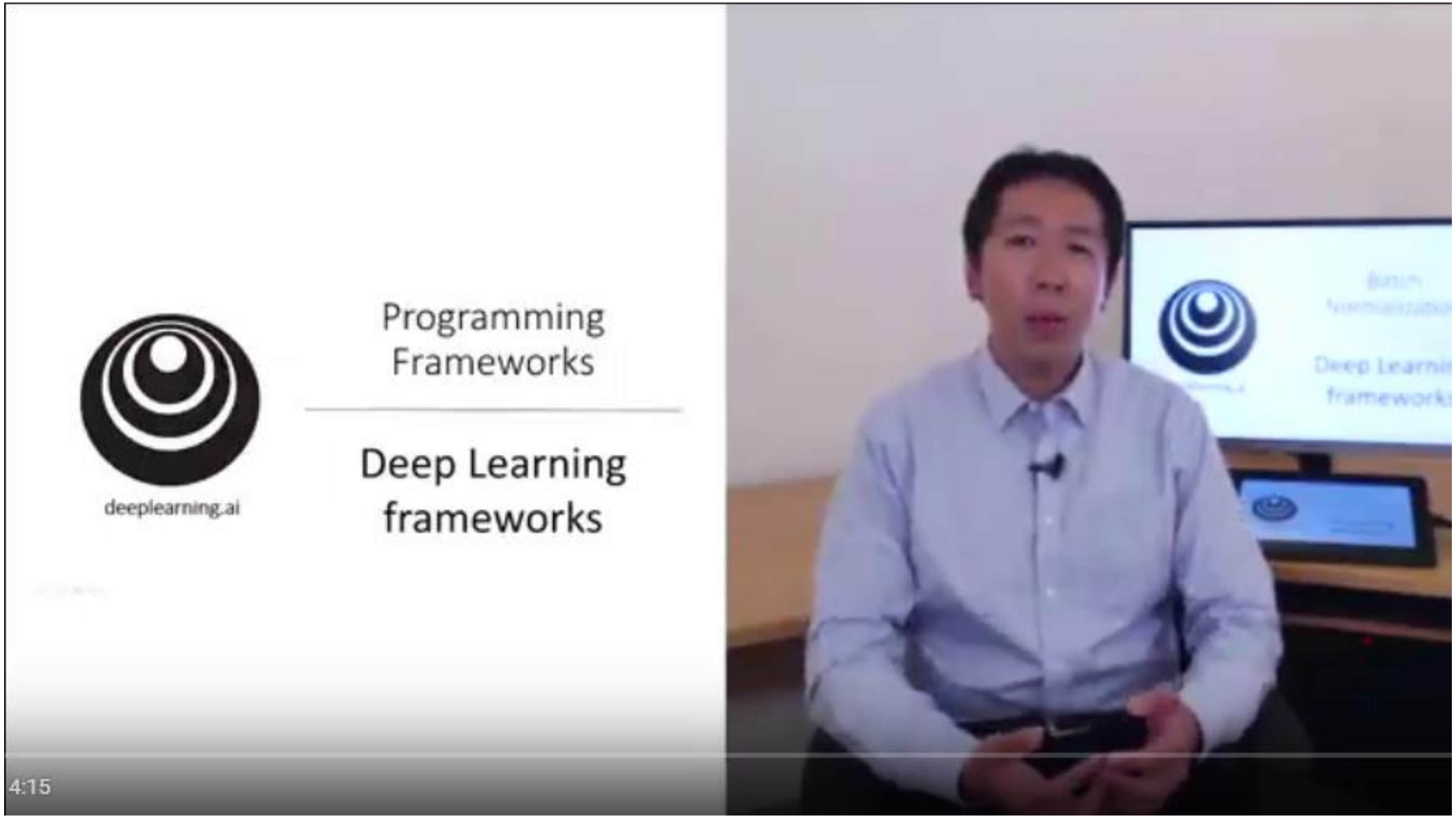
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Programming
Frameworks
Deep Learning
frameworks
4:15

Deep learning frameworks

- Caffe/Caffe2
- CNTK
- DL4J
- Keras
- Lasagne
- mxnet
- PaddlePaddle
- TensorFlow
- Theano
- Torch

Choosing deep learning frameworks

- Ease of programming (development and deployment)
- Running speed
- Truly open (open source with good governance)

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Programming Frameworks

TensorFlow

Motivating problem

$J(w) = \boxed{w^2 - 10w + 25}$

(cost)

$(w-5)^2$

$w = 5$

$J(w, b)$

$\uparrow \ \uparrow$

jupyter TensorFlow example Last Checkpoint: 4 minutes ago (unsaved changes)

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Trusted | Python 3

Code

In [1]:
```python
import numpy as np
import tensorflow as tf
```

In [2]:
```python
w = tf.Variable(0,dtype=tf.float32)
cost = tf.add(tf.add(w**2,tf.multiply(-10.,w)),25)
train = tf.train.GradientDescentOptimizer(0.01).minimize(cost)

init = tf.global_variables_initializer()
session = tf.Session()
session.run(init)
print(session.run(w))
```

```
0.0
```

In [3]:
```python
session.run(train)
print(session.run(w))
```

```
0.1
```

In [4]:
```python
for i in range(1000):
    session.run(train)
print(session.run(w))
```

```
4.99999
```

jupyter TensorFlow example Last Checkpoint: 10 minutes ago (autosaved)

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Notebook saved Trusted Python 3

Code

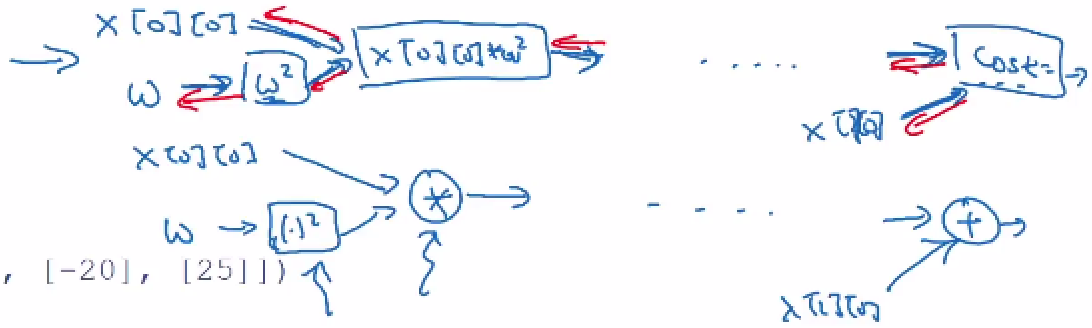
```python
In [1]: import numpy as np
        import tensorflow as tf
```

```python
In [8]: coefficients = np.array([[1.], [-10.], [25.]])

        w = tf.Variable(0,dtype=tf.float32)
        x = tf.placeholder(tf.float32, [3,1])
        #cost = tf.add(tf.add(w**2,tf.multiply(-10.,w)),25)
        #cost = w**2 - 10*w + 25
        cost = x[0][0]*w**2 + x[1][0]*w + x[2][0]
        train = tf.train.GradientDescentOptimizer(0.01).minimize(cost)

        init = tf.global_variables_initializer()
        session = tf.Session()
        session.run(init)
        print(session.run(w))

        0.0
```

```python
In [9]: session.run(train, feed_dict={x:coefficients})
        print(session.run(w))

        0.1
```

```python
In [10]: for i in range(1000):
             session.run(train, feed_dict={x:coefficients})
         print(session.run(w))
```

Code example




```
import numpy as np
import tensorflow as tf

coefficients = np.array([[1], [-20], [25]])

w = tf.Variable([0],dtype=tf.float32)
x = tf.placeholder(tf.float32, [3,1])
cost = x[0][0]*w**2 + x[1][0]*w + x[2][0]    # (w-5)**2
train = tf.train.GradientDescentOptimizer(0.01).minimize(cost)
init = tf.global_variables_initializer()
session = tf.Session()
session.run(init)
print(session.run(w))

for i in range(1000):
    session.run(train, feed_dict={x:coefficients})
print(session.run(w))
```

```
with tf.Session() as session:
    session.run(init)
    print(session.run(w))
```