

2nd law

$$\frac{\partial T}{\partial t} = \dots + \left(\begin{array}{c} \text{vert.} \\ \text{adv} \end{array} + \begin{array}{c} \text{adiabatic} \\ \text{compression} \end{array} \right) \text{Vertical motion term} + \dots$$
$$= \underline{W(\Gamma - \Gamma_d)} \leftarrow \text{HWS}$$

$$= -W \frac{\partial S}{\partial z} \left(\frac{1}{C_p} \right) = -W \frac{\partial S}{\partial p} \left(\frac{1}{C_p} \right) \quad \begin{array}{l} \text{dry static energy} \\ S = C_p T + gz \end{array}$$

$$= -W \frac{\partial \theta}{\partial z} \left(\frac{T}{\theta} \right) = -W \frac{\partial \theta}{\partial p} \left(\frac{T}{\theta} \right) \quad \theta = T \left(\frac{p_0}{p} \right)^{R/C_p}$$