

⌕ Statistical dynamics

- ⌕ Maximum Covariance “modes”
  - Rotated
  - Orthogonal
- ⌕ Impacts that integrate
  - Land: Precip, Evap, hydrology
  - ⌕ Ocean
    - Wind stress
    - Freshwater flux
- ⌕ Zonal mean and eddies
  - Momentum flux  $[u^*v^*]$  drives
  - Zonal PGF vanishes
- ⌕ Time mean and anomalies (or “transients”)
  - Anomaly covariance  $[w^*T^*]$  is eddy or transient heat flux
  - $\text{partial\_t} = \text{conv}(\text{flux})$  or  $=0$  if you assume balance

⌕ Statistics

- ⌕ Joint PDFs
  - Mutual information
  - Covariances
  - Marginal, conditional PDFs
- ⌕ PDF /histogram
  - Shannon information
  - ⌕ Moments
    - Skewness
    - variance (stdev is sqrt)
    - Mean

⌕ Phenomena

- ⌕ Features (coherent structures)
  - intensity
  - durations in time
  - ⌕ scales in space
    - convective
    - mesoscale
    - frontal
    - synoptic
    - planetary
  - boundaries? “systems”?
- ⌕ Maps/grids (MERRA2)
  - ⌕ Data collections: hourly, monthly, diurnal. 3D <https://goldsmr5.gesdisc.eosdis.nasa.gov/dods/>, 2D <https://goldsmr4.gesdisc.eosdis.nasa.gov/dods/>
  - State variables
  - Tendencies
  - Integrated Budgets
  - ⌕ Statistics
    - monthly or daily surface impacts <https://goldsmr4.gesdisc.eosdis.nasa.gov/dods/M2SDNXSLV.info>
    - EXTREMES: [https://disc.gsfc.nasa.gov/datasets/M2SMNXED1\\_1/summary](https://disc.gsfc.nasa.gov/datasets/M2SMNXED1_1/summary) , <https://goldsmr4.gesdisc.eosdis.nasa.gov/dods/M2SMNXED1>
  - Documentation <https://gmao.gsfc.nasa.gov/pubs/docs/Bosilovich785.pdf>
- ⌕ Pure obs (satellite, radar, in situ)
  - spectral imagery interpretations
  - clouds/particles easiest to see
  - hyperlocal values

⌕ Model Outputs

- Forecasts/ hindcasts/ reforecasts
- (Re)Analyses (data assimilation)
- Simulations

⌕ Numerical models: see MindMap Atmosphere.mm

- Regional (w/ neither virtue!)
- ⌕ Globe-covering
  - ⌕ physics
    - water phase changes
    - subgrid turbulence
    - surface interaction
  - ⌕ radiation
    - longwave
    - shortwave
  - ⌕ dynamics
    - spectral
    - gridpoint
  - ⌕ Process-resolving (LES, CRM)
    - microphysics
    - subgrid turbulence
    - resolution
    - boundary conditions
- THE GAP (explicit models help)

⌕ Logic: stability, waves, balance maintenance

- Ageostrophic in QG theory
- Momentum (vort) instabilities
- ⌕ Stratification and lifted-parcel instability
  - Conserved moist variable ( $h$ ,  $\theta_e$ ) lifted from PBL
  - ⌕ Comparison to environment’s saturated value of that indicates sign of  $T_{\text{parcel}} - T_{\text{env}}$ 
    - No Title
  - For linearly-mixing variable, entrainment pulls parcel toward env as it rises
- ⌕ Conservation laws  $d/dt = 0$  + sources-sinks (“tendencies”)
  - ⌕ PV: conserved even w/ horiz div, which affects vorticity and mass between  $\theta$  surfaces in the same (proportional) way
    - Huge in stratosphere (due to static stability part)
    - Mainly matters in strato-tropo sphere interactions
    - ⌕ Source and sink terms:
      1.  $\text{curl}(\text{Friction}) \cdot \text{grad}(\theta)$
      2.  $3D \text{vor} \cdot d(\text{heating})/dz$
    - Curl friction of course
    - Heating acts as a “downward flux” of PV, like how an upper cool-core cyclone spawns or strengthens a surface of warm-core cyclone with latent heat release. “PV substance” is globally conserved!
  - ⌕ Momentum
    - ⌕ Horizontal
      - ⌕ Cartesian tangent plane
        - ⌕  $\text{vort} = v_y - u_x$ , eliminates PGF
          - ⌕ Absolute vort cons:  $R_o$  waves
            - Phase west, energy east, equal
            - Goes as wavelength squared
            - Stationary: roughly continent scale wavelength
          - Relative vort cons: vortex interactions,  $V$  goes as  $1/r$
        - ⌕ aGeostrophic (non-gradient) wind
          - ⌕ Contains almost all of the divergent wind component
            - ⌕ Ooze to maintain balance (QG omega equation)
              - warm advection  $\rightarrow$  ascent
              - vorticity advection above  $\rightarrow$  up
            - gravity waves
            - convection
            - Frictional down-gradient flow
            - Governs change:  $dV/dt = fV_a \times k$
          - ⌕ “Gradient wind”: along isobars (Thereby almost no divergence)
            - ⌕ Vertical diff: “Thermal Wind”  $V_T$  directed along isotherms
              - “equivalent barotropic”  $V_T$  parallel to isobars
              - $V_g$  turns with height: temperature advection
              - Gradient: neglect  $\text{partial}_t(V)$
              - Geostrophic: neglect  $d/dt(V)$
            - Spherical
        - ⌕ Vertical in atm.
          - ⌕ hydrostatic approx.
            - Hypsometric equation relates thickness to  $T$ ,  $p$
            - Use hyd.  $p$  as coordinate
          - ⌕ Full  $dw/dt$  equation
            - Thermal buoyancy
            - Dynamic pressure
        - ⌕ 3D in atm.
          - ⌕ KE:  $V \cdot dV/dt$  eliminates Cor
            - Source:  $V \cdot \text{PGF}$
          - ⌕ Transport
            - Advective
            - Nonadvective
          - Sink:  $V \cdot \text{Fri}$
          - $\text{Curl}(V)$ : turbulence, tornadoes
        - ⌕ solutions (e.g. instabilities)
          - counterweight: stability (KH)
          - internal vorticity line or sheet rolls up into balls, rolls
        - ⌕ Navier-Stokes: Source = Force
          - ⌕ PGF: cop enforcing mass continuity
            - Hydrostatic: fights gravity, prevents collapse on sfc
            - Geostrophic: fights divergence of Coriolis force
            - Dynamic: fights divergence of (advection of momentum)
          - Coriolis if coords rotating
          - Gravity
      - ⌕ Thermo
        - ⌕ Stability & convection logic
          - shear & tornadoes filigree
          - skew- $T$ , log- $p$  plots (trad)
          - moist conserved plots (logical!)
        - ⌕ Moist conserved
          - Liquid water SE:  $s - Lq_{liq}$
          - MSE:  $h = s + Lq_v \cdot dh/dt = Q_{rad} + Q_{mix}$
          - $\theta_e$  (‘equivalent’) or  $\theta_w$  (‘wet bulb’) potential temp.
        - ⌕ Dry conserved
          - ⌕ hydrostatic  $z(p)$ : static energies
            - $s = C_p T + gz$
            - $ds/dt = 0$   
 $+ L \cdot dq/dt + Q_{rad} + Q_{mix}$
            - Enthalpy (heat content):  $C_p T$
          - ⌕ Divide by  $T$ : entropy  $S$ , or potential temperatures ( $\theta$ )
            - $\theta = T(1000 \text{ hPa} / p)^{(R/C_p)}$
          - ⌕ Temperature
            - Has adiabatic compression term, clearer to convert from conserved vars as needed
            - needed for density (thickness, buoyancy)

⌕ Transport tendencies in  $d/dt$

- ⌕ Advection  $-V \cdot \text{del}()$ 
  - separate: vertical, horizontal,...
  - (equals LS flux convergence, in 3D)
- ⌕ Convergence of flux
  - flux by Large-Scale (LS) flow
  - flux by small scales (down gradient: diffusion, viscosity)
  - Area average = flux into perimeter, \*zero for globe\*
- ⌕ Continuity of mass in space-time
  - $\rho \cdot \text{partial}_t$  derivative  $=0$  in Anelastic and Boussinesq sets
  - $\rho \cdot \text{partial}_t = -\text{div}(\rho \cdot V)$

⌕ Vector calculus

- ⌕ 2D: area  $\leftrightarrow$  perimeter
  - Circulation theorem
  - Divergence theorem
- ⌕ 3D Del operator
  - Curl of vector field: only in 3D
  - Divergence of vector field
  - Gradient of scalar field
  - \*fields\* of scalars and vectors
  - Vectors: mag (w/units), direction

⌕ Partial and total derivatives

- total  $d/dt$  in moving coordinate
- partials of  $T(x,y,z,t)$ ,  $T(x,y,p,t)$

⌕ Quantities and Units

- Special honorifics (N, J, W, Pa)
- MKS: Earth, water, 10fingers