## ATbounds-vignette-RHC

```
library(ATbounds)
```

## Right Heart Catheterization Dataset

In this vignette, we revisit the well-known Right Heart Catheterization Dataset available at Vanderbilt Biostatistics Datasets Page. A cleaned version of the dataset is available in the package.

```
Y <- RHC[,"survival"]
D <- RHC[,"RHC"]
X <- RHC[,-c(1,2)]
```

## Bounding the Average Treatment Effect

We take the reference propensity score to be  $\widehat{p}_{RPS}(X_i) = n^{-1} \sum_{i=1}^n D_i$  for each observation i. That is, we assign the sample proportion of the treated to the reference propensity scores uniformly for all observations. Of course, this is likely to be misspecified; however, it has the advantage that  $1/\widehat{p}_{RPS}(X_i)$  is never close to 0 or 1.

```
rps <- rep(mean(D),length(D))</pre>
```

We start with q = 1.

```
atebounds(Y, D, X, rps, q = 1)
#> $y1_lb
#> [1] 0.1217088
#>
#> $y1_ub
#> [1] 0.7408893
#>
#> $y0_lb
#> [1] 0.2292938
#>
#> $y0_ub
#> [1] 0.6101133
#>
#> $ate_lb
#> [1] -0.4884045
#> $ate_ub
#> [1] 0.5115955
#>
#> $ate_rps
#> [1] -0.05072115
#> attr(,"class")
#> [1] "ATbounds"
```

We now consider q=2

```
atebounds(Y, D, X, rps, q = 2)
#> $y1_lb
#> [1] 0.1919228
#>
#> $y1_ub
#> [1] 0.5253205
#>
#> $y0_lb
#> [1] 0.3108389
#>
#> $y0_ub
#> [1] 0.4505982
#> $ate_lb
#> [1] -0.2586755
#>
#> $ate_ub
#> [1] 0.2144815
#>
#> $ate_rps
#> [1] -0.05072115
#>
#> attr(,"class")
#> [1] "ATbounds"
and q = 3.
atebounds(Y, D, X, rps, q = 3)
#> $y1_lb
#> [1] 0.2390884
#>
```

```
#> $y1_ub
#> [1] 0.4545434
#>
#> $y0_lb
#> [1] 0.3437921
#>
#> $y0_ub
#> [1] 0.4073485
#> $ate_lb
#> [1] -0.1682601
#>
#> $ate_ub
#> [1] 0.1107513
#>
#> $ate_rps
#> [1] -0.05072115
#> attr(,"class")
#> [1] "ATbounds"
```

Finally, we take a relatively large q = 10.

```
atebounds(Y, D, X, rps, q = 10)
#> $y1_lb
#> [1] 0.1032951
#>
#> $y1_ub
#> [1] 0.4865839
#>
#> $y0_lb
#> [1] 0.3520645
#>
#> $y0_ub
#> [1] 0.3741887
#>
#> $ate_lb
#> [1] -0.2708936
#>
#> $ate_ub
#> [1] 0.1345195
#>
#> $ate_rps
#> [1] -0.05072115
#>
#> attr(,"class")
#> [1] "ATbounds"
```

## Bounding the Average Treatment Effect on the Treated

We now look at ATT with a few values of q.

```
attbounds(Y, D, X, rps, q = 3)
#> $lb
#> [1] -0.1479596
#>
#> $ub
#> [1] 0.01893426
#> $att_rps
#> [1] -0.05072115
#>
#> attr(,"class")
#> [1] "ATbounds"
attbounds(Y, D, X, rps, q = 5)
#> $lb
#> [1] -0.1059798
#>
#> $ub
#> [1] -0.01226633
#>
#> $att_rps
#> [1] -0.05072115
#>
#> attr(,"class")
#> [1] "ATbounds"
 attbounds(Y, D, X, rps, q = 10)
```

```
#> $lb
#> [1] -0.06088469
#>
#> $ub
#> [1] -0.002788356
#>
#> $att_rps
#> [1] -0.05072115
#>
#> attr(,"class")
#> [1] "ATbounds"
```