

ATbounds: An R vignette using the Right Heart Catheterization Dataset

```
library(ATbounds)
```

Right Heart Catheterization Dataset

In this vignette, we revisit the well-known Right Heart Catheterization Dataset available at Vanderbilt Biostatistics Datasets Page. A cleaned version of the dataset is available in the package.

```
Y <- RHC[, "survival"]
D <- RHC[, "RHC"]
X <- RHC[, -c(1, 2)]
```

Bounding the Average Treatment Effect

We take the reference propensity score to be $\hat{p}_{\text{RPS}}(X_i) = n^{-1} \sum_{i=1}^n D_i$ for each observation i . That is, we assign the sample proportion of the treated to the reference propensity scores uniformly for all observations. Of course, this is likely to be misspecified; however, it has the advantage that $1/\hat{p}_{\text{RPS}}(X_i)$ is never close to 0 or 1.

```
rps <- rep(mean(D), length(D))
```

We start with $Q = 1$.

```
summary(atebounds(Y, D, X, rps, Q = 1))
#> ATbounds: ATE
#> Call: atebounds(Y = Y, D = D, X = X, rps = rps, Q = 1)
#> Confidence Level: 0.95
#>
#> Lower_Bound Upper_Bound
#> Bound Estimate -0.47742 0.48753
#> Confidence Interval -0.54972 0.55664
```

We now consider $Q = 2$

```
summary(atebounds(Y, D, X, rps, Q = 2))
#> ATbounds: ATE
#> Call: atebounds(Y = Y, D = D, X = X, rps = rps, Q = 2)
#> Confidence Level: 0.95
#>
#> Lower_Bound Upper_Bound
#> Bound Estimate -0.17275 0.018032
#> Confidence Interval -0.21518 0.063421
```

and $Q = 3$.

```
summary(atebounds(Y, D, X, rps, Q = 3))
#> ATbounds: ATE
#> Call: atebounds(Y = Y, D = D, X = X, rps = rps, Q = 3)
#> Confidence Level: 0.95
#>
#> Lower_Bound Upper_Bound
#> Bound Estimate -0.11213 -0.058280
#> Confidence Interval -0.14658 -0.022432
```

Finally, we take $Q = 4$.

```
summary(atebounds(Y, D, X, rps, Q = 4))
#> ATbounds: ATE
#> Call: atebounds(Y = Y, D = D, X = X, rps = rps, Q = 4)
#> Confidence Level: 0.95
#>
#> Lower_Bound Upper_Bound
#> Bound Estimate -0.083816 -0.122172
#> Confidence Interval -0.143475 -0.057158
```

Bounding the Average Treatment Effect on the Treated

We now look at ATT with a few values of Q .

```
summary(attbounds(Y, D, X, rps, Q = 2))
#> ATbounds: ATT
#> Call: attbounds(Y = Y, D = D, X = X, rps = rps, Q = 2)
#> Confidence Level: 0.95
#>
#> Lower_Bound Upper_Bound
#> Bound Estimate -0.16859 0.003702
#> Confidence Interval -0.21617 0.038830
summary(attbounds(Y, D, X, rps, Q = 3))
#> ATbounds: ATT
#> Call: attbounds(Y = Y, D = D, X = X, rps = rps, Q = 3)
#> Confidence Level: 0.95
#>
#> Lower_Bound Upper_Bound
#> Bound Estimate -0.077412 -0.039280
#> Confidence Interval -0.116903 -0.006371
summary(attbounds(Y, D, X, rps, Q = 4))
#> ATbounds: ATT
#> Call: attbounds(Y = Y, D = D, X = X, rps = rps, Q = 4)
#> Confidence Level: 0.95
#>
#> Lower_Bound Upper_Bound
#> Bound Estimate -0.048803 -0.057035
#> Confidence Interval -0.090023 -0.016366
```