Data Mining Project (MaBAn 2020)

Predicting obesity levels according to daily habits

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Introduction

For this project, our objective is to predict the expected weight level (in Kg) for a given person depending on certain daily habits (eating and physical activity) and on the person's age, gender and height.

To do this, we found a quite interesting dataset (click here: http://archive.ics.uci.edu/ml/datasets/Estimation+of+obesity+levels+based+on+eating+habits+and+physical+condition+) containing 2111 observations and 17 variables (mainly categorical).

Please, find here a manually created metadata table:

```
# To adjust the page margins when knitting to PDF :
library(knitr)
opts_chunk$set(tidy.opts=list(width.cutoff=45),tidy=TRUE)
```

```
# Used packages :
library(pander)
library(dplyr)
library(gt)
library(car)
library(ggplot2)
library(gridExtra)
library(psych)
library(corrplot)
library(ellipse)
library(dummies)
library(nnet)
library(class)
library(caret)
library(rpart)
library(rpart.plot)
library(ehaGoF)
library(forecast)
library(randomForest)
# Working Directory :
setwd("~/GitHub/CVTDM_Project_MaBAn_2020")
# Reading the data :
obesity <- read.csv("Obesity.csv", header = T,
    sep = ",")
attach(obesity)
obesity original <- obesity
# Small metadata table :
tibble table <- tibble(`Variable Name` = c(colnames(obesity)[1:14],
    "", colnames(obesity)[15:17]), Description = c("Gender",
    "Age", "Height", "Weight", "Has a family member suffered or suffers from overweight?
    "Do you eat high caloric food frequently?",
    "Do you usually eat vegetables in your meals?",
    "How many main meals do you have daily?",
    "Do you eat any food between meals?", "Do you smoke?",
    "How much water do you drink daily?", "Do you monitor the calories you eat daily?",
    "How often do you have physical activity?",
```

```
"How much time do you use technological devices such as",
   "cell phone videogames, television, computer and others?",
   "How often do you drink alcohol?", "Which transportation do you usually use?",
   "Obesity level based on calculation of Mass Body Index"))

metadata <- gt(data = tibble_table)

metadata %>% tab_header(title = md("**Metadata**"),
   subtitle = "from the dataset we are using") %>%

tab_source_note(source_note = "Based on information in :
   https://www.sciencedirect.com/science/article/pii/S2352340919306985")
```

Metadata

from the dataset we are using

| Variable Name | Description |
|--------------------------------|--|
| Gender | Gender |
| Age | Age |
| Height | Height |
| Weight | Weight |
| family_history_with_overweight | Has a family member suffered or suffers from overweight? |
| FAVC | Do you eat high caloric food frequently? |
| FCVC | Do you usually eat vegetables in your meals? |
| NCP | How many main meals do you have daily? |
| CAEC | Do you eat any food between meals? |
| SMOKE | Do you smoke? |
| CH2O | How much water do you drink daily? |
| SCC | Do you monitor the calories you eat daily? |
| FAF | How often do you have physical activity? |
| TUE | How much time do you use technological devices such as |
| | cell phone videogames, television, computer and others? |
| CALC | How often do you drink alcohol? |
| MTRANS | Which transportation do you usually use? |
| NObeyesdad | Obesity level based on calculation of Mass Body Index |

Based on information in :

https://www.sciencedirect.com/science/article/pii/S2352340919306985

Here is a small overview of the first observations:

```
pander(head(obesity))
```

Table continues below

| Gender | Age | Height | Weight | family_history_with_overwe | eightFAVC | FCVC |
|--------|-----|--------|--------|----------------------------|-----------|------|
| Female | 21 | 1.62 | 64 | yes | no | 2 |
| Female | 21 | 1.52 | 56 | yes | no | 3 |
| Male | 23 | 1.8 | 77 | yes | no | 2 |
| Male | 27 | 1.8 | 87 | no | no | 3 |
| Male | 22 | 1.78 | 89.8 | no | no | 2 |
| Male | 29 | 1.62 | 53 | no | yes | 2 |

Table continues below

| NCP | CAEC | SMOKE | CH2O | SCC | FAF | TUE | CALC |
|-----|-----------|-------|------|-----|-----|-----|------------|
| 3 | Sometimes | no | 2 | no | 0 | 1 | no |
| 3 | Sometimes | yes | 3 | yes | 3 | 0 | Sometimes |
| 3 | Sometimes | no | 2 | no | 2 | 1 | Frequently |
| 3 | Sometimes | no | 2 | no | 2 | 0 | Frequently |
| 1 | Sometimes | no | 2 | no | 0 | 0 | Sometimes |
| 3 | Sometimes | no | 2 | no | 0 | 0 | Sometimes |

| MTRANS | NObeyesdad | |
|-----------------------|------------------------|--|
| Public_Transportation | Normal_Weight | |
| Public_Transportation | $Normal_Weight$ | |
| Public_Transportation | $Normal_Weight$ | |
| Walking | $Overweight_Level_I$ | |
| Public_Transportation | Overweight_Level_II | |
| Automobile | Normal_Weight | |

The variable of interest is "Weight", it will be our dependent variable.

This data set seems to be of high quality, because it has no missing observations, and our subsequent exploratory analysis will tell us if there are outliers to be handled with.

We will first begin with a basic data pre-processing which will be followed by a Data Exploratory Analysis. We will develop several models in order to accurately predict the level of weight of each individual.

The models will be:

- 1. Multiple Linear Regression
- 2. Regression tree
- 3. k-Nearest Neighbors
- 4. Ensemble Method

We will deploy the best model based on error metrics and prediction performance.

At the very end, we will make a **Shiny App** available, in which any user can fill-in a questionnaire concerning daily habits, age and height. Then, the App will tell the user what is the expected weight according to those characteristics, and will present the result in two forms:

- The expected weight in Kg.
- The expected obesity level based on the Body Mass Index, following the classification comming from the World Health Organisation.

The user will also be able to **select the type of model** that will predict the results. That way, it will be interesting to see with just a few clicks how each model will yield different results.

Data Pre-Processing

The first thing to do is to change the column names so that they are more visually meaningful and less confusing.

```
# Changing column names:

names(obesity)[5] = "family_history"
names(obesity)[6] = "eat_caloric"
names(obesity)[7] = "vegetables"
names(obesity)[8] = "main_meals"
names(obesity)[9] = "food_inbetween"
names(obesity)[12] = "monitor_cal"
names(obesity)[13] = "physical_act"
names(obesity)[14] = "tech_devices"
names(obesity)[15] = "alcohol"
```

```
# Checking the dataset structure :
pander(str(obesity))
```

'data.frame': 2111 obs. of 17 variables: \$ Gender : chr "Female" "Female" "Male" "Male" ... \$ Age : num 21 21 23 27 22 29 23 22 24 22 ... \$ Height : num 1.62 1.52 1.8 1.8 1.78 1.62 1.5 1.64 1.78 1.72 ... \$ Weight : num 64 56 77 87 89.8 53 55 53 64 68 ... \$ family_history: chr "yes" "yes" "yes" "no" ... \$ eat_caloric : chr "no" "no" "no" "no" ... \$ vegetables :

num 2 3 2 3 2 2 3 2 3 2 ... \$ main_meals : num 3 3 3 3 1 3 3 3 3 3 ... \$ food_inbetween: chr "Sometimes" "Sometimes" "Sometimes" ... \$ SMOKE : chr "no" "yes" "no" "no" ... \$ CH2O : num 2 3 2 2 2 2 2 2 2 2 2 ... \$ monitor_cal : chr "no" "yes" "no" ... \$ physical_act : num 0 3 2 2 0 0 1 3 1 1 ... \$ tech_devices : num 1 0 1 0 0 0 0 0 1 1 ... \$ alcohol : chr "no" "Sometimes" "Frequently" "Frequently" ... \$ MTRANS : chr "Public_Transportation" "Public_Transportation" "Public_Transportation" "Walking" ... \$ NObeyesdad : chr "Normal_Weight" "Normal_Weight" "Normal_Weight" "Overweight_Level_I" ...

pander(summary(obesity[, 2:4]))

| Age | Height | Weight |
|---------------|-----------------|----------------|
| Min. :14.00 | Min. :1.450 | Min.: 39.00 |
| 1st Qu.:19.95 | 1st Qu.:1.630 | 1st Qu.: 65.47 |
| Median :22.78 | Median $:1.700$ | Median: 83.00 |
| Mean $:24.31$ | Mean $:1.702$ | Mean: 86.59 |
| 3rd Qu.:26.00 | 3rd Qu.:1.768 | 3rd Qu.:107.43 |
| Max. $:61.00$ | Max. :1.980 | Max. $:173.00$ |

Since many variables are numerical and continuous between a range (for example vegetables, inside the range 1 to 3), we will transform them into categorical. This is, somehow, BINNING. For this, we will follow the names given in the information file refered to earlier (https://www.sciencedirect.com/science/article/pii/S2352340919306985).

To make this task easier, we created a function that bins variables. This function is called "binning"

```
# Binning some numerical variables :
binning <- function(x) {
    # vegetables
    x$vegetables[x$vegetables <= 1] <- "Never"

    x$vegetables[x$vegetables > 1 & x$vegetables <= 2] <- "Sometimes"

    x$vegetables[x$vegetables > 2 & x$vegetables <= 3] <- "Always"

# main_meals
x$main_meals[x$main_meals >= 1 & x$main_meals <</pre>
```

```
3] <- "Btw_1_&_2"
    x$main meals[x$main meals == 3] <- "Three"
    x$main meals[x$main meals > 3 & x$main meals <=
        4] <- "More than 3"
    # tech_devices
    x$tech_devices [x$tech_devices >= 0 & x$tech_devices <=
        0.5] <- "Zero_hours"
   x$tech_devices[x$tech_devices <= 1.5] <- "One_hour"</pre>
    x$tech_devices[x$tech_devices <= 2] <- "Two_hours"</pre>
    # physical_act
    x$physical act[x$physical act < 1] <- "I do not have"</pre>
    x$physical_act[x$physical_act >= 1 & x$physical_act <=</pre>
        2] <- "1 or 2 days"
    x$physical act[x$physical act >= 2 & x$physical act <=
        4] <- "2 or 4 days"
    x$physical act[x$physical act >= 4 & x$physical act <=
        5] <- "4 or 5 days"
    # CH20
    x$CH20[x$CH20 <= 2] <- "Between 1 and 2 L"
    x$CH20[x$CH20 <= 3] <- "More than 2 L"
    return(x)
}
obesity = binning(obesity)
```

As we saw with the "str()" function, all the categorical variables are treated as "character". Therefore, we will convert all the categorical variables to "factor" type.

Just as we did with the binning, we created a function to convert character variables to factor. This function is called "to_factor".

```
# Converting character variables to factor :
to_factor <- function(x) {</pre>
    x$Gender = as.factor(x$Gender)
    x$family history = as.factor(x$family history)
    x$eat caloric = as.factor(x$eat caloric)
    x$food_inbetween = as.factor(x$food_inbetween)
    x$SMOKE = as.factor(x$SMOKE)
    x$monitor cal = as.factor(x$monitor cal)
    x$alcohol = as.factor(x$alcohol)
    x$MTRANS = as.factor(x$MTRANS)
    x$NObeyesdad = as.factor(x$NObeyesdad)
    x$vegetables = as.factor(x$vegetables)
    x$main meals = as.factor(x$main meals)
    x$CH20 = as.factor(x$CH20)
    x$physical act = as.factor(x$physical act)
    x$tech_devices = as.factor(x$tech_devices)
    return(x)
}
obesity = to_factor(obesity)
```

Our next step will to remove any missing values.

```
# Checking if there are Missing Values :
sum(is.na(obesity))
```

[1] 0

There are no missing values within our dataset.

We will now proceed with the dummification of the categorical variables. All variables (with the exception of gender, age, height and weight) have already been dummyfied.

```
# Dummyfing the binary
# variables(family history, eat caloric,
# SMOKE, and monitor_cal) :
# Gender 1 = female, 0 = male
obesity dummy <- cbind(dummy(obesity$Gender, sep = " "),
    obesity[2:17])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
names(obesity dummy)[1] <- c("Gender")</pre>
obesity dummy \leftarrow subset(obesity dummy, select = -c(2))
# family history 1 = yes, 0 = no
obesity dummy <- cbind(obesity dummy[1:4], dummy(obesity dummy$family hist,
    sep = ""), obesity dummy[6:17])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
names(obesity dummy)[6] <- c("family hist")</pre>
obesity dummy \leftarrow subset(obesity dummy, select = -c(5))
# eat caloric with 1 = yes, 0 = no
obesity dummy <- cbind(obesity dummy[1:5], dummy(obesity dummy$eat caloric,
    sep = "_"), obesity_dummy[7:17])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
names(obesity dummy)[7] <- c("eat caloric")</pre>
obesity_dummy <- subset(obesity_dummy, select = -c(6))</pre>
\# SMOKE 1 = yes, 0 = no
obesity dummy <- cbind(obesity dummy[1:9], dummy(obesity dummy$SMOKE,
    sep = "_"), obesity_dummy[11:17])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
```

```
names(obesity dummy)[11] <- c("smoke")</pre>
obesity_dummy <- subset(obesity_dummy, select = -c(10))</pre>
# monitor cal 1 = yes, 0 = no
obesity dummy <- cbind(obesity dummy[1:11], dummy(obesity dummy$monitor cal,
    sep = "_"), obesity_dummy[13:17])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
names(obesity dummy)[13] <- c("monitor cal")</pre>
obesity dummy <- subset(obesity dummy, select = -c(12))
# Dummmyfying the categorical variables
# vegetables
obesity dum <- cbind(obesity dummy[1:6], dummy(obesity dummy$vegetables,
    sep = "_"), obesity_dummy[8:17])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
names(obesity dum)[7:9] <- c("vegetables never",</pre>
    "vegetables sometimes", "vegetables always")
# main meals
obesity dum <- cbind(obesity dum[1:9], dummy(obesity dum$main meals,
    sep = " "), obesity dum[11:19])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
names(obesity_dum)[10:12] <- c("main_meals_Btw_1_2",</pre>
    "main meals More than 3", "main meals three")
# food in between
obesity dum <- cbind(obesity dum[1:12], dummy(obesity dum$food inbetween,
    sep = " "), obesity dum[14:21])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
```

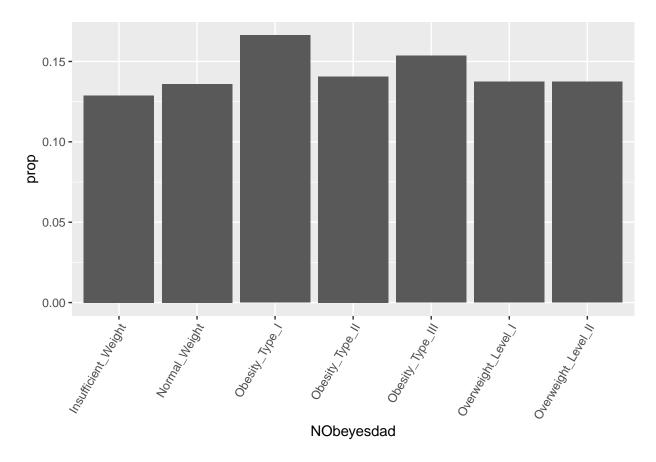
```
names(obesity_dum)[13:16] <- c("food_inbetween_always",</pre>
    "food inbetween frequently", "food_inbetween_no",
    "food inbetween sometimes")
# alcohol
obesity dum <- cbind(obesity dum[1:21], dummy(obesity dum$alcohol,
    sep = ""), obesity dum[23:24])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
names(obesity dum)[22:25] <- c("alcohol always",</pre>
    "alcohol_frequently", "alcohol_no", "alcohol sometimes")
# MTRANS
obesity dum <- cbind(obesity dum[1:25], dummy(obesity dum$MTRANS,
    sep = "_"), obesity_dum[27])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
names(obesity dum)[26:30] <- c("mtrans automobile",</pre>
    "mtrans_bike", "mtrans_motorbike", "mtrans_public_transportation",
    "mtrans walking")
# CH20
obesity_dum <- cbind(obesity_dum[1:17], dummy(obesity_dum$CH20,
    sep = "_"), obesity_dum[19:31])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
names(obesity dum)[18:20] <- c("CH20 less than a liter",</pre>
    "CH20_between_1_and_2", "CH20_more_than_2")
# physical act
obesity_dum <- cbind(obesity_dum[1:21], dummy(obesity_dum$physical_act,
    sep = "_"), obesity_dum[23:33])
## Warning in model.matrix.default(~x - 1, model.frame(~x - 1), contrasts = FALSE):
## non-list contrasts argument ignored
```

Finally, the last step in the data pre-processing is the partitionning of the data. We partitionned the data into a 60% training set and a 40% validation set. Because we have a relatively small number of observations (only 2111 observations), we thought it best to exclude a test set. However, better results could be obtained if we kept a third "test set".

Now that we have finished with the data pre-processing, we can proceed with the exploratory data analysis. While we have dumyfied variables in the steps above, the original non-dummified versions of the variables will be used in the exploratory data analysis for vizualisation purposes.

Exploratory Data Analysis

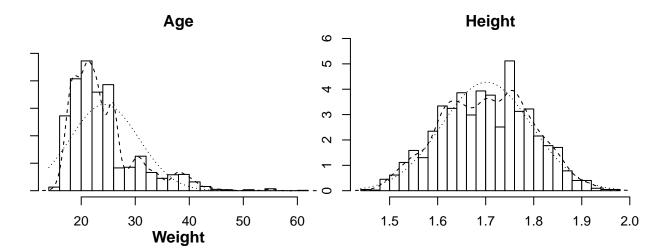
```
ggplot(data = obesity, aes(x = NObeyesdad)) +
    geom_bar(aes(y = ..prop.., group = 1)) + theme(axis.text.x = element_text(angle = 60
    hjust = 1))
```



We see that the distribution of observations across the different weights is quite uniform, meaning that we do not have an unbalanced data set with respect to our variable of interest (the weight).

Let's now look at some histograms for all the continuous variables in our dataset.

```
# Creating histograms :
multi.hist(obesity[, 2:4], density = TRUE)
```

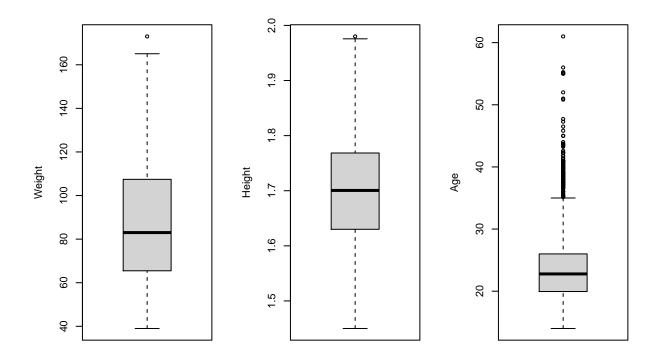


```
40 60 80 100 120 140 160 180
```

```
# Creating boxplots :

par(mfrow = c(1, 3))

boxplot(obesity$Weight, ylab = "Weight")
boxplot(obesity$Height, ylab = "Height")
boxplot(obesity$Age, ylab = "Age")
```



```
# We may have ONE outlier for Weight, and
# almost one for Height! Age is VERY right
# skewed!

# comment on why we are not removing the
# outliers
```

Interpretation:

. . .

Now, let's do some barplots in order to get an idea of the distribution of each of the categorical variables.

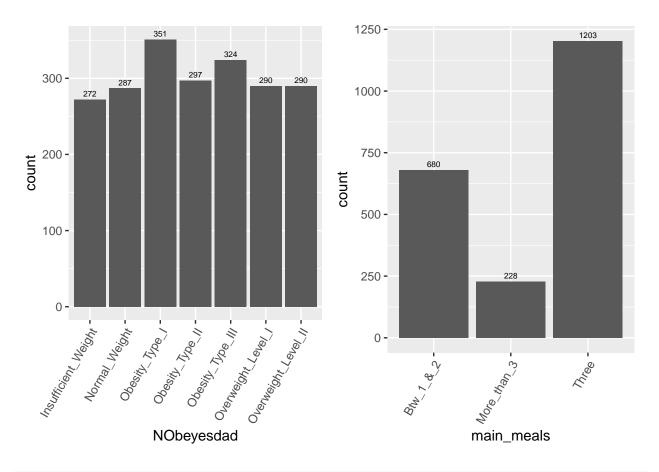
```
# Barplots :

plot_1 = ggplot(data = obesity, aes(x = NObeyesdad)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ..count..), vjust = -0.5, size = 2.2)

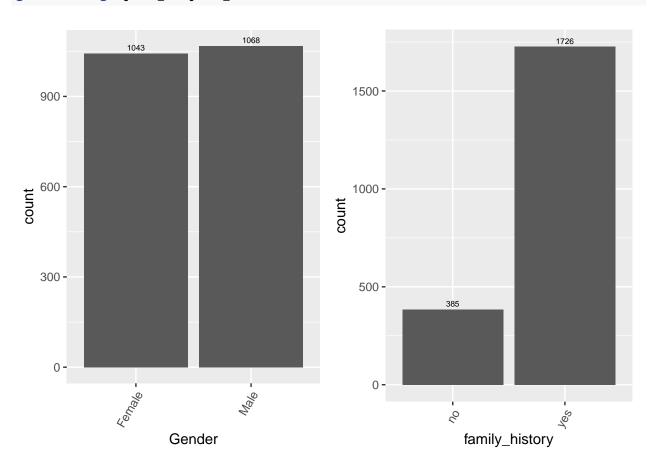
plot_2 = ggplot(data = obesity, aes(x = main_meals)) +
    geom_bar(aes(y = ..count.., group = 1)) +
```

```
theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ..count..), vjust = -0.5, size = 2.2)
plot 3 = ggplot(data = obesity, aes(x = Gender)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ...count...), vjust = -0.5, size = 2.2)
plot_4 = ggplot(data = obesity, aes(x = family_history)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ..count..), vjust = -0.5, size = 2.2)
plot 5 = ggplot(data = obesity, aes(x = vegetables)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ...count...), vjust = -0.5, size = 2.2)
plot_6 = ggplot(data = obesity, aes(x = food_inbetween)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ...count...), vjust = -0.5, size = 2.2)
plot 7 = ggplot(data = obesity, aes(x = tech devices)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ..count..), vjust = -0.5, size = 2.2)
plot_8 = ggplot(data = obesity, aes(x = eat_caloric)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ...count...), vjust = -0.5, size = 2.2)
plot_9 = ggplot(data = obesity, aes(x = SMOKE)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ...count...), vjust = -0.5, size = 2.2)
plot_10 = ggplot(data = obesity, aes(x = CH20)) +
```

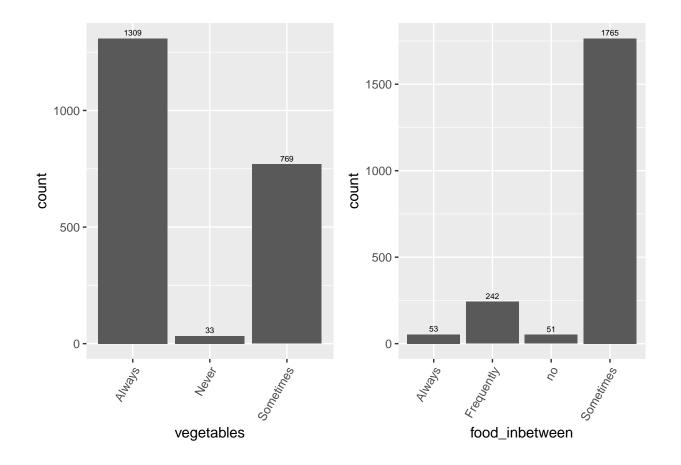
```
geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ..count..), vjust = -0.5, size = 2.2)
plot_11 = ggplot(data = obesity, aes(x = monitor_cal)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ...count...), vjust = -0.5, size = 2.2)
plot_12 = ggplot(data = obesity, aes(x = physical_act)) +
    geom bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ..count..), vjust = -0.5, size = 2.2)
plot 13 = ggplot(data = obesity, aes(x = alcohol)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ...count...), vjust = -0.5, size = 2.2)
plot_14 = ggplot(data = obesity, aes(x = MTRANS)) +
    geom_bar(aes(y = ..count.., group = 1)) +
    theme(axis.text.x = element_text(angle = 60,
        hjust = 1)) + geom_text(stat = "count",
    aes(label = ...count...), vjust = -0.5, size = 2.2)
# Arranging them two-by-two :
grid.arrange(plot 1, plot 2, ncol = 2)
```



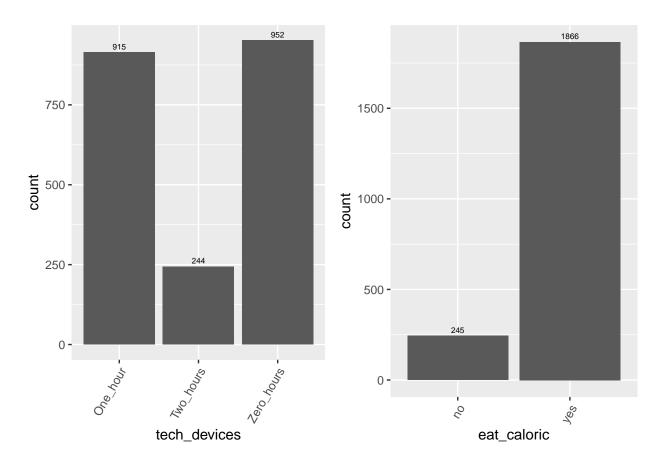
grid.arrange(plot_3, plot_4, ncol = 2)



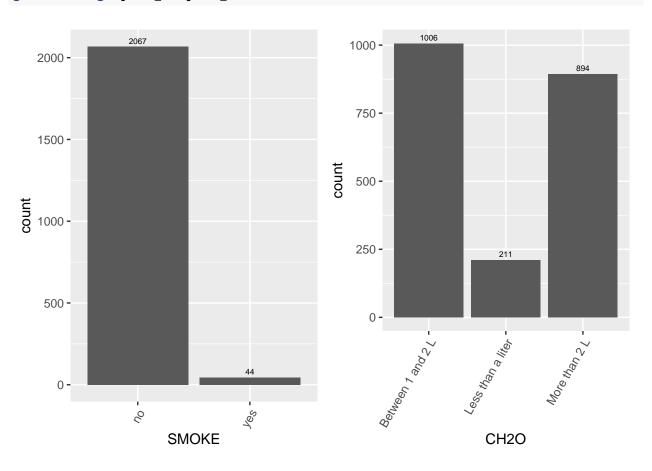
grid.arrange(plot_5, plot_6, ncol = 2)



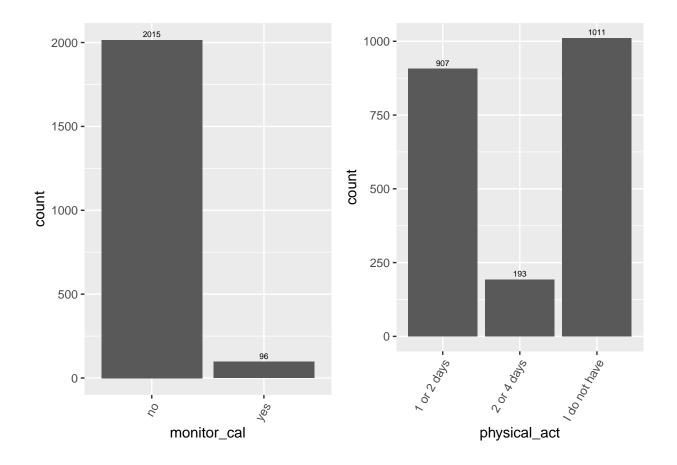
grid.arrange(plot_7, plot_8, ncol = 2)



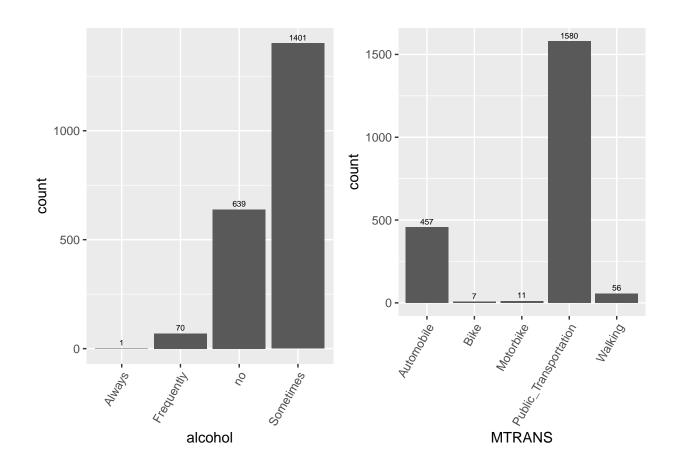
grid.arrange(plot_9, plot_10, ncol = 2)



grid.arrange(plot_11, plot_12, ncol = 2)

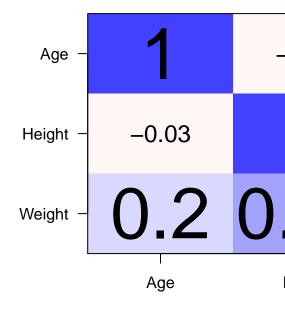


grid.arrange(plot_13, plot_14, ncol = 2)



```
# Correlation plot
cor.plot(na.omit(obesity[c(2, 3, 4)]))
```

Corre



Let's look at the correlations between the variables.

```
# comment on correlation and how we didnt do
# it for categorical variables
```

Data Analysis

Multiple Linear Regression

We begin with a multiple linear regression model. We will first run a full model with (n-1) dummy categories included for each variable. In most cases the dummy that was excluded from the formula this the dummy which refered to the variable category "no" or equivalent. For instance, for the variable alcohol, we excluded the variable alcohol_no from the model formula.

```
# Linear regression
# formula: Weight = Gender, Age, Height,

lm_weight <- lm(Weight ~ Gender + Age + Height +
    family_hist + eat_caloric + vegetables_sometimes +
    vegetables_always + main_meals_Btw_1_2 + main_meals_More_than_3 +</pre>
```

```
CH20 more than 2 + monitor cal + physical act 1 2 +
    physical_act_2_4 + tech_1_hour + tech_2_hours_or_more +
    alcohol_always + alcohol_frequently + alcohol_sometimes +
    mtrans_automobile + mtrans_bike + mtrans_public_transportation,
    data = train.set)
summary(lm_weight)
##
## Call:
## lm(formula = Weight ~ Gender + Age + Height + family_hist + eat_caloric +
       vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 +
##
       main meals More than 3 + food inbetween always + food inbetween frequently +
##
       food inbetween sometimes + smoke + CH2O between 1 and 2 +
##
       CH2O_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
##
##
       tech_1_hour + tech_2_hours_or_more + alcohol_always + alcohol_frequently +
##
       alcohol_sometimes + mtrans_automobile + mtrans_bike + mtrans_public_transportatio
##
       data = train.set)
##
## Residuals:
                1Q Median
                               3Q
##
      Min
                                      Max
## -54.921 -9.621
                    0.615
                            9.564 54.196
##
## Coefficients:
                                 Estimate Std. Error t value Pr(>|t|)
##
                               -156.56957
## (Intercept)
                                            13.02841 -12.018 < 2e-16 ***
                                             1.24684 3.413 0.000664 ***
## Gender
                                  4.25524
                                  0.81274
                                             0.09894 8.214 5.32e-16 ***
## Age
## Height
                                121.80520
                                             7.14305 17.052 < 2e-16 ***
## family hist
                                             1.32971 11.504 < 2e-16 ***
                                 15.29655
## eat caloric
                                             1.47926 2.683 0.007404 **
                                  3.96819
                                             3.44567 -2.764 0.005802 **
## vegetables_sometimes
                                 -9.52226
                                             0.99765 -7.346 3.70e-13 ***
## vegetables always
                                 -7.32851
                                             1.04130 -5.290 1.45e-07 ***
## main meals Btw 1 2
                                 -5.50831
## main_meals_More_than_3
                                -18.03950
                                             1.53632 -11.742 < 2e-16 ***
## food inbetween always
                                 -3.16154
                                             4.25233 -0.743 0.457330
## food inbetween frequently
                                -17.21409
                                             3.42556 -5.025 5.77e-07 ***
## food_inbetween_sometimes
                                  0.57720
                                             3.22714 0.179 0.858080
                                                      -0.070 0.944476
## smoke
                                 -0.22053
                                             3.16589
                                             1.59331 -0.331 0.740821
## CH20 between 1 and 2
                                 -0.52713
                                             0.98999 5.412 7.47e-08 ***
## CH20_more_than_2
                                  5.35807
                                                      -2.191 0.028626 *
## monitor cal
                                 -4.92421
                                             2.24731
## physical_act_1_2
                                 -9.38751
                                             1.63586 -5.739 1.20e-08 ***
## physical_act_2_4
                                  2.02866
                                             1.00094 2.027 0.042901 *
## tech 1 hour
                                 -5.45663
                                             1.55983 -3.498 0.000485 ***
```

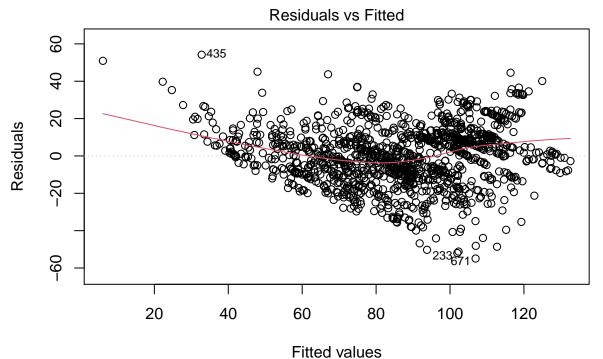
food_inbetween_always + food_inbetween_frequently +

food inbetween sometimes + smoke + CH20 between 1 and 2 +

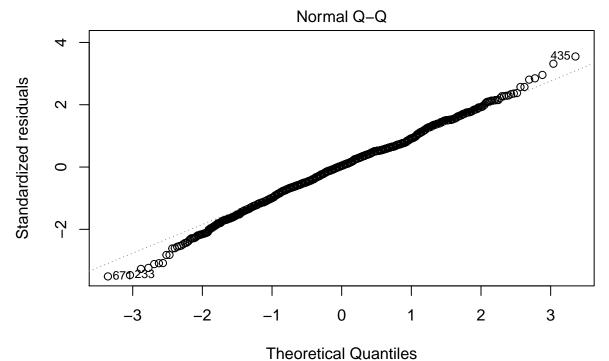
```
## tech_2_hours_or_more
                                 -1.47184
                                             1.00579
                                                      -1.463 0.143621
## alcohol always
                                            16.05482
                                                       0.852 0.394473
                                 13.67598
## alcohol frequently
                                                      -0.454 0.650030
                                 -1.19652
                                             2.63648
## alcohol sometimes
                                  4.61559
                                             1.04280
                                                       4.426 1.04e-05 ***
## mtrans automobile
                                 -7.08215
                                             2.83046
                                                      -2.502 0.012473 *
## mtrans bike
                                 -4.04084
                                             8.28314
                                                      -0.488 0.625750
## mtrans public transportation
                                  4.55777
                                             2.59702
                                                       1.755 0.079506 .
## --
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.7 on 1239 degrees of freedom
## Multiple R-squared: 0.6464, Adjusted R-squared: 0.639
## F-statistic: 87.11 on 26 and 1239 DF, p-value: < 2.2e-16
```

plot(lm_weight)

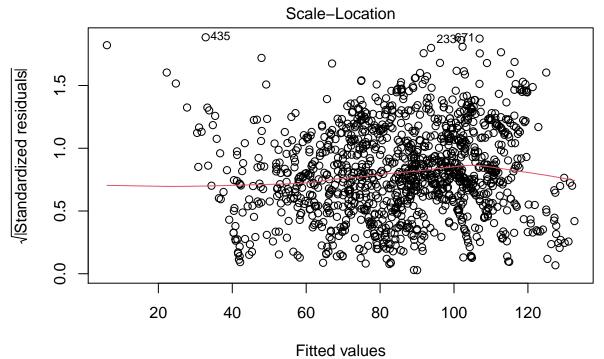
```
\#\# Warning: not plotting observations with leverage one: \#\# 768
```



Im(Weight ~ Gender + Age + Height + family_hist + eat_caloric + vegetables_ ...

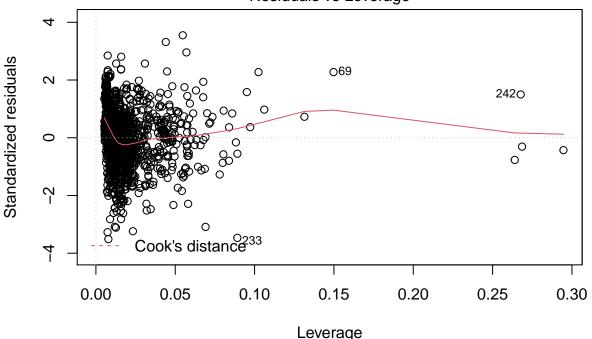


Im(Weight ~ Gender + Age + Height + family_hist + eat_caloric + vegetables_ ...



Im(Weight ~ Gender + Age + Height + family_hist + eat_caloric + vegetables_ ...

Residuals vs Leverage



Im(Weight ~ Gender + Age + Height + family_hist + eat_caloric + vegetables_ ...

Looking at the model above, we have quite a lot of variables that are significant at a confidence level of 95%. The variables that are not significant are: food_inbetween_always, food_inbetween_sometimes, smoke, CH2O_between_1_and_2, tech_1_hour,alcohol_always, alcohol_frequently, mtrans_bike and mtrans_public_transportation.

Because there are many significant variables, we will not interpret all of them, instead, we will interpret some that we find interesting.

- Age: An increase of 1 year of age corresponds to an average increase of 0.812 kg in weight, ceteris paribus.
- main_meals_Btw_1_2: An individual that eats between 1 and 2 main meals per day has an average decrease of 5.508 kg in comparison to an individual that eats three main meals per day.

Because we wish to select the best possible model for the linear regression, we will proceed with the stepwise selection method, in order to choose the most appropriate one. We will run a forward, backward, and both model selection.

```
# Stepwise model selection
# Forward
lm forward obesity <- step(lm weight, direction = "forward")</pre>
```

```
## Weight ~ Gender + Age + Height + family hist + eat caloric +
       vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 +
##
##
       main_meals_More_than_3 + food_inbetween_always + food_inbetween_frequently +
##
       food inbetween sometimes + smoke + CH2O between 1 and 2 +
##
       CH2O_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
##
       tech_1_hour + tech_2_hours_or_more + alcohol_always + alcohol_frequently +
##
       alcohol_sometimes + mtrans_automobile + mtrans_bike + mtrans_public_transportatio
summary(lm_forward_obesity)
##
## Call:
## lm(formula = Weight ~ Gender + Age + Height + family_hist + eat_caloric +
       vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 +
##
##
       main_meals_More_than_3 + food_inbetween_always + food_inbetween_frequently +
##
       food inbetween_sometimes + smoke + CH20_between_1_and_2 +
##
       CH2O_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
       tech 1 hour + tech 2 hours or more + alcohol always + alcohol frequently +
##
##
       alcohol_sometimes + mtrans_automobile + mtrans_bike + mtrans_public_transportatio
##
       data = train.set)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -54.921 -9.621
                    0.615
                             9.564 54.196
##
## Coefficients:
                                  Estimate Std. Error t value Pr(>|t|)
                                -156.56957 13.02841 -12.018 < 2e-16 ***
## (Intercept)
                                                        3.413 0.000664 ***
## Gender
                                   4.25524
                                              1.24684
## Age
                                   0.81274
                                              0.09894 8.214 5.32e-16 ***
## Height
                                 121.80520
                                              7.14305 17.052 < 2e-16 ***
## family hist
                                  15.29655
                                              1.32971 11.504 < 2e-16 ***
                                              1.47926 2.683 0.007404 **
## eat_caloric
                                   3.96819
                                              3.44567 -2.764 0.005802 **
## vegetables sometimes
                                  -9.52226
                                              0.99765 -7.346 3.70e-13 ***
## vegetables always
                                  -7.32851
                                              1.04130 -5.290 1.45e-07 ***
## main_meals_Btw_1_2
                                  -5.50831
## main meals More than 3
                                 -18.03950
                                              1.53632 -11.742 < 2e-16 ***
                                              4.25233 -0.743 0.457330
## food inbetween always
                                  -3.16154
                                              3.42556 -5.025 5.77e-07 ***
## food_inbetween_frequently
                                 -17.21409
                                                      0.179 0.858080
                                              3.22714
## food_inbetween_sometimes
                                   0.57720
## smoke
                                              3.16589 -0.070 0.944476
                                  -0.22053
                                              1.59331
                                                      -0.331 0.740821
## CH20_between_1_and_2
                                  -0.52713
                                              0.98999 5.412 7.47e-08 ***
## CH20_more_than_2
                                  5.35807
## monitor_cal
                                  -4.92421
                                              2.24731 -2.191 0.028626 *
                                              1.63586 -5.739 1.20e-08 ***
## physical act 1 2
                                  -9.38751
                                              1.00094 2.027 0.042901 *
## physical act 2 4
                                  2.02866
```

Start: AIC=6999.41

```
## tech_1_hour
                                  -5.45663
                                             1.55983 -3.498 0.000485 ***
                                             1.00579 -1.463 0.143621
## tech 2 hours or more
                                  -1.47184
## alcohol_always
                                  13.67598
                                             16.05482 0.852 0.394473
## alcohol_frequently
                                  -1.19652
                                             2.63648 -0.454 0.650030
                                           1.04280 4.426 1.04e-05 ***
## alcohol sometimes
                                  4.61559
## mtrans_automobile
                                  -7.08215
                                             2.83046 -2.502 0.012473 *
## mtrans bike
                                  -4.04084
                                             8.28314 -0.488 0.625750
                                  4.55777
                                             2.59702 1.755 0.079506 .
## mtrans_public_transportation
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.7 on 1239 degrees of freedom
## Multiple R-squared: 0.6464, Adjusted R-squared: 0.639
## F-statistic: 87.11 on 26 and 1239 DF, p-value: < 2.2e-16
# AIC: 6999.41 Model : Weight ~ Gender + Age +
# Height + family hist + eat caloric +
# vegetables_sometimes + vegetables_always +
# main_meals_Btw_1_2 + main_meals_More_than_3
# + food inbetween always +
# food_inbetween_frequently +
# food_inbetween_sometimes + smoke +
\# CH20_between_1_and_2 + CH20_more_than_2 +
# monitor_cal + physical_act_1_2 +
# physical_act_2_4 + tech_1_hour +
# tech_2_hours_or_more + alcohol_always +
# alcohol_frequently + alcohol_sometimes +
# mtrans automobile + mtrans bike +
# mtrans_public_transportation
# Backward
lm_backward_obesity <- step(lm_weight, direction = "backward")</pre>
## Start: AIC=6999.41
## Weight ~ Gender + Age + Height + family hist + eat caloric +
##
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
##
       main_meals_More_than_3 + food_inbetween_always + food_inbetween_frequently +
##
       food_inbetween_sometimes + smoke + CH20_between_1_and_2 +
##
       CH2O more than 2 + monitor cal + physical act 1 2 + physical act 2 4 +
##
       tech_1_hour + tech_2_hours_or_more + alcohol_always + alcohol_frequently +
##
       alcohol_sometimes + mtrans_automobile + mtrans_bike + mtrans_public_transportatio
##
##
                                  Df Sum of Sq
                                                  RSS
                                                         AIC
                                             1 305507 6997.4
## - smoke
                                   1
## - food_inbetween_sometimes
                                             8 305514 6997.4
                                   1
## - CH2O between 1 and 2
                                   1
                                           27 305533 6997.5
```

```
## - alcohol_frequently
                                    1
                                             51 305556 6997.6
## - mtrans bike
                                    1
                                             59 305564 6997.7
## - food_inbetween_always
                                    1
                                            136 305642 6998.0
                                            179 305685 6998.2
## - alcohol_always
                                    1
## <none>
                                                305506 6999.4
## - tech_2_hours_or_more
                                    1
                                            528 306034 6999.6
                                            759 306265 7000.6
## - mtrans_public_transportation
                                           1013 306518 7001.6
## - physical_act_2_4
                                    1
                                           1184 306689 7002.3
## - monitor cal
                                    1
                                           1544 307049 7003.8
## - mtrans_automobile
                                    1
                                           1774 307280 7004.7
## - eat_caloric
                                    1
                                           1883 307389 7005.2
## - vegetables_sometimes
                                    1
## - Gender
                                    1
                                           2872 308378 7009.3
                                           3017 308523 7009.9
## - tech_1_hour
                                    1
                                           4831 310336 7017.3
## - alcohol sometimes
                                    1
                                           6227 311732 7023.0
## - food inbetween frequently
                                    1
                                           6900 312405 7025.7
                                    1
## - main meals Btw 1 2
                                           7223 312728 7027.0
## - CH20 more than 2
                                    1
## - physical_act_1_2
                                           8120 313626 7030.6
                                    1
                                          13305 318811 7051.4
## - vegetables_always
                                    1
## - Age
                                          16637 322143 7064.5
                                    1
                                          32630 338136 7125.9
## - family hist
                                    1
                                          33997 339502 7131.0
## - main_meals_More_than_3
                                    1
                                          71699 377204 7264.3
                                    1
## - Height
##
## Step: AIC=6997.41
## Weight ~ Gender + Age + Height + family_hist + eat_caloric +
##
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
##
       main meals More than 3 + food inbetween always + food inbetween frequently +
##
       food_inbetween_sometimes + CH20_between_1_and_2 + CH20_more_than_2 +
##
       monitor_cal + physical_act_1_2 + physical_act_2_4 + tech_1_hour +
##
       tech 2 hours or more + alcohol always + alcohol frequently +
##
       alcohol_sometimes + mtrans_automobile + mtrans_bike + mtrans_public_transportatio
##
                                   Df Sum of Sq
                                                   RSS
##
                                                          AIC
                                    1
                                             8 305515 6995.4
## - food inbetween sometimes
                                             27 305534 6995.5
\#\# - CH2O between 1 and 2
                                    1
## - alcohol_frequently
                                             53 305560 6995.6
                                    1
                                            58 305565 6995.7
## - mtrans_bike
                                    1
## - food inbetween always
                                   1
                                            136 305643 6996.0
## - alcohol always
                                    1
                                            179 305686 6996.2
                                                305507 6997.4
## <none>
                                            527 306034 6997.6
## - tech_2_hours_or_more
                                            760 306267 6998.6
## - mtrans_public_transportation
                                   1
                                           1012 306519 6999.6
## - physical act 2 4
                                    1
## - monitor_cal
                                    1
                                           1194 306701 7000.4
                                           1547 307054 7001.8
## - mtrans_automobile
                                   1
                                           1776 307283 7002.8
## - eat caloric
```

```
## - vegetables sometimes
                                    1
                                           1884 307391 7003.2
## - Gender
                                    1
                                           2871 308378 7007.3
                                    1
                                           3030 308537 7007.9
## - tech_1_hour
                                           4830 310336 7015.3
## - alcohol sometimes
                                    1
                                           6234 311741 7021.0
## - food inbetween frequently
## - main meals Btw 1 2
                                    1
                                           6901 312408 7023.7
## - CH2O more than 2
                                    1
                                           7315 312822 7025.4
                                           8119 313626 7028.6
## - physical act 1 2
                                    1
## - vegetables always
                                    1
                                          13310 318817 7049.4
                                    1
                                          17080 322587 7064.3
## - Age
## - family hist
                                    1
                                          32631 338138 7123.9
                                          34024 339531 7129.1
## - main_meals_More_than_3
                                    1
## - Height
                                    1
                                          72330 377837 7264.4
##
## Step: AIC=6995.45
## Weight ~ Gender + Age + Height + family hist + eat caloric +
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
##
##
       main meals More than 3 + food inbetween always + food inbetween frequently +
##
       CH20_between_1_and_2 + CH20_more_than_2 + monitor_cal + physical_act_1_2 +
##
       physical_act_2_4 + tech_1_hour + tech_2_hours_or_more + alcohol_always +
##
       alcohol frequently + alcohol sometimes + mtrans automobile +
##
       mtrans bike + mtrans public transportation
##
##
                                                   RSS
                                   Df Sum of Sq
                                                          AIC
\#\# - CH2O between 1 and 2
                                    1
                                             26 305541 6993.6
                                             54 305569 6993.7
## - alcohol frequently
                                    1
## - mtrans_bike
                                   1
                                             58 305573 6993.7
## - alcohol always
                                    1
                                            179 305694 6994.2
## - food inbetween always
                                            381 305896 6995.0
## <none>
                                                305515 6995.4
## - tech_2_hours_or_more
                                    1
                                            548 306063 6995.7
                                            762 306277 6996.6
## - mtrans public transportation
                                           1022 306537 6997.7
## - physical act 2 4
                                    1
## - monitor cal
                                    1
                                           1192 306707 6998.4
                                           1543 307058 6999.8
## - mtrans_automobile
                                    1
## - eat caloric
                                   1
                                           1772 307287 7000.8
                                           1935 307451 7001.4
                                   1
## - vegetables sometimes
## - Gender
                                   1
                                           2917 308432 7005.5
                                   1
                                           3022 308537 7005.9
## - tech 1 hour
## - alcohol sometimes
                                   1
                                           4822 310337 7013.3
## - main meals Btw 1 2
                                    1
                                           6938 312453 7021.9
                                           7374 312889 7023.6
## - CH20 more than 2
                                    1
## - physical_act_1_2
                                    1
                                           8113 313628 7026.6
                                    1
                                          13669 319185 7048.9
## - vegetables always
## - Age
                                    1
                                          17150 322665 7062.6
## - family_hist
                                    1
                                          33606 339121 7125.6
## - food inbetween frequently
                                    1
                                          34095 339610 7127.4
## - main meals More than 3
                                    1
                                          34346 339862 7128.3
```

```
## - Height
                                    1
                                          73963 379478 7267.9
##
## Step: AIC=6993.56
## Weight ~ Gender + Age + Height + family_hist + eat_caloric +
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
##
##
       main_meals_More_than_3 + food_inbetween_always + food_inbetween_frequently +
##
       CH20_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
       tech_1_hour + tech_2_hours_or_more + alcohol_always + alcohol_frequently +
##
##
       alcohol_sometimes + mtrans_automobile + mtrans_bike + mtrans_public_transportatio
##
##
                                   Df Sum of Sq
                                                   RSS
                                                           AIC
## - mtrans_bike
                                    1
                                             55 305596 6991.8
## - alcohol frequently
                                    1
                                             55 305596 6991.8
## - alcohol_always
                                    1
                                            184 305724 6992.3
                                            383 305924 6993.1
## - food inbetween always
                                    1
                                                305541 6993.6
## <none>
## - tech_2_hours_or_more
                                            557 306098 6993.9
                                    1
                                            770 306311 6994.7
## - mtrans public transportation
                                           1054 306595 6995.9
## - physical_act_2_4
                                    1
                                    1
                                           1176 306717 6996.4
## - monitor_cal
                                           1543 307084 6997.9
## - mtrans automobile
                                    1
## - eat_caloric
                                    1
                                           1783 307324 6998.9
                                           1952 307492 6999.6
## - vegetables_sometimes
                                    1
## - Gender
                                           2918 308458 7003.6
                                    1
## - tech 1 hour
                                    1
                                           3031 308572 7004.1
                                           4859 310400 7011.5
## - alcohol sometimes
                                    1
## - main_meals_Btw_1_2
                                    1
                                           6914 312455 7019.9
                                           7968 313509 7024.1
## - CH20 more than 2
                                    1
## - physical act 1 2
                                    1
                                           8091 313632 7024.6
## - vegetables_always
                                          13723 319264 7047.2
                                    1
## - Age
                                    1
                                          17130 322671 7060.6
                                          34377 339917 7126.5
## - main_meals_More_than_3
                                    1
## - family_hist
                                    1
                                          34502 340042 7127.0
## - food inbetween frequently
                                    1
                                          35247 340787 7129.8
                                          74497 380038 7267.8
## - Height
                                    1
##
## Step: AIC=6991.78
## Weight ~ Gender + Age + Height + family_hist + eat_caloric +
       vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 +
##
##
       main meals More than 3 + food inbetween always + food inbetween frequently +
##
       CH20_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
##
       tech_1_hour + tech_2_hours_or_more + alcohol_always + alcohol_frequently +
##
       alcohol_sometimes + mtrans_automobile + mtrans_public_transportation
##
##
                                   Df Sum of Sq
                                                   RSS
                                                          AIC
                                             53 305649 6990.0
## - alcohol_frequently
                                    1
## - alcohol_always
                                    1
                                            192 305787 6990.6
## - food inbetween always
                                    1
                                            397 305993 6991.4
```

```
## <none>
                                                305596 6991.8
## - tech 2 hours or more
                                           569 306164 6992.1
                                           947 306542 6993.7
## - mtrans_public_transportation
## - physical act 2 4
                                   1
                                           1064 306660 6994.2
## - monitor cal
                                   1
                                           1193 306789 6994.7
## - mtrans automobile
                                   1
                                           1495 307091 6996.0
## - eat caloric
                                   1
                                           1774 307370 6997.1
## - vegetables sometimes
                                           1940 307536 6997.8
                                  1
## - Gender
                                   1
                                           2966 308562 7002.0
## - tech 1 hour
                                  1
                                           3036 308632 7002.3
## - alcohol sometimes
                                  1
                                           4874 310470 7009.8
## - main meals Btw 1 2
                                   1
                                           6874 312469 7017.9
## - CH20 more than 2
                                   1
                                          7994 313590 7022.5
## - physical act 1 2
                                   1
                                          8120 313716 7023.0
                                          13704 319299 7045.3
## - vegetables always
                                   1
                                          17101 322697 7058.7
## - Age
                                   1
## - main meals More than 3
                                   1
                                          34322 339918 7124.5
## - family hist
                                          34559 340154 7125.4
## - food_inbetween_frequently
                                          35192 340787 7127.8
                                   1
## - Height
                                   1
                                         74674 380270 7266.6
##
## Step: AIC=6990
## Weight ~ Gender + Age + Height + family hist + eat caloric +
##
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
       main meals More than 3 + food inbetween always + food inbetween frequently +
##
##
       CH20_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
##
       tech_1_hour + tech_2_hours_or_more + alcohol_always + alcohol_sometimes +
##
       mtrans automobile + mtrans public transportation
##
##
                                  Df Sum of Sq
                                                   RSS
                                                          AIC
## - alcohol always
                                   1
                                            194 305843 6988.8
                                           414 306063 6989.7
## - food inbetween always
                                   1
## <none>
                                                305649 6990.0
## - tech 2 hours or more
                                           548 306197 6990.3
                                   1
                                           935 306584 6991.9
## - mtrans_public_transportation
                                   1
                                           1077 306725 6992.5
## - physical act 2 4
                                   1
                                           1230 306879 6993.1
## - monitor cal
## - mtrans automobile
                                           1519 307168 6994.3
                                   1
                                           1766 307415 6995.3
## - eat caloric
                                   1
## - vegetables sometimes
                                  1
                                           1957 307606 6996.1
## - Gender
                                  1
                                           2968 308617 7000.2
                                           3005 308654 7000.4
## - tech 1 hour
                                  1
## - alcohol_sometimes
                                  1
                                           5478 311127 7010.5
## - main meals Btw 1 2
                                   1
                                           6846 312495 7016.0
## - CH20 more than 2
                                   1
                                          7945 313594 7020.5
## - physical_act_1_2
                                   1
                                          8110 313759 7021.2
## - vegetables always
                                   1
                                          13749 319398 7043.7
                                          17050 322699 7056.7
## - Age
```

```
## - main_meals_More_than_3
                                    1
                                          34337 339986 7122.8
## - family hist
                                    1
                                          34597 340246 7123.8
## - food_inbetween_frequently
                                    1
                                          35440 341089 7126.9
## - Height
                                    1
                                          74647 380296 7264.6
##
## Step: AIC=6988.81
## Weight ~ Gender + Age + Height + family hist + eat caloric +
##
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
##
       main meals More than 3 + food inbetween always + food inbetween frequently +
##
       CH2O more than 2 + monitor cal + physical act 1 2 + physical act 2 4 +
##
       tech_1_hour + tech_2_hours_or_more + alcohol_sometimes +
##
       mtrans_automobile + mtrans_public_transportation
##
##
                                   Df Sum of Sq
                                                   RSS
                                                          AIC
                                    1
## - food inbetween always
                                            415 306258 6988.5
## <none>
                                                305843 6988.8
                                            553 306396 6989.1
## - tech 2 hours or more
                                    1
                                            834 306678 6990.3
## - mtrans public transportation
                                           1049 306892 6991.1
## - physical_act_2_4
                                    1
                                    1
                                           1243 307087 6991.9
## - monitor cal
## - mtrans automobile
                                    1
                                           1687 307530 6993.8
## - eat caloric
                                    1
                                           1826 307670 6994.3
                                           1971 307814 6994.9
## - vegetables sometimes
                                    1
                                           2934 308778 6998.9
## - tech 1 hour
                                    1
## - Gender
                                    1
                                           2938 308782 6998.9
                                    1
                                           5449 311292 7009.2
## - alcohol sometimes
## - main_meals_Btw_1_2
                                    1
                                           6764 312607 7014.5
## - CH20 more than 2
                                    1
                                           7912 313755 7019.1
## - physical act 1 2
                                    1
                                           8226 314070 7020.4
## - vegetables always
                                          13705 319549 7042.3
                                    1
## - Age
                                    1
                                          17016 322860 7055.4
## - main meals More than 3
                                    1
                                          34420 340264 7121.8
## - family hist
                                    1
                                          34869 340713 7123.5
## - food inbetween frequently
                                    1
                                          35247 341090 7124.9
                                          74523 380367 7262.9
## - Height
                                    1
##
## Step: AIC=6988.52
## Weight ~ Gender + Age + Height + family_hist + eat_caloric +
       vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 +
##
##
       main meals More than 3 + food inbetween frequently + CH20 more than 2 +
##
       monitor_cal + physical_act_1_2 + physical_act_2_4 + tech_1_hour +
##
       tech 2 hours or more + alcohol sometimes + mtrans automobile +
##
       mtrans_public_transportation
##
##
                                                   RSS
                                                          AIC
                                   Df Sum of Sq
                                                306258 6988.5
## <none>
## - tech 2 hours or more
                                    1
                                            574 306832 6988.9
## - mtrans public transportation 1
                                            926 307184 6990.3
```

```
## - physical_act_2_4
                                   1
                                          1012 307270 6990.7
## - monitor cal
                                   1
                                          1335 307593 6992.0
## - mtrans_automobile
                                   1
                                          1602 307860 6993.1
                                          1883 308141 6994.3
## - eat caloric
                                   1
## - vegetables sometimes
                                   1
                                          2252 308510 6995.8
## - tech 1 hour
                                   1
                                          2952 309210 6998.7
## - Gender
                                   1
                                          3001 309259 6998.9
## - alcohol sometimes
                                          5572 311830 7009.3
                                   1
## - main meals Btw 1 2
                                   1
                                          6579 312837 7013.4
## - CH2O more than 2
                                   1
                                          8041 314299 7019.3
## - physical act 1 2
                                   1
                                          8493 314751 7021.2
## - vegetables_always
                                   1
                                         13718 319976 7042.0
## - Age
                                   1
                                         17193 323451 7055.7
## - food inbetween frequently
                                   1
                                         34859 341116 7123.0
                                         35162 341419 7124.1
## - main meals More than 3
                                   1
                                         36034 342292 7127.4
## - family hist
                                   1
## - Height
                                   1
                                         74621 380879 7262.6
summary(lm_backward_obesity)
##
## Call:
## lm(formula = Weight ~ Gender + Age + Height + family hist + eat caloric +
##
       vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 +
##
       main meals More than 3 + food inbetween frequently + CH20 more than 2 +
##
       monitor_cal + physical_act_1_2 + physical_act_2_4 + tech_1_hour +
##
       tech 2 hours or more + alcohol sometimes + mtrans automobile +
##
       mtrans public transportation, data = train.set)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -54.796 -9.651
                     0.799
                             9.613 53.566
##
## Coefficients:
##
                                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                -157.25649
                                             12.73878 -12.345 < 2e-16 ***
## Gender
                                   4.32640
                                              1.23821
                                                        3.494 0.000492 ***
                                   0.81187
                                              0.09707
                                                       8.363 < 2e-16 ***
## Age
## Height
                                 121.98641
                                              7.00108 17.424 < 2e-16 ***
## family hist
                                  15.62919
                                              1.29081 12.108 < 2e-16 ***
## eat caloric
                                   4.07848
                                              1.47335
                                                       2.768 0.005721 **
```

-10.25052

-7.35775

-5.33322

-18.11019

-17.48159

5.42381

vegetables sometimes

main_meals_More_than_3

food inbetween frequently

vegetables always

CH20 more than 2

main meals Btw 1 2

3.38653 -3.027 0.002522 **

1.03086 -5.174 2.67e-07 ***

1.51417 -11.960 < 2e-16 ***

1.46795 -11.909 < 2e-16 ***

0.98489

0.94825

-7.471 1.50e-13 ***

5.720 1.33e-08 ***

```
1.62130 -5.878 5.32e-09 ***
## physical act 1 2
                                 -9.53018
                                             0.99354 2.029 0.042624 *
## physical_act_2_4
                                  2.01635
## tech_1_hour
                                  -5.36631
                                             1.54856 -3.465 0.000548 ***
                                             0.99466 -1.528 0.126783
## tech 2 hours or more
                                 -1.51977
## alcohol_sometimes
                                  4.78278
                                             1.00453
                                                      4.761 2.15e-06 ***
## mtrans_automobile
                                 -6.88857
                                             2.69795 -2.553 0.010790 *
## mtrans_public_transportation
                                  4.79038
                                             2.46791 1.941 0.052475 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.68 on 1246 degrees of freedom
## Multiple R-squared: 0.6455, Adjusted R-squared: 0.6401
## F-statistic: 119.4 on 19 and 1246 DF, p-value: < 2.2e-16
# formula: Weight ~ Gender + Age + Height +
# family hist + eat caloric +
# vegetables_sometimes + vegetables_always +
# main_meals_Btw_1_2 + main_meals_More_than_3
# + food_inbetween_frequently +
# CH20_more_than_2 + monitor_cal +
# physical_act_1_2 + physical_act_2_4 +
# tech_1_hour + tech_2_hours_or_more +
# alcohol_sometimes + mtrans_automobile +
# mtrans_public_transportation
# AIC: 6988.52
# Both
lm both obesity <- step(lm weight, direction = "both")</pre>
## Start: AIC=6999.41
## Weight ~ Gender + Age + Height + family hist + eat caloric +
##
       vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 +
##
       main_meals_More_than_3 + food_inbetween_always + food_inbetween_frequently +
##
       food_inbetween_sometimes + smoke + CH20_between_1_and_2 +
##
       CH2O_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
##
       tech_1_hour + tech_2_hours_or_more + alcohol_always + alcohol_frequently +
##
       alcohol_sometimes + mtrans_automobile + mtrans_bike + mtrans_public_transportatio
##
##
                                  Df Sum of Sq
                                                 RSS
                                                        AIC
## - smoke
                                   1
                                            1 305507 6997.4
## - food inbetween sometimes
                                   1
                                            8 305514 6997.4
                                           27 305533 6997.5
## - CH20_between_1_and_2
                                   1
                                           51 305556 6997.6
## - alcohol_frequently
                                  1
                                  1
                                           59 305564 6997.7
## - mtrans_bike
                                          136 305642 6998.0
## - food inbetween always
                                  1
```

-5.18724

2.22576 -2.331 0.019936 *

monitor_cal

```
## - alcohol_always
                                    1
                                            179 305685 6998.2
## <none>
                                                305506 6999.4
                                            528 306034 6999.6
## - tech_2_hours_or_more
                                    1
                                            759 306265 7000.6
## - mtrans_public_transportation
                                           1013 306518 7001.6
## - physical_act_2_4
## - monitor cal
                                    1
                                           1184 306689 7002.3
                                           1544 307049 7003.8
## - mtrans_automobile
                                    1
                                           1774 307280 7004.7
## - eat caloric
                                    1
                                           1883 307389 7005.2
                                    1
## - vegetables sometimes
                                           2872 308378 7009.3
## - Gender
                                    1
## - tech_1_hour
                                           3017 308523 7009.9
                                    1
                                           4831 310336 7017.3
## - alcohol_sometimes
                                    1
                                           6227 311732 7023.0
                                    1
## - food inbetween frequently
## - main_meals_Btw_1_2
                                    1
                                           6900 312405 7025.7
## - CH20_more_than_2
                                           7223 312728 7027.0
                                    1
                                           8120 313626 7030.6
## - physical_act_1_2
                                    1
                                          13305 318811 7051.4
## - vegetables always
                                    1
                                          16637 322143 7064.5
                                   1
## - Age
## - family_hist
                                          32630 338136 7125.9
                                   1
                                    1
                                          33997 339502 7131.0
## - main_meals_More_than_3
## - Height
                                          71699 377204 7264.3
                                    1
##
## Step: AIC=6997.41
## Weight ~ Gender + Age + Height + family_hist + eat_caloric +
       vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 +
##
##
       main_meals_More_than_3 + food_inbetween_always + food_inbetween_frequently +
       food inbetween_sometimes + CH20_between_1_and_2 + CH20_more_than_2 +
##
##
       monitor_cal + physical_act_1_2 + physical_act_2_4 + tech_1_hour +
##
       tech_2_hours_or_more + alcohol_always + alcohol_frequently +
##
       alcohol_sometimes + mtrans_automobile + mtrans_bike + mtrans_public_transportatio
##
##
                                   Df Sum of Sq
                                                   RSS
                                                          AIC
                                              8 305515 6995.4
## - food_inbetween_sometimes
                                    1
                                             27 305534 6995.5
## - CH20_between_1_and_2
                                    1
                                             53 305560 6995.6
## - alcohol_frequently
                                    1
## - mtrans bike
                                    1
                                            58 305565 6995.7
                                            136 305643 6996.0
## - food_inbetween_always
## - alcohol_always
                                    1
                                            179 305686 6996.2
                                                305507 6997.4
## <none>
## - tech_2_hours_or_more
                                            527 306034 6997.6
## - mtrans_public_transportation
                                           760 306267 6998.6
                                              1 305506 6999.4
## + smoke
                                    1
                                           1012 306519 6999.6
## - physical_act_2_4
                                    1
## - monitor cal
                                   1
                                           1194 306701 7000.4
## - mtrans_automobile
                                           1547 307054 7001.8
                                  1
## - eat_caloric
                                   1
                                           1776 307283 7002.8
                                           1884 307391 7003.2
## - vegetables_sometimes
                                   1
                                           2871 308378 7007.3
## - Gender
```

```
## - tech_1_hour
                                    1
                                           3030 308537 7007.9
## - alcohol sometimes
                                    1
                                           4830 310336 7015.3
## - food_inbetween_frequently
                                    1
                                           6234 311741 7021.0
                                           6901 312408 7023.7
## - main meals Btw 1 2
                                    1
                                           7315 312822 7025.4
## - CH20 more than 2
                                    1
## - physical act 1 2
                                    1
                                           8119 313626 7028.6
## - vegetables always
                                    1
                                          13310 318817 7049.4
## - Age
                                          17080 322587 7064.3
                                    1
                                    1
                                          32631 338138 7123.9
## - family hist
## - main meals More than 3
                                    1
                                          34024 339531 7129.1
## - Height
                                    1
                                          72330 377837 7264.4
##
## Step: AIC=6995.45
## Weight ~ Gender + Age + Height + family hist + eat caloric +
##
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
##
       main_meals_More_than_3 + food_inbetween_always + food_inbetween_frequently +
##
       CH20 between 1 and 2 + CH20 more than 2 + monitor cal + physical act 1 2 +
##
       physical act 2 4 + tech 1 hour + tech 2 hours or more + alcohol always +
##
       alcohol_frequently + alcohol_sometimes + mtrans_automobile +
##
       mtrans_bike + mtrans_public_transportation
##
##
                                   Df Sum of Sq
                                                   RSS
                                                          AIC
                                             26 305541 6993.6
\#\# - CH2O between 1 and 2
                                    1
                                    1
                                             54 305569 6993.7
## - alcohol_frequently
## - mtrans bike
                                    1
                                             58 305573 6993.7
                                    1
                                            179 305694 6994.2
## - alcohol always
## - food_inbetween_always
                                    1
                                            381 305896 6995.0
## <none>
                                                305515 6995.4
## - tech 2 hours or more
                                    1
                                            548 306063 6995.7
## - mtrans_public_transportation
                                            762 306277 6996.6
                                    1
## + food_inbetween_sometimes
                                    1
                                              8 305507 6997.4
                                              2 305514 6997.4
## + smoke
                                    1
## - physical act 2 4
                                    1
                                           1022 306537 6997.7
## - monitor cal
                                    1
                                           1192 306707 6998.4
                                           1543 307058 6999.8
## - mtrans_automobile
                                    1
## - eat caloric
                                    1
                                           1772 307287 7000.8
                                           1935 307451 7001.4
                                   1
## - vegetables sometimes
## - Gender
                                    1
                                           2917 308432 7005.5
                                    1
                                           3022 308537 7005.9
## - tech 1 hour
## - alcohol sometimes
                                    1
                                           4822 310337 7013.3
## - main meals Btw 1 2
                                    1
                                           6938 312453 7021.9
                                           7374 312889 7023.6
## - CH20 more than 2
                                    1
## - physical_act_1_2
                                    1
                                           8113 313628 7026.6
                                    1
                                          13669 319185 7048.9
## - vegetables always
## - Age
                                    1
                                          17150 322665 7062.6
## - family_hist
                                    1
                                          33606 339121 7125.6
## - food inbetween frequently
                                    1
                                          34095 339610 7127.4
## - main meals More than 3
                                    1
                                          34346 339862 7128.3
```

```
## - Height
                                    1
                                          73963 379478 7267.9
##
## Step: AIC=6993.56
## Weight ~ Gender + Age + Height + family_hist + eat_caloric +
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
##
##
       main_meals_More_than_3 + food_inbetween_always + food_inbetween_frequently +
##
       CH20_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
##
       tech_1_hour + tech_2_hours_or_more + alcohol_always + alcohol_frequently +
##
       alcohol_sometimes + mtrans_automobile + mtrans_bike + mtrans_public_transportatio
##
##
                                   Df Sum of Sq
                                                   RSS
                                                          AIC
## - mtrans_bike
                                    1
                                             55 305596 6991.8
## - alcohol frequently
                                    1
                                             55 305596 6991.8
## - alcohol_always
                                    1
                                            184 305724 6992.3
## - food inbetween always
                                    1
                                            383 305924 6993.1
## <none>
                                                305541 6993.6
                                            557 306098 6993.9
## - tech 2 hours or more
                                    1
                                            770 306311 6994.7
## - mtrans public transportation 1
## + CH20_between_1_and_2
                                             26 305515 6995.4
                                    1
                                    1
                                              6 305534 6995.5
## + food_inbetween_sometimes
## + smoke
                                    1
                                              2 305539 6995.5
## - physical_act_2_4
                                    1
                                           1054 306595 6995.9
## - monitor cal
                                    1
                                           1176 306717 6996.4
                                           1543 307084 6997.9
## - mtrans automobile
                                    1
                                           1783 307324 6998.9
## - eat caloric
                                    1
## - vegetables_sometimes
                                           1952 307492 6999.6
                                    1
## - Gender
                                    1
                                           2918 308458 7003.6
## - tech 1 hour
                                    1
                                           3031 308572 7004.1
## - alcohol sometimes
                                    1
                                           4859 310400 7011.5
                                           6914 312455 7019.9
## - main_meals_Btw_1_2
                                    1
## - CH20_more_than_2
                                    1
                                           7968 313509 7024.1
                                           8091 313632 7024.6
## - physical act 1 2
                                    1
                                          13723 319264 7047.2
## - vegetables_always
                                    1
## - Age
                                    1
                                          17130 322671 7060.6
## - main_meals_More_than_3
                                    1
                                          34377 339917 7126.5
                                          34502 340042 7127.0
## - family hist
                                    1
                                          35247 340787 7129.8
## - food inbetween frequently
## - Height
                                          74497 380038 7267.8
                                    1
##
## Step: AIC=6991.78
## Weight ~ Gender + Age + Height + family hist + eat caloric +
##
       vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 +
##
       main_meals_More_than_3 + food_inbetween_always + food_inbetween_frequently +
##
       CH20_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
##
       tech 1 hour + tech 2 hours or more + alcohol always + alcohol frequently +
       alcohol_sometimes + mtrans_automobile + mtrans_public_transportation
##
##
##
                                   Df Sum of Sq
                                                   RSS
                                                          AIC
```

```
## - alcohol_frequently
                                   1
                                             53 305649 6990.0
## - alcohol always
                                   1
                                            192 305787 6990.6
## - food inbetween always
                                            397 305993 6991.4
                                   1
## <none>
                                                305596 6991.8
## - tech 2 hours or more
                                            569 306164 6992.1
                                   1
## + mtrans bike
                                    1
                                             55 305541 6993.6
## + CH20 between 1 and 2
                                    1
                                             23 305573 6993.7
                                            947 306542 6993.7
## - mtrans public transportation
                                   1
## + food inbetween sometimes
                                    1
                                              6 305590 6993.8
## + smoke
                                    1
                                              2 305594 6993.8
## - physical_act_2_4
                                    1
                                           1064 306660 6994.2
## - monitor cal
                                   1
                                           1193 306789 6994.7
## - mtrans automobile
                                   1
                                           1495 307091 6996.0
## - eat_caloric
                                   1
                                           1774 307370 6997.1
                                           1940 307536 6997.8
## - vegetables sometimes
                                   1
                                           2966 308562 7002.0
                                   1
## - Gender
## - tech 1 hour
                                  1
                                           3036 308632 7002.3
                                           4874 310470 7009.8
## - alcohol sometimes
                                  1
## - main meals Btw 1 2
                                           6874 312469 7017.9
                                  1
                                           7994 313590 7022.5
## - CH20_more_than_2
                                   1
                                          8120 313716 7023.0
## - physical act 1 2
                                   1
## - vegetables always
                                   1
                                          13704 319299 7045.3
                                          17101 322697 7058.7
## - Age
                                   1
                                          34322 339918 7124.5
## - main meals More than 3
                                   1
## - family hist
                                   1
                                          34559 340154 7125.4
## - food inbetween frequently
                                   1
                                          35192 340787 7127.8
## - Height
                                    1
                                          74674 380270 7266.6
##
## Step: AIC=6990
## Weight ~ Gender + Age + Height + family hist + eat caloric +
##
       vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 +
##
       main meals More than 3 + food inbetween always + food inbetween frequently +
##
       CH20_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
##
       tech 1 hour + tech 2 hours or more + alcohol always + alcohol sometimes +
##
       mtrans_automobile + mtrans_public_transportation
##
##
                                  Df Sum of Sq
                                                   RSS
                                                          AIC
## - alcohol_always
                                            194 305843 6988.8
                                   1
## - food_inbetween_always
                                   1
                                            414 306063 6989.7
## <none>
                                                305649 6990.0
## - tech 2 hours or more
                                    1
                                            548 306197 6990.3
                                            53 305596 6991.8
## + alcohol frequently
                                    1
                                    1
                                             53 305596 6991.8
## + mtrans_bike
## - mtrans public transportation 1
                                          935 306584 6991.9
                                             24 305625 6991.9
## + CH20 between 1 and 2
                                    1
## + food_inbetween_sometimes
                                             7 305642 6992.0
                                   1
## + smoke
                                   1
                                              4 305645 6992.0
                                           1077 306725 6992.5
## - physical act 2 4
                                   1
```

```
## - monitor cal
                                   1
                                           1230 306879 6993.1
## - mtrans automobile
                                   1
                                           1519 307168 6994.3
## - eat_caloric
                                  1
                                           1766 307415 6995.3
                                           1957 307606 6996.1
## - vegetables sometimes
                                   1
                                           2968 308617 7000.2
## - Gender
                                   1
## - tech 1 hour
                                   1
                                           3005 308654 7000.4
## - alcohol sometimes
                                   1
                                           5478 311127 7010.5
                                           6846 312495 7016.0
## - main meals Btw 1 2
                                   1
\#\# - CH2O more than 2
                                   1
                                           7945 313594 7020.5
## - physical act 1 2
                                   1
                                           8110 313759 7021.2
## - vegetables always
                                   1
                                          13749 319398 7043.7
## - Age
                                    1
                                          17050 322699 7056.7
## - main meals More than 3
                                   1
                                          34337 339986 7122.8
## - family hist
                                    1
                                          34597 340246 7123.8
                                   1
                                          35440 341089 7126.9
## - food inbetween frequently
                                          74647 380296 7264.6
## - Height
                                    1
##
## Step: AIC=6988.81
## Weight ~ Gender + Age + Height + family_hist + eat_caloric +
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
##
##
       main meals More than 3 + food inbetween always + food inbetween frequently +
##
       CH2O_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 +
##
       tech 1 hour + tech 2 hours or more + alcohol sometimes +
##
       mtrans automobile + mtrans public transportation
##
##
                                  Df Sum of Sq
                                                          AIC
                                                   RSS
## - food_inbetween_always
                                    1
                                            415 306258 6988.5
## <none>
                                                305843 6988.8
## - tech 2 hours or more
                                            553 306396 6989.1
                                    1
                                    1
                                            194 305649 6990.0
## + alcohol always
## - mtrans_public_transportation
                                            834 306678 6990.3
                                    1
                                             62 305782 6990.6
## + mtrans bike
                                    1
                                            56 305787 6990.6
## + alcohol frequently
## + CH20 between 1 and 2
                                    1
                                             28 305815 6990.7
                                             7 305837 6990.8
## + food_inbetween_sometimes
                                   1
                                             4 305839 6990.8
## + smoke
                                    1
                                           1049 306892 6991.1
## - physical act 2 4
## - monitor cal
                                   1
                                           1243 307087 6991.9
                                   1
                                           1687 307530 6993.8
## - mtrans automobile
## - eat caloric
                                   1
                                           1826 307670 6994.3
## - vegetables sometimes
                                   1
                                           1971 307814 6994.9
                                           2934 308778 6998.9
## - tech 1 hour
                                   1
## - Gender
                                   1
                                           2938 308782 6998.9
## - alcohol sometimes
                                  1
                                           5449 311292 7009.2
                                           6764 312607 7014.5
## - main meals Btw 1 2
                                  1
## - CH20_more_than_2
                                  1
                                           7912 313755 7019.1
## - physical act 1 2
                                   1
                                           8226 314070 7020.4
                                          13705 319549 7042.3
## - vegetables always
```

```
## - Age
                                    1
                                          17016 322860 7055.4
## - main meals More than 3
                                    1
                                          34420 340264 7121.8
## - family hist
                                    1
                                          34869 340713 7123.5
## - food inbetween frequently
                                    1
                                          35247 341090 7124.9
## - Height
                                    1
                                          74523 380367 7262.9
##
## Step: AIC=6988.52
## Weight ~ Gender + Age + Height + family hist + eat caloric +
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
##
##
       main meals More than 3 + food inbetween frequently + CH20 more than 2 +
##
       monitor_cal + physical_act_1_2 + physical_act_2_4 + tech_1_hour +
##
       tech_2_hours_or_more + alcohol_sometimes + mtrans_automobile +
##
       mtrans public transportation
##
##
                                                   RSS
                                   Df Sum of Sq
                                                           AIC
                                                306258 6988.5
## <none>
                                            415 305843 6988.8
## + food inbetween always
                                    1
## - tech 2 hours or more
                                            574 306832 6988.9
## + food_inbetween_sometimes
                                            266 305992 6989.4
                                    1
## + alcohol always
                                    1
                                            195 306063 6989.7
                                            77 306181 6990.2
## + mtrans bike
                                    1
## + alcohol frequently
                                    1
                                            73 306185 6990.2
                                            926 307184 6990.3
## - mtrans public transportation
## + CH20 between 1 and 2
                                             30 306228 6990.4
                                    1
## + smoke
                                    1
                                              9 306249 6990.5
                                    1
                                           1012 307270 6990.7
## - physical act 2 4
## - monitor_cal
                                    1
                                           1335 307593 6992.0
                                           1602 307860 6993.1
## - mtrans automobile
                                    1
                                           1883 308141 6994.3
## - eat caloric
                                    1
## - vegetables sometimes
                                    1
                                           2252 308510 6995.8
                                           2952 309210 6998.7
## - tech 1 hour
                                    1
## - Gender
                                    1
                                           3001 309259 6998.9
## - alcohol sometimes
                                    1
                                           5572 311830 7009.3
## - main meals Btw 1 2
                                    1
                                           6579 312837 7013.4
                                           8041 314299 7019.3
## - CH20_more_than_2
                                    1
## - physical act 1 2
                                    1
                                           8493 314751 7021.2
## - vegetables always
                                          13718 319976 7042.0
## - Age
                                          17193 323451 7055.7
                                    1
## - food inbetween frequently
                                    1
                                          34859 341116 7123.0
## - main meals More than 3
                                    1
                                          35162 341419 7124.1
## - family hist
                                    1
                                          36034 342292 7127.4
## - Height
                                    1
                                          74621 380879 7262.6
summary(lm both obesity)
```

Call:

```
## lm(formula = Weight ~ Gender + Age + Height + family hist + eat caloric +
##
       vegetables sometimes + vegetables always + main meals Btw 1 2 +
##
       main_meals_More_than_3 + food_inbetween_frequently + CH20_more_than_2 +
##
       monitor_cal + physical_act_1_2 + physical_act_2_4 + tech_1_hour +
##
       tech 2 hours or more + alcohol sometimes + mtrans automobile +
##
       mtrans_public_transportation, data = train.set)
##
## Residuals:
##
      Min
                1Q Median
                               3Q
                                      Max
## -54.796 -9.651
                    0.799
                            9.613 53.566
##
## Coefficients:
                                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                               -157.25649
                                            12.73878 -12.345 < 2e-16 ***
## Gender
                                                       3.494 0.000492 ***
                                  4.32640
                                             1.23821
## Age
                                             0.09707
                                                      8.363 < 2e-16 ***
                                  0.81187
## Height
                                             7.00108 17.424 < 2e-16 ***
                                121.98641
## family hist
                                 15.62919
                                             1.29081 12.108 < 2e-16 ***
## eat caloric
                                  4.07848
                                             1.47335
                                                      2.768 0.005721 **
## vegetables_sometimes
                                             3.38653 -3.027 0.002522 **
                                -10.25052
                                             0.98489 -7.471 1.50e-13 ***
## vegetables always
                                 -7.35775
## main meals Btw 1 2
                                 -5.33322
                                             1.03086 -5.174 2.67e-07 ***
                                             1.51417 -11.960 < 2e-16 ***
## main meals More than 3
                                -18.11019
                                -17.48159
                                             1.46795 -11.909 < 2e-16 ***
## food inbetween frequently
## CH20 more than 2
                                             0.94825
                                                       5.720 1.33e-08 ***
                                  5.42381
                                             2.22576 -2.331 0.019936 *
## monitor cal
                                 -5.18724
## physical_act_1_2
                                 -9.53018
                                             1.62130 -5.878 5.32e-09 ***
## physical act 2 4
                                  2.01635
                                             0.99354
                                                      2.029 0.042624 *
## tech 1 hour
                                 -5.36631
                                             1.54856 -3.465 0.000548 ***
## tech_2_hours_or_more
                                 -1.51977
                                             0.99466
                                                      -1.528 0.126783
                                                      4.761 2.15e-06 ***
## alcohol_sometimes
                                  4.78278
                                             1.00453
                                             2.69795 -2.553 0.010790 *
## mtrans automobile
                                 -6.88857
## mtrans_public_transportation
                                             2.46791
                                                      1.941 0.052475 .
                                 4.79038
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.68 on 1246 degrees of freedom
## Multiple R-squared: 0.6455, Adjusted R-squared: 0.6401
## F-statistic: 119.4 on 19 and 1246 DF, p-value: < 2.2e-16
# AIC: 6988.52 model:Weight ~ Gender + Age +
# Height + family_hist + eat_caloric +
# vegetables sometimes + vegetables always +
# main_meals_Btw_1_2 + main_meals_More_than_3
# + food_inbetween_frequently +
# CH20 more than 2 + monitor cal +
# physical_act_1_2 + physical_act_2_4 +
# tech_1_hour + tech_2_hours_or_more +
```

```
# alcohol_sometimes + mtrans_automobile +
# mtrans_public_transportation

# Simplet model(both, backward)

# Add comments +Assumptions
```

For the forward model, the stepwise selection shows us that the best model is:

```
Weight \sim Gender + Age + Height + family_hist + eat_caloric + vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 + main_meals_More_than_3 + food_inbetween_always + food_inbetween_frequently + food_inbetween_sometimes + smoke + CH2O_between_1_and_2 + CH2O_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 + tech_1_hour + tech_2_hours_or_more + alcohol_always + alcohol_frequently + alcohol_sometimes + mtrans_automobile + mtrans_bike + mtrans_public_transportation
```

This is in fact the same model as the full model. It has an AIC of 6999.41, an R-Squared of 0.6464 and an ajusted R-Squared of 0.639.

For the backward model, the stepwise selection shows us that the best model is:

```
Weight \sim Gender + Age + Height + family_hist + eat_caloric + vegetables_sometimes + vegetables_always + main_meals_Btw_1_2 + main_meals_More_than_3 + food_inbetween_frequently + CH2O_more_than_2 + monitor_cal + physical_act_1_2 + physical_act_2_4 + tech_1_hour + tech_2_hours_or_more + alcohol_sometimes + mtrans_automobile + mtrans_public_transportation
```

This model is a reduced version of the full model. The AIC is 6988.52, the R-Squared is 0.6455 and the adjusted R-Squared is 0.6401.

For the both model we obtain the same results as the backward model. The best model is:

```
\label{lem:weight} Weight \sim Gender + Age + Height + family\_hist + eat\_caloric + vegetables\_sometimes + vegetables\_always + main\_meals\_Btw\_1\_2 + main\_meals\_More\_than\_3 + food\_inbetween\_frequently + CH2O\_more\_than\_2 + monitor\_cal + physical\_act\_1\_2 + physical\_act\_2\_4 + tech\_1\_hour + tech\_2\_hours\_or\_more + alcohol\_sometimes + mtrans\_automobile + mtrans\_public\_transportation
```

This model is a reduced version of the full model. The AIC is 6988.52, the R-Squared is 0.6455 and the adjusted R-Squared is 0.6401.

When looking at all three models, the best model would seem to be the backward model (or the both model). It's adusted R-Squared is higher than the forward model by very little but is reduced and therefore favorable. We have very very similar results and insights from all

three models but the backward model and the both model allow us to obtain those insights without having to drag around those variables that are not significant.

To confirm our choice of model for the linear regression, we will proceed with the validation of the accuracy of the predictions on the validation set with the help of 3 metrics: RMSE, Mean error and MAPE.

```
# Predictions on the validation set
# Forward model:
forward_pred_obesity <- predict(lm_forward_obesity,</pre>
    valid.set)
# RMSE
gofRMSE(valid.set$Weight, forward_pred_obesity,
    dgt = 3) #16.376
## [1] 16.376
# Mean error
gofME(valid.set$Weight, forward_pred_obesity,
    dgt = 3) #1.038
## [1] 1.038
# MAPE
gofMAPE(valid.set$Weight, forward pred obesity,
    dgt = 3) #16.344
## [1] 16.344
# Backward model:
backward pred obesity <- predict(lm backward obesity,</pre>
    valid.set)
# RMSE
gofRMSE(valid.set$Weight, backward_pred obesity,
    dgt = 3) #16.416
## [1] 16.416
# Mean error
gofME(valid.set$Weight, backward_pred obesity,
    dgt = 3) #1.002
```

[1] 1.002

```
# MAPE
gofMAPE(valid.set$Weight, backward_pred_obesity,
    dgt = 3) #16.363
## [1] 16.363
# Both model:
both pred obesity <- predict(lm both obesity,
    valid.set)
# RMSE
gofRMSE(valid.set$Weight, both pred obesity, dgt = 3) #16.416
## [1] 16.416
# Mean error
gofME(valid.set$Weight, both pred obesity, dgt = 3)
## [1] 1.002
# MAPE
gofMAPE(valid.set$Weight, both pred obesity, dgt = 3)
## [1] 16.363
# Add comments +Assumptions
```

Just as we had mentionned above, the backward model and the both model seem to represent the best model for our data. The difference in the three metrics for each model are very very small. This enables us to choose the backward/both model as the best model, since it yields very similar results as the full model, without all the cumbersome variables that are not relevant in the full (forward) model.

k-Nearest Neighbors

First of all, we should normalize the data, since we have different scales and big values can dominate small values! We normalize only the numerical data.

A "denormalize" function will be very handy when converting the predicted weight back to its normal scale :

```
denormalize <- function(x, y) {
    return((x * (max(y) - min(y))) + min(y))
}</pre>
```

Now we will run the model JUST in order to identify different values of the **Root Mean Squared Error (RMSE)**:

```
# Creating dataframe :

rmse.df = data.frame(k = seq(1, 40, 1), RMSE = rep(0, 40))

# Running the model :

set.seed(1)

for (i in 1:40) {

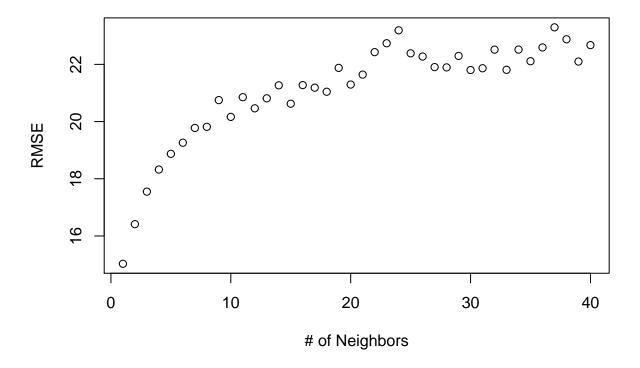
    knn.pred = knn(train = train.final[, -3],
```

| k | RMSE | |
|----|-------|--|
| 1 | 15.03 | |
| 2 | 16.41 | |
| 3 | 17.55 | |
| 4 | 18.32 | |
| 5 | 18.87 | |
| 6 | 19.26 | |
| 7 | 19.78 | |
| 8 | 19.82 | |
| 9 | 20.75 | |
| 10 | 20.16 | |
| 11 | 20.85 | |
| 12 | 20.46 | |
| 13 | 20.81 | |
| 14 | 21.27 | |
| 15 | 20.62 | |
| 16 | 21.27 | |
| 17 | 21.18 | |
| 18 | 21.04 | |
| 19 | 21.88 | |
| 20 | 21.29 | |
| 21 | 21.64 | |
| 22 | 22.43 | |
| 23 | 22.74 | |
| 24 | 23.19 | |
| 25 | 22.39 | |
| 26 | 22.27 | |
| 27 | 21.9 | |
| 28 | 21.89 | |
| 29 | 22.3 | |
| | | |

| k | RMSE |
|----|-------|
| 30 | 21.8 |
| 31 | 21.86 |
| 32 | 22.52 |
| 33 | 21.81 |
| 34 | 22.52 |
| 35 | 22.11 |
| 36 | 22.59 |
| 37 | 23.29 |
| 38 | 22.88 |
| 39 | 22.1 |
| 40 | 22.67 |
| | |

```
plot(rmse.df$k, rmse.df$RMSE, xlab = "# of Neighbors",
   ylab = "RMSE", main = "Selecting the best 'k'")
```

Selecting the best 'k'



We can see from this plot (but also from the table above) that the best k is equal to 1. With this k = 1, we are able to minimize the RMSE.

```
# Running the FINAL model (with k = 1):
set.seed(1)
```

```
## [1] 15.02754
```

The resulting RMSE is equal to 15.02754.

Let's now do a Regression Tree and ultimately compare its RMSE with the one of the k-NN! Weird! If we change the set.seed, the results for RMSE change!! So, which set.seed to choose?

Regression Tree

We will first focus on selecting the appropriate value for the Complexity Parameter (CP hereafter), which is a "penalty" factor concerning the size of the tree. A smaller CP will result in a bigger tree, and viceversa.

To do this, we will do a Cross-Validation approach. The computer will create many different partitions of the dataset into training and validation, and we want to find the CP that corresponds to the minimum Cross-Validation error.

This procedure is meant to help addressing the **tree instability** issue.

```
# First run a quite big tree (CP = 0.00001) :
set.seed(1)

tree_1 <- rpart(Weight ~ ., data = train.set,
    method = "anova", control = rpart.control(cp = 1e-05,
        minbucket = 1, maxdepth = 10))

# We do a CV : must locate in the table the
# point from which the CV error starts to rise
# :
pander(printcp(tree_1))</pre>
```

Regression tree: $rpart(formula = Weight \sim ., data = train.set, method = "anova", control = rpart.control(cp = 1e-05, minbucket = 1, maxdepth = 10))$

Variables actually used in tree construction: [1] Age alcohol frequently

- [3] alcohol no alcohol sometimes
- [5] CH2O_between_1_and_2 CH2O_less_than_a_liter
- [7] CH2O_more_than_2 eat_caloric
- [9] family hist food inbetween always
- [11] food_inbetween_frequently food_inbetween_no
- [13] food inbetween sometimes Gender
- [15] Height main_meals_Btw_1_2
- [17] main_meals_More_than_3 main_meals_three
- [19] mtrans_automobile mtrans_public_transportation [21] mtrans_walking physical_act_1_2
- [23] physical_act_2_4 physical_act_do_not_have
- [25] smoke tech 0 hours
- [27] tech_1_hour tech_2_hours_or_more
- [29] vegetables_always vegetables_never
- [31] vegetables_sometimes

Root node error: 863970/1266 = 682.44

n = 1266

CP nsplit rel error xerror xstd

 $02\ 2\ 0.645126\ 0.69143\ 0.024380\ 4\ 4.8885e-02\ 3\ 0.553440\ 0.57874\ 0.020532\ 5\ 4.7976e-02\ 4$ $0.504555\ 0.53189\ 0.020062\ 6\ 3.9913e-02\ 5\ 0.456579\ 0.50260\ 0.019309\ 7\ 3.1797e-02\ 6\ 0.416666$ $0.45833\ 0.018216\ 8\ 3.0705 e-02\ 7\ 0.384869\ 0.42132\ 0.017611\ 9\ 2.9898 e-02\ 8\ 0.354164\ 0.41031$ $0.017666\ 10\ 2.6283e-02\ 9\ 0.324267\ 0.39900\ 0.017759\ 11\ 2.1389e-02\ 10\ 0.297984\ 0.34518$ $0.016298\ 12\ 1.4922e-02\ 11\ 0.276595\ 0.31477\ 0.016084\ 13\ 1.3678e-02\ 13\ 0.246750\ 0.29319$ $0.015334\ 14\ 1.0733e-02\ 14\ 0.233073\ 0.27831\ 0.014811\ 15\ 6.7323e-03\ 15\ 0.222340\ 0.26197$ $0.014367\ 16\ 6.7285e{-}03\ 16\ 0.215608\ 0.25555\ 0.014318\ 17\ 6.4250e{-}03\ 17\ 0.208879\ 0.25484$ $0.014315\ 18\ 5.2398e{-}03\ 18\ 0.202454\ 0.24153\ 0.013774\ 19\ 5.1561e{-}03\ 19\ 0.197215\ 0.23718$ $0.013701\ 20\ 5.0756 e-03\ 21\ 0.186902\ 0.23511\ 0.013704\ 21\ 5.0536 e-03\ 22\ 0.181827\ 0.23474$ $0.013738\ 22\ 4.9464e\text{-}03\ 23\ 0.176773\ 0.23230\ 0.013641\ 23\ 4.8132e\text{-}03\ 24\ 0.171827\ 0.23098$ $0.013587\ 24\ 4.6777e-03\ 25\ 0.167013\ 0.22768\ 0.013597\ 25\ 4.5455e-03\ 26\ 0.162336\ 0.22770$ $0.013596\ 26\ 4.3459e - 03\ 27\ 0.157790\ 0.22790\ 0.013646\ 27\ 4.0019e - 03\ 28\ 0.153444\ 0.22284$ $0.013330\ 28\ 3.2234\text{e-}03\ 29\ 0.149442\ 0.20174\ 0.012413\ 29\ 3.0930\text{e-}03\ 30\ 0.146219\ 0.19889$ $0.012444\ 30\ 2.9916e\text{-}03\ 31\ 0.143126\ 0.19541\ 0.012417\ 31\ 2.8585e\text{-}03\ 32\ 0.140135\ 0.19581$ $0.012535\ 32\ 2.8075 e-03\ 33\ 0.137276\ 0.19605\ 0.012634\ 33\ 2.4839 e-03\ 35\ 0.131661\ 0.19153$ $0.012459\ 34\ 2.3938e-03\ 36\ 0.129177\ 0.19138\ 0.012666\ 35\ 2.3641e-03\ 38\ 0.124390\ 0.19672$ $0.014034\ 36\ 2.2876e-03\ 39\ 0.122025\ 0.19559\ 0.014017\ 37\ 2.1836e-03\ 40\ 0.119738\ 0.19980$ $0.014878\ 38\ 2.0813e-03\ 41\ 0.117554\ 0.20200\ 0.015113\ 39\ 2.0295e-03\ 43\ 0.113392\ 0.20369$ $0.015226\ 40\ 2.0205e\text{-}03\ 44\ 0.111362\ 0.20314\ 0.015217\ 41\ 1.9247e\text{-}03\ 45\ 0.109342\ 0.20182$ $0.015190\ 42\ 1.6986e-03\ 48\ 0.103567\ 0.19405\ 0.014685\ 43\ 1.6464e-03\ 50\ 0.100170\ 0.19487$ $0.014878\ 44\ 1.4059e\text{-}03\ 52\ 0.096878\ 0.19288\ 0.014810\ 45\ 1.4007e\text{-}03\ 53\ 0.095472\ 0.19279$ $0.015014\ 46\ 1.3517e - 03\ 54\ 0.094071\ 0.19258\ 0.015012\ 47\ 1.3113e - 03\ 55\ 0.092719\ 0.19280$

 $0.015044\ 48\ 1.1903e\text{-}03\ 56\ 0.091408\ 0.19241\ 0.015191\ 49\ 1.1791e\text{-}03\ 57\ 0.090218\ 0.19372$ $0.015187 \ 50 \ 1.0896e - 03 \ 58 \ 0.089039 \ 0.19450 \ 0.015269 \ 51 \ 1.0834e - 03 \ 59 \ 0.087949 \ 0.19447$ $0.015282\ 52\ 1.0806e-03\ 60\ 0.086866\ 0.19455\ 0.015281\ 53\ 1.0409e-03\ 61\ 0.085785\ 0.19446$ $0.015286\ 54\ 1.0146e-03\ 62\ 0.084744\ 0.19419\ 0.015298\ 55\ 1.0047e-03\ 63\ 0.083730\ 0.19496$ $0.015378\ 56\ 1.0036e\text{-}03\ 64\ 0.082725\ 0.19493\ 0.015378\ 57\ 9.9494e\text{-}04\ 65\ 0.081721\ 0.19493$ $0.015378\ 58\ 9.4526e-04\ 66\ 0.080726\ 0.19454\ 0.015409\ 59\ 9.3369e-04\ 67\ 0.079781\ 0.19457$ $0.015410\ 60\ 8.9659e-04\ 68\ 0.078847\ 0.19605\ 0.015490\ 61\ 8.8696e-04\ 69\ 0.077951\ 0.19705$ $0.015511 \ 62 \ 8.7917e - 04 \ 70 \ 0.077064 \ 0.19663 \ 0.015498 \ 63 \ 8.7664e - 04 \ 71 \ 0.076185 \ 0.19667$ $0.015498\ 64\ 8.6872e-04\ 72\ 0.075308\ 0.19651\ 0.015504\ 65\ 8.5579e-04\ 73\ 0.074439\ 0.19666$ $0.015512\ 66\ 7.9067e\text{-}04\ 74\ 0.073584\ 0.19647\ 0.015546\ 67\ 7.6136e\text{-}04\ 75\ 0.072793\ 0.19610$ $0.015630\ 68\ 7.5874e\text{-}04\ 76\ 0.072032\ 0.19637\ 0.015648\ 69\ 7.3475e\text{-}04\ 77\ 0.071273\ 0.19719$ $0.015678 \ 70 \ 7.1505e-04 \ 78 \ 0.070538 \ 0.19624 \ 0.015649 \ 71 \ 7.0739e-04 \ 79 \ 0.069823 \ 0.19622$ $0.015632\ 72\ 7.0003e\text{-}04\ 80\ 0.069116\ 0.19478\ 0.015445\ 73\ 6.9885e\text{-}04\ 81\ 0.068416\ 0.19442$ $0.015445\ 74\ 6.9317e\text{-}04\ 82\ 0.067717\ 0.19345\ 0.015439\ 75\ 6.8168e\text{-}04\ 86\ 0.064944\ 0.19321$ $0.015441\ 76\ 6.6291e\text{-}04\ 87\ 0.064262\ 0.19329\ 0.015462\ 77\ 6.4968e\text{-}04\ 88\ 0.063600\ 0.19127$ $0.015334\ 78\ 6.1187e\text{-}04\ 90\ 0.062300\ 0.19127\ 0.015325\ 79\ 5.7700e\text{-}04\ 92\ 0.061076\ 0.19191$ $0.015362\ 80\ 5.6197e\text{-}04\ 93\ 0.060499\ 0.19226\ 0.015343\ 81\ 5.6012e\text{-}04\ 94\ 0.059937\ 0.19295$ $0.015399\ 82\ 5.5551e\text{-}04\ 95\ 0.059377\ 0.19295\ 0.015399\ 83\ 5.3345e\text{-}04\ 96\ 0.058822\ 0.19193$ $0.015366\ 84\ 5.2949e\text{-}04\ 97\ 0.058288\ 0.19083\ 0.015368\ 85\ 5.2886e\text{-}04\ 98\ 0.057759\ 0.19080$ $0.015368\ 86\ 5.2750e{-}04\ 99\ 0.057230\ 0.19089\ 0.015368\ 87\ 5.1885e{-}04\ 100\ 0.056703\ 0.19050$ $0.015368\ 88\ 5.1087e\text{-}04\ 101\ 0.056184\ 0.19026\ 0.015362\ 89\ 4.9588e\text{-}04\ 103\ 0.055162\ 0.18986$ $0.015354\ 90\ 4.8486e-04\ 104\ 0.054666\ 0.19013\ 0.015457\ 91\ 4.7963e-04\ 107\ 0.053211\ 0.19138$ $0.015509 \ 92 \ 4.7509 e-04 \ 109 \ 0.052252 \ 0.19157 \ 0.015508 \ 93 \ 4.5473 e-04 \ 110 \ 0.051777 \ 0.19067$ $0.015507\ 94\ 4.5147e-04\ 111\ 0.051322\ 0.19007\ 0.015501\ 95\ 4.1846e-04\ 113\ 0.050419\ 0.19114$ $0.015572\ 96\ 4.1701e-04\ 114\ 0.050001\ 0.19072\ 0.015578\ 97\ 4.0408e-04\ 115\ 0.049584\ 0.19061$ $0.015585\ 98\ 3.8493e-04\ 117\ 0.048776\ 0.18972\ 0.015600\ 99\ 3.7460e-04\ 118\ 0.048391\ 0.18979$ $0.015638\ 100\ 3.1367e-04\ 119\ 0.048016\ 0.18852\ 0.015599\ 101\ 3.0365e-04\ 122\ 0.047075\ 0.18864$ $0.015630\ 102\ 3.0357e\text{-}04\ 123\ 0.046772\ 0.18918\ 0.015645\ 103\ 3.0112e\text{-}04\ 124\ 0.046468\ 0.18904$ $0.015644\ 104\ 2.9037e\text{-}04\ 125\ 0.046167\ 0.18888\ 0.015646\ 105\ 2.8594e\text{-}04\ 126\ 0.045877\ 0.18885$ $0.015646\ 106\ 2.8317e\text{-}04\ 128\ 0.045305\ 0.18871\ 0.015648\ 107\ 2.7999e\text{-}04\ 129\ 0.045022\ 0.18871$ $0.015648\ 108\ 2.6409e-04\ 130\ 0.044742\ 0.18896\ 0.015658\ 109\ 2.6396e-04\ 131\ 0.044477\ 0.18867$ $0.015658\ 110\ 2.5313e\text{-}04\ 132\ 0.044213\ 0.18853\ 0.015660\ 111\ 2.4891e\text{-}04\ 133\ 0.043960\ 0.18866$ $0.015658\ 112\ 2.4321e\text{-}04\ 134\ 0.043711\ 0.18871\ 0.015661\ 113\ 2.2199e\text{-}04\ 135\ 0.043468\ 0.18916$ $0.015678\ 114\ 2.1902e-04\ 136\ 0.043246\ 0.18922\ 0.015690\ 115\ 2.1789e-04\ 137\ 0.043027\ 0.19004$ $0.015712\ 116\ 2.1609e-04\ 138\ 0.042809\ 0.19016\ 0.015713\ 117\ 2.0894e-04\ 139\ 0.042593\ 0.19264$ $0.015872\ 118\ 2.0355e\text{-}04\ 140\ 0.042384\ 0.19292\ 0.015887\ 119\ 2.0283e\text{-}04\ 141\ 0.042181\ 0.19331$ $0.015891\ 120\ 2.0174e\text{-}04\ 143\ 0.041775\ 0.19323\ 0.015892\ 121\ 1.9844e\text{-}04\ 144\ 0.041573\ 0.19336$ $0.015891\ 122\ 1.9533e-04\ 145\ 0.041375\ 0.19338\ 0.015895\ 123\ 1.9267e-04\ 146\ 0.041180\ 0.19335$ $0.015895\ 124\ 1.8506e-04\ 147\ 0.040987\ 0.19336\ 0.015896\ 125\ 1.7948e-04\ 149\ 0.040617\ 0.19340$ $0.015924\ 126\ 1.7349e\text{-}04\ 150\ 0.040437\ 0.19324\ 0.015923\ 127\ 1.7314e\text{-}04\ 151\ 0.040264\ 0.19322$ $0.015923\ 128\ 1.7105e\text{-}04\ 152\ 0.040091\ 0.19331\ 0.015925\ 129\ 1.6556e\text{-}04\ 153\ 0.039920\ 0.19332$ $0.015925\ 130\ 1.6526e-04\ 154\ 0.039754\ 0.19325\ 0.015925\ 131\ 1.6449e-04\ 155\ 0.039589\ 0.19325$ $0.015925\ 132\ 1.6278e-04\ 156\ 0.039424\ 0.19317\ 0.015926\ 133\ 1.6224e-04\ 157\ 0.039262\ 0.19342$ $0.015943\ 134\ 1.6005e\text{-}04\ 158\ 0.039099\ 0.19356\ 0.015951\ 135\ 1.5929e\text{-}04\ 160\ 0.038779\ 0.19349$ $0.015951\ 136\ 1.4593e\text{-}04\ 161\ 0.038620\ 0.19395\ 0.015975\ 137\ 1.4356e\text{-}04\ 162\ 0.038474\ 0.19491$ $0.016003\ 138\ 1.4168e-04\ 163\ 0.038330\ 0.19491\ 0.016003\ 139\ 1.3681e-04\ 164\ 0.038189\ 0.19514$ $0.016001\ 140\ 1.3370e-04\ 165\ 0.038052\ 0.19491\ 0.015997\ 141\ 1.3356e-04\ 166\ 0.037918\ 0.19483$ $0.015969\ 142\ 1.3092e\text{-}04\ 167\ 0.037785\ 0.19494\ 0.015969\ 143\ 1.2761e\text{-}04\ 168\ 0.037654\ 0.19463$ $0.015969\ 144\ 1.2457e-04\ 170\ 0.037399\ 0.19460\ 0.015969\ 145\ 1.2415e-04\ 171\ 0.037274\ 0.19461$ $0.015969\ 146\ 1.2226e-04\ 172\ 0.037150\ 0.19460\ 0.015969\ 147\ 1.1984e-04\ 173\ 0.037028\ 0.19416$ $0.015970\ 148\ 1.1818e-04\ 174\ 0.036908\ 0.19435\ 0.015969\ 149\ 1.1353e-04\ 175\ 0.036790\ 0.19450$ $0.016003\ 150\ 1.1202e-04\ 176\ 0.036676\ 0.19443\ 0.016105\ 151\ 1.1111e-04\ 177\ 0.036564\ 0.19458$ $0.016105\ 152\ 1.1067e\text{-}04\ 178\ 0.036453\ 0.19470\ 0.016110\ 153\ 1.0856e\text{-}04\ 179\ 0.036342\ 0.19469$ $0.016110\ 154\ 1.0700e\text{-}04\ 180\ 0.036234\ 0.19468\ 0.016110\ 155\ 1.0669e\text{-}04\ 181\ 0.036127\ 0.19468$ $0.016110\ 156\ 1.0508e-04\ 182\ 0.036020\ 0.19479\ 0.016116\ 157\ 1.0460e-04\ 183\ 0.035915\ 0.19477$ $0.016116\ 158\ 1.0419e\text{-}04\ 185\ 0.035706\ 0.19477\ 0.016116\ 159\ 1.0363e\text{-}04\ 186\ 0.035601\ 0.19476$ $0.016116\ 160\ 9.9800e\text{-}05\ 187\ 0.035498\ 0.19471\ 0.016117\ 161\ 9.9712e\text{-}05\ 188\ 0.035398\ 0.19461$ $0.016117\ 162\ 9.8810e\text{-}05\ 189\ 0.035298\ 0.19461\ 0.016117\ 163\ 9.3753e\text{-}05\ 190\ 0.035200\ 0.19485$ $0.016136\ 164\ 9.2613e\text{-}05\ 191\ 0.035106\ 0.19516\ 0.016135\ 165\ 9.0585e\text{-}05\ 192\ 0.035013\ 0.19517$ $0.016135\ 166\ 7.8345e\text{-}05\ 193\ 0.034923\ 0.19551\ 0.016170\ 167\ 7.7127e\text{-}05\ 194\ 0.034844\ 0.19558$ $0.016194\ 168\ 7.5068e-05\ 195\ 0.034767\ 0.19512\ 0.016138\ 169\ 7.1679e-05\ 196\ 0.034692\ 0.19509$ $0.016137\ 170\ 7.1332e-05\ 197\ 0.034620\ 0.19489\ 0.016124\ 171\ 7.0450e-05\ 198\ 0.034549\ 0.19496$ $0.016125\ 172\ 6.7110e-05\ 199\ 0.034479\ 0.19495\ 0.016125\ 173\ 6.4467e-05\ 200\ 0.034411\ 0.19497$ $0.016124\ 174\ 5.9261e-05\ 201\ 0.034347\ 0.19492\ 0.016125\ 175\ 5.9063e-05\ 202\ 0.034288\ 0.19487$ $0.016123\ 176\ 5.7612e\text{-}05\ 203\ 0.034229\ 0.19501\ 0.016124\ 177\ 5.7072e\text{-}05\ 204\ 0.034171\ 0.19490$ $0.016126\ 178\ 5.7045e\text{-}05\ 205\ 0.034114\ 0.19490\ 0.016126\ 179\ 5.7025e\text{-}05\ 206\ 0.034057\ 0.19490$ $0.016126\ 180\ 5.5750e-05\ 207\ 0.034000\ 0.19490\ 0.016126\ 181\ 5.5750e-05\ 208\ 0.033944\ 0.19487$ $0.016124\ 182\ 5.5599e-05\ 209\ 0.033888\ 0.19487\ 0.016124\ 183\ 5.1566e-05\ 210\ 0.033833\ 0.19472$ $0.016115\ 184\ 4.5550e-05\ 212\ 0.033730\ 0.19510\ 0.016122\ 185\ 4.3404e-05\ 214\ 0.033639\ 0.19526$ $0.016128\ 186\ 4.2536e\text{-}05\ 215\ 0.033595\ 0.19530\ 0.016129\ 187\ 3.9508e\text{-}05\ 216\ 0.033553\ 0.19613$ $0.016187\ 188\ 3.7810 e-05\ 217\ 0.033513\ 0.19553\ 0.016148\ 189\ 3.7077 e-05\ 218\ 0.033475\ 0.19558$ $0.016147\ 190\ 3.6889e-05\ 219\ 0.033438\ 0.19557\ 0.016147\ 191\ 3.6696e-05\ 220\ 0.033401\ 0.19557$ $0.016147\ 192\ 3.3334e\text{-}05\ 221\ 0.033365\ 0.19558\ 0.016148\ 193\ 3.2199e\text{-}05\ 222\ 0.033331\ 0.19567$ $0.016149\ 194\ 2.7875e\text{-}05\ 223\ 0.033299\ 0.19556\ 0.016140\ 195\ 2.7795e\text{-}05\ 224\ 0.033271\ 0.19532$ $0.016137\ 196\ 2.7779e-05\ 225\ 0.033243\ 0.19521\ 0.016132\ 197\ 2.5058e-05\ 226\ 0.033216\ 0.19520$ $0.016133\ 198\ 2.3457e\text{-}05\ 227\ 0.033191\ 0.19558\ 0.016135\ 199\ 2.3342e\text{-}05\ 228\ 0.033167\ 0.19544$ $0.016134\ 200\ 2.2630e-05\ 229\ 0.033144\ 0.19544\ 0.016134\ 201\ 2.1898e-05\ 230\ 0.033121\ 0.19544$ $0.016134\ 202\ 2.1507e-05\ 231\ 0.033099\ 0.19530\ 0.016122\ 203\ 2.0965e-05\ 232\ 0.033078\ 0.19536$ $0.016123\ 204\ 2.0395e\text{-}05\ 233\ 0.033057\ 0.19532\ 0.016123\ 205\ 1.9845e\text{-}05\ 234\ 0.033036\ 0.19526$ $0.016123\ 206\ 1.9291e\text{-}05\ 235\ 0.033017\ 0.19541\ 0.016127\ 207\ 1.8322e\text{-}05\ 237\ 0.032978\ 0.19551$ $0.016129\ 208\ 1.7738e-05\ 238\ 0.032960\ 0.19547\ 0.016127\ 209\ 1.7688e-05\ 239\ 0.032942\ 0.19549$ $0.016127\ 210\ 1.7662e-05\ 240\ 0.032924\ 0.19549\ 0.016127\ 211\ 1.7469e-05\ 241\ 0.032907\ 0.19549$ $0.016127\ 212\ 1.7358e-05\ 242\ 0.032889\ 0.19549\ 0.016127\ 213\ 1.7223e-05\ 243\ 0.032872\ 0.19524$ $0.016126\ 214\ 1.5626e-05\ 244\ 0.032855\ 0.19524\ 0.016126\ 215\ 1.3938e-05\ 246\ 0.032823\ 0.19516$ $0.016126\ 216\ 1.3206e-05\ 247\ 0.032809\ 0.19535\ 0.016125\ 217\ 1.2756e-05\ 248\ 0.032796\ 0.19535$ $0.016125\ 218\ 1.1386e-05\ 249\ 0.032783\ 0.19540\ 0.016125\ 219\ 1.0390e-05\ 250\ 0.032772\ 0.19553$ $0.016126\ 220\ 1.0000e\text{-}05\ 251\ 0.032762\ 0.19547\ 0.016127$

| СР | nsplit | rel error | xerror | xstd |
|---------|--------|-----------|--------|---------|
| 0.2345 | 0 | 1 | 1.002 | 0.03161 |
| 0.1203 | 1 | 0.7655 | 0.7672 | 0.02651 |
| 0.09169 | 2 | 0.6451 | 0.6914 | 0.02438 |
| 0.04889 | 3 | 0.5534 | 0.5787 | 0.02053 |
| 0.04798 | 4 | 0.5046 | 0.5319 | 0.02006 |
| 0.03991 | 5 | 0.4566 | 0.5026 | 0.01931 |
| 0.0318 | 6 | 0.4167 | 0.4583 | 0.01822 |
| | | | | |

| СР | nsplit | rel error | xerror | xstd |
|----------|--------|-----------|--------|---------|
| 0.03071 | 7 | 0.3849 | 0.4213 | 0.01761 |
| 0.0299 | 8 | 0.3542 | 0.4103 | 0.01767 |
| 0.02628 | 9 | 0.3243 | 0.399 | 0.01776 |
| 0.02139 | 10 | 0.298 | 0.3452 | 0.0163 |
| 0.01492 | 11 | 0.2766 | 0.3148 | 0.01608 |
| 0.01368 | 13 | 0.2468 | 0.2932 | 0.01533 |
| 0.01073 | 14 | 0.2331 | 0.2783 | 0.01481 |
| 0.006732 | 15 | 0.2223 | 0.262 | 0.01437 |
| 0.006728 | 16 | 0.2156 | 0.2555 | 0.01432 |
| 0.006425 | 17 | 0.2089 | 0.2548 | 0.01432 |
| 0.00524 | 18 | 0.2025 | 0.2415 | 0.01377 |
| 0.005156 | 19 | 0.1972 | 0.2372 | 0.0137 |
| 0.005076 | 21 | 0.1869 | 0.2351 | 0.0137 |
| 0.005054 | 22 | 0.1818 | 0.2347 | 0.01374 |
| 0.004946 | 23 | 0.1768 | 0.2323 | 0.01364 |
| 0.004813 | 24 | 0.1718 | 0.231 | 0.01359 |
| 0.004678 | 25 | 0.167 | 0.2277 | 0.0136 |
| 0.004546 | 26 | 0.1623 | 0.2277 | 0.0136 |
| 0.004346 | 27 | 0.1578 | 0.2279 | 0.01365 |
| 0.004002 | 28 | 0.1534 | 0.2228 | 0.01333 |
| 0.003223 | 29 | 0.1494 | 0.2017 | 0.01241 |
| 0.003093 | 30 | 0.1462 | 0.1989 | 0.01244 |
| 0.002992 | 31 | 0.1431 | 0.1954 | 0.01242 |
| 0.002859 | 32 | 0.1401 | 0.1958 | 0.01253 |
| 0.002808 | 33 | 0.1373 | 0.196 | 0.01263 |
| 0.002484 | 35 | 0.1317 | 0.1915 | 0.01246 |
| 0.002394 | 36 | 0.1292 | 0.1914 | 0.01267 |
| 0.002364 | 38 | 0.1244 | 0.1967 | 0.01403 |
| 0.002288 | 39 | 0.122 | 0.1956 | 0.01402 |
| 0.002184 | 40 | 0.1197 | 0.1998 | 0.01488 |
| 0.002081 | 41 | 0.1176 | 0.202 | 0.01511 |
| 0.002029 | 43 | 0.1134 | 0.2037 | 0.01523 |
| 0.002021 | 44 | 0.1114 | 0.2031 | 0.01522 |
| 0.001925 | 45 | 0.1093 | 0.2018 | 0.01519 |
| 0.001699 | 48 | 0.1036 | 0.194 | 0.01468 |
| 0.001646 | 50 | 0.1002 | 0.1949 | 0.01488 |
| 0.001406 | 52 | 0.09688 | 0.1929 | 0.01481 |
| 0.001401 | 53 | 0.09547 | 0.1928 | 0.01501 |
| 0.001352 | 54 | 0.09407 | 0.1926 | 0.01501 |
| 0.001311 | 55 | 0.09272 | 0.1928 | 0.01504 |
| 0.00119 | 56 | 0.09141 | 0.1924 | 0.01519 |
| 0.001179 | 57 | 0.09022 | 0.1937 | 0.01519 |
| 0.00109 | 58 | 0.08904 | 0.1945 | 0.01527 |
| 0.001083 | 59 | 0.08795 | 0.1945 | 0.01528 |
| 0.001081 | 60 | 0.08687 | 0.1946 | 0.01528 |
| 0.001041 | 61 | 0.08579 | 0.1945 | 0.01529 |
| | | | | |

| CP | nsplit | rel error | xerror | xstd |
|-----------|--------|-----------|--------|---------|
| 0.001015 | 62 | 0.08474 | 0.1942 | 0.0153 |
| 0.001005 | 63 | 0.08373 | 0.195 | 0.01538 |
| 0.001004 | 64 | 0.08272 | 0.1949 | 0.01538 |
| 0.0009949 | 65 | 0.08172 | 0.1949 | 0.01538 |
| 0.0009453 | 66 | 0.08073 | 0.1945 | 0.01541 |
| 0.0009337 | 67 | 0.07978 | 0.1946 | 0.01541 |
| 0.0008966 | 68 | 0.07885 | 0.196 | 0.01549 |
| 0.000887 | 69 | 0.07795 | 0.197 | 0.01551 |
| 0.0008792 | 70 | 0.07706 | 0.1966 | 0.0155 |
| 0.0008766 | 71 | 0.07618 | 0.1967 | 0.0155 |
| 0.0008687 | 72 | 0.07531 | 0.1965 | 0.0155 |
| 0.0008558 | 73 | 0.07444 | 0.1967 | 0.01551 |
| 0.0007907 | 74 | 0.07358 | 0.1965 | 0.01555 |
| 0.0007614 | 75 | 0.07279 | 0.1961 | 0.01563 |
| 0.0007587 | 76 | 0.07203 | 0.1964 | 0.01565 |
| 0.0007347 | 77 | 0.07127 | 0.1972 | 0.01568 |
| 0.0007151 | 78 | 0.07054 | 0.1962 | 0.01565 |
| 0.0007074 | 79 | 0.06982 | 0.1962 | 0.01563 |
| 7e-04 | 80 | 0.06912 | 0.1948 | 0.01544 |
| 0.0006988 | 81 | 0.06842 | 0.1944 | 0.01545 |
| 0.0006932 | 82 | 0.06772 | 0.1935 | 0.01544 |
| 0.0006817 | 86 | 0.06494 | 0.1932 | 0.01544 |
| 0.0006629 | 87 | 0.06426 | 0.1933 | 0.01546 |
| 0.0006497 | 88 | 0.0636 | 0.1913 | 0.01533 |
| 0.0006119 | 90 | 0.0623 | 0.1913 | 0.01532 |
| 0.000577 | 92 | 0.06108 | 0.1919 | 0.01536 |
| 0.000562 | 93 | 0.0605 | 0.1923 | 0.01534 |
| 0.0005601 | 94 | 0.05994 | 0.1929 | 0.0154 |
| 0.0005555 | 95 | 0.05938 | 0.1929 | 0.0154 |
| 0.0005334 | 96 | 0.05882 | 0.1919 | 0.01537 |
| 0.0005295 | 97 | 0.05829 | 0.1908 | 0.01537 |
| 0.0005289 | 98 | 0.05776 | 0.1908 | 0.01537 |
| 0.0005275 | 99 | 0.05723 | 0.1909 | 0.01537 |
| 0.0005188 | 100 | 0.0567 | 0.1905 | 0.01537 |
| 0.0005109 | 101 | 0.05618 | 0.1903 | 0.01536 |
| 0.0004959 | 103 | 0.05516 | 0.1899 | 0.01535 |
| 0.0004849 | 104 | 0.05467 | 0.1901 | 0.01546 |
| 0.0004796 | 107 | 0.05321 | 0.1914 | 0.01551 |
| 0.0004751 | 109 | 0.05225 | 0.1916 | 0.01551 |
| 0.0004547 | 110 | 0.05178 | 0.1907 | 0.01551 |
| 0.0004515 | 111 | 0.05132 | 0.1901 | 0.0155 |
| 0.0004185 | 113 | 0.05042 | 0.1911 | 0.01557 |
| 0.000417 | 114 | 0.05 | 0.1907 | 0.01558 |
| 0.0004041 | 115 | 0.04958 | 0.1906 | 0.01558 |
| 0.0003849 | 117 | 0.04878 | 0.1897 | 0.0156 |
| 0.0003746 | 118 | 0.04839 | 0.1898 | 0.01564 |
| | | | | |

| CP | nsplit | rel error | xerror | xstd |
|-----------|--------|-----------|--------|---------|
| 0.0003137 | 119 | 0.04802 | 0.1885 | 0.0156 |
| 0.0003037 | 122 | 0.04708 | 0.1886 | 0.01563 |
| 0.0003036 | 123 | 0.04677 | 0.1892 | 0.01564 |
| 0.0003011 | 124 | 0.04647 | 0.189 | 0.01564 |
| 0.0002904 | 125 | 0.04617 | 0.1889 | 0.01565 |
| 0.0002859 | 126 | 0.04588 | 0.1888 | 0.01565 |
| 0.0002832 | 128 | 0.0453 | 0.1887 | 0.01565 |
| 0.00028 | 129 | 0.04502 | 0.1887 | 0.01565 |
| 0.0002641 | 130 | 0.04474 | 0.189 | 0.01566 |
| 0.000264 | 131 | 0.04448 | 0.1887 | 0.01566 |
| 0.0002531 | 132 | 0.04421 | 0.1885 | 0.01566 |
| 0.0002489 | 133 | 0.04396 | 0.1887 | 0.01566 |
| 0.0002432 | 134 | 0.04371 | 0.1887 | 0.01566 |
| 0.000222 | 135 | 0.04347 | 0.1892 | 0.01568 |
| 0.000219 | 136 | 0.04325 | 0.1892 | 0.01569 |
| 0.0002179 | 137 | 0.04303 | 0.19 | 0.01571 |
| 0.0002161 | 138 | 0.04281 | 0.1902 | 0.01571 |
| 0.0002089 | 139 | 0.04259 | 0.1926 | 0.01587 |
| 0.0002036 | 140 | 0.04238 | 0.1929 | 0.01589 |
| 0.0002028 | 141 | 0.04218 | 0.1933 | 0.01589 |
| 0.0002017 | 143 | 0.04178 | 0.1932 | 0.01589 |
| 0.0001984 | 144 | 0.04157 | 0.1934 | 0.01589 |
| 0.0001953 | 145 | 0.04137 | 0.1934 | 0.0159 |
| 0.0001927 | 146 | 0.04118 | 0.1934 | 0.0159 |
| 0.0001851 | 147 | 0.04099 | 0.1934 | 0.0159 |
| 0.0001795 | 149 | 0.04062 | 0.1934 | 0.01592 |
| 0.0001735 | 150 | 0.04044 | 0.1932 | 0.01592 |
| 0.0001731 | 151 | 0.04026 | 0.1932 | 0.01592 |
| 0.0001711 | 152 | 0.04009 | 0.1933 | 0.01593 |
| 0.0001656 | 153 | 0.03992 | 0.1933 | 0.01593 |
| 0.0001653 | 154 | 0.03975 | 0.1932 | 0.01593 |
| 0.0001645 | 155 | 0.03959 | 0.1932 | 0.01593 |
| 0.0001628 | 156 | 0.03942 | 0.1932 | 0.01593 |
| 0.0001622 | 157 | 0.03926 | 0.1934 | 0.01594 |
| 0.0001601 | 158 | 0.0391 | 0.1936 | 0.01595 |
| 0.0001593 | 160 | 0.03878 | 0.1935 | 0.01595 |
| 0.0001459 | 161 | 0.03862 | 0.194 | 0.01597 |
| 0.0001436 | 162 | 0.03847 | 0.1949 | 0.016 |
| 0.0001417 | 163 | 0.03833 | 0.1949 | 0.016 |
| 0.0001368 | 164 | 0.03819 | 0.1951 | 0.016 |
| 0.0001337 | 165 | 0.03805 | 0.1949 | 0.016 |
| 0.0001336 | 166 | 0.03792 | 0.1948 | 0.01597 |
| 0.0001309 | 167 | 0.03778 | 0.1949 | 0.01597 |
| 0.0001276 | 168 | 0.03765 | 0.1946 | 0.01597 |
| 0.0001246 | 170 | 0.0374 | 0.1946 | 0.01597 |
| 0.0001241 | 171 | 0.03727 | 0.1946 | 0.01597 |
| | | | | |

| СР | nsplit | rel error | xerror | xstd |
|------------|--------|-----------|--------|---------|
| 0.0001223 | 172 | 0.03715 | 0.1946 | 0.01597 |
| 0.0001198 | 173 | 0.03703 | 0.1942 | 0.01597 |
| 0.0001182 | 174 | 0.03691 | 0.1943 | 0.01597 |
| 0.0001135 | 175 | 0.03679 | 0.1945 | 0.016 |
| 0.000112 | 176 | 0.03668 | 0.1944 | 0.0161 |
| 0.0001111 | 177 | 0.03656 | 0.1946 | 0.01611 |
| 0.0001107 | 178 | 0.03645 | 0.1947 | 0.01611 |
| 0.0001086 | 179 | 0.03634 | 0.1947 | 0.01611 |
| 0.000107 | 180 | 0.03623 | 0.1947 | 0.01611 |
| 0.0001067 | 181 | 0.03613 | 0.1947 | 0.01611 |
| 0.0001051 | 182 | 0.03602 | 0.1948 | 0.01612 |
| 0.0001046 | 183 | 0.03591 | 0.1948 | 0.01612 |
| 0.0001042 | 185 | 0.03571 | 0.1948 | 0.01612 |
| 0.0001036 | 186 | 0.0356 | 0.1948 | 0.01612 |
| 9.98e-05 | 187 | 0.0355 | 0.1947 | 0.01612 |
| 9.971 e-05 | 188 | 0.0354 | 0.1946 | 0.01612 |
| 9.881e-05 | 189 | 0.0353 | 0.1946 | 0.01612 |
| 9.375 e-05 | 190 | 0.0352 | 0.1948 | 0.01614 |
| 9.261 e-05 | 191 | 0.03511 | 0.1952 | 0.01614 |
| 9.058e-05 | 192 | 0.03501 | 0.1952 | 0.01614 |
| 7.834e-05 | 193 | 0.03492 | 0.1955 | 0.01617 |
| 7.713e-05 | 194 | 0.03484 | 0.1956 | 0.01619 |
| 7.507e-05 | 195 | 0.03477 | 0.1951 | 0.01614 |
| 7.168e-05 | 196 | 0.03469 | 0.1951 | 0.01614 |
| 7.133e-05 | 197 | 0.03462 | 0.1949 | 0.01612 |
| 7.045e-05 | 198 | 0.03455 | 0.195 | 0.01612 |
| 6.711e-05 | 199 | 0.03448 | 0.1949 | 0.01612 |
| 6.447e-05 | 200 | 0.03441 | 0.195 | 0.01612 |
| 5.926e-05 | 201 | 0.03435 | 0.1949 | 0.01613 |
| 5.906e-05 | 202 | 0.03429 | 0.1949 | 0.01612 |
| 5.761e-05 | 203 | 0.03423 | 0.195 | 0.01612 |
| 5.707e-05 | 204 | 0.03417 | 0.1949 | 0.01613 |
| 5.704e-05 | 205 | 0.03411 | 0.1949 | 0.01613 |
| 5.702e-05 | 206 | 0.03406 | 0.1949 | 0.01613 |
| 5.575e-05 | 207 | 0.034 | 0.1949 | 0.01613 |
| 5.575e-05 | 208 | 0.03394 | 0.1949 | 0.01612 |
| 5.56e-05 | 209 | 0.03389 | 0.1949 | 0.01612 |
| 5.157e-05 | 210 | 0.03383 | 0.1947 | 0.01611 |
| 4.555e-05 | 212 | 0.03373 | 0.1951 | 0.01612 |
| 4.34e-05 | 214 | 0.03364 | 0.1953 | 0.01613 |
| 4.254e-05 | 215 | 0.0336 | 0.1953 | 0.01613 |
| 3.951e-05 | 216 | 0.03355 | 0.1961 | 0.01619 |
| 3.781e-05 | 217 | 0.03351 | 0.1955 | 0.01615 |
| 3.708e-05 | 218 | 0.03348 | 0.1956 | 0.01615 |
| 3.689e-05 | 219 | 0.03344 | 0.1956 | 0.01615 |
| 3.67e-05 | 220 | 0.0334 | 0.1956 | 0.01615 |
| | | | | |

| СР | nsplit | rel error | xerror | xstd |
|------------|--------|-----------|--------|---------|
| 3.333e-05 | 221 | 0.03336 | 0.1956 | 0.01615 |
| 3.22e-05 | 222 | 0.03333 | 0.1957 | 0.01615 |
| 2.788e-05 | 223 | 0.0333 | 0.1956 | 0.01614 |
| 2.78e-05 | 224 | 0.03327 | 0.1953 | 0.01614 |
| 2.778e-05 | 225 | 0.03324 | 0.1952 | 0.01613 |
| 2.506e-05 | 226 | 0.03322 | 0.1952 | 0.01613 |
| 2.346e-05 | 227 | 0.03319 | 0.1956 | 0.01614 |
| 2.334e-05 | 228 | 0.03317 | 0.1954 | 0.01613 |
| 2.263e-05 | 229 | 0.03314 | 0.1954 | 0.01613 |
| 2.19e-05 | 230 | 0.03312 | 0.1954 | 0.01613 |
| 2.151e-05 | 231 | 0.0331 | 0.1953 | 0.01612 |
| 2.097e-05 | 232 | 0.03308 | 0.1954 | 0.01612 |
| 2.04e-05 | 233 | 0.03306 | 0.1953 | 0.01612 |
| 1.985e-05 | 234 | 0.03304 | 0.1953 | 0.01612 |
| 1.929e-05 | 235 | 0.03302 | 0.1954 | 0.01613 |
| 1.832e-05 | 237 | 0.03298 | 0.1955 | 0.01613 |
| 1.774e-05 | 238 | 0.03296 | 0.1955 | 0.01613 |
| 1.769 e-05 | 239 | 0.03294 | 0.1955 | 0.01613 |
| 1.766e-05 | 240 | 0.03292 | 0.1955 | 0.01613 |
| 1.747e-05 | 241 | 0.03291 | 0.1955 | 0.01613 |
| 1.736e-05 | 242 | 0.03289 | 0.1955 | 0.01613 |
| 1.722 e-05 | 243 | 0.03287 | 0.1952 | 0.01613 |
| 1.563 e-05 | 244 | 0.03285 | 0.1952 | 0.01613 |
| 1.394 e-05 | 246 | 0.03282 | 0.1952 | 0.01613 |
| 1.321e-05 | 247 | 0.03281 | 0.1953 | 0.01612 |
| 1.276e-05 | 248 | 0.0328 | 0.1953 | 0.01612 |
| 1.139e-05 | 249 | 0.03278 | 0.1954 | 0.01612 |
| 1.039 e-05 | 250 | 0.03277 | 0.1955 | 0.01613 |
| 1e-05 | 251 | 0.03276 | 0.1955 | 0.01613 |

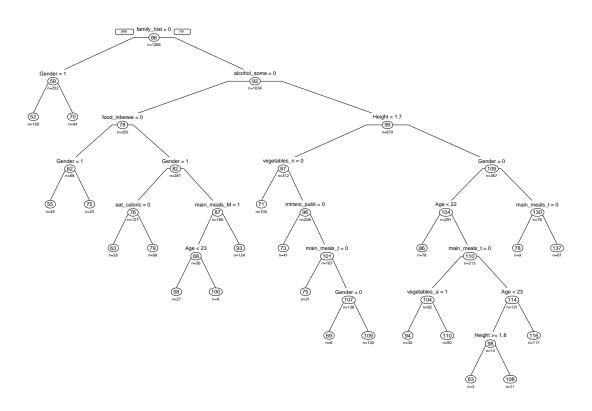
We can see from the results above that, in this case, the CV error starts to rise when CP = 0.0046777.

BUT, there is a standard error in that point estimate! If we do 0.22768+0.013597=0.241277 So, we can go for a SMALLER (and thus better) tree with 19 splits instead of 24, which corresponds to a CP of 0.0051561.

So now we will fit the FINAL prediction tree with a CP of 0.0051561, which is the best value for CP because we calculated it with a Cross-Validation approach!

```
set.seed(1)

tree_2 <- rpart(Weight ~ ., data = train.set,
    method = "anova", control = rpart.control(cp = 0.0051561,
        minbucket = 1, maxdepth = 10))</pre>
```



Now, let's compare the RMSE for validation and training sets.

```
# First, let's create two vectors, one for the
# predicted values, and another for the actual
# values :

predicted_train <- predict(tree_2, train.set)

actual_train <- train.set$Weight

# And lastly, we make use of the RSME formula
# to calculate it :

RMSE_train = sqrt(mean((predicted_train - actual_train)^2))</pre>
RMSE_train
```

[1] 11.29379

We have RMSE = 11.29379

Now, we do the same but for the validation set.

```
predicted_valid <- predict(tree_2, valid.set)
actual_valid <- valid.set$Weight

RMSE_valid = sqrt(mean((predicted_valid - actual_valid)^2))

RMSE_valid</pre>
```

```
## [1] 13.25937
```

The RMSE for the validation data is 13.25937.

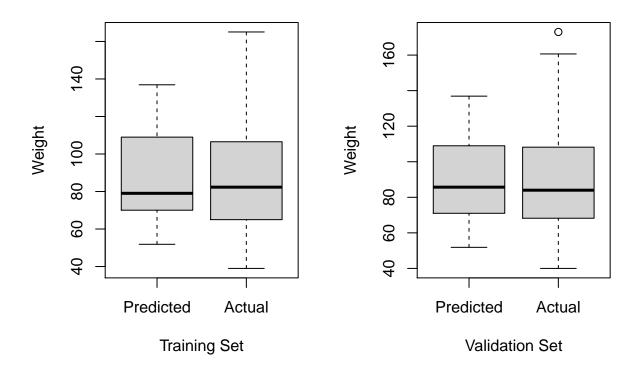
It is very normal that RMSE is smaller with the training data, because we have selected the optimal CP according to the training data. However, the difference seems not so big.

Let's now look at some boxplots to compare the performance of the tree on both sets (training and validation).

```
par(mfrow = c(1, 2))

boxplot(predicted_train, actual_train, names = c("Predicted",
    "Actual"), ylab = "Weight", xlab = "Training Set")

boxplot(predicted_valid, actual_valid, names = c("Predicted",
    "Actual"), ylab = "Weight", xlab = "Validation Set")
```



It is difficult to judge on which set the tree has performed better. Probably the higer RMSE for the validation set is due to the presence of an outlier!

But the training set boxplot seems a bit right skeewed, so one could conclude that the validation set did even a better job.

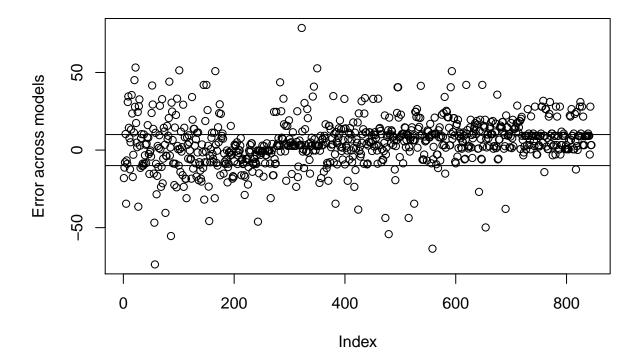
So now we are finished with the regression tree.

We can leave the CP as it is, and the tree will grow until 19 splits.

Now, let's do something quite interesting! We will do a comparison of both KNN and regression tree on the validation set.

We will plot the errors "across the models", so the difference between the predicted weights by both models.

```
plot(predicted - predicted_valid, ylab = "Error across models")
abline(h = 10)
abline(h = -10)
```



We can see that although there is quite a lot of variance, at times both models seem to behave almost equally at predicting the weight.

Inside the range of [-10; 10] there seems to be the majority of the points, so the range is not so big.

Let's take a more precise look at each method compared with the validation data.

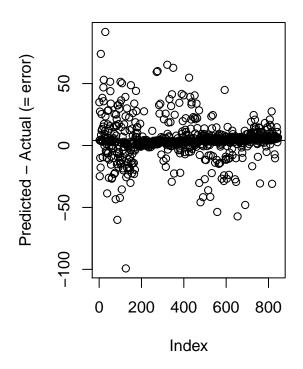
```
par(mfrow = c(1, 2))

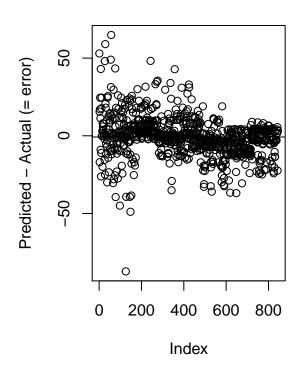
# For KNN :
plot(predicted - valid.set[, 4], main = "k-Nearest Neighbors",
    ylab = "Predicted - Actual (= error)")
abline(h = mean(predicted - valid.set[, 4]))

# For tree :
plot(predicted_valid - valid.set[, 4], main = "Regression Tree",
    ylab = "Predicted - Actual (= error)")
abline(h = mean(predicted_valid - valid.set[,
    4]))
```

k-Nearest Neighbors

Regression Tree





VERY INTERESTING!

Actually we can see that we have the typical trade-off between BIAS and VARIANCE.

Certainly, the k-NN seems to be more precise (less variance), since the points are less far apart from each other. BUT, we observe an upward trend, and the mean of the points (= errors) is at around 4, not 0!

So there is small bias in the k-NN.

However, the regression tree has a lot of variance, BUT on average it is very precise (the mean of the errros is almost at zero). Indeed :

```
# For k-NN :
mean(predicted - valid.set[, 4])

## [1] 4.079884

# For tree :
mean(predicted_valid - valid.set[, 4])

## [1] -0.7759031
```

For the regression tree, the mean is very close to zero.

So now we can discuss which model is better for us. Do we want a very accurate prediction although it may be around on average 4 Kg away from the truth? Or do we want a prediction which is very far from the truth but, taking into account all predictions, on average we are almost exactly on the target?

Probably we want something like the k-NN, since 4 Kg is not much.

The regression tree is less biased and has smaller RMSE, BUT certainly the amount of error is very big (the differences predicted - actual are quite big).

Therefore, we may prefer the k-NN after all!

Ensemble Method (MLR + k-NN + Regression Tree)

The aim of this ensemble method is to combine the Multiple Linear Regression, the k-NN and the Regression Tree in order to obtain even better results. This combination of methods will be done by taking the average prediction of the variable of interest (Weight).

This means that the predicted weight using this ensemble method will be obtained by running the three methods separately and then taking the average over the results.

| ## | | actual | MLR | knn | Regression_tree | ${\tt Ensemble_Method}$ |
|----|----|--------|-----------|-----------|-----------------|--------------------------|
| ## | 2 | 56 | 63.92756 | 90.93895 | 108.99283 | 87.95311 |
| ## | 3 | 77 | 94.05396 | 81.22554 | 92.50013 | 89.25988 |
| ## | 4 | 87 | 82.71985 | 62.15660 | 70.03409 | 71.63685 |
| ## | 6 | 53 | 59.01734 | 80.37579 | 70.03409 | 69.80907 |
| ## | 10 | 68 | 87.56165 | 57.93629 | 92.50013 | 79.33269 |
| ## | 11 | 105 | 101.38382 | 109.66225 | 116.34191 | 109.12933 |

Creating a person for prediction

```
# Creating a person for prediction :
example.df = obesity[1, ]
example.df$Gender = "Male"
example.df\$Age = 25
example.df$Height = 1.78
example.df$Weight = 70
example.df$family history = "no"
example.df\( eat_caloric = "no" \)
example.df$vegetables = "Always"
example.df$main meals = "More than 3"
example.df$food inbetween = "no"
example.df$SMOKE = "no"
example.df$CH20 = "Between 1 and 2 L"
example.df$monitor cal = "no"
example.df$physical act = "2 or 4 days"
example.df$tech devices = "0-2 hours"
example.df$alcohol = "no"
example.df$MTRANS = "Walking"
example.df$NObeyesdad = "Normal weight"
norm.values <- preProcess(obesity[, c(2:4)], method = "range")</pre>
example.norm <- predict(norm.values, example.df)</pre>
example.df = to_factor(example.df)
# example.df = dummy(example.df) Create a
# SINGLE function for dummyfication (need to
# eliminate the _dummy dataset)
# predict(k_nn, example.df) predict(tree_2,
\# example.df) ...
# for Multiple Linear Regression, simply
# replace coefficients and variable values
# into the formula to get the predicted
# weight. Maybe create a function called
# 'MLR()' for this!
```