

Homework Report #8

Problem 1.

In order to compute this expression more efficiently I used the variable elimination method discussed in lecture.

I started with the full joint distribution (with B set = to T and E set = to T) represented as the products of conditionals present in the BBN given by the problem.

I followed the variable elimination procedure assuming the order of elimination $F \rightarrow A \rightarrow D \rightarrow C$

$$\begin{aligned}
 P(B=T, E=T) &= \sum_{a \in T, F} \sum_{c \in T, F} \sum_{d \in T, F, X} \sum_{f \in T, F} P(A=a) P(B=T) P(C=c) P(D=d | A=a, B=T, C=c) P(E=T | C=c) P(F=f | D=d) \\
 &= \sum_{a \in T, F} \sum_{c \in T, F} \sum_{d \in T, F, X} P(A=a) P(B=T) P(C=c) P(D=d | A=a, B=T, C=c) P(E=T | C=c) \left[\sum_{f \in T, F} P(F=f | D=d) \right] \\
 &= \sum_{c \in T, F} \sum_{d \in T, F, X} P(B=T) P(C=c) P(E=T | C=c) \left[\sum_{a \in T, F} P(D=d | A=a, B=T, C=c) P(A=a) \right] \quad \downarrow \\
 &\quad \tau_1(D=d, B=T, C=c) \\
 &= \sum_{c \in T, F} P(B=T) P(C=c) P(E=T | C=c) \left[\sum_{d \in T, F, X} \tau_1(D=d, B=T, C=c) \right] \quad \downarrow \\
 &\quad \tau_2(B=T, C=c) \\
 &= P(B=T) \cdot \left[\sum_{c \in T, F} P(C=c) P(E=T | C=c) \tau_2(B=T, C=c) \right] \quad \downarrow \\
 &\quad \tau_3(B=T, E=T) \\
 &= P(B=T) \cdot \tau_3(B=T, E=T)
 \end{aligned}$$

Problem 2.

Part a.

P -> Pneumonia, F -> Fever, Pa -> Paleness, C -> cough, and HWB -> HighWBCCount

Parameters:

$$p(P=T) = 0.02$$

$$p(P=F) = 0.98$$

$$p(F=T \mid P=T) = 0.9$$

$$p(F=F \mid P=T) = 0.1$$

$$p(F=T \mid P=F) = 0.6$$

$$p(F=F \mid P=F) = 0.4$$

$$p(F=T) = 0.6060$$

$$p(F=F) = 0.3940$$

$$p(Pa=T \mid P=T) = 0.7$$

$$p(Pa=F \mid P=T) = 0.3$$

$$p(Pa=T \mid P=F) = 0.5$$

$$p(Pa=F \mid P=F) = 0.5$$

$$p(Pa=T) = 0.5040$$

$$p(Pa=F) = 0.4960$$

$$p(C=T \mid P=T) = 0.9$$

$$p(C=F \mid P=T) = 0.1$$

$$p(C=T \mid P=F) = 0.1$$

$$p(C=F \mid P=F) = 0.9$$

$$p(C=T) = 0.1160$$

$$p(C=F) = 0.8840$$

$$p(HWB=T \mid P=T) = 0.8$$

$$p(HWB=F \mid P=T) = 0.2$$

$$p(HWB=T \mid P=F) = 0.5$$

$$p(HWB=F \mid P=F) = 0.5$$

$$p(HWB=T) = 0.5060$$

$$p(HWB=F) = 0.4940$$

Part b.

$$P(\text{Pneumonia} = T \mid \text{Fever} = T, \text{Paleness} = F, \text{Cough} = T, \text{HighWBCcount} = F) = 0.0564$$

Part c.

$$P(\text{Pneumonia} = T | \text{Fever} = T, \text{Cough} = T) = 0.2305$$

Since we are classifying a patient with missing values and not learning the parameters of the network, we do not have to include/model the missing values in our calculation since this is a Naïve Bayes model and all attributes are independent of one another.

Part d.

The code has been written and submitted.

$$p(\text{Pneumonia} = T | \text{given symptoms}) =$$

0.0564 for row 1 of example.txt

0.1394 for row 2 of example.txt

0.0029 for row 3 of example.txt