Stats to parse out DM and pH effects

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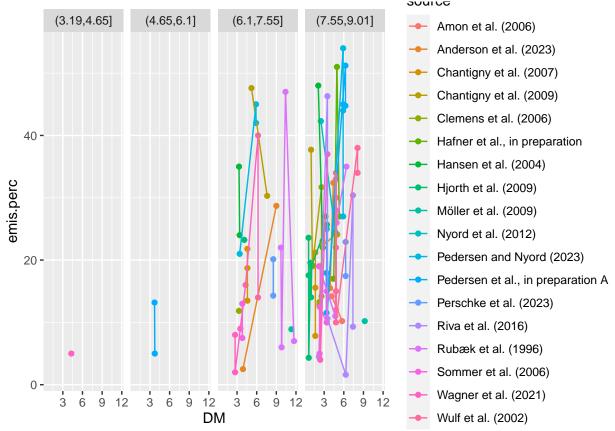
28 april, 2023

Plots

```
dat$DMgrp <- cut(dat$DM, 4)</pre>
dat$pHgrp <- cut(dat$pH, 4)</pre>
dd <- subset(dat, !is.na(pH) & !is.na(DM))</pre>
ggplot(dd, aes(pH, emis.perc, colour = source)) +
  geom_point() +
  geom_line() +
  facet_wrap(~ DMgrp, ncol = 4)
                                                                         30ui 0<del>0</del>
         (0.609, 3.39]
                         (3.39, 6.16]
                                         (6.16, 8.93]
                                                         (8.93, 11.7]
                                                                              Amon et al. (2006)
                                                                               Anderson et al. (2023)
                                                                               Chantigny et al. (2007)
                                                                               Chantigny et al. (2009)
                                                                               Clemens et al. (2006)
    40 -
                                                                               Hafner et al., in preparation
                                                                               Hansen et al. (2004)
emis.perc
                                                                               Hjorth et al. (2009)
                                                                               Möller et al. (2009)
                                                                               Nyord et al. (2012)
                                                                               Pedersen and Nyord (2023)
    20 -
                                                                               Pedersen et al., in preparation A
                                                                               Perschke et al. (2023)
                                                                               Riva et al. (2016)
                                                                               Rubæk et al. (1996)
                                                                               Sommer et al. (2006)
                                                                               Wagner et al. (2021)
                                  8 9 3 4 5 6 7 8 9 3 4 5 6 7 8 9
                                     pΗ
                                                                               Wulf et al. (2002)
ggplot(dd, aes(DM, emis.perc, colour = source)) +
  geom_point() +
  geom_line() +
```

```
facet_wrap(~ pHgrp, ncol = 4)
```

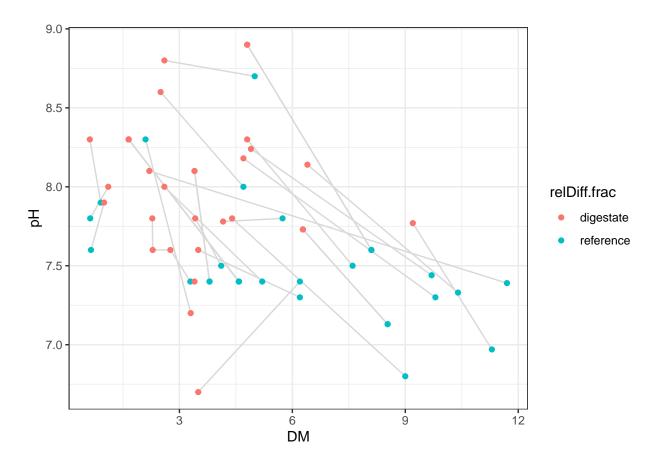
geom_path: Each group consists of only one observation. Do you need to adjust the group aesthetic?



Not pretty but there do seem to be correlations for both DM and pH.

How did digestion change DM and pH?

```
dd <- subset(dd, !is.na(relDiff.set))
ggplot(dd, aes(DM, pH, colour = relDiff.frac, group = interaction(source, relDiff.set))) +
  geom_line(colour = 'gray85') +
  geom_point() +
  theme_bw()</pre>
```



Generally increased pH and decreased DM, as expected in the absence of added high DM substrates.

Models

```
Summary.
```

```
dfsumm(dat[, c('source', 'app.meth', 'DM', 'pH', 'relDiff.frac', 'emis.perc')])
##
    119 rows and 6 columns
##
##
    119 unique rows
                                                                                     pH relDiff.frac emis.pe
##
                                                                            DM
                                    source
                                                              app.meth
## Class
                                 character
                                                            character numeric numeric
                                                                                           character
                                                                                                        numer
## Minimum
                       Amon et al. (2006)
                                                                                    3.2
                                                                                           digestate
                                                            broadcast
                                                                          0.62
## Maximum
                       Wulf et al. (2002) trailing shoe + harrowing
                                                                          11.7
                                                                                      9
                                                                                           reference
## Mean
                                      <NA>
                                                                  <NA>
                                                                          4.43
                                                                                   7.75
                                                                                                 <NA>
                                                                                                           22
## Unique (excld. NA)
                                        20
                                                                     6
                                                                             68
                                                                                     36
                                                                                                    2
## Missing values
                                         0
                                                                     4
                                                                             2
                                                                                     14
                                                                                                   46
## Sorted
                                     FALSE
                                                                FALSE
                                                                         FALSE
                                                                                 FALSE
                                                                                                FALSE
                                                                                                          FAL
##
Overall digestion effect (not expecting much)
```

```
m1 <- lm(emis.perc ~ source + app.meth + relDiff.frac, data = dat)
summary.aov(m1)
```

```
##
                Df Sum Sq Mean Sq F value
                                             Pr(>F)
                     4828
                                      3.98 0.000137 ***
## source
                             344.9
```

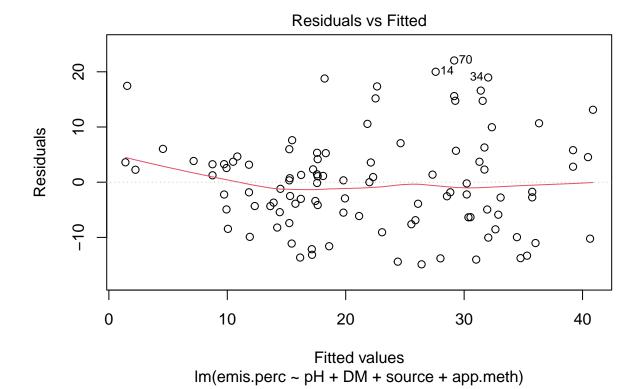
```
## app.meth
                2
                    1324
                           662.1
                                    7.64 0.001252 **
## relDiff.frac 1
                            63.2
                                    0.73 0.397011
                    63
## Residuals
                            86.7
              51
                    4420
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## 50 observations deleted due to missingness
tail(coef(m1))
   sourceWagner et al. (2021)
                                 sourceWulf et al. (2002) app.methopen slot injection
##
##
                    12.798830
                                                20.298830
                                                                          -13.750000
##
        relDiff.fracreference
##
                     1.933273
Nothing.
Separate DM and pH effects.
m2 <- lm(emis.perc ~ pH + DM + relDiff.frac + source + app.meth, data = dat)
summary.aov(m2)
##
               Df Sum Sq Mean Sq F value Pr(>F)
                            67.9
## pH
                1
                    67.9
                                   0.914 0.34486
## DM
                1
                  346.3
                           346.3
                                   4.661 0.03692 *
## relDiff.frac 1
                     1.8
                            1.8
                                   0.024 0.87754
                          208.0
               12 2495.8
                                   2.799 0.00724 **
## source
                          913.2 12.289 0.00114 **
## app.meth
                1 913.2
## Residuals
               40 2972.6
                           74.3
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## 62 observations deleted due to missingness
drop1(m2, test = 'F')
## Single term deletions
##
## Model:
## emis.perc ~ pH + DM + relDiff.frac + source + app.meth
               Df Sum of Sq
                               RSS
                                     AIC F value Pr(>F)
                            2972.6 259.38
## <none>
## pH
                       2.11 2974.7 257.43 0.0284 0.867126
## DM
                       1.59 2974.2 257.42 0.0213 0.884604
                1
                       2.86 2975.4 257.44 0.0385 0.845358
## relDiff.frac 1
               10
                    2404.38 5377.0 273.17 3.2354 0.003866 **
## source
## app.meth
                1
                     913.25 3885.8 272.66 12.2890 0.001139 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
m3 <- lm(emis.perc ~ pH + DM + source + app.meth, data = dat)
summary.aov(m3)
##
              Df Sum Sq Mean Sq F value
                                          Pr(>F)
                    463
                          463.0
                                4.694 0.033286 *
## pH
               1
                   1312 1312.4 13.305 0.000473 ***
## DM
               1
                   4701
                          293.8
                                2.979 0.000678 ***
## source
              16
                          604.6
                                6.130 7.55e-05 ***
               5
                   3023
## app.meth
## Residuals
              79
                   7792
                           98.6
```

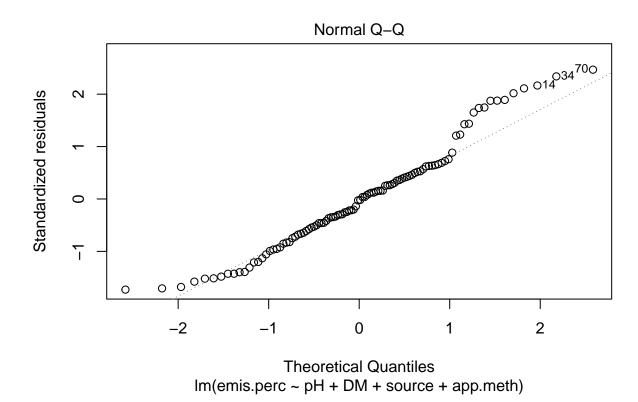
app.methtr

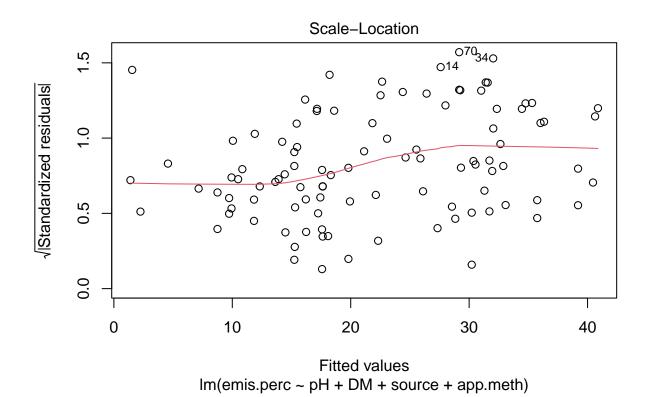
```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## 16 observations deleted due to missingness
drop1(m3, test = 'F')
## Single term deletions
##
## Model:
## emis.perc ~ pH + DM + source + app.meth
                             RSS
                                    AIC F value
            Df Sum of Sq
                                                    Pr(>F)
## <none>
                           7792.1 493.59
## pH
             1
                   529.9 8322.0 498.37 5.3722 0.0230494 *
## DM
             1
                   981.9 8774.1 503.82 9.9554 0.0022695 **
                  4917.5 12709.6 511.98 3.1160 0.0004117 ***
            16
## source
                  3023.1 10815.2 517.36 6.1300 7.548e-05 ***
## app.meth 5
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
cc \leftarrow coef(m3)[1:3]
СС
                                     DM
## (Intercept)
                        pН
## -25.475142
                  4.205796
                               2.109639
confint(m3)[1:3, ]
##
                     2.5 %
                               97.5 %
## (Intercept) -63.6388860 12.688603
## pH
                 0.5939860 7.817605
## DM
                 0.7787866 3.440491
cc['pH'] / cc['DM']
         рΗ
## 1.993609
m3 is where it gets interesting. Clear positive effects of DM and pH, although the pH effect seems small
(+4% emission (frac. of TAN) per unit pH change). Effect of pH is about 2x DM effect (1 unit pH change:
1% DM change).
plot(m3, ask = FALSE)
## Warning: not plotting observations with leverage one:
```

##

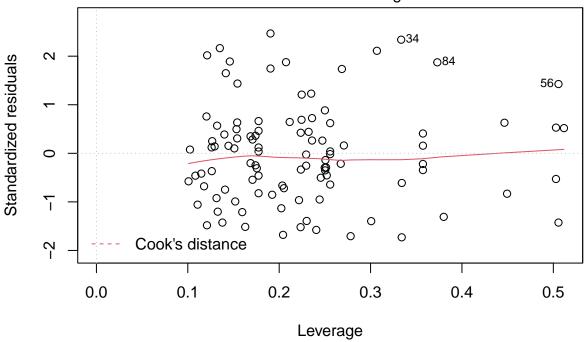
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Residuals vs Leverage



Leverage Im(emis.perc ~ pH + DM + source + app.meth)

We might look at relative effect.

```
m4 <- lm(log10(emis.perc) ~ pH + DM + source + app.meth, data = dat)
summary.aov(m4)
##
               Df Sum Sq Mean Sq F value
                   0.726 0.7257
                                   12.252 0.000767 ***
## pH
## DM
                   0.574
                           0.5744
                                    9.698 0.002570 **
                   2.545
                                    2.686 0.001971 **
##
  source
               16
                           0.1591
## app.meth
                5
                   1.689
                           0.3377
                                    5.702 0.000153 ***
## Residuals
               79
                   4.679
                          0.0592
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## 16 observations deleted due to missingness
cc \leftarrow 100 * (10^coef(m4)[1:3] - 1)
СС
                                     DM
## (Intercept)
                         рΗ
##
     -24.47896
                  38.27664
                               11.86561
100 * (10<sup>confint(m4)[1:3, ] - 1)</sup>
                    2.5 %
##
                              97.5 %
## (Intercept) -91.232586 550.52562
                12.782575
## pH
                            69.53354
## DM
                 3.772978
                           20.58934
```

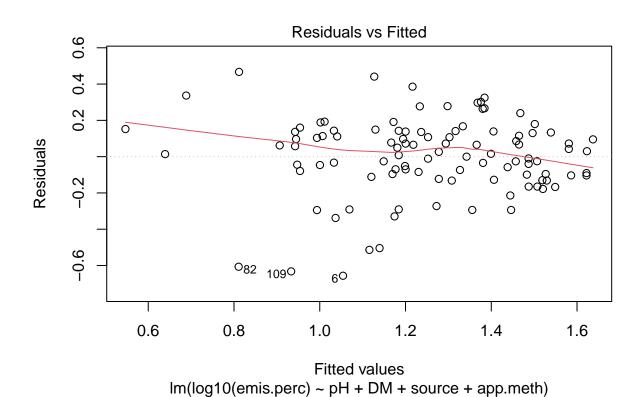
cc['pH'] / cc['DM']

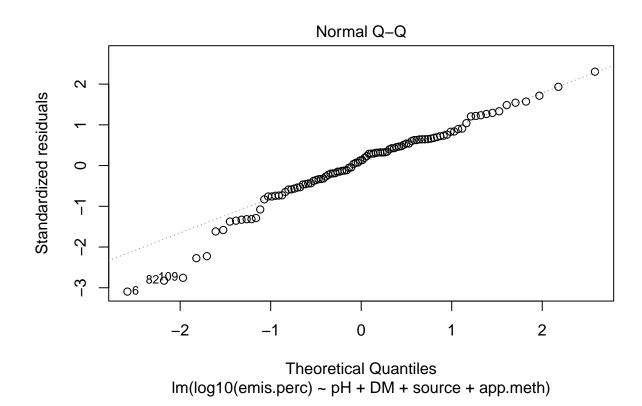
```
## pH
## 3.225847
```

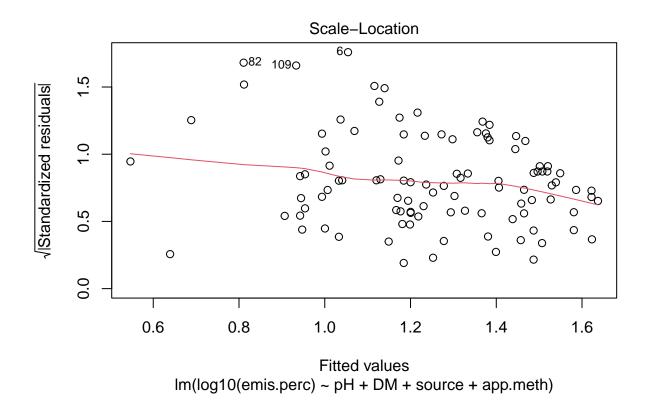
38% increase in emission with a 1 unit increase in pH, seems plausible. Effect of pH here 3x DM effect. Seems more plausible.

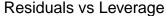
```
plot(m4, ask = FALSE)
```

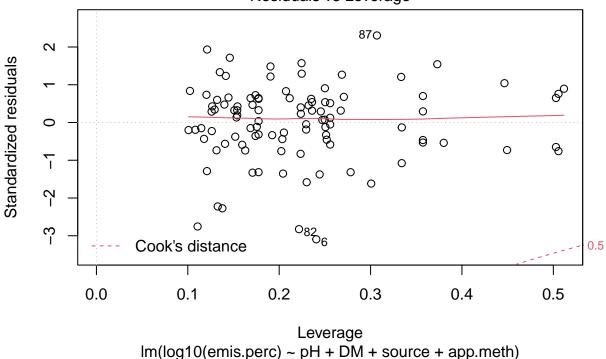
Warning: not plotting observations with leverage one: ## $\,$ 102











Mixed-effects model

As Johanna pointed out, source is really a random effect.

```
dfsumm(dd[, c('pH', 'DM', 'app.meth', 'source')])
##
##
    59 rows and 4 columns
    49 unique rows
##
                            рΗ
##
                                     DM
                                             app.meth
                                                                   source
## Class
                       numeric numeric
                                            character
                                                                character
## Minimum
                           6.7
                                   0.62
                                            broadcast Amon et al. (2006)
## Maximum
                           8.9
                                   11.7 trailing shoe Wulf et al. (2002)
## Mean
                          7.77
                                   4.72
                                                 <NA>
                                                                      <NA>
## Unique (excld. NA)
                            27
                                     43
                                                     4
                                                                        14
## Missing values
                             0
                                      0
                                                     2
                                                                         0
## Sorted
                         FALSE
                                 FALSE
                                                FALSE
                                                                      TRUE
##
dsub <- subset(dat, !is.na(pH) & !is.na(DM) & !is.na(app.meth))</pre>
m5 <- lmer(log10(emis.perc) ~ pH + DM + app.meth + (1|source), data = dsub)
summary(m5)
## Linear mixed model fit by REML ['lmerMod']
## Formula: log10(emis.perc) ~ pH + DM + app.meth + (1 | source)
##
      Data: dsub
```

```
##
## REML criterion at convergence: 35.5
##
## Scaled residuals:
                  1Q
                       Median
                                    3Q
## -2.69602 -0.37275 0.00472 0.58206 1.67428
##
## Random effects:
## Groups
             Name
                         Variance Std.Dev.
## source
             (Intercept) 0.01438 0.1199
## Residual
                         0.05913 0.2432
## Number of obs: 103, groups: source, 17
## Fixed effects:
##
                                     Estimate Std. Error t value
## (Intercept)
                                     -0.02950
                                                  0.35422 -0.083
                                                  0.03999
                                                            3.775
## pH
                                      0.15097
## DM
                                      0.04846
                                                  0.01355
                                                            3.575
                                                  0.13515
                                                          -4.699
## app.methclosed slot injection
                                     -0.63499
## app.methopen slot injection
                                     -0.35685
                                                  0.14158
                                                          -2.520
## app.methtrailing hose
                                     -0.06463
                                                  0.09715
                                                          -0.665
## app.methtrailing shoe
                                     -0.05203
                                                  0.12593
                                                          -0.413
## app.methtrailing shoe + harrowing -0.20991
                                                  0.26252 -0.800
## Correlation of Fixed Effects:
##
               (Intr) pH
                                    app.mthcsi app.mthpsi app.mh app.ms
## pH
               -0.961
               -0.405 0.281
## DM
## app.mthclsi -0.089 -0.017 -0.034
## app.mthpnsi -0.210 0.088 -0.079
## app.mthtrlh -0.375 0.194 -0.040
                                     0.412
                                                 0.575
## app.mthtrls -0.281 0.134 0.018
                                    0.317
                                                 0.539
                                                            0.608
## app.mthts+h -0.024 -0.038 -0.015
                                     0.184
                                                 0.160
                                                            0.240 0.187
ccm < -100 * (10^fixef(m5) - 1)
ccm
##
                         (Intercept)
                                                                     рН
##
                           -6.566185
                                                              41.569348
                                                                                                 11.80528
##
         app.methopen slot injection
                                                  app.methtrailing hose
                                                                                    app.methtrailing sho
##
                          -56.030607
                                                             -13.827757
                                                                                                -11.29042
100 * (10^{confint(m5)}[4:5, ] - 1)
## Computing profile confidence intervals ...
          2.5 %
                  97.5 %
## pH 19.334246 69.27394
## DM 5.430987 18.50035
ccm['pH'] / ccm['DM']
         Нq
## 3.521251
```

D

Large t statistics and similar coefficients as classical linear model m4. Compare:

```
DM
## (Intercept)
                        рΗ
     -24.47896
##
                  38.27664
                              11.86561
ccm
##
                         (Intercept)
##
                           -6.566185
                                                             41.569348
##
         app.methopen slot injection
                                                 app.methtrailing hose
                                                                                   app.methtrailing sho
##
                          -56.030607
                                                            -13.827757
But, let's try likelihood ratio test (I think that's what anova() is doing here).
m0 <- lmer(log10(emis.perc) ~ app.meth + (1|source), data = dsub)</pre>
mOpH <- lmer(log10(emis.perc) ~ DM + app.meth + (1|source), data = dsub)
mODM <- lmer(log10(emis.perc) ~ pH + app.meth + (1|source), data = dsub)
anova(m5, m0pH)
## refitting model(s) with ML (instead of REML)
## Data: dsub
## Models:
## mOpH: log10(emis.perc) ~ DM + app.meth + (1 | source)
## m5: log10(emis.perc) ~ pH + DM + app.meth + (1 | source)
        npar
                      BIC logLik deviance Chisq Df Pr(>Chisq)
##
                AIC
## mOpH
          9 39.919 63.631 -10.9594 21.9189
                                    7.2932 14.626 1 0.0001311 ***
          10 27.293 53.641 -3.6466
## m5
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
anova(m5, m0DM)
## refitting model(s) with ML (instead of REML)
## Data: dsub
## Models:
## mODM: log10(emis.perc) ~ pH + app.meth + (1 | source)
## m5: log10(emis.perc) ~ pH + DM + app.meth + (1 | source)
                      BIC logLik deviance Chisq Df Pr(>Chisq)
               AIC
          9 38.512 62.225 -10.2561 20.5123
## mODM
## m5
         10 27.293 53.641 -3.6466
                                    7.2932 13.219 1 0.0002771 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
anova(m5, m0)
## refitting model(s) with ML (instead of REML)
## Data: dsub
## Models:
## m0: log10(emis.perc) ~ app.meth + (1 | source)
## m5: log10(emis.perc) \sim pH + DM + app.meth + (1 | source)
                    BIC
                         logLik deviance Chisq Df Pr(>Chisq)
             AIC
## mO
        8 44.082 65.160 -14.0409 28.0817
                                   7.2932 20.788 2 3.061e-05 ***
        10 27.293 53.641 -3.6466
## m5
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

D

11.80528

-11.29042

Look at raw and digestate separately.

```
m4r <- lm(log10(emis.perc) ~ pH + DM + app.meth, data = dsub, subset = relDiff.frac == 'reference')
summary(m4r)
##
## Call:
## lm(formula = log10(emis.perc) ~ pH + DM + app.meth, data = dsub,
##
      subset = relDiff.frac == "reference")
##
## Residuals:
##
       Min
                 1Q
                     Median
                                   30
## -0.41478 -0.15717 0.00526 0.14443 0.39722
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
                                          1.11683 -0.540 0.594897
## (Intercept)
                              -0.60305
## pH
                               0.22291
                                          0.13906 1.603 0.123868
## DM
                               0.05360
                                          0.01919
                                                  2.794 0.010878 *
## app.methopen slot injection -0.79886
                                          0.20876 -3.827 0.000983 ***
## app.methtrailing hose
                         -0.07566
                                          0.10865 -0.696 0.493867
## app.methtrailing shoe
                              -0.14913
                                          0.25432 -0.586 0.563853
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2287 on 21 degrees of freedom
    (46 observations deleted due to missingness)
## Multiple R-squared: 0.4666, Adjusted R-squared: 0.3396
## F-statistic: 3.674 on 5 and 21 DF, p-value: 0.01519
drop1(m4r, test = 'F')
## Single term deletions
## Model:
## log10(emis.perc) ~ pH + DM + app.meth
                                   AIC F value
                                                 Pr(>F)
           Df Sum of Sq
                           RSS
                        1.0987 -74.446
## <none>
                0.13444 1.2331 -73.329 2.5696 0.123868
            1
## DM
            1
                0.40839 1.5071 -67.913 7.8058 0.010878 *
                0.82686 1.9256 -65.297 5.2681 0.007231 **
## app.meth 3
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
m4d <- lm(log10(emis.perc) ~ pH + DM + app.meth, data = dsub, subset = relDiff.frac == 'digestate')
summary(m4d)
##
## Call:
## lm(formula = log10(emis.perc) ~ pH + DM + app.meth, data = dsub,
      subset = relDiff.frac == "digestate")
##
##
## Residuals:
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -0.35417 -0.13536 0.00286 0.11649 0.28672
##
## Coefficients:
```

```
##
                               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                0.44423
                                           0.68138
                                                     0.652
                                                              0.521
                                                     1.098
## pH
                                0.08905
                                           0.08113
                                                              0.283
                                                     0.905
                                                              0.374
## DM
                                0.02219
                                           0.02451
## app.methopen slot injection -0.08560
                                           0.15933 -0.537
                                                              0.596
## app.methtrailing hose
                                                              0.271
                                0.11317
                                           0.10046
                                                     1.127
## app.methtrailing shoe
                                0.01676
                                           0.14610
                                                              0.910
                                                     0.115
##
## Residual standard error: 0.1919 on 24 degrees of freedom
     (46 observations deleted due to missingness)
## Multiple R-squared: 0.193, Adjusted R-squared: 0.02487
## F-statistic: 1.148 on 5 and 24 DF, p-value: 0.3629
drop1(m4d, test = 'F')
## Single term deletions
##
## Model:
## log10(emis.perc) ~ pH + DM + app.meth
##
            Df Sum of Sq
                             RSS
                                     AIC F value Pr(>F)
## <none>
                         0.88427 -93.726
## pH
             1 0.044386 0.92866 -94.256 1.2047 0.2833
## DM
             1 0.030200 0.91447 -94.718 0.8197 0.3743
## app.meth 3 0.108323 0.99259 -96.259 0.9800 0.4186
```

Predictions

Might be interesting to see how predictions here stack up against current DK EFs (based on ALFAM2).

```
dat$si <- factor(as.integer(factor(dat$source)))
m6 <- lm(log10(emis.perc) ~ pH + DM + si + app.meth, data = dat)
coef(m6)</pre>
```

```
##
                           (Intercept)
                                                                                                              D
                                                                         pН
                           -0.12193204
                                                                                                     0.0486966
##
                                                                 0.14074882
##
                                   si3
                                                                        si4
##
                            0.05756898
                                                                0.20300552
                                                                                                     0.4039757
##
##
                            0.48801250
                                                                 0.29512484
                                                                                                     0.4211790
##
                                  si14
                                                                       si15
                                                                                                            si1
                                                                                                     0.2076906
##
                            0.26718720
                                                                 0.11573208
##
                                  si18
                                                                       si19
                                                                                                            si2
##
                           -0.01567678
                                                                0.14392388
                                                                                                     0.2576019
##
         app.methopen slot injection
                                                    app.methtrailing hose
                                                                                         app.methtrailing sho
                           -0.57136678
                                                               -0.13501678
                                                                                                    -0.3141407
##
preddat <- data.frame(scenario = c('ref', 'dig', 'dig+'), si = factor(19),</pre>
```

app.meth = 'trailing hose',

DM = c(6.5, 5.1, 6.5), pH = c(7, 7.9, 7.9))

preddat\$emis <- 10^predict(m6, newdata = preddat)

knitr::kable(preddat)

scenario	si	app.meth	DM	pH	emis
ref	19	trailing hose	6.5	7.0	15.44346

scenario	si	app.meth	DM	рН	emis
dig	19	trailing hose	5.1	7.9	17.67028
dig+	19	trailing hose	6.5	7.9	20.67372

Different approach

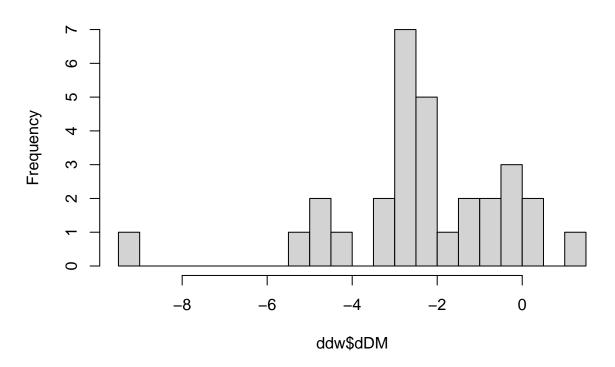
```
ddw <- subset(dw, !is.na(emis.perc.ref + emis.perc.dig + DM.ref + DM.dig + pH.ref + pH.dig))
ddw$demis <- ddw$emis.perc.dig - ddw$emis.perc.ref</pre>
ddw$dpH <- ddw$pH.dig - ddw$pH.ref
ddw$dDM <- ddw$DM.dig - ddw$DM.ref</pre>
m7 <- lm(log10(emis.perc.dig) ~ log10(emis.perc.ref) + dpH + dDM, data = ddw)
summary(m7)
##
## Call:
## lm(formula = log10(emis.perc.dig) ~ log10(emis.perc.ref) + dpH +
       dDM, data = ddw)
##
## Residuals:
       Min
                  1Q
                      Median
                                    30
                                            Max
## -0.33780 -0.05069 0.00758 0.07053 0.26165
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.57702
                                    0.12075
                                              4.779 6.03e-05 ***
                                              6.021 2.33e-06 ***
## log10(emis.perc.ref) 0.55047
                                    0.09142
## dpH
                         0.01750
                                    0.05700
                                              0.307
                                                       0.761
## dDM
                        -0.00567
                                    0.01393 -0.407
                                                       0.687
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1364 on 26 degrees of freedom
## Multiple R-squared: 0.5862, Adjusted R-squared: 0.5385
## F-statistic: 12.28 on 3 and 26 DF, p-value: 3.42e-05
m8 <- lm(demis ~ dpH + dDM, data = ddw)
summary(m8)
##
## lm(formula = demis ~ dpH + dDM, data = ddw)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
                             3.240 17.662
## -16.083 -4.786
                    1.936
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -0.8593
                            2.3139 -0.371
                                              0.713
## dpH
                 1.2468
                            3.3006
                                     0.378
                                              0.709
## dDM
                -0.1133
                            0.8066 -0.140
                                              0.889
##
```

```
## Residual standard error: 7.9 on 27 degrees of freedom
## Multiple R-squared: 0.0103, Adjusted R-squared: -0.06301
## F-statistic: 0.1405 on 2 and 27 DF, p-value: 0.8695
```

Wow. Nothing going on.

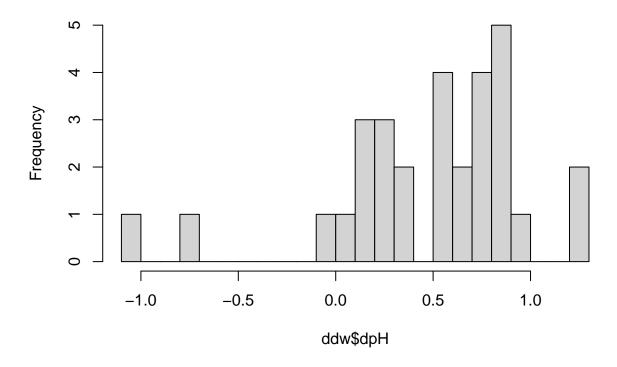
hist(ddw\$dDM, breaks = 20)

Histogram of ddw\$dDM



hist(ddw\$dpH, breaks = 20)

Histogram of ddw\$dpH



Include interaction.

```
m9 <- lm(log10(emis.perc.dig) ~ log10(emis.perc.ref) + dpH*dDM, data = ddw)
summary(m9)</pre>
```

```
##
## Call:
## lm(formula = log10(emis.perc.dig) ~ log10(emis.perc.ref) + dpH *
##
      dDM, data = ddw)
##
## Residuals:
                  1Q
                       Median
                                    ЗQ
                                            Max
##
  -0.34652 -0.06666 -0.00179 0.06010 0.28448
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.64078
                                    0.12425
                                              5.157 2.48e-05 ***
                                              5.521 9.75e-06 ***
## log10(emis.perc.ref)
                         0.51054
                                    0.09248
                                             -0.539
## dpH
                        -0.03484
                                    0.06465
                                                       0.595
## dDM
                         0.01932
                                    0.02087
                                              0.926
                                                       0.363
                        -0.04188
## dpH:dDM
                                    0.02660
                                            -1.574
                                                       0.128
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1327 on 25 degrees of freedom
## Multiple R-squared: 0.6235, Adjusted R-squared: 0.5633
## F-statistic: 10.35 on 4 and 25 DF, p-value: 4.371e-05
```