

Figure 9.14: Bode plots for first- and second-order systems. (a) The first-order system G(s) = a/(s+a) can be approximated by asymptotic curves (dashed) in both the gain and the frequency, with the breakpoint in the gain curve at  $\omega = a$  and the phase decreasing by 90° over a factor of 100 in frequency. (b) The second-order system  $G(s) = \omega_0^2/(s^2 + 2\zeta\omega_0 s + \omega_0^2)$  has a peak at frequency  $\omega_0$  and then a slope of -2 beyond the peak; the phase decreases from 0° to  $-180^\circ$ . The height of the peak and the rate of change of phase depending on the damping ratio  $\zeta$  ( $\zeta = 0.02, 0.1, 0.2, 0.5,$  and 1.0 shown).