

Signals and Systems

Assignment 3

Spring 2021

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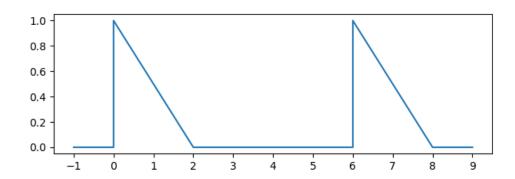
Question 1

Determine the Fourier Series coefficients \boldsymbol{a}_k for the following periodic signals:

(a)
$$x(t) = 3\cos(\frac{2\pi t}{3} + \frac{\pi}{3}) + 5\sin(\frac{2\pi t}{18})$$

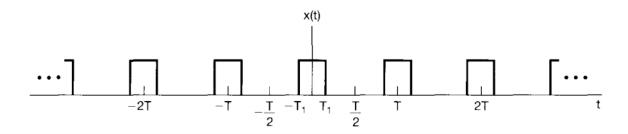
(b)
$$x(t) = 2\sin(\frac{2\pi t}{3} + \frac{\pi}{6})$$

(c) (Using the definition integral)

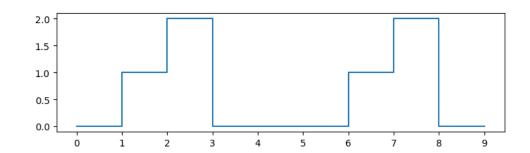


Question 2

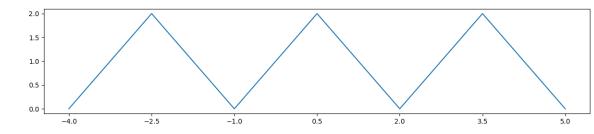
Determine the Fourier Series coefficients a_k for x(t):



(a) .



(b) .



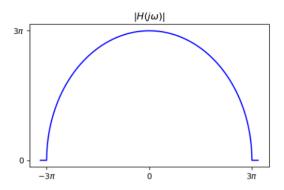
Question 3

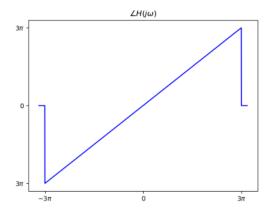
(Textbook Section 3.8 - Fourier Series and LTI Systems) Consider a signal x(t) with Fourier Series representation like this:

$$a_{-2} = a_2 = \frac{1}{16}$$

$$a_{-1} = a_1 = \frac{1}{8}$$
$$a_0 = 1$$

And otherwise $a_k=0$. Keep in mind that T=4. Consider an LTI System with frequency response $H(j\omega)$ as plotted below.





- (a) Determine the output y(t), and its Fourier Series coefficients b_k , if we apply x(t) as input.
- (b) Using Parseval's relation, determine the average power of y(t).