

Real Valued Functions Of Two or More Variables:-

- A real-valued function is a function whose values are real numbers.
- It is a function that assigns a real number to each member of its domain.
- A real valued function of two variables denoted $z=f(x,y)$ is a rule that assigns to each point $(x,y) \in D(f)$ a unique real number $f(x,y) \in R(f)$.

```
In[1]:= f[x_, y_] := Sin[x^2 - y^2]
```

To make it more convenient, we can write it as:-

```
In[2]:= Clear[f, x, y];  
f = Sin[x^2 - y^2];
```

A function of three variable can be written as:-

```
In[4]:= Clear[g, x, y, z];  
g = x^2 * y^3 - 3 x z;
```

To evaluate the value of a function at a given point:-

- At $(0, \sqrt{(\pi/4)})$:

```
In[7]:= f /. {x -> 0, y -> Sqrt[Pi/4]}
```

```
Out[7]= -\frac{1}{\sqrt{2}}
```

- At $(1-\pi, 1+\pi)$:

```
In[8]:= f /. {x -> 1 - Pi, y -> 1 + Pi}
```

```
Out[8]= Sin[(1 - Pi)^2 - (1 + Pi)^2]
```

```
In[9]:= Simplify[%]
```

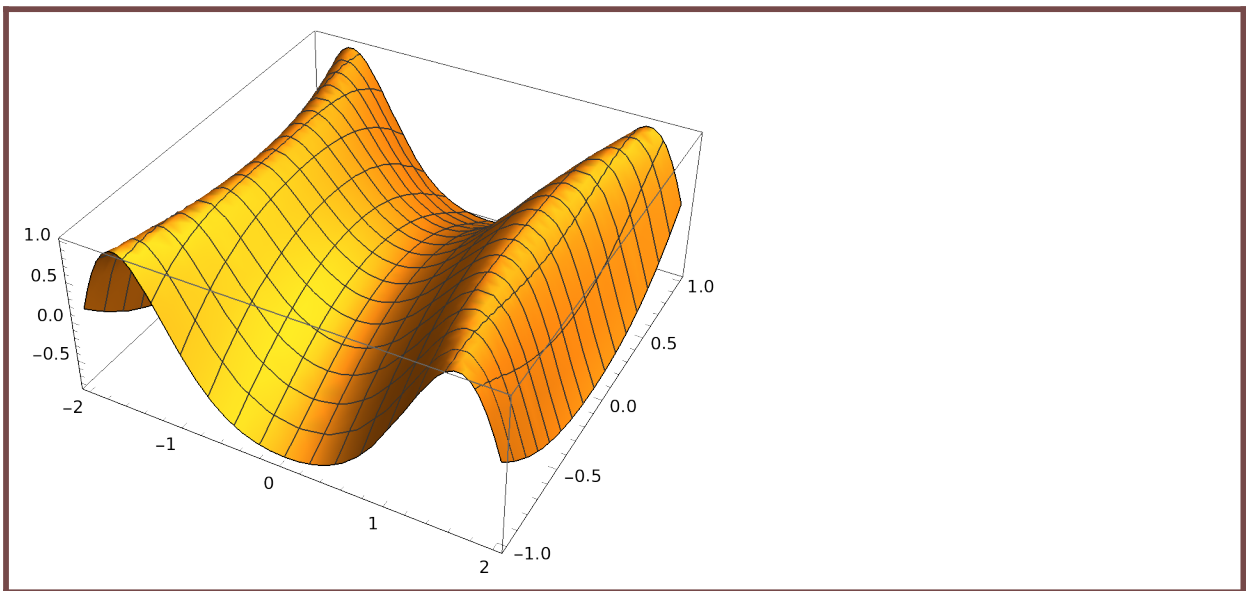
```
Out[9]= 0
```

Plotting functions of two variables with Plot3D:-

- The plotting of functions of two variables can be performed with the command **Plot3D**.
- Here we need an iterator specifying the span of values assumed by each of two variables. The plot will be shown over the rectangular domain in the plane determined by the two iterators.

```
In[11]:= Plot3D[f, {x, -2, 2}, {y, -1, 1}]
```

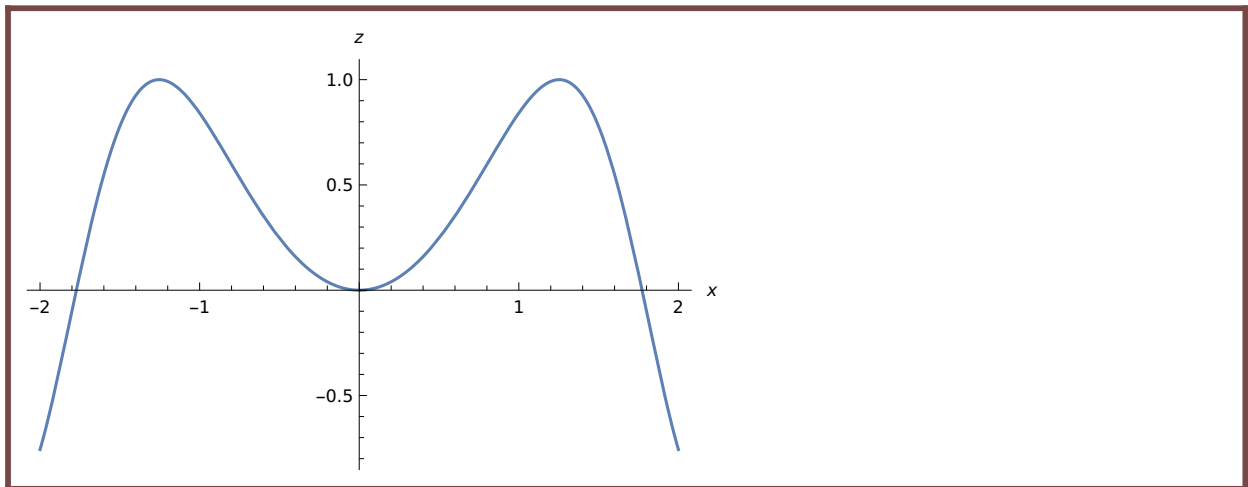
Out[11]=



- To find traces or to sketch any vertical cross-section, we will use the following commands:-

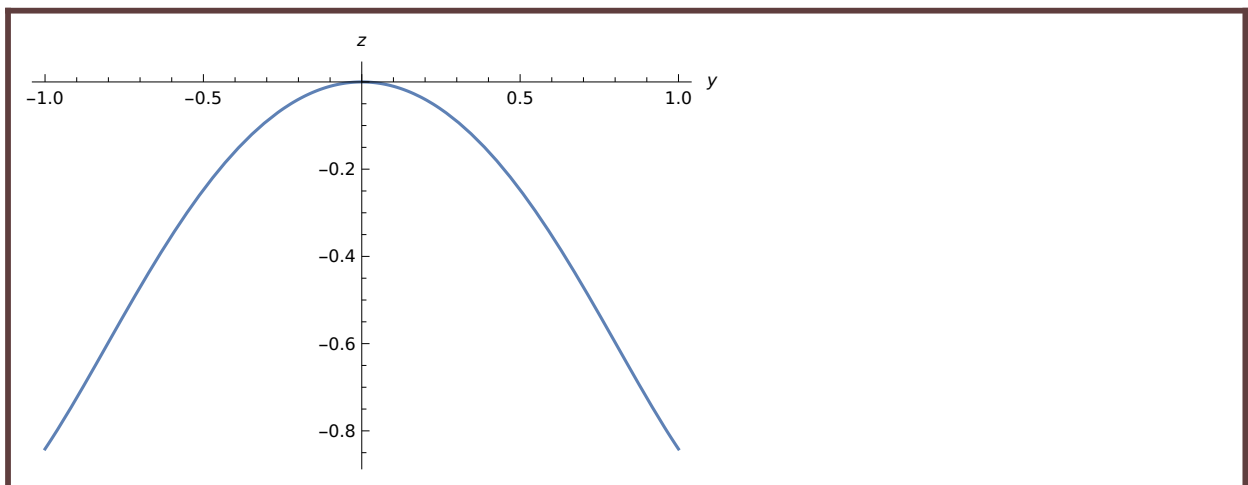
In[12]:= `Plot[f /. y → 0, {x, -2, 2}, AxesLabel → {x, z}]`

Out[12]=



In[13]:= `Plot[f /. x → 0, {y, -1, 1}, AxesLabel → {y, z}]`

Out[13]=



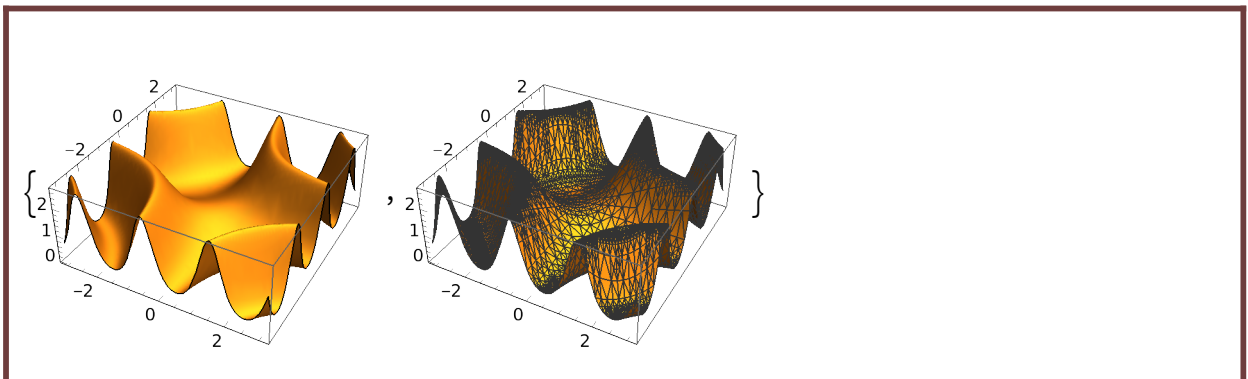
To tweak the output of these plotting commands in some incredible ways.

Some common settings are : **AxesLabel, PlotLabel, PlotPoints, MaxRecursion PlotRange, Mesh and MeshFunctions**

- **Mesh** command will display the polygons produced by Plot3D to render the image.
- **PlotPoints** settings control how many equally spaced points are initially sampled in each direction
- **MaxRecursion** controls the number of recursive subdivisions permitted to fine-tune the image.

```
In[18]:= Table[Plot3D[e^Sin[x*y], {x, - $\pi$ ,  $\pi$ },
  {y, - $\pi$ ,  $\pi$ }, Mesh  $\rightarrow$  m, MaxRecursion  $\rightarrow$  4], {m, {None, All}}]
```

Out[18]=

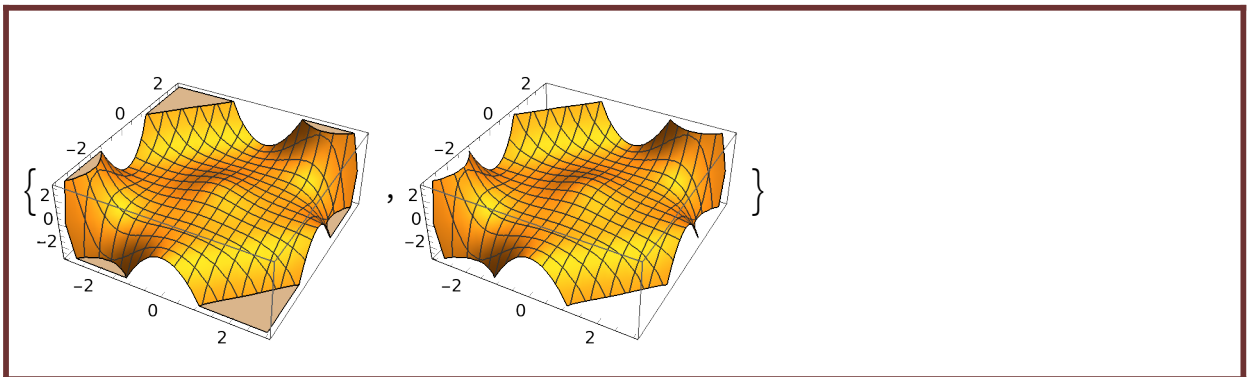


Adjusting the PlotRange and BoxRatios:-

- The option setting `ClippingStyle -> None` will remove the default horizontal planes placed into the clipped areas.
- `PlotRange` is an option for graphics functions that specifies what range of coordinates to include in a plot.
- `PlotRange -> All` will show the entire graph.
- `BoxRatios` determines the relative dimensions of the bounding box.
- `BoxRatios -> Automatic` will scale the bounding box so that all axes have the same scale.

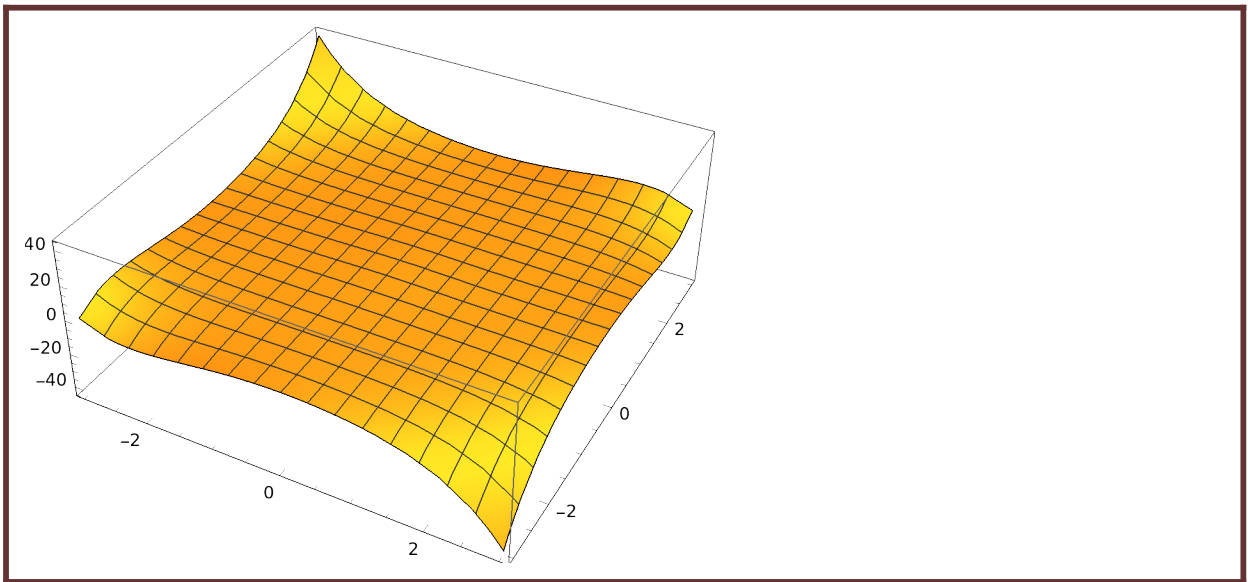
```
In[19]:= Table[Plot3D[{x^2 y^5 - x^5 y^2}/100 + e^{-(x^2 + y^2)},
  {x, -3, 3}, {y, -3, 3}, ClippingStyle -> k], {k, {Automatic, None}}
```

Out[19]=



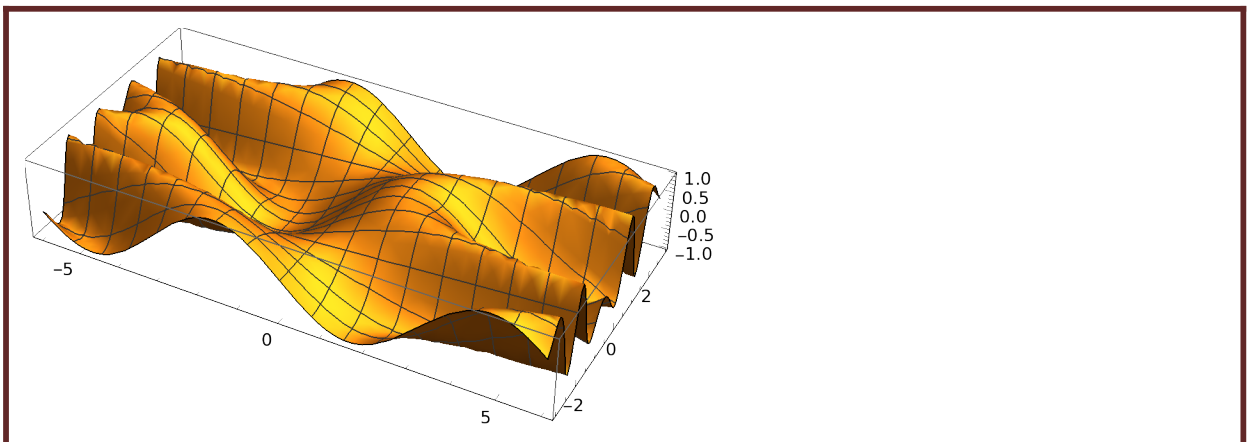
In[20]:= `Plot3D[(x^2 y^5 - x^5 y^2)/100 + e^{-(x^2 + y^2)}, {x, -3, 3}, {y, -3, 3}, PlotRange -> All]`

Out[20]=



In[22]:= `Plot3D[Sin[x * Cos[y]], {x, -6, 6}, {y, -3, 3}, BoxRatios -> Automatic]`

Out[22]=

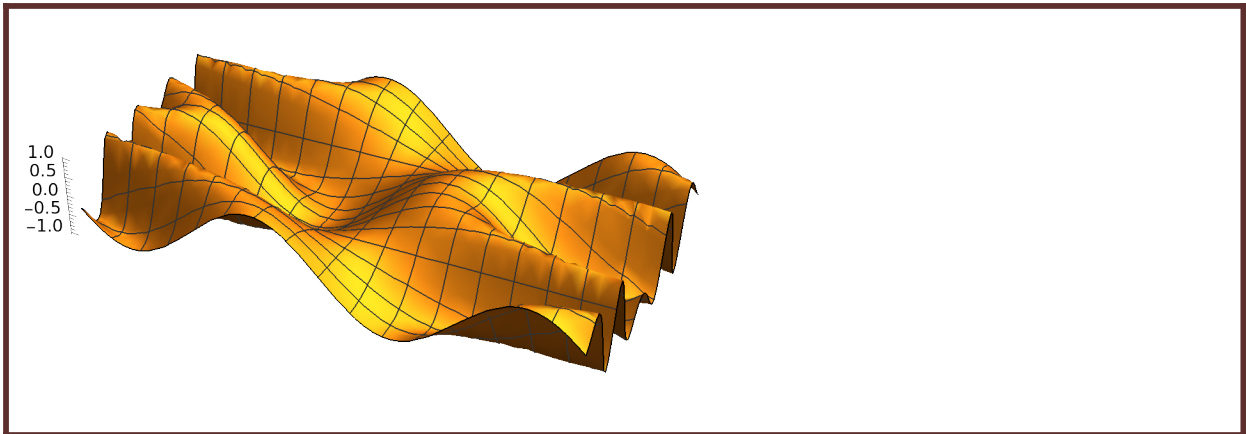


The Bounding Box, Axes, and ViewPoint:-

- The options **Boxed** and **Axes** can be used to modify the appearance of the bounding box and the tick marks that appear on three of its sides.
- By default, both options are set to **True**. To remove the bounding box entirely, set both to **False**.
- **Axes** can also be set to a list to display only selected axes.
- **AxesEdge** controls in each of the three coordinate directions which of the four parallel sides of the bounding box in that direction are to be used as an axis.
- **ViewPoint** specifies the position in space from which it is seen.

```
In[24]:= Plot3D[Sin[x * Cos[y]], {x, -6, 6}, {y, -3, 3}, BoxRatios -> Automatic, Boxed -> False,
        Axes -> {False, False, True}, AxesEdge -> {Automatic, Automatic, {-1, -1}}]
```

Out[24]=



```
In[25]:= Plot3D[Sin[x * Cos[y]], {x, -6, 6}, {y, -3, 3},  
BoxRatios -> Automatic, ViewPoint -> {3, 0, 1}]
```

Out[25]=

