Simple linear regression

Import the relevant libraries

```
In [1]: import numpy as np
        import pandas as pd
        import matplotlib.pyplot as plt
        import statsmodels.api as sm
        # We can override the default matplotlib styles with those of Seaborn
        #import seaborn as sns
        #sns.set()
```

Load the data

```
In [2]: # Load the data from a .csv in the same folder
        data = pd.read csv('1.01.Simple linear regression.csv')
In [3]: # Let's check what's inside this data frame
Out[3]:
            SAT GPA
         0 1714 2.40
         1 1664 2.52
         2 1760 2.54
         3 1685 2.74
         4 1693 2.83
        79 1936 3.71
        80 1810 3.71
        81 1987 3.73
        82 1962 3.76
        83 2050 3.81
```

In [4]: # This method gives us very nice descriptive statistics. We don't need this as of now, but will later on! data.describe()

Out[4]: SAT **GPA** 84.000000 84.000000 count mean 1845.273810 3.330238 104.530661 0.271617 std **min** 1634.000000 2.400000 **25%** 1772.000000 3.190000 **50%** 1846.000000 3.380000 **75%** 1934.000000 3.502500 3.810000 **max** 2050.000000

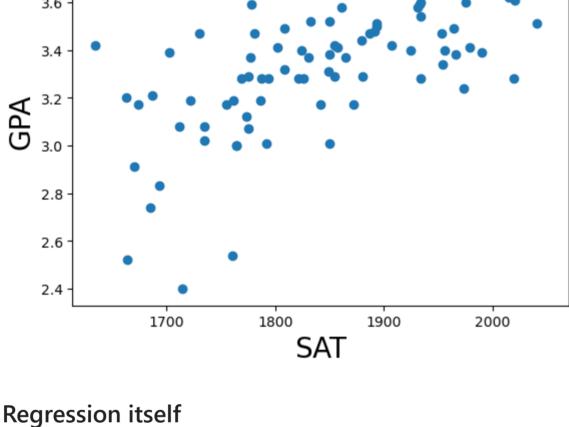
84 rows × 2 columns

Create regression

```
In [5]: # Following the regression equation, our dependent variable (y) is the GPA
        y = data ['GPA']
        # Similarly, our independent variable (x) is the SAT score
        x1 = data ['SAT']
```

Explore the data

```
In [6]: # Plot a scatter plot (first we put the horizontal axis, then the vertical axis)
        plt.scatter(x1,y)
        # Name the axes
        plt.xlabel('SAT', fontsize = 20)
        plt.ylabel('GPA', fontsize = 20)
        # Show the plot
        plt.show()
             3.8
             3.6
             3.4
```



Define the dependent and the independent variables

$x = sm.add_constant(x1)$

In [7]:

Fit the model, according to the OLS (ordinary least squares) method with a dependent variable y and an idepen results = sm.OLS(y,x).fit()# Print a nice summary of the regression. That's one of the strong points of statsmodels -> the summaries results.summary() **OLS Regression Results** Out[7]: Dep. Variable: **GPA** R-squared: 0.406 Model: OLS Adj. R-squared: 0.399

Add a constant. Essentially, we are adding a new column (equal in length to x), which consists only of 1s

Method: Least Squares F-statistic: 56.05 Wed, 21 Sep 2022 **Prob (F-statistic):** 7.20e-11 Time: 14:40:06 Log-Likelihood: 12.672 No. Observations: AIC: -21.34 **Df Residuals:** 82 BIC: -16.48 **Df Model: Covariance Type:** nonrobust coef std err t P>|t| [0.025 0.975] **const** 0.2750 0.409 0.673 0.503 1.088 **SAT** 0.0017 0.000 7.487 0.000 0.001 0.002 **Omnibus:** 12.839 **Durbin-Watson:** 0.950

Prob(Omnibus): 0.002 Jarque-Bera (JB): **Prob(JB):** 0.000310 **Kurtosis:** 4.590 **Cond. No.** 3.29e+04 Notes:

strong multicollinearity or other numerical problems.

2.4

1700

1800

SAT

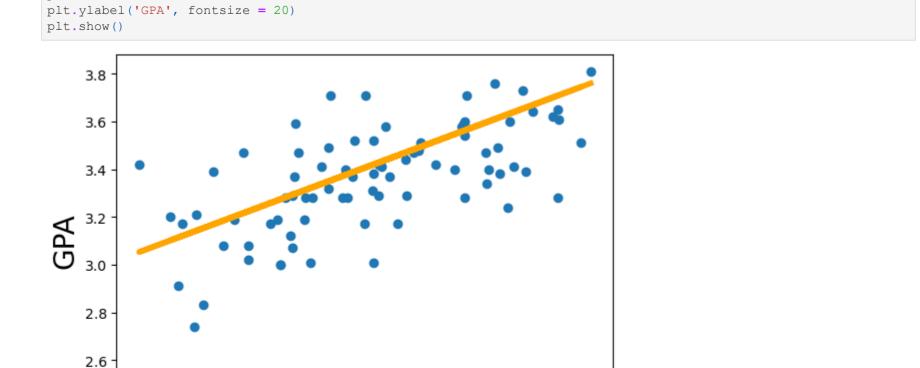
In [8]: # Create a scatter plot plt.scatter(x1,y)

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Define the regression equation, so we can plot it later yhat = 0.0017*x1 + 0.275# Plot the regression line against the independent variable (SAT)

[2] The condition number is large, 3.29e+04. This might indicate that there are

```
fig = plt.plot(x1, yhat, lw=4, c='orange', label ='regression line')
# Label the axes
plt.xlabel('SAT', fontsize = 20)
plt.ylabel('GPA', fontsize = 20)
plt.show()
     3.8
```



2000

1900