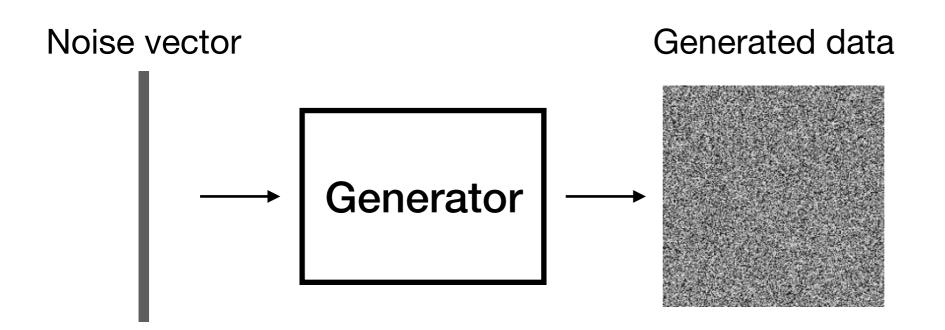
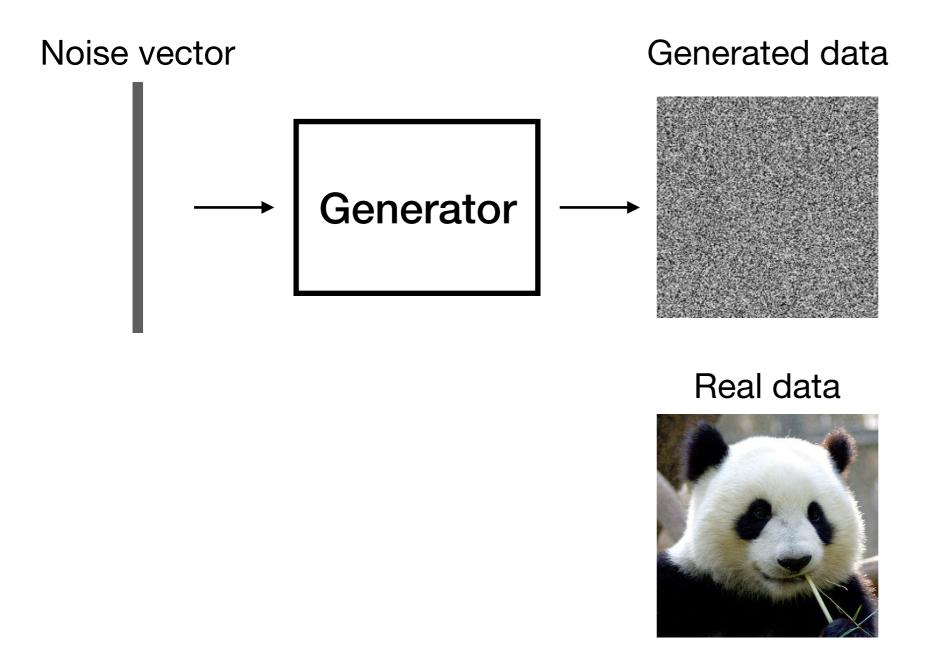
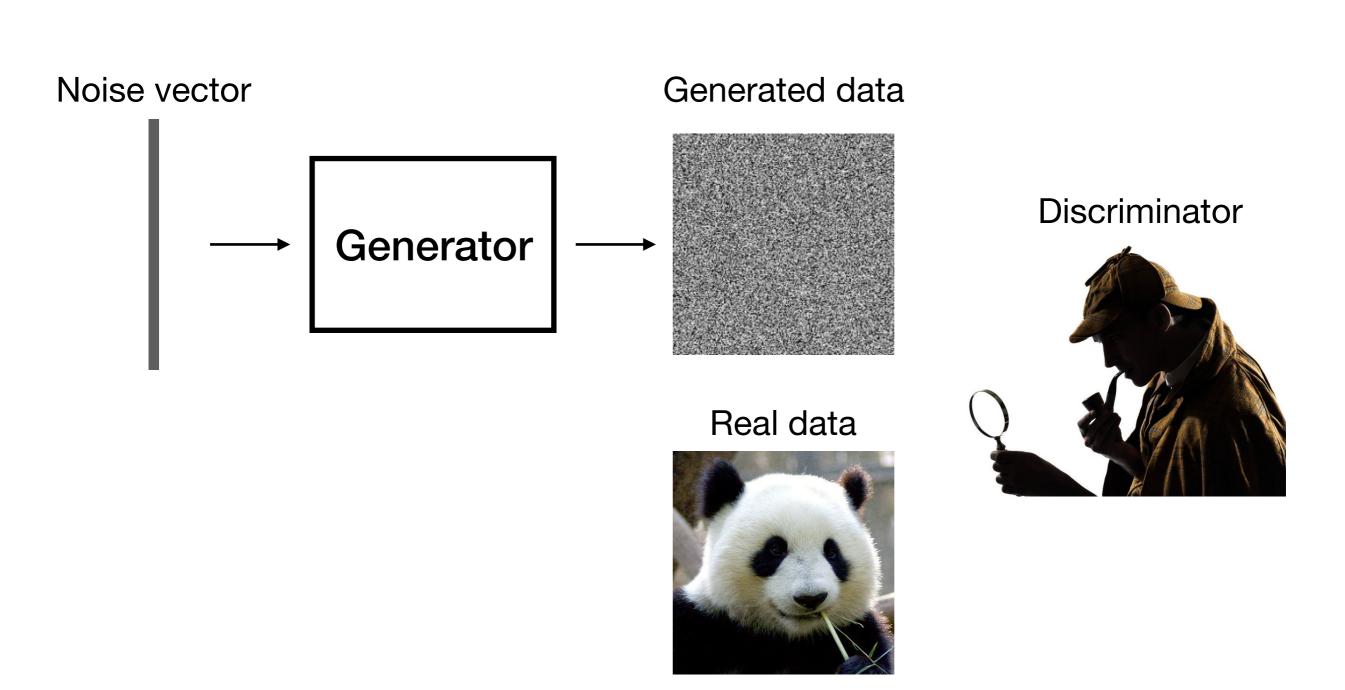
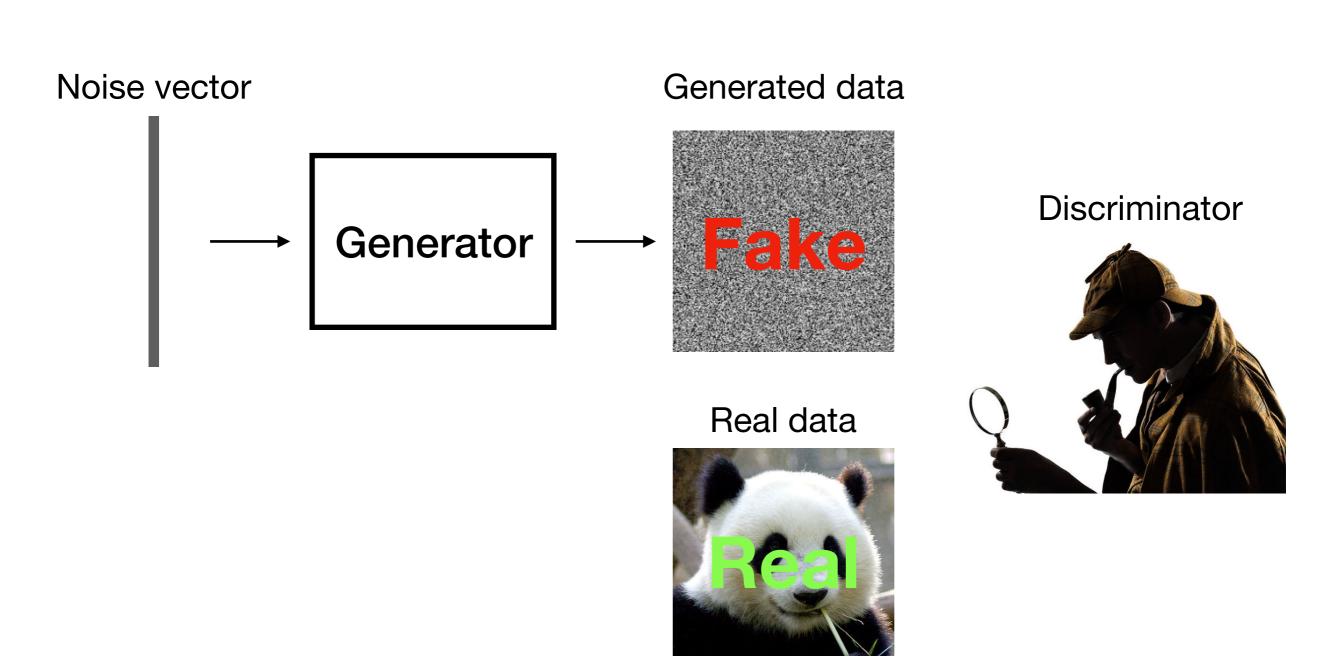
## **GAN**

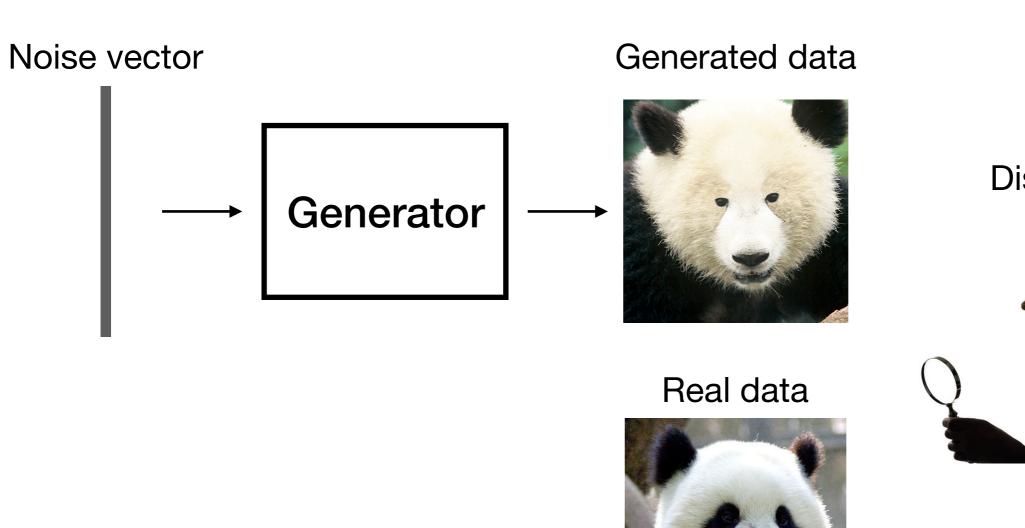
- Generative adversarial network
- Generative model
- Map a latent code to high dimension data
- Training in an adversarial way



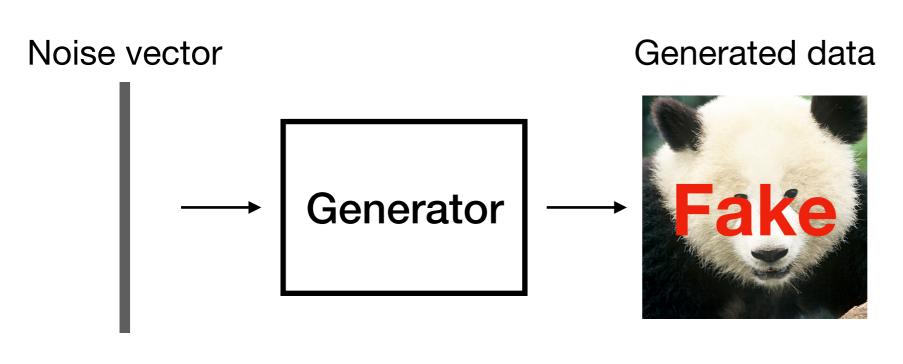






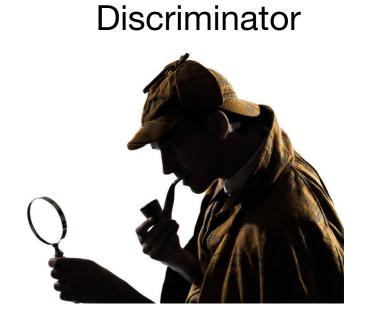


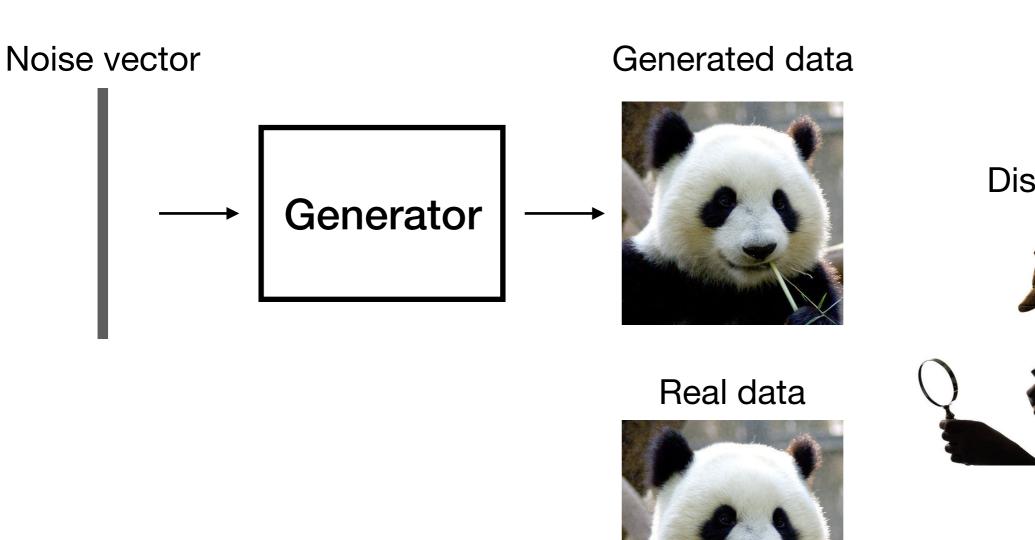




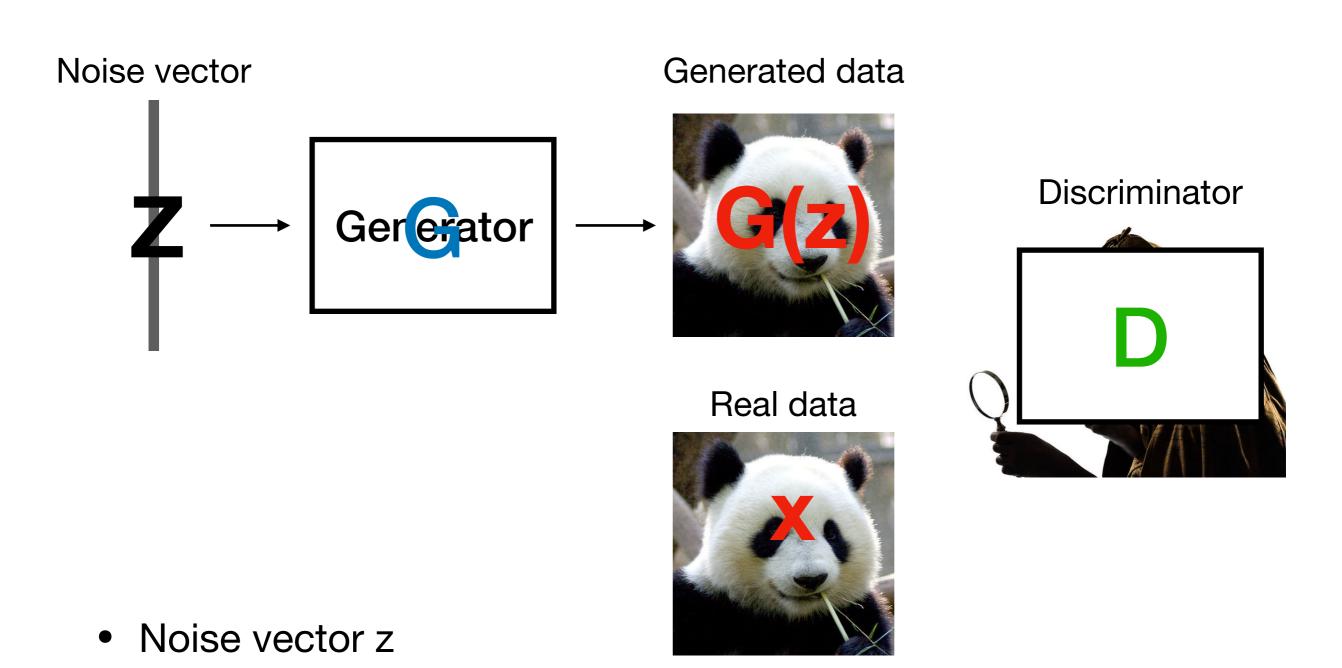












Discriminator D distinguishes G(z) and real data x

Generator G maps from noise z to data space G(z)

- Noise vector z
- Generator G maps from noise z to data space G(z)
- Discriminator D distinguishes G(z) and real data x

## Minimax Game

$$Z \rightarrow \boxed{G} \rightarrow G(z) \rightarrow D(G(z)) 0$$

$$X \rightarrow D(x) 1$$

- Train discriminator D to **maximise** the probability of assigning the correct label to both training samples x (label as 1, i.e. D(x):1) and samples from G (label as 0, i.e. D(G(z)):0)
- Train generator G to minimise the distance between the distribution of generated samples G(z) and the distribution of training samples x

## Minimax Game

#### Full objective:

$$\min_{G} \max_{D} V(D,G) = \mathbb{E}_{\boldsymbol{x} \sim p_{\text{data}}(\boldsymbol{x})}[\log D(\boldsymbol{x})] + \mathbb{E}_{\boldsymbol{z} \sim p_{\boldsymbol{z}}(\boldsymbol{z})}[\log(1 - D(G(\boldsymbol{z})))]$$

# Global optimum

$$Z \rightarrow G \longrightarrow G(z) \longrightarrow D(G(z))$$

$$X \longrightarrow D(x)$$

$$\min_{G} \max_{D} V(D,G) = \mathbb{E}_{\boldsymbol{x} \sim p_{\text{data}}(\boldsymbol{x})}[\log D(\boldsymbol{x})] + \mathbb{E}_{\boldsymbol{z} \sim p_{\boldsymbol{z}}(\boldsymbol{z})}[\log(1 - D(G(\boldsymbol{z})))]$$

- For G,  $p_g = p_{data}$
- For D, it outputs D\*(x) = D\*(G(z))

## Loss function

$$Z \rightarrow G \longrightarrow G(z) \longrightarrow D(G(z))$$

$$X \longrightarrow D(x)$$

$$\min_{G} \max_{D} V(D,G) = \mathbb{E}_{\boldsymbol{x} \sim p_{\text{data}}(\boldsymbol{x})}[\log D(\boldsymbol{x})] + \mathbb{E}_{\boldsymbol{z} \sim p_{\boldsymbol{z}}(\boldsymbol{z})}[\log (1 - D(G(\boldsymbol{z})))]$$

- For G, 
$$\frac{1}{m} \sum_{i=1}^{m} \log \left(1 - D\left(G\left(\boldsymbol{z}^{(i)}\right)\right)\right)$$

- For D, 
$$\frac{1}{m} \sum_{i=1}^{m} \left[ \log D\left(\boldsymbol{x}^{(i)}\right) + \log\left(1 - D\left(G\left(\boldsymbol{z}^{(i)}\right)\right)\right) \right]$$

## Loss function

$$Z \rightarrow \boxed{G} \rightarrow G(z) \rightarrow D(G(z))$$

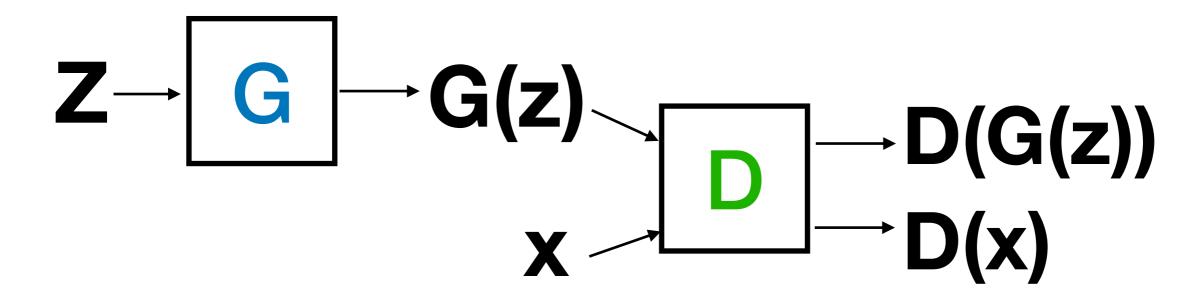
$$\downarrow D \rightarrow D(x)$$

$$\min_{G} \max_{D} V(D,G) = \mathbb{E}_{\boldsymbol{x} \sim p_{\text{data}}(\boldsymbol{x})}[\log D(\boldsymbol{x})] + \mathbb{E}_{\boldsymbol{z} \sim p_{\boldsymbol{z}}(\boldsymbol{z})}[\log (1 - D(G(\boldsymbol{z})))]$$

- For G, 
$$\frac{1}{m}\sum_{i=1}^m\log\left(1-D\left(G\left(\boldsymbol{z}^{(i)}\right)\right)\right)$$
 
$$\text{tf.nn.sigmoid\_cross\_entropy\_with\_logits}$$

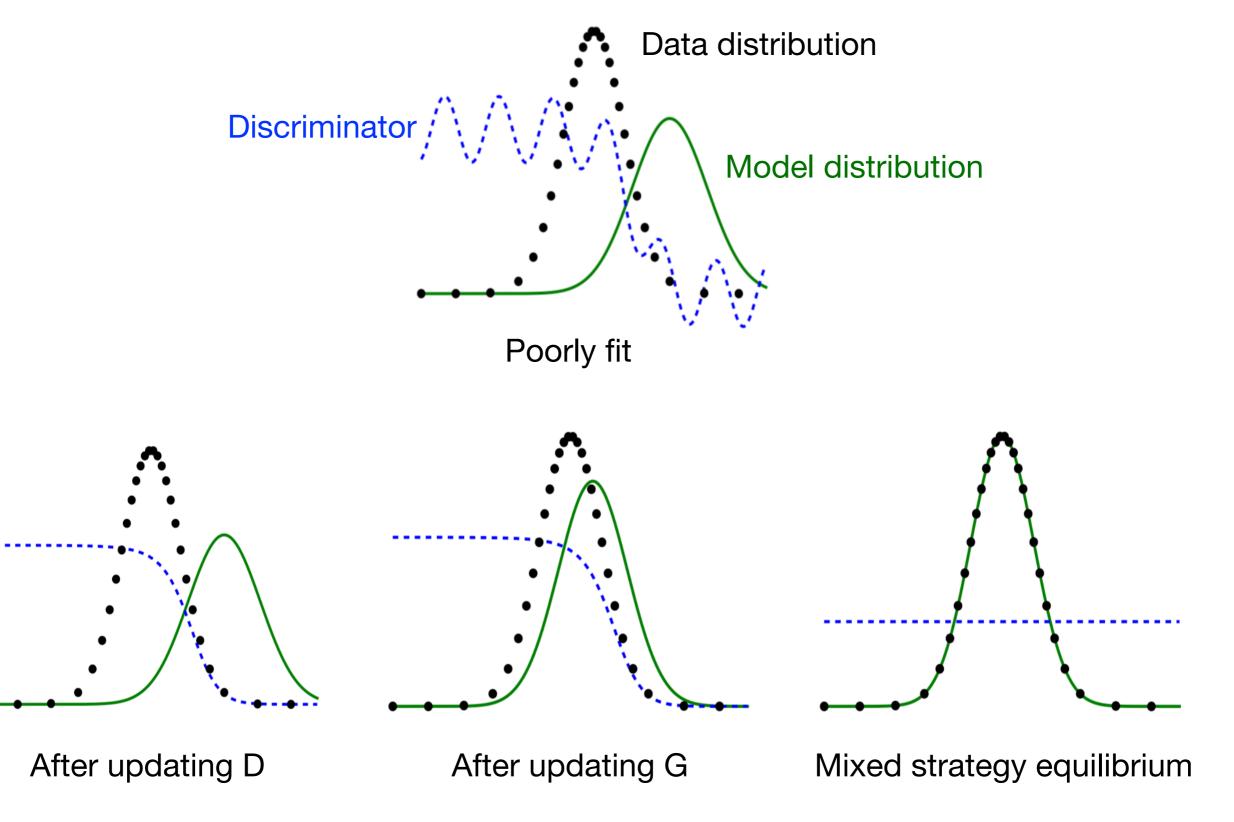
- For D, 
$$\frac{1}{m} \sum_{i=1}^{m} \left[ \log D\left(\boldsymbol{x}^{(i)}\right) + \log\left(1 - D\left(G\left(\boldsymbol{z}^{(i)}\right)\right)\right) \right]$$

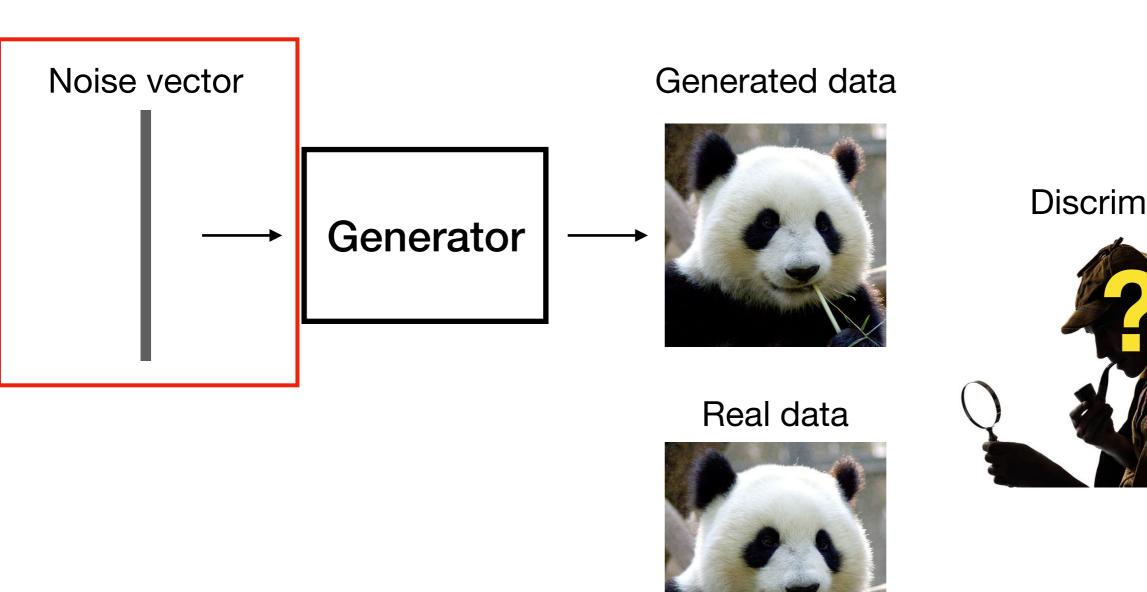
# Training Procedure



- Use SGD (Stochastic gradient descent) or Adam optimiser on generator and discriminator
- Alternately update G and D until converge

## GAN

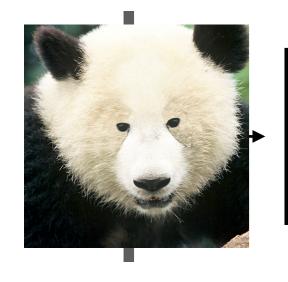






Input image

Noise vector



Generator

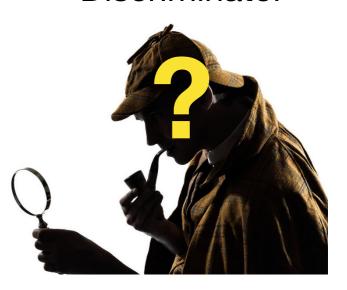
Generated data



Real data



Discriminator



## GAN with Autoencoder

Input image Encoded feature Ger

Generated data



Discriminator



Real data



Input image



Encoded feature

Decoder

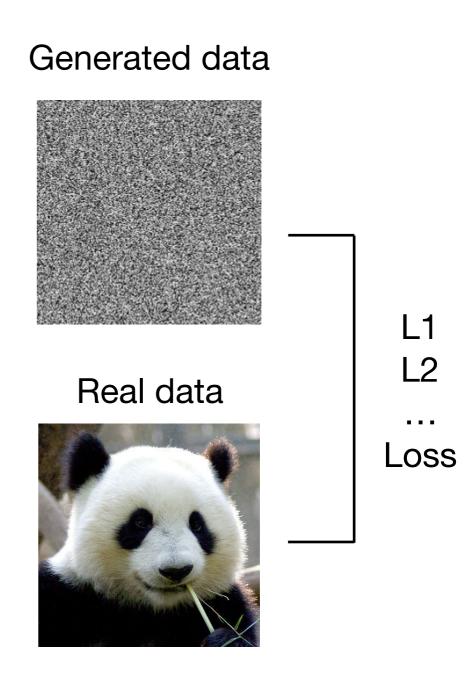
Decoder

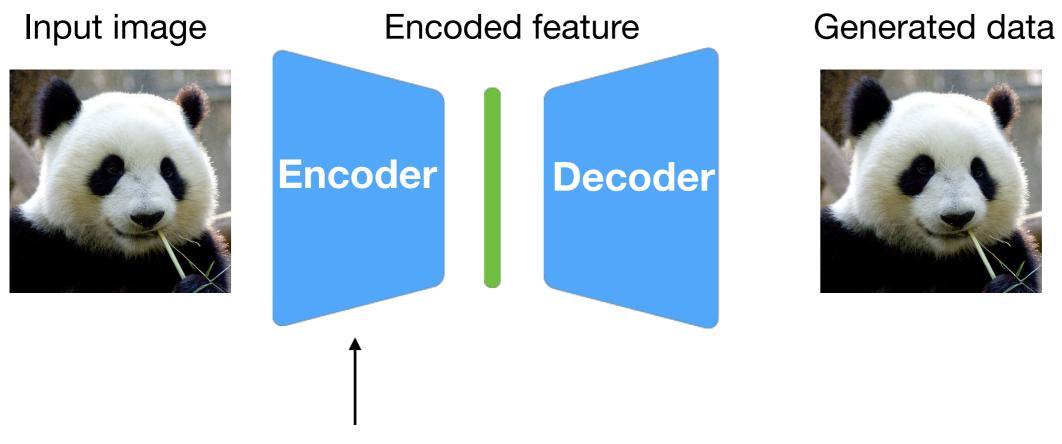
Generated data



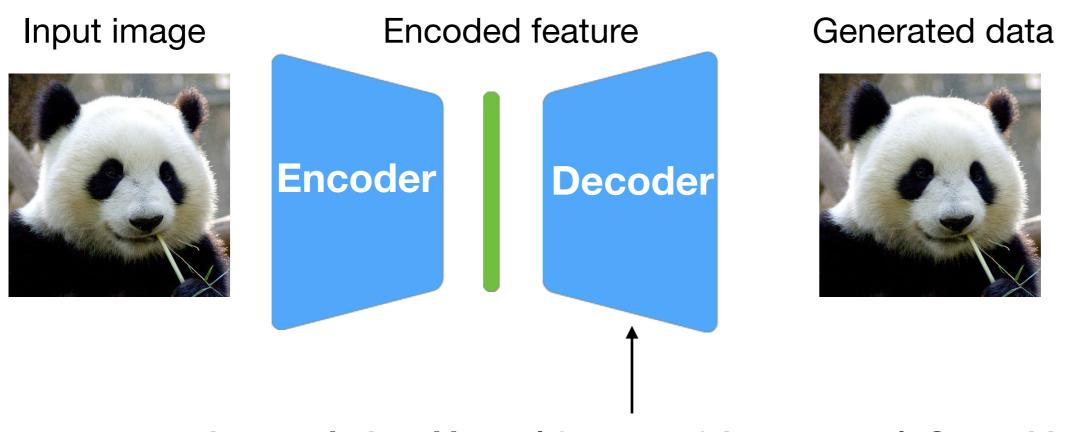
Input image Encoded feature

Encoder Decoder



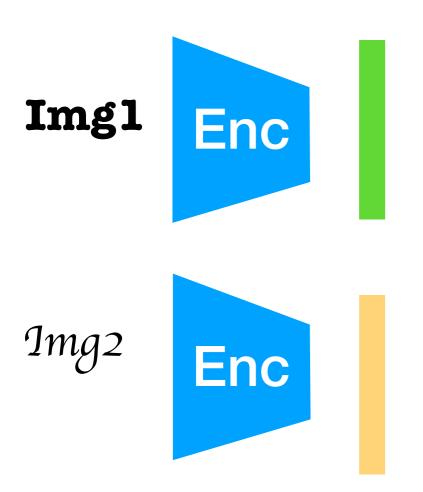


- Convolutional layer (tf.nn.conv2d). Set stride>1 to downsample
- Convolutional layer + pooling
- fully connected layer (tf.layers.dense)

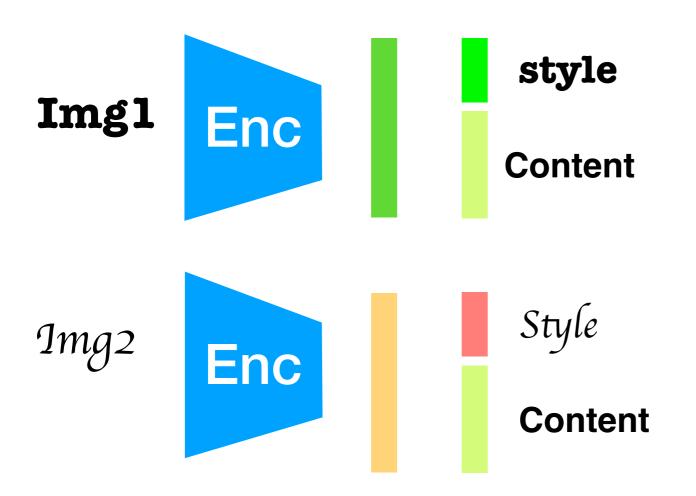


- deconvolutional layer (tf.nn.conv2d\_transpose). Set stride>1 to upsample
- fully connected layer (tf.layers.dense) and reshape the output of last layer to the scale of the image

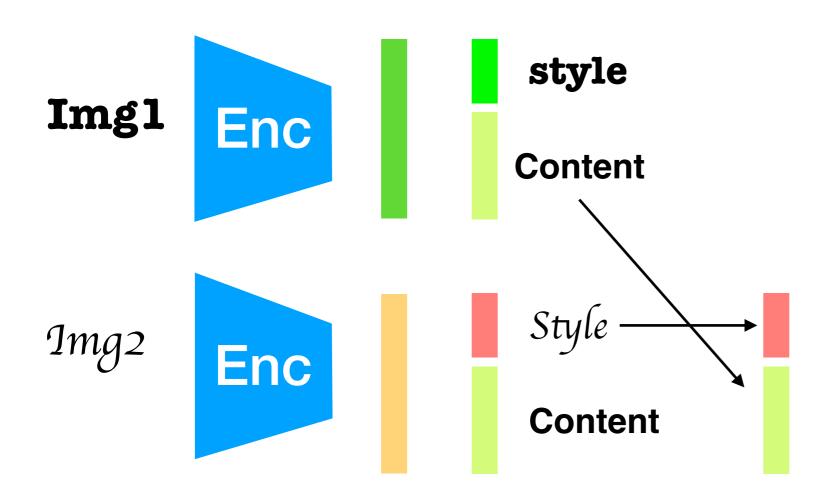
 Approach: Disentangling content and the rest (style, noise etc.) (supervise with weak label)



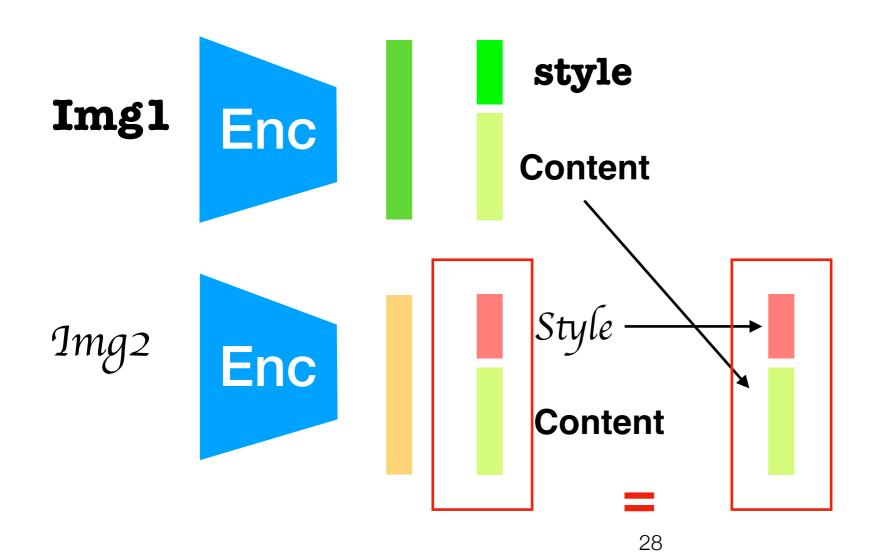
 Approach: Disentangling content and the rest (style, noise etc.)



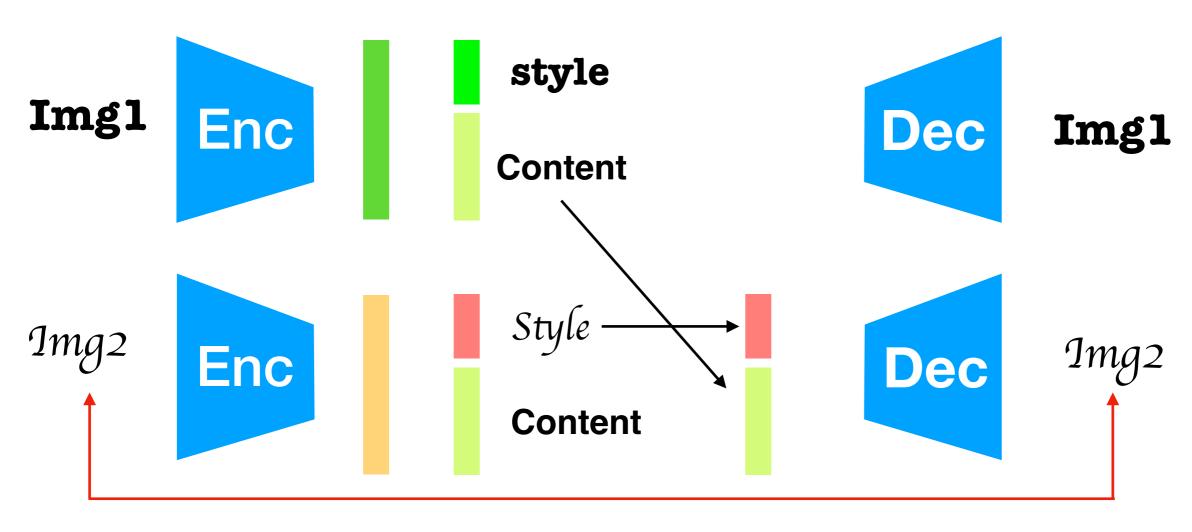
 Approach: Disentangling content and the rest (style, noise etc.)



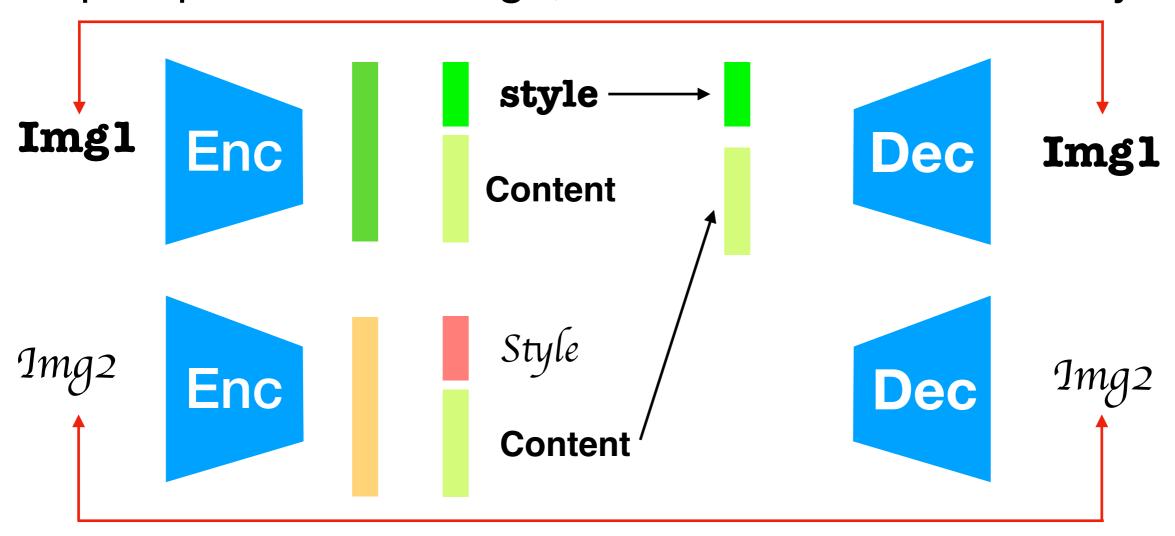
 Approach: Disentangling content and the rest (style, noise etc.)



 Approach: Disentangling content and the rest (style, noise etc.)



 Approach: Disentangling content and the rest (style, noise etc.)



 Approach: Disentangling content and the rest (style, noise etc.)

Output: Real data content + synthetic style

