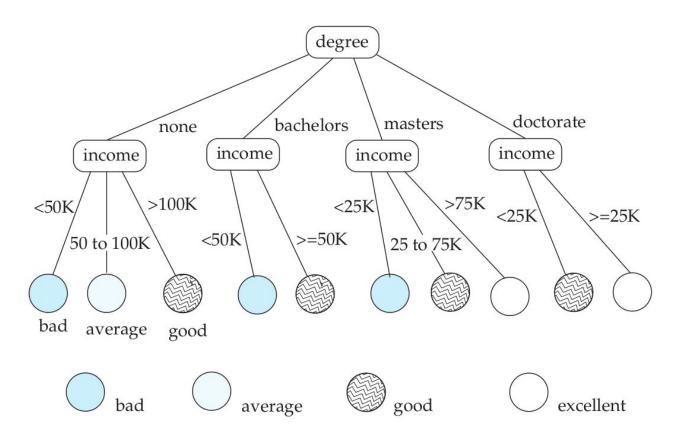
Databases and Information Systems CS303

Data Mining 08-11-2023

Recap: Decision-Tree Classifiers



Building Decision Tree Classifiers

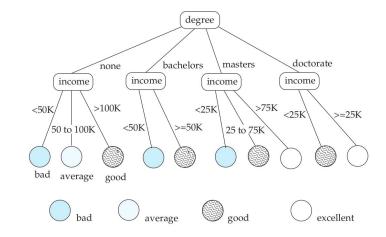
Build a decision-tree classifier, given a set of training instances

Greedy algorithm

- Works recursively, starting at the root and building the tree downward
- o Initially there is only one node, the root, and all training instances are associated with that node
- At each node, if all, or "almost all" training instances associated with the node belong to the same class, then the node becomes a leaf node associated with that class
- Otherwise, a partitioning attribute and partitioning conditions must be selected to create child nodes
- The data associated with each child node is the set of training instances that satisfy the partitioning condition for that child node.

Building Decision Tree Classifiers

- In the example,
 - The attribute degree is chosen, and four children, one for each value of degree, are created.
 - The conditions for the four children nodes are
 - degree= none
 - degree = bachelors
 - degree = masters
 - degree = doctorate
 - At the node corresponding to masters, the attribute income is chosen with the range of values partitioned into intervals
 - 0 to 25K, 25K to 50K, 50K to 75K, and over 75K
 - Since the class for the range 25K to 50K and the range 50K to 75K is the same under the node degree = masters, the two ranges have been merged into a single range 25K to 75K.



- We start with the set of all training instances, which is impure
 - It contains instances from many classes

- Ends up with leaves which are pure
 - All most all training instances belong to only one class
- Pick a particular attribute and condition for partitioning of the data at a node:
 - o measure the purity of the data at the children resulting from partitioning by that attribute
 - The attribute and condition that result in the maximum purity are chosen.

- The purity of a set S of training instances can be measured quantitatively in several ways.
- Suppose there are k classes, and of the instances in S the fraction of instances in class i is p_i .
 - Gini measure, is defined as: $Gini(S) = 1 \sum_{i=1}^{k} p_i^2$
 - Gini value is 0 (minimum) if there is a single class in S
 - Maximum ? (Exercise)
 - Entropy is defined as: Entropy(S) = $-\sum_{i=1}^{k} p_i \log_2 p_i$
 - Entropy is 0 (minimum) if there is a single class in S
 - Maximum ? (Exercise)

• When S is split into $S_1 S_2 \dots S_r$ (purity can be either entropy or Gini value)

$$Purity(S_1, S_2, ..., S_r) = \sum_{i=1}^r \frac{|S_i|}{|S|} purity(S_i)$$
Information_gain(S, {S₁, S₂, ..., S_r}) = purity(S) - purity(S₁, S₂, ..., S_r)

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- The number of elements in each S_i should also be taken into account
 - Whether S_i has 0 or non-zero element makes a big difference

Information_content(
$$S$$
, { S_1 , S_2 , ..., S_r }) = $-\sum_{i=1}^r \frac{|S_i|}{|S|} \log_2 \frac{|S_i|}{|S|}$

Best split has maximum information gain ratio

$$\frac{\text{Information_gain}(S, \{S_1, S_2, \dots, S_r\})}{\text{Information_content}(S, \{S_1, S_2, \dots, S_r\})}$$

- Depends on the type of the attribute
 - Can be either continuous valued : ordered in a fashion meaningful to classification
 - such as age or income
 - Can be categorical: have no meaningful order
 - such as department names or country names
- Splitting continuous attributes:
 - Consider binary splits (Multiway splits is more complicated)
 - First sort the attribute values in the training instances.
 - Then compute the information gain obtained by splitting at each value
 - Example: if the training instances have values 1, 10, 15, and 25 for an attribute, the split points considered are 1, 10, and 15
 - In each case values less than or equal to the split point form one partition and the rest of the values form the other partition.
 - Best binary split for the attribute is the split that gives the maximum information gain.

- Depends on the type of the attribute
 - Can be either continuous valued : ordered in a fashion meaningful to classification
 - such as age or income
 - Can be categorical: have no meaningful order
 - such as department names or country names
- Splitting Categorical attributes:
 - One child for each value of the attribute.
 - Works well with only a few distinct values, such as degree or gender
 - If the attribute has many distinct values
 - creating a child for each value is not a good idea
 - In such cases, try to combine multiple values into each child, to create a smaller number of children

Decision Tree construction Algorithm

- Evaluate different attributes and different partitioning conditions
- Pick the attribute and partitioning condition that results in the maximum information-gain ratio
- Works recursively
 - On each of the sets resulting from the split, recursively construct a decision tree
- The parameters δ_p and δ_s define cutoffs for purity and size

```
procedure GrowTree(S)
Partition(S);

procedure Partition (S)

if (purity(S) > \delta_p or |S| < \delta_s) then
return;
for each attribute A
evaluate splits on attribute A;
Use best split found (across all attributes) to partition
S into S_1, S_2, \ldots, S_r;
for i = 1, 2, \ldots, r
Partition(S_i);
```

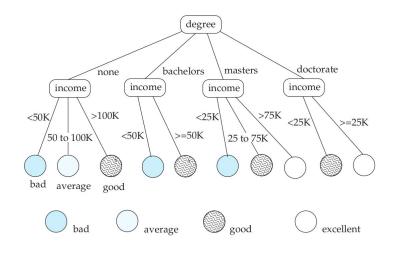
Decision Tree construction Algorithm

- Several of the algorithms also prune subtrees of the generated decision tree to reduce overfitting
 - A subtree is overfitted if it has been so highly tuned to the specifics of the training data that it makes many classification errors on other data
 - A subtree is pruned by replacing it with a leaf node
 - There are different pruning heuristics
 - uses part of the training data to build the tree and another part of the training data to test
 - The heuristic prunes a subtree if it finds that misclassification on the test instances would be reduced if the subtree were replaced by a leaf node

Decision Tree construction Algorithm

- We can generate classification rules from a decision tree
- For each leaf we generate a rule as follows:
 - Left-hand side is the conjunction of all the split conditions on the path to the leaf,
 - Class is the class of the majority of the training instances at the leaf.
- Example:

degree = masters and income > 75000 ⇒ excellent



- Find the distribution of attribute values for each class in the training data
- When given a new instance d:
 - \circ Use the distribution information to estimate, for each class c_j , the probability that instance d belongs to class c_i
 - The class with maximum probability becomes the predicted class for instance d

Formula to find the probability of instance d belonging to class c_i

$$p(c_j|d) = \frac{p(d|c_j)p(c_j)}{p(d)}$$

- \circ p(d | c_j) is the probability of generating instance d in the class c_j
- \circ $p(c_j)$ is the probability of the occurrence of the class c_j
- o p(d) is the probability of occurrence of the instance d

- Example:
 - One attribute, income, is used for classification; input person has income is 76000
 - Assume that income values are broken up into buckets and the bucket containing 76000 contains values in the range (75000, 80000)
 - Suppose
 - Among instances of class excellent, the probability of income being in (75000, 80000) is 0.1
 - Among instances of class good, the probability of income being in (75000, 80000) is 0.05
 - Among instances of class bad and average, the probability of income being in (75000, 80000) is 0

 $p(c_j|d) = \frac{p(d|c_j)p(c_j)}{p(d)}$

- Suppose
 - Overall 0.1 fraction of people are classified as excellent
 - Overall 0.3 are classified as good.
- Then.

 - p(d | c_j) p(c_j) for class excellent is 0.01
 p(d | c_i) p(c_j) for class good is 0.015
- The person would therefore be classified in class good.

- Calculating p(d | c_i) with multiple attributes is complex
- With a limited training set used to find the distribution:
 - Most combinations would not have even a single training set matching them
 - Leads to incorrect classification decisions
- Naive Bayesian classifiers assume attributes have independent distributions

$$p(d|c_j) = p(d_1|c_j) * p(d_2|c_j) * \cdots * p(d_n|c_j)$$

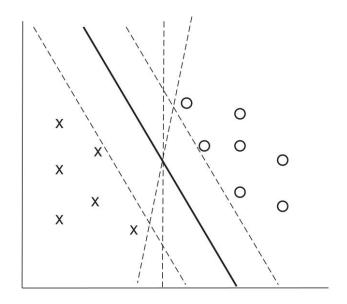
Probability of the instance d occurring is the product of the probability of occurrence of each of the attribute values d_i of d, given the class is c_i

- Benefits of Bayesian classifiers
 - They can classify instances with unknown and null attribute values
 - o unknown or null attributes are just omitted from the probability computation.

 Decision-tree classifiers cannot handle situations where an instance to be classified has a null value for a partitioning attribute used to traverse further down the decision tree

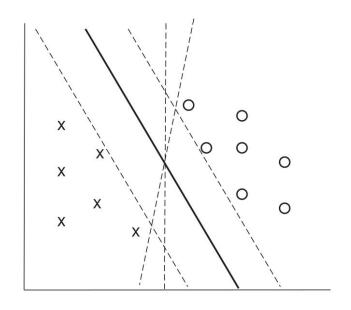
Support Vector Machines

- Gives accurate classification across a range of applications
 - Geometric classification
- In the simplest case, consider a set of points in a two-dimensional plane, some belonging to class A, and some belonging to class B
- We are given a training set of points whose class (A or B) is known, and we need to build a classifier of points, using these training points
- Draw a line on the plane, such that all points in class A lie to one side and all points in line B lie to the other
 - Which line to choose?



Support Vector Machines

- Choose the line whose distance from the nearest point in either class (from the points in the training data set) is maximum
 - o maximum margin line
- Can be generalized to more than two dimensions, allowing multiple attributes to be used for classification
 - Classifier finds a dividing hyperplane
- Can find nonlinear separating curves also
- Can be used for non-binary classification too



Regression

- Deals with the prediction of a value (as supposed to classification)
- Given values for a set of variables X_1, X_2, \dots, X_n
 - Predict the value of a variable Y
- Example: Treat the level of education as a number and income as another number
 - on the basis of these two variables, predict the likelihood of default
- Find a curve that fits the data (Curve fitting)
- Linear regression: Find values of a a using the training data

$$Y = a_0 + a_1 * X_1 + a_2 * X_2 + \cdots + a_n * X_n$$

Validating a Classifier

- Measure the classification error rate, before deciding to use it for an application
- A set of test cases where the outcome is already known is used to measure the quality of the classifier
- For binary classifiers we can assume that input is classified into positive / negative

```
• True positive (t_pos) : Positive instance classified as positive (correct decision)
```

- False positive (f_pos) : Negative instance classified as positive (wrong decision)
- True negative (t_neg) : Negative instance classified as negative (correct decision)
- False negative (f_neg) : Positive instance classified as negative (wrong decision)
- Quality of a classifier: Let pos = t_pos + f_neg and neg = t_neg + f_pos

```
    Accuracy : (t_pos + t_neg) / (pos + neg) fraction of time when classifier is correct
```

- Recall : t_pos / pos how many of the actual positive classes are classified as positive
- Precision : t_pos / (t_pos + f_pos) how often is the positive prediction correct
- Specificity: t_neg / neg
 Dual notion of Recall

Validating a Classifier

- It is a bad idea to use exactly the same set of test cases to train as well as to measure the quality of the classifier
 - Can lead to artificially high measures of quality.
 - The quality of a classifier must measured on test cases that have not been seen during training
- A subset of the available test cases is used for training and a disjoint subset is used for validation.
- In cross validation, the available test cases are divided into k parts numbered 1 to k, from which k different test sets are created as follows:
 - \circ Test set i uses the i-th part for validation, after training the classifier using the other k –1 parts.
 - The results from all k test sets are added up before computing the quality measures.
- Cross validation provides much more accurate measures than merely partitioning the data into a single training and a single test set

- Books frequently bought together
- Movies frequently watched together
- Bread => Milk

(A person who buys bread has a high probability of buying milk)

- Place them close in the store (customer time is reduced)
- Place them far away (customer has to look at many other things before buying what he wants)

- An association rule must have an associated population
 - The population consists of a set of instances.
 - o In the example, population is the grocery purchases, every purchase being an instance

- Rules have a support and confidence
 - Support: Measure of what fraction of the population satisfies both the antecedent and the consequent of the rule
 - 0.001 percent of purchases include milk and stapler (so there is very less support for Milk => Stapler)
 - Minimum degree of support is considered desirable depends on the application
 - o Confidence: Measure of how often the consequent is true when the antecedent is true
 - if 80 % of the purchases that include milk also include bread
 (Milk => Bread has 0.8 confidence)
 - Rule with a low confidence is not meaningful
 - In business applications, rules usually have confidences significantly less than 100 %
 - In other domains, such as in physics, rules may have high confidences.

How to discover association rules of the form

$$0 \quad i_1 i_2 \dots i_n => i_0$$

- First find items with sufficient support, called large itemsets
- For each large itemset output all rules with sufficient confidence that involve all and only the elements of the set.
 - For each large itemset S, output a rule $S s \Rightarrow s$ for every subset $s \subseteq S$
 - If $S s \Rightarrow s$ has sufficient confidence
 - the confidence of the rule is given by support of s divided by support of S

- How to generate large itemsets
 - If the number of possible sets of items is small
 - Single pass over the data suffices
 - A count, initialized to 0, is maintained for each set of items
 - When a purchase record is fetched, the count is incremented for each set of items such that all items in the set are contained in the purchase.
 - Example : If a purchase included items a , b, and c
 - counts would be incremented for {a }, {b}, {c}, {a , b}, {b, c}, {a , c}, and {a , b, c}.
 - Those sets with a sufficiently high count at the end of the pass correspond to items that have a high degree of association
 - The number of sets grows exponentially,
 - But most of the sets would normally have very low support
 - Optimizations have been developed to eliminate most such sets from consideration.
 - Use multiple passes on the database, considering only some sets in each pass.

- How to generate large itemsets
 - For generating large itemsets
 - only sets with single items are considered in the first pass.
 - In the second pass, sets with two items are considered, and so on
 - At the end of each pass, all sets with sufficient support are output as large itemsets.
 - Sets found to have too little support at the end of a pass are eliminated
 - Once a set is eliminated, none of its supersets needs to be considered
 - In pass i count only supports for sets of size i such that all subsets of the set have been found to have sufficiently high support
 - Suffices to test all subsets of size i 1 to ensure this property.
 - At the end of some pass i, if no set of size i has sufficient support then computation terminates.

Other types of Association

- Many associations are not very interesting
 - They can be predicted
 - Example: if many people buy shoes and many people buy milk, we can predict that a fairly large number of people would buy both, even if there is no connection between the two purchases
- Is there is a deviation from the expected co-occurrence of the two?
 - Look for correlations between items;
 - correlations can be positive
 - There are standard measures of correlation used in statistics

Other types of Association

- Sequence associations (or sequence correlations) in Time-series data
 - Stock prices on a sequence of days
 - Find associations among stock-market price sequences.
 - "Whenever bond rates go up, the stock prices go down within 2 days"

- Find deviations from what one would have expected on the basis of past temporal or sequential patterns
 - If sales of winter clothes go down in summer, it is not surprising

Clustering

- Finding clusters of points in the given data
 - Grouping points into k sets (for a given k) so that the average distance of points from the centroid of their assigned cluster is minimized
 - Grouping points so that the average distance between every pair of points in each cluster is minimized

- Scalable clustering algorithms can cluster very large data set (Birch clustering algorithm):
 - Data points are inserted into a multidimensional tree structure (based on R-trees)
 - Nearby points are clustered together in leaf nodes
 - summarized if there are more points than fit in memory
 - Result of first phase of clustering is to create a partially clustered data set that fits in memory
 - Standard clustering techniques can be executed on the in-memory data to get the final clustering

Clustering

- Example of clustering: Predict what new movies a person is likely to be interested in
 - The person's past preferences in movies
 - Other people with similar past preferences
 - The preferences of such people for new movies
- Find people with similar past preferences
- Create clusters of people based on their preferences for movies
 - The accuracy can be improved by previously clustering movies by their similarity
 - If people have seen similar movies they would be clustered together.
- Given a new user, find a cluster of users most similar to that user
 - On the basis of the user's preferences for movies already seen.
 - Predict movies in movie clusters that are popular with that user's cluster as likely to be interesting

Other forms of Data Mining

- Text mining applies data-mining techniques to textual documents.
 - Form clusters on pages that a user has visited
 - Helps users when they browse the history of their browsing to find pages they have visited earlier
- Data-visualization systems help users to examine large volumes of data, and to detect patterns visually.
 - Maps, charts ...
 - Example: if the user wants to find out whether production problems at plants are correlated to the locations of the plants
 - Problem locations can be encoded in a special color on a map.
 - User can quickly discover locations where problems are occurring
 - The user may form hypotheses about why problems are occurring in those locations, and verify the hypotheses quantitatively against the database.
 - Data-visualization systems do not automatically detect patterns
 - Provide support for users to detect patterns

Reference:

Database System Concepts by Silberschatz, Korth and Sudarshan (6th edition)

Chapter 20