

Question 1 solution

Students are encouraged to write the algorithm in pseudocode form using this code.

```
#include<iostream>
#include<string>
using namespace std;

int main()
{
    int matrix1[9][9] = { 'A', 'B', 'C', 'B', 'A', 'B', 'C', 'T', 'Y',
                          'F', 'G', 'H', 'J', 'K', 'L', 'H', 'G', 'V',
                          'D', 'V', 'T', 'B', 'Y', 'N', 'G', 'B', 'G',
                          'F', 'D', 'G', 'A', 'B', 'C', 'V', 'D', 'E',
                          'V', 'J', 'O', 'F', 'G', 'H', 'H', 'F', 'W',
                          'S', 'R', 'V', 'D', 'V', 'T', 'W', 'F', 'G',
                          'K', 'C', 'D', 'E', 'C', 'C', 'A', 'B', 'C',
                          'X', 'Q', 'R', 'T', 'U', 'O', 'F', 'G', 'H',
                          'T', 'Y', 'I', 'O', 'B', 'F', 'D', 'V', 'T' };

    int pattern[3][3] = {'A', 'B', 'C', 'F', 'G', 'H', 'D', 'V', 'T'};

    int patternsum = 0;
    for (int i = 0; i < 3; i++)
    {
        for (int j = 0; j < 3; j++)
        {
            patternsum += pattern[i][j];
        }
    }
    int num1 = 11;
    int num2 = 13;
    int mod1=patternsum % num1;
    int mod2=patternsum % num2;
    int col1=0,col2=0,col3 = 0;
    int hash1;
    int hash2;
    int temp = 0;
    int spurious = 0;
    int valid = 0;
    bool flag = false;

    for (int i = 0; i < 7; i++)
    {
        for (int j = 0; j < 7; j++)
        {
            if (j == 0)
            {
                col1 = col2 = col3 = 0;
                for (int k = i; k < i+3; k++)
                {
                    col1 += matrix1[k][0];
                    col2 += matrix1[k][1];
                    col3 += matrix1[k][2];
                }
                hash1 = (col1 + col2 + col3) % num1;
                hash2 = (col1 + col2 + col3) % num2;

            }
            else
            {
                temp = 0;
```

```

        col1 = col2;
        col2 = col3;
        col3 = matrix1[i][j + 2] + matrix1[i + 1][j + 2] +
matrix1[i + 2][j + 2];
        hash1 = (col1 + col2 + col3) % num1;
        hash2 = (col1 + col2 + col3) % num2;
    }
    if (hash1 == mod1 && hash2 == mod2)
    {
        flag = false;
        int x = 0;
        int counter = 0;
        for (int m = i; m < i + 3; m++)
        {
            int y = 0;
            for (int n = j; n < j + 3; n++)
            {
                if (matrix1[m][n] == pattern[x][y])
                {
                    counter++;
                }
                else
                {
                    cout << "spurious hit at: " << i
<< " " << j << endl;
                    spurious++;
                    flag = true;
                    break;
                }
                y++;
            }
            x++;
            if (flag == true)
            {
                break;
            }
        }
        if (counter == 9)
        {
            cout << "Pattern found at: " << i << " " << j
<< endl;
            valid++;
        }
    }
    else {}
}
cout << "Valid: " << valid << endl;
cout << "Spurious: " << spurious << endl;
}

```

Question 2: Heapsort

- a) Starting with the procedure MAX-HEAPIFY, write pseudocode for the procedure MIN-HEAPIFY (A, i, n), which performs the corresponding manipulation on a min-heap. How does the running time of MIN-HEAPIFY compare with that of MAX-HEAPIFY?

```

MIN-HEAPIFY(A, i, n)
L = LEFT(i)
R = RIGHT(i)
if L ≤ A.heap-size and A[L] < A[i]:
    smallest = L
else smallest = 1
if R ≤ A.heap-size and A[R] < A[smallest]:
    smallest = R
if smallest ≠ i:
    exchange A[i] with A[smallest]
    MIN-HEAPIFY(A, smallest, n)

```

There is no difference in running time between MAX-HEAPIFY and MIN-HEAPIFY.

- b) Considering the function of Build-Max-Heap, write pseudocode for the procedure BUILD-MIN-HEAP.

BUILD-MIN-HEAP(A)

```

n = length[A]
for i ← ⌊n/2⌋ downto 1
    do MIN-HEAPIFY(A, i, n)

```

- c) Comment on whether or not will there be any change in the procedure HEAP-SORT keeping in mind the modifications done in part (a) and 9(b). Give valid arguments.

HEAPSORT(A)

```

BUILD-MIN-HEAP(A)
for i ← length[A] downto 2
    do exchange A[1] ↔ A[i]
MIN-HEAPIFY(A, 1, i - 1)

```

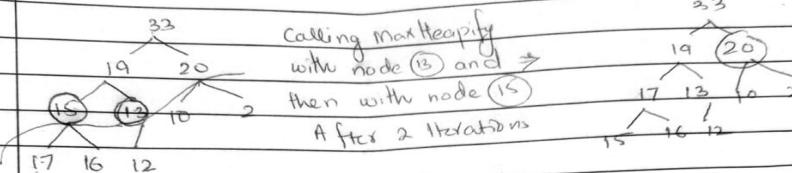
The sort will now produce data in descending order.

- d) Illustrate the operation of BUILD-MAX-HEAP and then HEAP-SORT on the array A= <33, 19, 20, 15, 13, 4, 2, 17, 16, 12> with root at index 1. Show complete steps with elements of array after each operation.

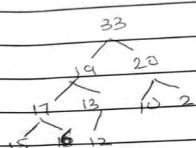
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$$A = 33, 18, 20, 18, 13, 10, 2, 17, 16, 12$$

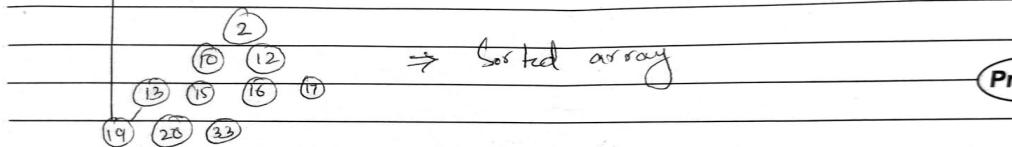
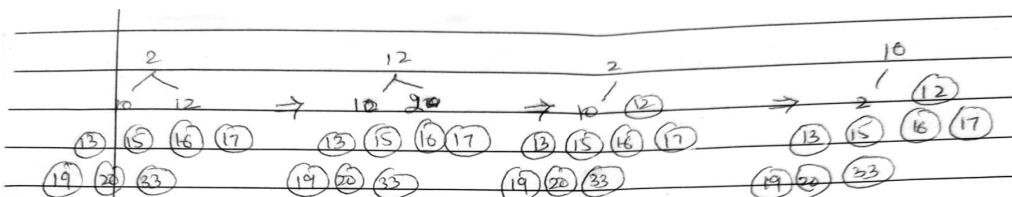
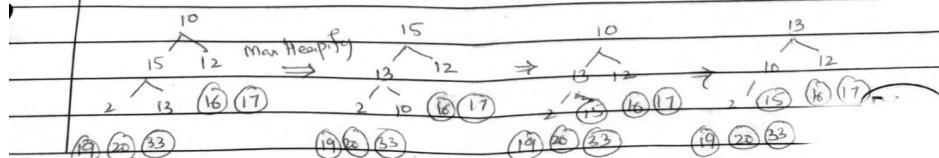
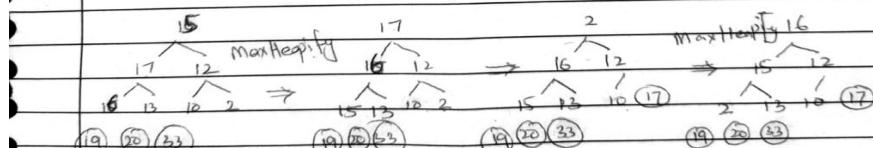
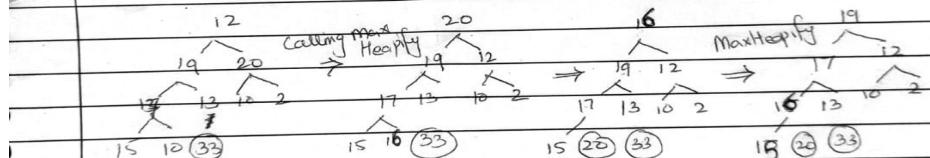
Build-MaxHeap working



Calling with node 60
=> then with 19



HEAP SORT WORKING :



Question 3: String Matching

- a) Suppose that all characters in the pattern P are different. Show how to accelerate NAIIVE-STRING-MATCHER to run in O(n) time on an n-character text T.

```
Accelerated_naive_algo(T,P,n,m)
BEGIN
    s ← 0
    WHILE s ≤ n-m DO
        FOR (j : 1 to m) DO
            IF P[j] ≠ T[s+1] THEN
                break
            END IF

            IF j = m THEN
                PRNT "Pattern occurs at shift : ", s-m
            END IF

            s ← s + 1
        END FOR
    END WHILE
END
```

- b) You are supposed to find out how many spurious hits does the Rabin-Karp matcher encounter in the text $T = 3141592653589793$ when looking for the pattern $P = 26$ working with modulo q calculated by using the given formula.

$i = 11$

$q = (\text{Your registration number}) \bmod i$

if $q = 0$ repeat calculation after incrementing i by 1 and keep repeating until a legal value is found.

For example

- i) if registration number is 23-2159 then $q = 2159 \bmod 11 = 3$.
- ii) If $q = \text{registration number} \bmod 11 = 0$ then do
 $q = \text{registration number} \bmod 12$ if again $q = 0$ then do
 $q = \text{registration number} \bmod 13$ until a valid value is found

Given, $P=26$

$T = 3141592653589793$

Here, we have taken $q=11$

$P \bmod Q = 26 \bmod 11 = 4$

Now find the exact match of $P \bmod Q$

Now if $S=0$, $31 \bmod 11 = 9 \neq 4$

If $S=1$, $14 \bmod 11 = 3 \neq 4$

If $S=2$, $41 \bmod 11 \neq 4$

$S=3$, $15 \bmod 11 = 4$ (Spurious Hit)

$S=4$, $59 \bmod 11 = 4$ (Spurious Hit)

$S=5$, $92 \bmod 11 = 4$ (Spurious Hit)

$S=6$, $26 \bmod 11 = 4$ (Valid Match)

... $65 \bmod 11 \neq 4$

... $53 \bmod 11 \neq 4$

... $35 \bmod 11 \neq 4$

... $58 \bmod 11 \neq 4$

... $89 \bmod 11 \neq 4$

... $97 \bmod 11 \neq 4$

... $79 \bmod 11 \neq 4$

... $93 \bmod 11 \neq 4$

Therefore, pattern P occurs at shift = 6

Hence, the number of times spurious hits the Rabin-Karp matcher encounter in the text T, when looking for the pattern P = 26 is 3.

Question # 4

Create a transition table for the pattern $P = AAB\$#C\$#\$\$$ by computing transition function for all states:

- Create Finite Automaton using the transition table, which you have formulated above.
- Show the trace of using your automaton for the text, $T = \$\$CAAB\$#C\$#\$\B

$P = AAB\$#C\$#\$\$$		
Sol		
$\delta(0, A) = 1$	$\delta(0, C) = 0$	$\delta(0, \$) = 0$
$\delta(0, B) = 0$	$\delta(0, \$) = 0$	
$\delta(1, AA) = 2$	$\delta(1, AC) = 0$	$\delta(1, A\$) = 0$
$\delta(1, AB) = 0$	$\delta(1, A\$) = 0$	
$\delta(2, AAA) = 1$	$\delta(2, AAC) = 0$	$\delta(2, AA\$) = 0$
$\delta(2, AAB) = 3$	$\delta(2, AA\$) = 0$	
$\delta(3, AA BA) = 1$	$\delta(3, AA BC) = 0$	$\delta(3, AAB\$) = 0$
$\delta(3, AA BB) = 0$	$\delta(3, AAB\$) = 4$	

$$\begin{array}{lll} S(4, AAB\$A) = 1 & S(4, AAB\$C) = 0 & S(4, AAB\$ \#) = 5 \\ S(4, AAB\$B) = 0 & S(4, AAB\$ \#C) = 0 & \end{array}$$

$$\begin{array}{ll} S(5, AAB\$ \#A) = 1 & S(5, AAB\$ \#\#\$\$) = 0 \\ S(5, AAB\$ \#B) = 0 & S(5, AAB\$ \#\#\#) = 0 \\ S(5, AAB\$ \#C) = 6 & \end{array}$$

$$\begin{array}{ll} S(6, AAB\$ \#CA) = 1 & S(6, AAB\$ \#C\$) = 7 \\ S(6, AAB\$ \#CB) = 0 & S(6, AAB\$ \#C\#) = 0 \\ S(6, AAB\$ \#CC) = 0 & \end{array}$$

$$\begin{array}{ll} S(7, AAB\$ \#C\$A) = 1 & S(7, AAB\$ \#C\$ \$\$) = 0 \\ S(7, AAB\$ \#C\$B) = 0 & S(7, AAB\$ \#C\$ \#) = 8 \\ S(7, AAB\$ \#C\$C) = 0 & \end{array}$$

$$\begin{array}{ll} S(8, AAB\$ \#C\$ \#A) = 1 & S(8, AAB\$ \#C\$ \#\#\$\$) = 9 \\ S(8, AAB\$ \#C\$ \#B) = 0 & S(8, AAB\$ \#C\$ \#\#\#) = 0 \\ S(8, AAB\$ \#C\$ \#C) = 0 & \end{array}$$

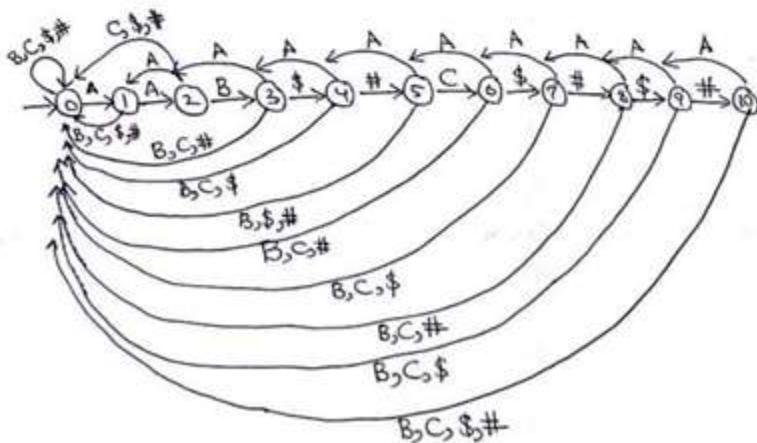
$$\begin{array}{ll} S(9, AAB\$ \#C\$ \#\#A) = 1 & S(9, AAB\$ \#C\$ \#\#\$\$\$) = 0 \\ S(9, AAB\$ \#C\$ \#\#B) = 0 & S(9, AAB\$ \#C\$ \#\#\#\#) = 10 \\ S(9, AAB\$ \#C\$ \#\#C) = 0 & \end{array}$$

$$\begin{array}{ll} S(10, AAB\$ \#C\$ \#\#\#A) = 1 & S(10, AAB\$ \#C\$ \#\#\#\$\$) = 0 \\ S(10, AAB\$ \#C\$ \#\#\#B) = 0 & S(10, AAB\$ \#C\$ \#\#\#\#\#) = 0 \\ S(10, AAB\$ \#C\$ \#\#\#C) = 0 & \end{array}$$

Stage	A	B	C	\$	#
0	1	0	0	0	0
1	2	0	0	0	0
2	1	3	0	0	0
3	1	0	0	4	0
4	1	0	0	0	5
5	1	0	6	0	0
6	1	0	0	7	0
7	1	0	0	0	8
8	1	0	0	9	0
9	1	0	0	0	10
10	1	0	0	0	0

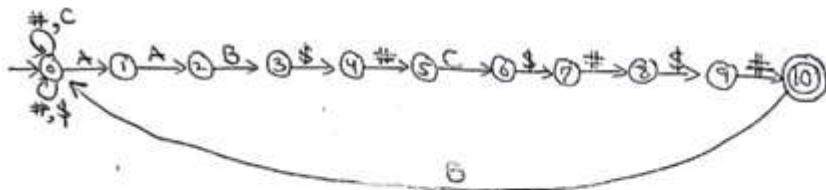
(a) $P = AAB\$ \# C\$ \# \$ \#$

→ Finite automata of given pattern.



(b) $T = \# \# \$ C A A B \$ \# C \$ \# \$ \# B$

Trace of the text through finite automata



The pattern is found in the given text, because it reaches the end stage ⑩ in the Finite automata.

Question # 5

- Compute the Prefix function of pattern, $P = ABCACBCAB$ using Knuth-Morris-Pratt algorithm for String matching.
- Dry run the Knuth-Morris-Pratt Algorithm on text, $T = ABABABCACBCABCAB$ using the pattern P defined in part a. Show all the steps.

(a) $P = ABCACBCAB$

$$\pi_{\text{prefix}} = \{0, 0, 0, 1, 0, 0, 0, 1, 2\}$$

- A
- AB
- ABC
- ABC A
- ABC AC
- ABC AC B
- ABC AC BC
- ABC AC BC A
- ABC AC BC AB

So, π_{prefix} is filled now, tells find text in the given text

$T = ABABCACBCABCAB$

i) ABCACBCAB

$\{0, 0, 0, 1, 0, 0, 0, 1, 2\}$ again start from 0 index {Pattern}

ii) ABCACBCAB

$\{0, 0, 0, 1, 0, 0, 0, 1, 2\}$ again start from 0 index {Pattern}

iii) ABCACBCAB Hence, pattern is found