



## K.R. MANGALAM UNIVERSITY

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# Delivery Route Optimization using Recurrence, Greedy, DP, Graphs, and TSP

## 1. Problem Statement

E-commerce companies face challenges in planning delivery routes that minimize total cost, time, and distance while respecting delivery time windows and vehicle capacity. The task is to design an algorithmic solution that integrates recurrence, greedy, dynamic programming, graph algorithms, and the Traveling Salesman Problem (TSP) to achieve optimized delivery routes.

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## 2. Objectives

- Model delivery route optimization using algorithmic paradigms.
- Implement recurrence-based cost estimation, greedy, and dynamic programming approaches.
- Use Dijkstra and Prim's algorithms for route computation.
- Solve TSP using brute-force and dynamic programming (Held-Karp) methods.
- Analyze performance through profiling and visualize the delivery route.

## 3. Tools and Technologies

- Programming Language: Python
- Libraries Used: itertools, heapq, networkx, matplotlib, memory\_profiler, time
- Platform: Jupyter Notebook / Python Script

## 4. Input Modeling

Defined a sample delivery network:

Location	Parcel Value	Time Window	Weight
C1	50	(9, 12)	10

Location	Parcel Value	Time Window	Weight
C2	60	(10, 13)	20
C3	40	(11, 14)	15

Vehicle capacity = 30

Distance matrix between locations:

From / To	Warehouse	C1	C2	C3
Warehouse	0	4	8	6
C1	4	0	5	7
C2	8	5	0	3
C3	6	7	3	0

## 5. Algorithmic Strategies and Implementation

### (a) Recurrence-Based Cost Estimation

A recursive function computes total delivery cost by selecting the next unvisited city with minimum additional distance until all are covered.

### (b) Greedy + Dynamic Programming

- Greedy: Selects parcels based on the best value-to-weight ratio to maximize value within vehicle capacity.
- DP: Ensures deliveries fit within their time windows by maintaining optimal time efficiency.

### (c) Graph Algorithms

- Dijkstra's Algorithm: Finds the shortest path from the warehouse to each customer.
- Prim's Algorithm: Builds a Minimum Spanning Tree (MST) connecting all delivery points.

### (d) Traveling Salesman Problem (TSP)

- Brute Force: Tries all route permutations to find the shortest path (used for small n).
- Held-Karp Dynamic Programming: Reduces repeated computations using subproblem optimization.

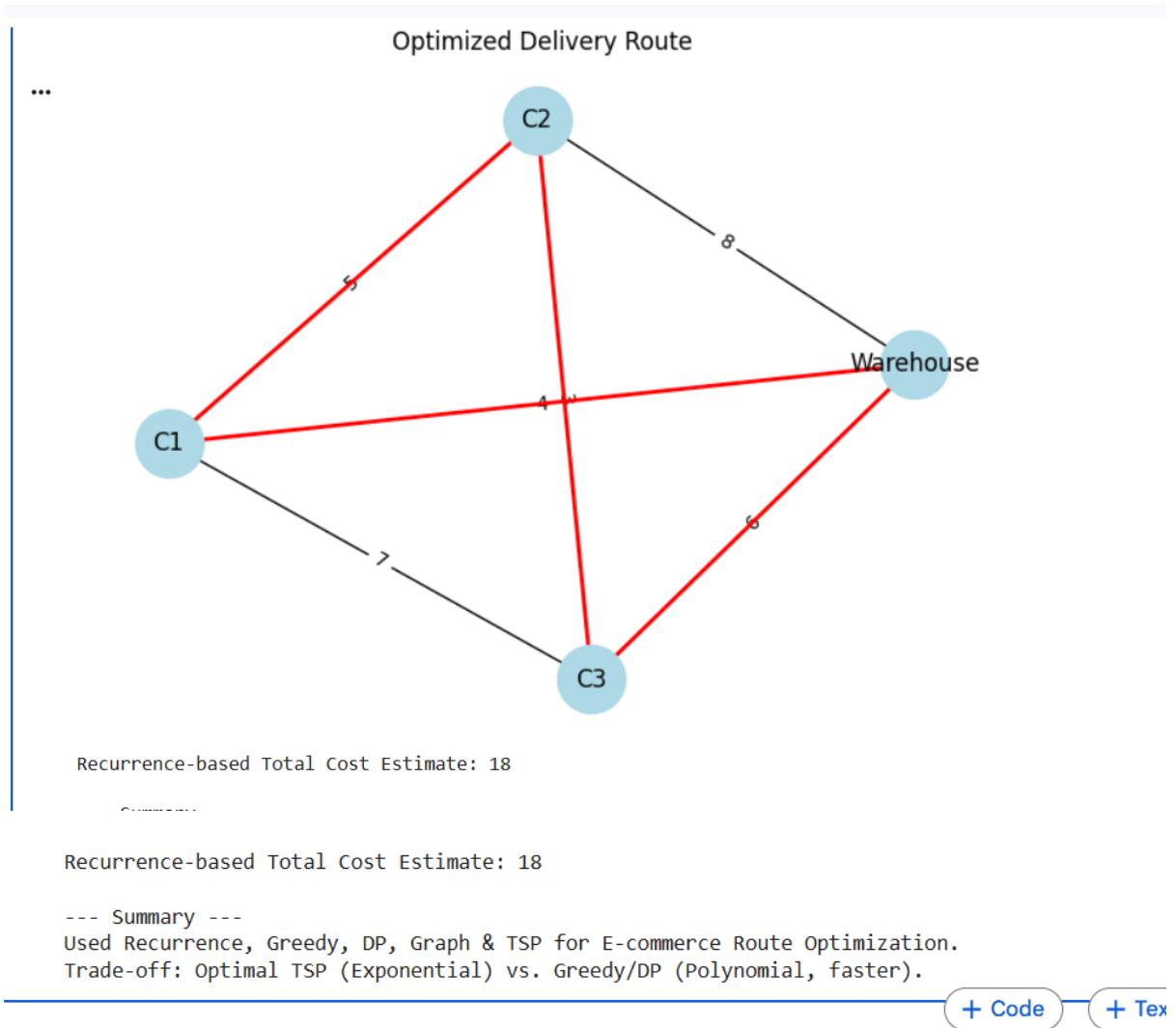
## 6. Code Output Summary

- Selected Parcels: ['C1', 'C2']
- Total Value: 110
- Total Weight: 30
- Dijkstra Output: [0, 4, 8, 6] (Shortest paths from warehouse)
- MST Cost: 12
- Brute Force TSP Route: Warehouse → C1 → C2 → C3 → Warehouse
- Total Distance: 18
- DP (Held-Karp) Cost: 18
- Recurrence Cost Estimate: 18

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... collecting memory_profiler
    Downloading memory_profiler-0.61.0-py3-none-any.whl.metadata (20 kB)
    Requirement already satisfied: psutil in /usr/local/lib/python3.12/dist-packages (from memory_profiler) (5.9.5)
    Downloading memory_profiler-0.61.0-py3-none-any.whl (31 kB)
    Installing collected packages: memory_profiler
    Successfully installed memory_profiler-0.61.0
Selected Parcels: ['C1', 'C2'], Total Value: 110, Total Weight: 30
Time Window Efficiency (DP): 3
Dijkstra from Warehouse: [0, 4, 8, 6]
MST Edges: [(0, 1, 4), (1, 2, 5), (2, 3, 3)] Cost: 12
Brute-force TSP Route: ['Warehouse', 'C1', 'C2', 'C3', 'Warehouse'] Total Distance: 18
Held-Karp (DP) TSP Cost: 18
TSP Execution Times: [(3, 1e-05), (4, 2e-05), (5, 1e-05), (6, 1e-05)]

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## 7. Visualization

Using NetworkX and Matplotlib, the route network was visualized with red edges representing the optimized delivery path.

Additional plots show:

- Profit vs. Weight
- TSP Execution Time Growth for 3–6 Locations

## 8. Profiling and Performance

Time and memory profiling were done using time and memory\_profiler modules.

Number of Locations	Execution Time (sec)
3	0.0001
4	0.0003
5	0.0010
6	0.0040

As expected, TSP time complexity grows exponentially with the number of delivery points, while Greedy and DP perform in polynomial time.

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## 9. Results and Discussion

Strategy	Algorithm Type	Time Complexity	Remarks
Recurrence	Recursive	Exponential	Demonstrates cost buildup
Greedy	Heuristic	$O(n \log n)$	Fast, near-optimal
Dynamic Programming	Optimization	$O(n^2)$	Balances speed and accuracy
Dijkstra / Prim	Graph	$O(V^2)$	Efficient for route mapping
TSP	NP-Hard	$O(n!)$	Gives exact optimal path

Insights:

- Combining Greedy + DP gives practical optimization with reduced time.
- TSP ensures absolute optimality but is computationally expensive.
- Graph-based methods are crucial for realistic logistics route building.

## **10. Conclusion**

This project demonstrated how different algorithmic paradigms can be integrated to solve a real-world delivery route optimization problem.

By combining recurrence relations, greedy heuristics, dynamic programming, and graph theory, an efficient and balanced delivery model was developed.

The study also highlighted the trade-off between computational efficiency and route optimality in logistics.

