

# Database Management System.

- ① Need for normalization.
- ② Normal forms.
- ③ Higher normal form  $\leftrightarrow$  More joins.
- ④ Functional Dependency.

↳ fully  
↳ Partially  
↳ Transitive

Ques)

R	A	B	C
1	2	3	
4	2	3	
5	3	3	

which of the following dependency  
can you infer does not hold.  
over R?

(a)  $A \rightarrow B$  (b)  $B \rightarrow C$

~~(c)  $BC \rightarrow A$~~  (d)  $AC \rightarrow B$

Ques) Consider the following relation instance

X	Y	Z
1	4	3
1	5	3
4	6	3
3	2	2

which of the following FD are  
satisfied.

(a)  $XY \rightarrow Z, Z \rightarrow Y$

~~(b)  $XZ \rightarrow X, Y \rightarrow Z$~~

(c)  $XY \rightarrow Z, Z \rightarrow X$

(d)  $XZ \rightarrow Y, Y \rightarrow Z$

⑤ Trivial F.D

⑥ Non-trivial F.D

↳ at least one attribute in R.H.S that  
is not part of L.H.S.

$AB \rightarrow BC$

⑦ Closure of set of F.D. ( $F^+$ )

→ Set of all f.d.'s logically implied by  $F$  is the closure of  $F$ .

⑧ Inference Rules / closure Properties.

→ 8.1 Reflexivity:

if  $X \supseteq Y$  then  $X \rightarrow Y$ .



eg:  $AB \rightarrow A$

→ 8.2 Augmentation:

if  $X \rightarrow Y$ , then

$XZ \rightarrow YZ$

→ 8.3 Transitivity:

if  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then

$X \rightarrow Z$ .

→ 8.4 Union.

if  $X \rightarrow Y$  and  $X \rightarrow Z$ , then

$X \rightarrow YZ$

→ 8.5 Decomposition

if  $X \rightarrow YZ$  then

$X \rightarrow Y$  and

$X \rightarrow Z$ .

Armstrong's

Axioms.

## ⑨ Closure of Attribute Sets ( $X^+$ )

Ques)  $R(ABCDEF)$

$\{AB \rightarrow C, BC \rightarrow AD, D \rightarrow E, CE \rightarrow B\}$

$\left. \begin{array}{l} AB^+ \\ BC^+ \\ D^+ \\ CE^+ \end{array} \right\} ?$

Ques) FD  $\{A \rightarrow B, B \rightarrow C, AB \rightarrow D\}$

compute  $A^+$ .

## ⑩ Applications of attribute closure

↳ 10.1 Find additional F.D's

↳ 10.2 Find keys of a relation

Ques)  $R(ABCDE)$

$\{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$

Find candidate keys  
of R.

$[A, BC, CD, E]$  Ans.

Ques)  $R(ABCD)$

$F = \{A \rightarrow B, B \rightarrow C\}$

Find candidate key.

$[AD]$  Ans.

Ques)  $R(AB CDE)$

$\{AB \rightarrow C, CD \rightarrow E, DE \rightarrow B\}$

Is 'AB' a Candidate Key? If not, is 'ABD'?

Explain.

Ques)  $R(ABCD)$

$\{BC \rightarrow A, AD \rightarrow B, CD \rightarrow B, AC \rightarrow D\}$

Find all Candidate Keys of R.

[BC, CD, AC]

① Canonical Cover

→ 11.1 Equivalent ( $E^+ = F^+$ )

F.D in F from E



every F.D in E can be inferred from F.

→ 11.2 Redundant F.D

→ 11.3 Minimal Cover

→ Single attribute on R.H.S

→ Non Redundant F.D's only

→ 11.4 Canonical Cover.

→ No extraneous attribute

$\{A \rightarrow C, \underline{AB} \rightarrow C\}$

B is extraneous

Ques)  $R(ABC)$

$$F = \{ A \rightarrow BC, B \rightarrow C, A \rightarrow B, AB \rightarrow C \}$$

Compute Canonical Cover for F.

$$\left[ \begin{array}{l} A \rightarrow B \\ B \rightarrow C \end{array} \right] \text{ Ans.}$$

$$\left[ \begin{array}{l} A \rightarrow BC \\ A \rightarrow B \end{array} \right] \xrightarrow{B \rightarrow C} \left[ \begin{array}{l} A \rightarrow BC \\ AB \rightarrow C \end{array} \right] \xrightarrow{B \rightarrow C} \left[ \begin{array}{l} A \rightarrow BC \\ AB \rightarrow C \\ B \rightarrow C \end{array} \right]$$

Note: Canonical Cover might not be unique.

(12) Decomposition

↳ 12.1 Loss-less join decomposition

$(R_1 \cap R_2) \rightarrow$  Superkey of either  $R_1$  or  $R_2$ .

↳ 12.2 Lossy

Ques)  $R(ABC)$   $F\{A \rightarrow B\}$   $\left. \begin{array}{l} \nearrow R_1(AB) \\ \searrow R_2(BC) \end{array} \right\}$  lossless/lossy.

$R_1\{A \rightarrow B\}$   $R_2\{\}$ .

Common attribute (B)  $\rightarrow$  Not Superkey in either  $R_1$  or  $R_2$ .

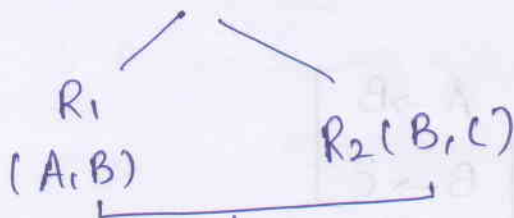
So lossy.



Ques)  $R(A, B, C)$  decomposition of  $R$  into  $\{F = A \rightarrow B\}$   $R_1(A, B)$  and  $R_2(A, C)$  lossless or lossy?

Lossless Common attribute 'A' is a Key in  $R_1$ .

Ques)  $R(A, B, C)$   $\{A \rightarrow B\}$  } lossless or lossy?



Common attribute 'B' = Not a Key in  $R_1$  or  $R_2$ .

Lossy

Ques)  $R(A, B, C, D)$   $\{A \rightarrow B, A \rightarrow C, C \rightarrow D\}$  } lossless or lossy?

$R_1(A, B, C)$   $\{A \rightarrow B, A \rightarrow C\}$   $R_2(C, D)$   $\{C \rightarrow D\}$  } Dependency Preserving?

Common attribute is 'C' = Key in  $R_2$ , hence lossless.

$(F^+) = (A \rightarrow B, A \rightarrow C, C \rightarrow D)$

$(F_1 \cup F_2)^+ = (F^+)$

Hence dependency Preserving.

## ⑫ Dependency Preserving Decomposition

$$F^+ = (F_1 \cup F_2)^+$$

Ques)  $R(A, B, C, D)$

$$F \{ A \rightarrow B, A \rightarrow C, A \rightarrow D \}$$

$R_1(ABD)$

$R_2(BC)$

$$\{ A \rightarrow B, A \rightarrow D \}$$

$$\{ \}$$

Lossless or Lossy?

Dependency Preserving?

Common attribute =  $\textcircled{B}$  not a Key in  $R_1$  or  $R_2$ , so  
lossy.

$$(F_1^+) = \{ A \rightarrow B, A \rightarrow D, A \rightarrow BD \}$$

$$(F_2^+) = \{ \}$$

Cannot be implied, hence  
not dependency Preserving.

$$(F^+) = A \rightarrow B, \textcircled{A \rightarrow C}, A \rightarrow D, A \rightarrow BC, A \rightarrow CD, A \rightarrow BD, A \rightarrow BCD, \dots$$

Ques)  $R(A, B, C, D)$

$$F \{ A \rightarrow B, A \rightarrow C, C \rightarrow D \}$$

$R_1(ABC)$  and  $R_2(CD)$

Lossless or Lossy?

	A	B	C	D
$R_1$	$a_A$	$a_B$	$a_C$	$p_{1D} \rightarrow d_D$
$R_2$	$p_{2A}$	$p_{2B}$	$a_C$	$a_D$

$C \rightarrow D$

Lossless.

Ques)  $R(ABCDE)$

$F \{ AB \rightarrow CD, A \rightarrow E, C \rightarrow D \}$

$R_1(ABC), R_2(BCD), R_3(CDE)$

Lossless or  
lossy decomposition?

Ans:- Lossy.

Normal Forms

Ques) Find minimal cover for the following  
Set of F.D's.

$PQ \rightarrow R$

$PS \rightarrow Q$

$QS \rightarrow P$

$PR \rightarrow Q$

$S \rightarrow R$

$\{ P \rightarrow R, P \rightarrow Q, S \rightarrow R \}$

Ques)  $F = \{ A \rightarrow C, AC \rightarrow D, E \rightarrow AD, E \rightarrow H \}$   
 $G = \{ A \rightarrow DC, E \rightarrow A \}$

Both FD's are  
equivalent or  
not.

Qu Compute FD's closure of G w.r.t F and  
vice-versa.

Equivalent

Ques)  $R(ABCDE)$  Find closure of FD's  
 $A \rightarrow BC$   
 $CD \rightarrow E$   
 $B \rightarrow D$   
 $E \rightarrow A$

Check whether  $E \rightarrow D$  holds or  
not.

compute  $E^+$

Yes



Ques)  $R(AB C D E F)$

$\{ AB \rightarrow C, C \rightarrow A, BC \rightarrow D, AC \rightarrow B, BE \rightarrow C, CE \rightarrow FA, CF \rightarrow BD, D \rightarrow EF \}$  ] Find closure of FD's.

Ques)  $R(AB C D E F G)$

$F \{ A \rightarrow B, BC \rightarrow DE, AEF \rightarrow G \}$  ] Find  $[AC]^+$

### Normalization

1NF: A relation is in 1NF if every field contains only atomic values i.e. the attribute of any tuple must be a single value or null value.

<u>Emp</u>	<u>eno</u>	<u>ename</u>	<u>Contact</u>		<u>eno</u>	<u>ename</u>	<u>Contact</u>
	1	A	{98, 99}	$\Rightarrow$	1	A	98
					1	A	99
	2	B	{99, 100}		2	B	99
					2	B	100

2NF: Based on the concept of full functional dependency (FFD).

→ Relation is in 2NF, if every non-prime (key) attribute of R is fully functional dependent on the key of R.

or

No Non-prime Attribute should be determined by the part of candidate key.

or

No Partial F.D.

Ques)  $R(ABCD)$

$F: \{ AB \rightarrow C, B \rightarrow D \}$

CK: AB, Not in 2NF

$B \rightarrow D$  (Partial F.D)

Find N.F.

Ques)  $R(ABC)$

$F: \{ A \rightarrow B, B \rightarrow C \}$

CK: A (R) is in 2NF.

Find N-F

Ques)  $R(ABCD)$

$F: \{ AB \rightarrow C, A \rightarrow D \}$

decompose 'R' into

2NF

C.K = AB.

$R_1(AD)$

2NF

$R_2(ABC)$

Note: Decomposition requires the closure of violating dependencies into separate relation and remaining attributes and key attributes of decomposed relations forms another rel<sup>n</sup>.

Ques)  $R(ABCDE)$

$F: \{ AB \rightarrow C, A \rightarrow D, B \rightarrow E \}$

decompose 'R'

into 2NF

$R_1(AD), R_2(BE), R_3(ABC)$

3NF: A relation is in 3NF if F.D ' $X \rightarrow Y$ ' satisfy any one of the following cond<sup>n</sup>:

i)  $X \rightarrow Y$  is a trivial F.D, i.e.  $Y \supseteq X$ .

ii) if  $X \rightarrow Y$ , then  $X$  is a Superkey.

iii) if  $X \rightarrow Y$ , then  $(Y-X)$  is a prime attribute.

or

↳ No Transitive dependencies.

Ques)  $R(ABC)$   
 $F \{ A \rightarrow B, B \rightarrow C \}$  } ' $R$ ' is in which Normal form.

' $R$ ' is in 2NF but not in 3NF.

Ques)  $R(ABCDE)$   
 $F \{ AB \rightarrow C, B \rightarrow D, D \rightarrow E \}$  } Decompose the relation upto 3NF.

$R_1 \{ABC\}, R_2 \{DE\}, R_3 \{BD\}$ .

Ques)  $R(ABC)$   
 $F: \{ AB \rightarrow C, C \rightarrow A \}$  } ' $R$ ' is in which Normal form.

3NF, 2NF, 1NF.

BCNF: A relation is in BCNF if at least one of the cond<sup>n</sup> hold:

i)  $X \rightarrow Y$  is a trivial F.D

ii)  $X \rightarrow Y$ ,  $X$  is a Superkey.

Ques)  $R(ABC)$

$F: \{ AB \rightarrow C, C \rightarrow A \}$

} Relation 'R' is in  
BCNF or 3NF

3NF only.

Ques)  $R(ABCDEFGHIJ)$

$F: \{ AB \rightarrow C, A \rightarrow DE, B \rightarrow F, F \rightarrow GH, D \rightarrow IJ \}$

Decompose R into 2NF and 3NF relations.

Ques)  $Book(Book\_title, Authorname, Book\_type, listprice, author\_affil, publisher)$

F.D {  $Book\_title \rightarrow Publisher, Book\_type$   
 $Book\_type \rightarrow listprice$   
 $Authorname \rightarrow Author\_affil$  }

Find N.F of the relation and decompose it  
upto 3NF.

Ques)  $Car\_Sale(Car\#, Salesman\#, Date\ sold, Comm\%, discount)$

F.D {  $Date\ sold \rightarrow discount$   
 $Salesman\# \rightarrow Comm\%$   
 $Car\# \rightarrow Date\ sold$  }

} Find key of relation and  
Normalize it till BCNF.

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