

## ECE 418 Lab 11

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In this lab, we evaluate lossy image compression methods which belong to transform coding. The transform coding method takes advantages of energy compaction properties of Transform and finds the most optimal number of coefficients to keep so that the compressed image doesn't lose information. We implement Discrete Cosine Transform and Karhunen-Loeve Transform and examine the properties of the JPEG image compression.

Upon running the code, we obtained the following images:



*Figure 1: DCT - 8x8, Coefficients: 5*



*Figure 2: DCT - 8x8, Coefficient:10*



Figure 3: DCT - 16x16, Coefficients: 10



Figure 4: DCT - 16x16, Coefficients: 40



Figure 5: KLT - 8x8. Coefficients: 5



Figure 6: KLT - 8x8, Coefficient:10

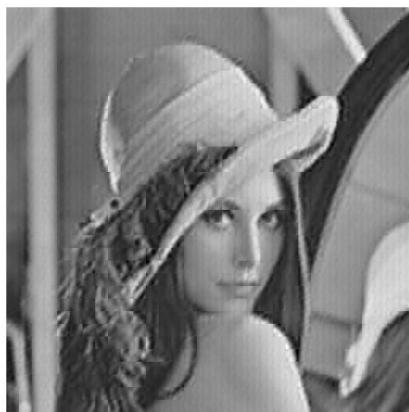


Figure 7: KLT - 16x16, Coefficient:10



Figure 8: KLT - 16x16, Coefficients: 40

## Q1. Plots of Energy Matrix

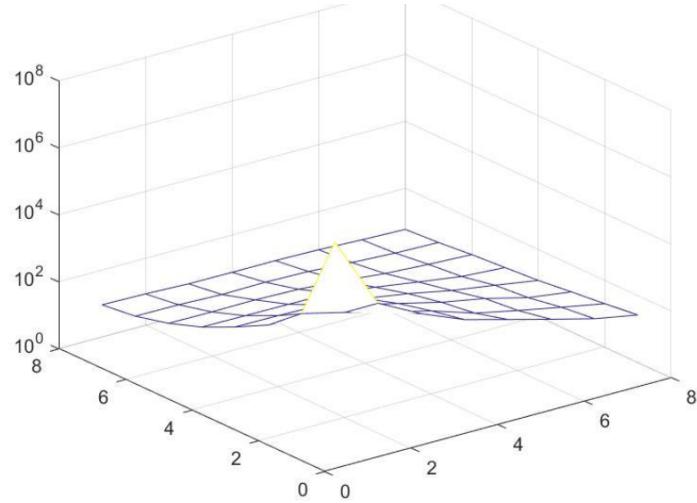


Figure 9: Energy Matrix Block-size 8x8, DCT

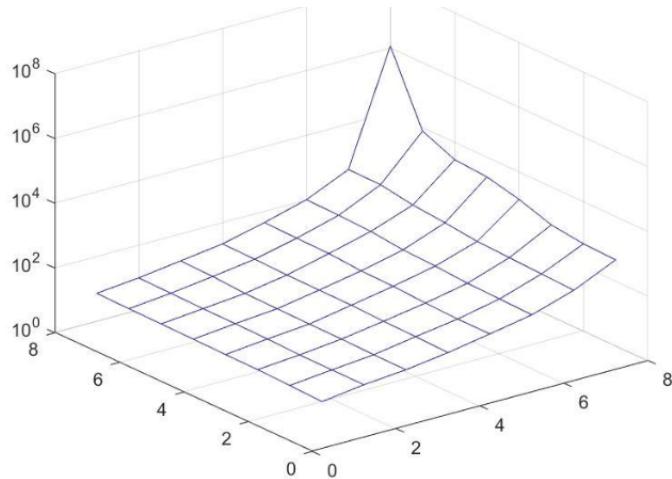


Figure 10: Energy Matrix Block-size 8x8, KLT

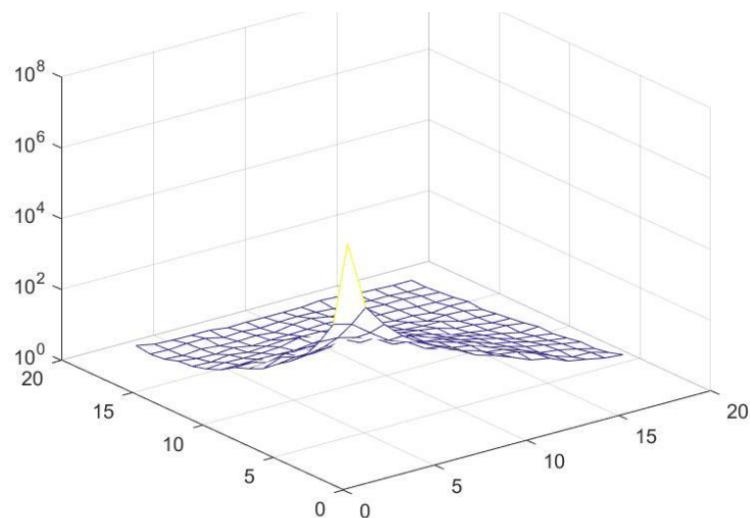


Figure 11: Energy Matrix Block-size 16x16, DCT

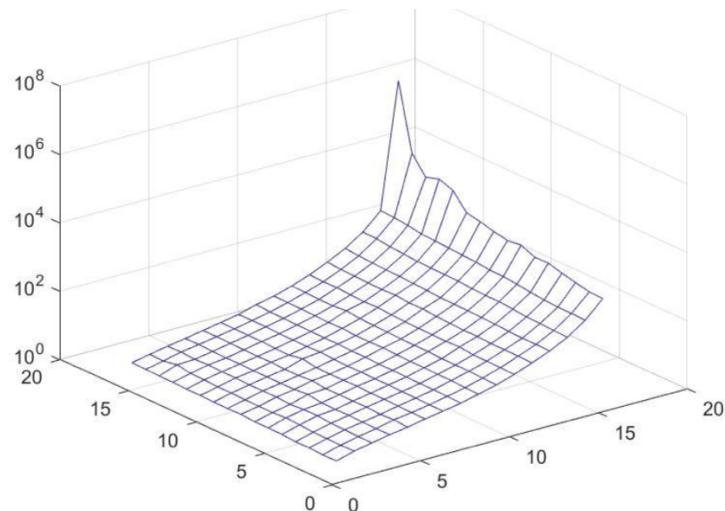


Figure 12: Energy Matrix Block-size 16x16, KLT

DCT:

- i. 8x8, 10 coefficients kept
  - a. Average Block Energy

1113526.26	7369.495	1600.408	472.6202	212.2493	95.93018	44.43204	25.64177
2845.291889	1366.788	619.1983	300.9496	114.7786	61.09009	34.09324	19.33793
447.4468234	458.6184	354.6095	173.9751	84.28035	48.7527	22.99782	15.20656
136.3994807	133.3624	123.5172	86.11809	53.05185	29.35361	18.75848	11.62838
47.24636078	46.06798	44.77216	43.36764	28.81882	18.46549	11.93056	9.827922
21.34602531	20.81486	21.23125	19.53493	15.60878	11.43845	9.589914	8.333294
12.14941378	11.84354	10.66156	11.08766	10.32013	8.49496	7.257209	6.675492
9.229664694	8.716275	7.755715	7.597281	7.562072	7.136904	6.278756	5.739915

b. Block Coefficient Mask

1	1	1	1	0	0	0	0
1	1	1	0	0	0	0	0
1	1	1	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

c. MSE per pixel: 36.92

ii. 8x8, 5 coefficients kept

a. Average Block Energy

1113526.26	7369.495	1600.408	472.6202	212.2493	95.93018	44.43204	25.64177
2845.291889	1366.788	619.1983	300.9496	114.7786	61.09009	34.09324	19.33793
447.4468234	458.6184	354.6095	173.9751	84.28035	48.7527	22.99782	15.20656
136.3994807	133.3624	123.5172	86.11809	53.05185	29.35361	18.75848	11.62838
47.24636078	46.06798	44.77216	43.36764	28.81882	18.46549	11.93056	9.827922
21.34602531	20.81486	21.23125	19.53493	15.60878	11.43845	9.589914	8.333294
12.14941378	11.84354	10.66156	11.08766	10.32013	8.49496	7.257209	6.675492
9.229664694	8.716275	7.755715	7.597281	7.562072	7.136904	6.278756	5.739915

b. Block Coefficient Mask

1	1	1	0	0	0	0	0
1	1	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

c. MSE per pixel: 73.67

iii. 16x16, 40 coefficients kept

a. Average Block Energy

4392481	4936.74	11955.11	4077.505	1892.138	1036.197	612.6555	319.2826	226.6707	144.3699	88.40918	71.27611	43.15714	34.82272	27.50977	24.65898
15099.27	10924.3	4356.448	1995.914	1310.457	615.3602	439.0047	281.5795	200.0729	116.8899	97.8373	64.2986	39.12767	26.70002	26.02746	18.53388
3104.02	2964.131	2190.862	1520.635	735.3763	584.9146	378.1431	204.5901	125.1485	86.04491	57.23078	52.0329	31.88623	27.42288	21.26908	15.75085
836.3508	1044.851	1279.093	744.259	733.6491	460.8319	251.3699	170.8372	106.7711	87.82005	56.6841	43.5182	31.00032	24.9745	19.48683	15.9719
388.7273	473.3987	480.1467	512.3895	418.6958	343.176	226.3727	147.0129	100.2263	70.92014	52.23671	34.00944	27.2799	19.936	15.98933	13.54172
206.8159	237.9029	220.7121	254.8958	282.0208	176.1841	143.0812	107.7534	68.17244	57.5767	39.84725	30.6647	22.79646	16.02337	14.00933	11.79908
101.6062	154.1746	115.423	141.1013	129.8546	136.1411	88.8316	66.32727	64.15353	41.71907	30.67936	24.68797	18.29884	14.8153	11.52714	12.18307
66.32012	71.76375	93.54336	76.19965	81.66236	67.66155	62.1832	63.00507	39.39582	33.44795	24.52823	16.9069	14.52143	12.10482	11.91042	10.13436
47.43298	47.66199	38.73416	46.33573	48.36397	47.53638	52.61275	41.13357	36.66602	24.77069	20.73646	17.30207	12.30504	11.26728	9.270624	8.946931
26.69206	26.58424	27.59643	26.67322	25.37542	29.12826	33.55545	27.65029	23.05822	18.21636	14.3248	13.12901	12.82623	9.344511	8.619672	7.932869
18.50789	20.2182	19.38841	19.69557	21.00017	27.23799	18.72978	19.86903	16.35357	13.32703	11.49989	10.92042	8.558529	9.150146	8.666635	6.856937
14.37901	13.69518	15.82048	13.48313	14.5229	15.57437	14.48063	14.37639	12.56665	10.56793	9.078033	7.904033	7.956674	6.899917	7.813554	7.583004
13.16958	11.3224	10.82248	11.87467	9.72323	10.30125	10.45291	10.89348	11.40377	11.00344	8.32724	7.708645	7.526664	6.806164	6.520124	6.438296
9.876284	9.005196	9.934769	8.862251	8.656709	9.053695	8.046934	9.744921	10.51647	8.501338	7.826323	7.494233	7.064021	7.261719	6.42101	5.916919
9.008136	8.561001	9.346854	9.46984	7.267325	7.796683	7.000182	7.542821	7.810984	7.42938	6.758444	6.56169	5.983596	5.975297	5.48827	5.406686
10.22306	8.112308	7.650061	7.544255	7.618819	6.477731	6.761943	6.650168	6.645195	6.690302	7.467806	7.007751	6.090077	5.844769	5.518064	5.562819

b. Block Coefficient Mask

c. MSE per pixel: 30.22

iv. 16x16, 10 coefficients kept

a. Average Block Energy

4392481	49936.74	11955.11	4077.505	1892.138	1036.197	612.6555	319.2826	226.6707	144.3699	88.40918	71.27611	43.15714	34.82272	27.50977	24.65898	
15099.27	10924.3	4536.444	1995.914	1310.457	615.3602	349.0047	281.5795	200.0729	116.8899	97.8373	64.2986	39.27667	26.70000	26.02746	18.55388	
3104.02	2964.131	1209.863	150.635	375.363	584.914	378.343	204.5011	125.1485	86.04091	75.23078	52.03298	31.88623	27.42284	21.26908	15.75085	
863.3508	1044.851	1279.093	744.256	733.6491	460.8319	251.3699	170.8372	106.7716	87.82005	56.6841	43.51826	31.00033	24.9745	19.48863	15.9719	
388.773	472.3987	480.1467	513.3895	481.6958	343.176	226.3732	147.0129	100.2263	70.92014	52.26371	34.00944	27.2799	19.936	15.98933	13.54172	
206.8159	237.9029	220.7121	254.8958	282.0208	176.1841	143.0812	107.7534	68.1724	57.5767	39.84725	30.6647	22.79646	16.02337	14.00933	11.79908	
101.6062	154.1746	115.423	141.1013	129.8546	136.1411	88.18619	66.32777	64.15353	41.71907	30.6796	24.68797	18.2984	14.8153	11.52174	12.18307	
66.32012	71.76375	93.54336	79.9658	19.16632	66.62366	47.61555	18.62384	16.03507	39.39582	33.44795	24.52823	16.09066	14.52143	12.10482	11.91042	10.14346
47.43238	47.66199	38.73416	46.33573	48.36397	47.53638	52.61275	41.13357	36.66002	24.77069	20.7646	17.30207	12.30504	11.26728	9.702624	8.946931	
6.69206	26.58424	27.59643	26.67322	25.37542	29.19228	33.25555	27.65029	23.05822	18.21636	14.23448	13.12901	12.82623	9.344511	8.16972	7.932869	
18.50789	20.2182	19.38841	19.69557	20.0017	23.27399	18.72978	19.86903	16.35357	13.32703	11.49889	10.92042	8.558259	9.15014	8.666635	8.659567	
13.37901	13.69518	15.82048	13.48313	14.5229	15.57437	14.48063	14.37639	12.55665	10.5679	10.80733	9.704033	7.95669	6.899917	7.18354	5.783004	
13.16958	11.3224	10.82248	11.87467	7.92332	10.3015	10.42554	10.89348	11.40377	11.00344	8.32724	7.08645	5.726664	6.80168	5.620124	4.638296	
9.87628	0.50196	9.93476	8.8862251	8.856709	9.053695	8.046934	7.944921	10.15647	8.501338	7.826323	7.494232	7.064021	7.261719	6.41201	5.916919	
9.008136	8.561001	9.346854	9.46984	7.627352	7.796683	7.000182	7.54821	7.810988	7.42938	7.568444	6.516994	5.98359	5.97597	5.48827	5.406686	
10.22306	8.112308	7.605061	5.744555	2.81689	4.17771	6.76194	6.550368	5.645198	6.659032	7.467608	7.00751	6.009077	5.84476	5.518064	5.562819	

b. Block Coefficient Mask

c. MSE per pixel: 111.03

KLT:

i. 8x8, 10 coefficients kept:

a. Average Block Energy

5.351883	7.930937	10.22555	15.36457	25.93932	44.80842	114.2088	443.5506
5.885588	7.92351	10.35506	16.73876	26.01835	48.58515	127.9724	483.8919
6.326544	8.033769	11.01865	17.34049	28.21662	51.41986	141.3714	648.2377
6.427366	8.660772	11.16527	18.98026	32.498	60.86006	156.5932	1383.661
6.692372	8.957912	11.54252	19.3611	33.83434	67.06095	205.4076	2379.973
6.905103	9.064157	11.98473	19.74052	40.47456	86.88672	252.9087	2822.254
7.063862	9.479951	13.86675	21.11186	41.91792	95.21659	373.3221	7520.321
7.383065	9.829814	14.6635	21.85588	44.48344	100.6153	383.3447	1112790

b. Block Coefficient Matrix

0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	1
0	0	0	0	0	0	1	1
0	0	0	0	0	0	1	1

c. MSE per pixel: 34.29

ii. 8x8, 5 coefficients kept

a. Average Block Energy

5.351883	7.930937	10.22555	15.36457	25.93932	44.80842	114.2088	443.5506
5.885588	7.92351	10.35506	16.73876	26.01835	48.58515	127.9724	483.8919
6.326544	8.033769	11.01865	17.34049	28.21662	51.41986	141.3714	648.2377
6.427366	8.660772	11.16527	18.98026	32.498	60.86006	156.5932	1383.661
6.692372	8.957912	11.54252	19.3611	33.83434	67.06095	205.4076	2379.973
6.905103	9.064157	11.98473	19.74052	40.47456	86.88672	252.9087	2822.254
7.063862	9.479951	13.86675	21.11186	41.91792	95.21659	373.3221	7520.321
7.383065	9.829814	14.6635	21.85588	44.48344	100.6153	383.3447	1112790

b. Block Coefficient Matrix

0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	1

c. MSE per pixel: 70.73

iii. 16x16, 40 coefficients kept

a. Average Block Energy

2.369953	3.330917	4.190329	5.272102	6.285074	7.700502	9.771789	12.01169	16.07049	21.39375	31.37526	50.22407	81.38747	148.0723	336.6625	1078.561
3.233576	3.258263	4.190301	5.193961	6.843746	8.019167	9.78912	12.47162	16.11246	21.44353	31.19362	52.18233	82.73848	154.0184	349.8959	1078.561
2.464427	3.311163	4.35079	5.277805	6.442939	8.125175	10.01929	12.77011	17.24256	23.4297	33.65978	52.75084	83.2223	161.4805	352.7122	1326.202
4.230561	3.361487	4.420327	5.511939	6.878993	8.411145	10.28121	12.78018	17.12574	23.68536	34.00095	52.04022	85.98721	164.1955	372.8812	1611.109
6.264678	5.359541	8.458384	5.354226	6.755071	8.538274	10.49844	12.94955	17.22732	23.76548	37.37941	56.54411	91.26381	189.0319	405.2023	1010.816
6.550481	8.180372	8.039549	5.451827	6.846963	7.853415	10.43553	13.46219	17.90354	25.01998	36.25061	54.90406	93.86685	197.4762	462.7796	2066.699
6.459179	5.547336	4.447454	6.333937	7.637682	8.612563	10.78504	13.4715	18.7636	25.02211	36.3742	57.52008	97.67374	194.7374	510.0237	1023.852
8.719098	5.362888	4.767493	5.806558	7.53895	8.486599	10.7168	14.16106	19.23741	25.30775	37.46025	60.05066	99.3309	204.5193	519.3437	7079.517
7.769809	5.392576	4.767447	5.739499	7.019576	7.878146	11.1189	14.01586	18.73567	23.26060	38.00233	65.56791	100.334	222.5532	574.9593	3295.725
7.299466	3.742006	4.674233	5.80817	7.0464	10.44122	11.82797	14.71859	18.82149	26.92142	39.66801	64.54438	107.6545	225.0982	604.4366	1451.314
8.884659	6.388501	4.887327	5.767117	5.758063	8.709721	11.31072	14.55557	20.098	27.99197	43.04267	70.88000	124.581	230.700	624.0932	998.474
2.905679	3.900327	4.900709	6.045012	7.279824	8.970615	11.44229	14.79919	19.63581	31.28725	41.36983	67.85254	119.4715	236.255	675.2414	14625.96
2.982081	3.979957	5.162129	5.945883	7.453368	9.414494	11.49229	15.0268	20.0348	28.58731	43.25427	69.49195	121.561	255.1312	708.216	2069.35
3.025331	4.703513	4.92744	6.028686	7.524042	9.383009	12.04748	15.28803	20.85696	28.89395	43.65510	72.52137	126.2609	277.6729	812.415	1504.87
3.116713	3.980041	2.562513	6.161686	7.794121	9.494704	11.99778	15.54002	20.99277	29.90184	45.01557	73.85646	134.9505	303.912	915.2131	5055.00
3.203931	0.074746	5.103386	6.219151	7.72297	9.560438	11.85235	16.75137	21.73130	30.64433	47.1028	79.5575	144.7886	286.701	761.9587	4379.732

b. Block Coefficient Matrix

c. MSE per pixel: 24.86

iv. 16x16, 10 coefficients kept

a. Average Block Energy

2.369953	3.330917	4.190329	5.272102	6.285074	7.700502	9.771789	12.01169	16.07049	21.39375	31.37526	50.22407	81.38747	148.0723	336.6625	1078.561
3.233576	3.258263	4.190301	5.193961	6.843746	8.019167	9.78912	12.47162	16.11246	21.44353	31.19362	52.18233	82.73848	154.0184	349.8959	1078.561
2.464427	3.311163	4.35079	5.277805	6.442939	8.125175	10.01929	12.77011	17.24256	23.4297	33.65978	52.75084	83.2223	161.4805	352.7122	1326.202
4.230561	3.361487	4.420327	5.511939	6.878993	8.411145	10.28121	12.78018	17.12574	23.68536	34.00095	52.04022	85.98721	164.1955	372.8812	1611.109
6.264678	5.359541	8.458384	5.354226	6.755071	8.538274	10.49844	12.94955	17.22732	23.76548	37.37941	56.54411	91.26381	189.0319	405.2023	1010.816
6.550481	8.180372	8.039549	5.451827	6.846963	7.853415	10.43553	13.46219	17.90354	25.01998	36.25061	54.90406	93.86685	197.4762	462.7796	2066.699
6.459179	5.547336	4.447454	6.333937	7.637682	8.612563	10.78504	13.4715	18.7636	25.02211	36.3742	57.52008	97.67374	194.7374	510.0237	1023.852
8.719098	5.362888	4.767493	5.806558	7.53895	8.486599	10.7168	14.16106	19.23741	25.30775	37.46025	60.05066	99.3309	204.5193	519.3437	7079.517
7.769809	5.392576	4.767447	5.739499	7.019576	7.878146	11.1189	14.01586	18.73567	23.26060	38.00233	65.56791	100.334	222.5532	574.9593	3295.725
7.299466	3.742006	4.674233	5.80817	7.0464	10.44122	11.82797	14.71859	18.82149	26.92142	39.66801	64.54438	107.6545	225.0982	604.4366	1451.314
8.884659	6.388501	4.887327	5.767117	5.758063	8.709721	11.31072	14.55557	20.098	27.99197	43.04267	70.88000	124.581	230.700	624.0932	998.474
2.905679	3.900327	4.900709	6.045012	7.279824	8.970615	11.44229	14.79919	19.63581	31.28725	41.36983	67.85254	119.4715	236.255	675.2414	14625.96
2.982081	3.979957	5.162129	5.945883	7.453368	9.414494	11.49229	15.0268	20.0348	28.58731	43.25427	69.49195	121.561	255.1312	708.216	2069.35
3.025331	4.703513	4.92744	6.028686	7.524042	9.383009	12.04748	15.28803	20.85696	28.89395	43.65510	72.52137	126.2609	277.6729	812.415	1504.87
3.116713	3.980041	2.562513	6.161686	7.794121	9.494704	11.99778	15.54002	20.99277	29.90184	45.01557	73.85646	134.9505	303.912	915.2131	5055.00
3.203931	0.074746	5.103386	6.219151	7.72297	9.560438	11.85235	16.75137	21.73130	30.64433	47.1028	79.5575	144.7886	286.701	761.9587	4379.732

b. Block Coefficient Matrix

c. MSE per pixel: 105.13

Q2. As we can see from the data above, for both methods (KLT and DCT) as the number of coefficient increase keeping the block size same, the visual quality of the compressed image becomes better. Moreover, the distortion and the MSE will be lower as well. If we keep the

number of coefficient same while increasing the block size, the visual quality of image becomes worse for both methods. The distortion and MSE will be higher. When we keep the number of coefficients and the block size same, KLT gives better visual quality image with lower MSE when compared to DCT.

Q3. Zonal masking proves to be efficient when a significant portion of the energy is focused on the low-frequency range. However, the effectiveness of zonal masking decreases when there are numerous high-frequency components, as it tends to eliminate small high-frequency elements. In such cases, applying thresholding to each block works well since only the energy exceeding the set threshold value is retained, and the remaining is discarded.

Q4.

DCT:

- i. 8x8 block, 10 coefficients kept : 0.9966
- ii. 8x8 block, 5 coefficients kept : 0.9958
- iii. 16x16 block, 40 coefficients kept : 0.9982
- iv. 16x16 block, 10 coefficients kept : 0.9937

KLT:

- i. 8x8 block, 10 coefficients kept : 0.9981
- ii. 8x8 block, 5 coefficients kept : 0.9959
- iii. 16x16 block, 40 coefficients kept : 0.99859
- iv. 16x16 block, 10 coefficients kept : 0.99405

Q5. If the block size and number of coefficients are constant, KLT demonstrates superior compression efficiency to DCT, resulting in better visual quality and a lower MSE of compressed images. However, KLT computation necessitates correlation matrix computation followed by eigenvector decomposition, adding to the execution time. Unlike DCT, there is no speedy algorithm available for computing the transformed coefficients using the KLT method. While DCT is nearly optimal for stationary images with high correlation, KLT is better suited for images with low correlation when it comes to compression quality.

Q6. Upon comparing the DCT and KLT matrices, we can observe stark differences between the two. DCT exhibits high energy concentration in the top left corner of the matrices (low frequency part), whereas KLT has high energy concentrated in the bottom right corner (high frequency part). KLT works best when the image is highly uncorrelated, whereas DCT is optimal when the image is highly correlated.

In this lab, we evaluated two methods of transform coding, namely DCT and KLT. DCT proved to be faster and more efficient than KLT, particularly when dealing with highly-correlated stationary images. However, when it came to the Lena image which is not highly correlated, KLT produced compressed images with better visual quality and lower MSE than DCT. It is worth noting that the execution time of KLT is longer due to the additional computation required for

correlation matrix and eigenvector decomposition. Nevertheless, KLT is the better option for images with random correlation as it produces compressed images with superior quality.