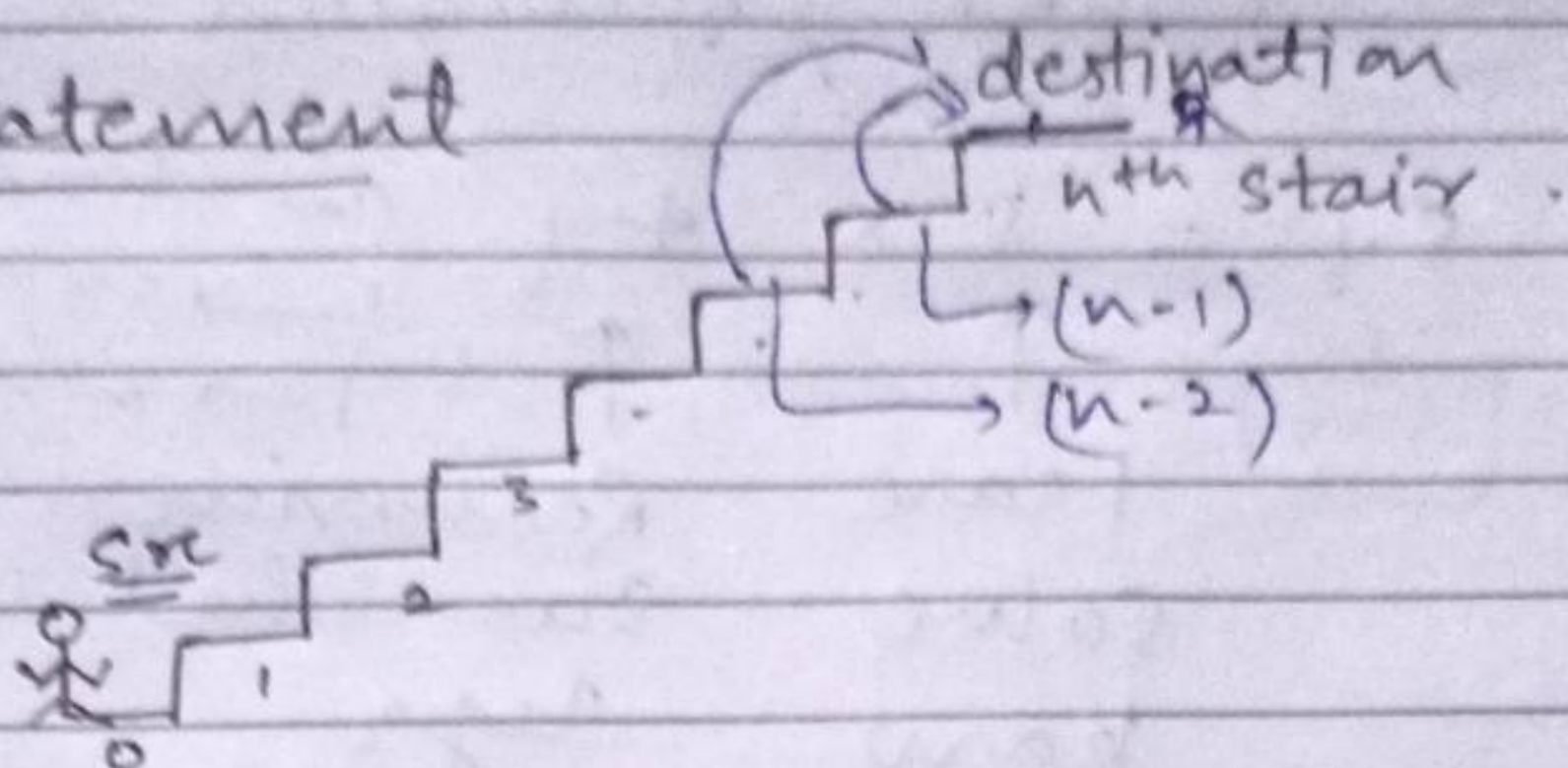


Recursion

Lecture 2

Climb Stairs

Problem Statement



steps allowed \Rightarrow

- \hookrightarrow 1 stair at a time
- \hookrightarrow 2 stairs at a time

Find no. of ways to reach n^{th} stair

One can reach n^{th} stair only by 2 ways.

Total no. of ways to reach n^{th} stairs

$$f(n) = f(n-1) + f(n-2)$$

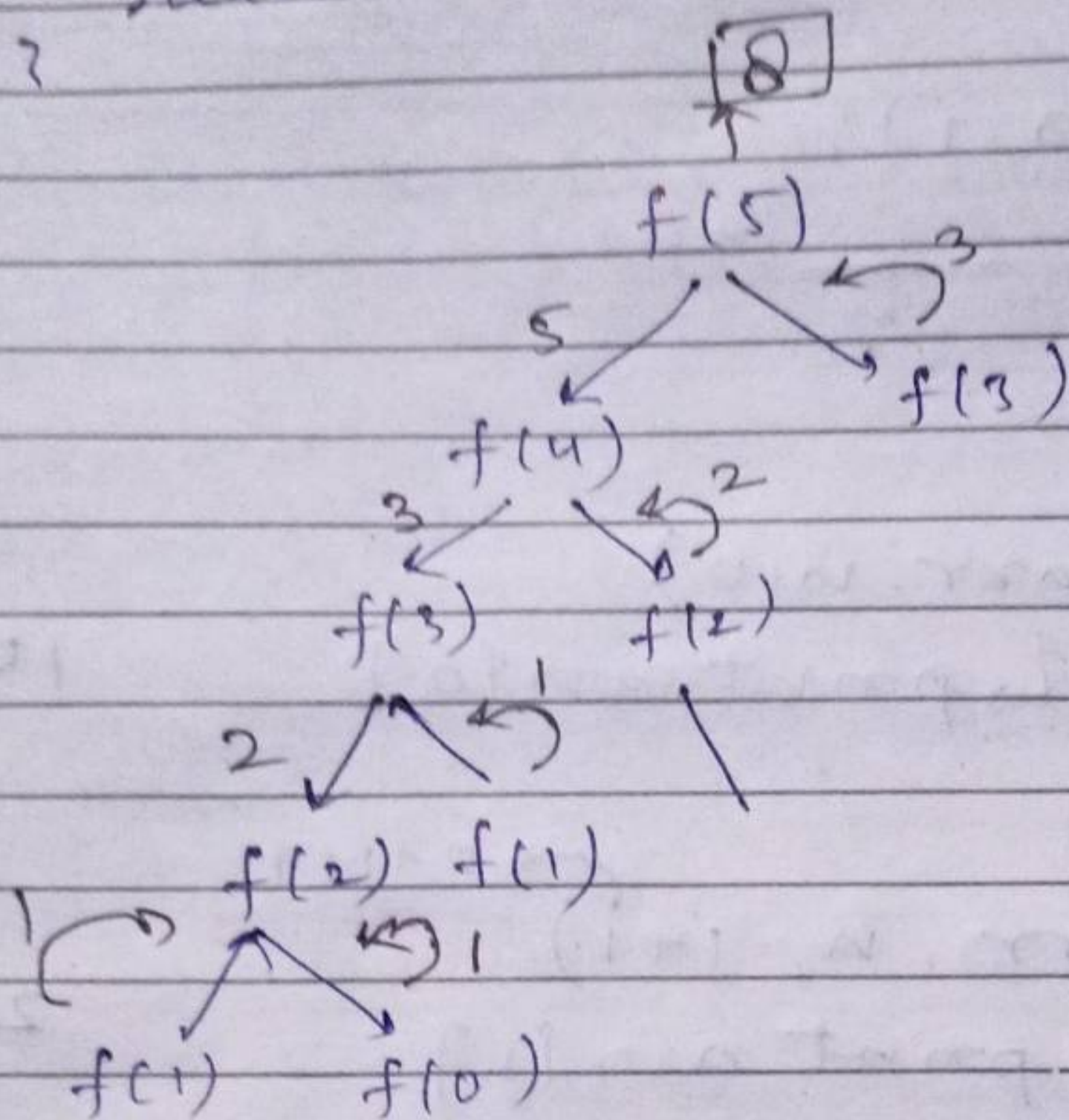
Code

```
int main() {
    int n;
    cin >> n;
    int ans = climbStairs(n);
    cout << ans << endl;
}

int climbStairs(int n) {
    if (n == 0 || n == 1)
        return 1;
```



```
int ans = climbStairs(n-1) + climbStairs(n-2);
return ans;
```



Ques.

10	20	30	40	50
----	----	----	----	----

Print all elements

With loop

```
for (int i=0; i<n; i++)
{
    cout << arr[i];
}
```

With Recursion

```
void print (int arr[], int n, int i) {
    if (i < n)
        if (i >= n) {
            return;
        }
    cout << arr[i] << " "; // 1 case solve
    print (arr, n, i+1);
}
```



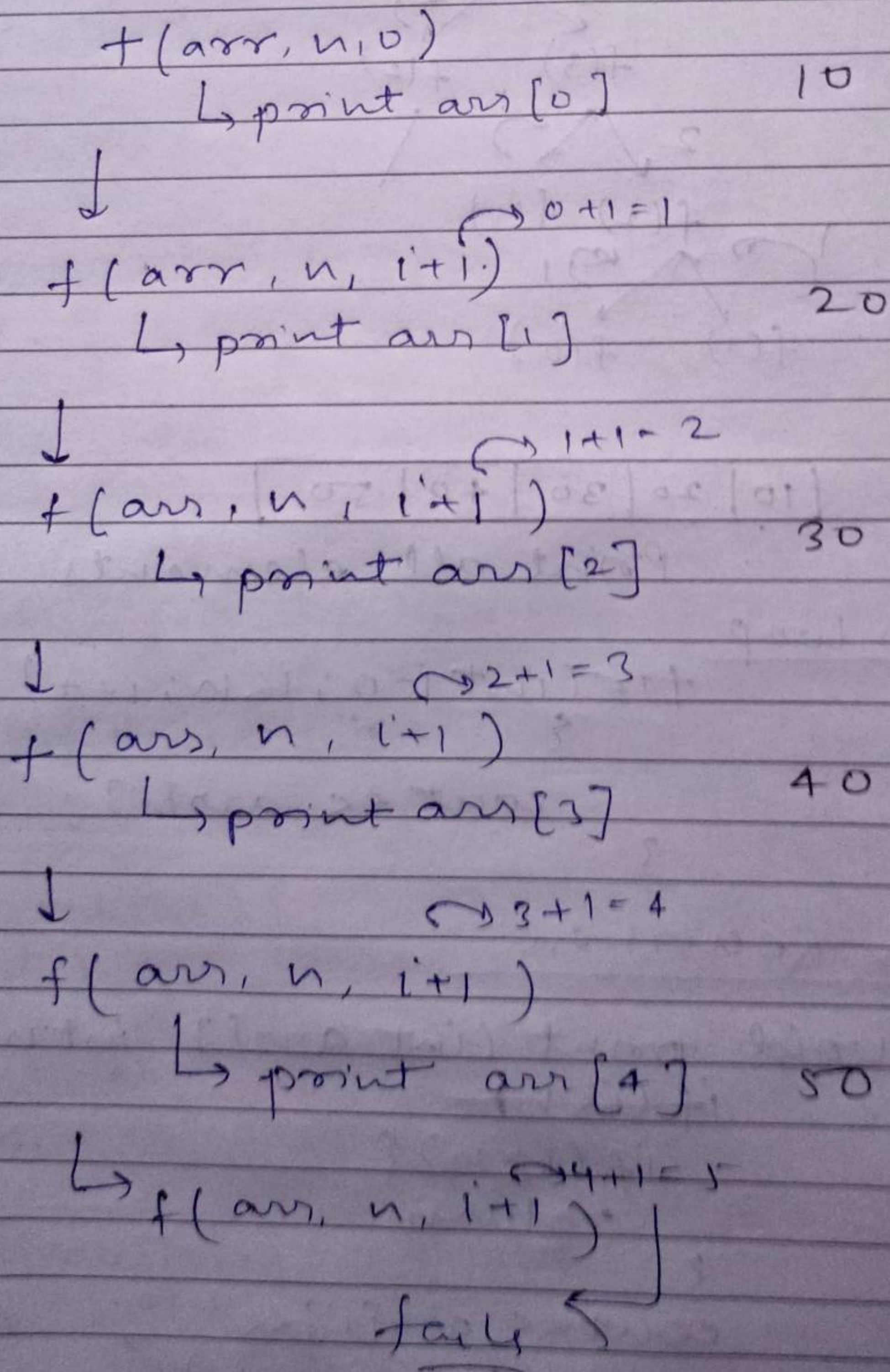
```

int main() {
    int arr[5] = {10, 20, 30, 40, 50};
    int n = 5;
    int i = 0;
    print(arr, n, i);
}

```

Working

arr
n=5
i=0



Maximum no. in array using Recursion

```
int main() {
    int arr[] = {10, 20, 30, 21, 44, 32, 17, 19};
    int n = 8;
    int maxi = INT_MIN;
    int i = 0;
    findmax(arr, n, i, maxi);
    cout << "Max no. is = " << maxi << endl;
    return 0;
}
```

pass by reference

```
void findmax(int arr[], int n, int i, int &maxi) {
```

```
    if (i == n) { // array khtm, traverse hogya pura
        return;
    }
```

```
    if (arr[i] > maxi) {
        maxi = arr[i];
    }
```

// ek case solve karo, current element check karo.

```
    findmax(arr, n, i+1, maxi);
```

```
}
```


Working -

10	30	41	20
0	1	2	3

$f(arr, 4, 0, INTMIN)$

maxi updated ($10 > 0$)

$f(arr, 4, 1, 10)$

maxi updated ($30 > 10$)

$f(arr, 4, 2, 30)$

maxi updated ($41 > 30$)

$f(arr, 4, 3, 41)$

maxi not update ($41 > 20$)

$f(arr, 4, 4, 41)$

Base case So.

So maximum no here will be printed garbage value that is of INTMIN as it is called by value

So we have to call it by reference.

Thus output will be 41.

[10 | 44 | 30]

0 1 2

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(arr, 3, 0, INT_MIN)

void findmax(arr, n, maxi)

{

if (i == n) return; → [F]

maxi = max(maxi, arr[i]);

findmax(arr, n, i+1, maxi);

}

[10] ← maxi

arr, 3, 3, 44

void findmax(arr, n, maxi)

{

if (i == n) return; [True]

}

(arr, 3, 1, 10)

void findmax(arr, n, maxi)

{

[F]

[44] ← maxi

arr, 3, 2, 44

void findmax(arr, n, maxi)

{

[F]

[44] ← maxi

→ cout << maxi; → in main function
So here garbage value of INT_MIN will
be printed.

for maxi

main()

{

[INT_MIN] → [10] → [44] → [44]

}

same box we have bar bar

value update logi main

function main

this is call by reference

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Minimum no. in array using recursion

```
void findmin( int arr[], int n, int i, int &mini ) {  
    if ( i == n ) {  
        return;  
    }  
    mini = min( mini, arr[i] );  
    findMin( arr, n, i+1, mini );  
}
```

Q.

I/p → string str = "love babbar"
key → 'r'.

check 'r' is present in
str or not using recursion.

l|o|v|e|b|a|b|b|a|r

first wala ko check karne
baki recursion sambhal lega.

```
int main() {
```

```
    string str = "lovebabbar";
```

```
    int n = str.length();
```

```
    char key = 'r', int i = 0;
```

```
    bool ans = checkKey( str, n, key );
```

```
    cout << "ans is " << ans << endl;
```

```
    return 0;
```



```

bool checkkey (string str, int i, int n,
               char key) {
    if (i >= n) {
        return false;
    }
    if (str[i] == key)
        return true;
    bool ans = checkkey (str, i+1, n, key);
    return ans;
}

```

[NOTE] → Kisi variable ya data structure ko function mein pass karna ho val store karane keliye to by reference pass karna.

Q. I/p → 647
O/p → print all digit of this no.

Using loop →

```

      647  % 10 → 7
      /10 ↓
      64  % 10 → 4
      /10 ↓
      6   % 10 → 6
      /10 ↓
      0

```

0 → Rukna hai (Base case)

Code

```
int main() {
    int n = 647;
    printdigits(n);
    return 0;
}
```

```
void printdigits(int n) {
    if (n == 0) {
        return;
    }
    printdigits(newval);
    int digit = n % 10;
    cout << digit << " ";
    int newval = n / 10;
}
```

Working

PD(647)

↓ 7 print

PD(64)

↓ 4 print

PD(6)

↓ 6 print

PD(0)

↳ Base case

Correct order \rightarrow Recursion call karu
pehle fir print karu.

PD(647)

digit = $647 \% 10$
 $\text{cout} \ll \text{digit}$
 $647 \rightarrow \frac{647}{10} = 64$

PD(64)

$64 \% 10 \rightarrow 4$
 $64 \% 10 \rightarrow 6$

PD(6)

$6 \% 10 \rightarrow 6$
 $6 \% 10 \rightarrow 0$

PD(0)

\rightarrow Base Case