# Comp-2540: Lab Assignment 4: Heap and Hashing (2025)

```
Your Marks (For TA Use Only)

3.1 3.2 4.1 4.2 Bonus Total Marked by

1.5 0.5 1 1
```

### 1 Due Date and Submission

The due time is your lab section in the due week. To be submitted 10 minutes before the end of your lab section. You can also submit in the labs one week earlier or during office hours. Submit the PDF file to BrightSpace, and test your code at our test site.

Make sure that you add your signature below to reaffirm that you followed Senate Bylaws 31 (click here for the document). Some PDF readers may not support digital signature well. We recommend you to use Acrobat Reader that is free for downloading.



# 2 Objective

The aim of this assignment is to understand Heap and Hashing. We will implement the Heap ADT, and use our Heap class to implement Heap sort. For the Hashing method, we will implement our own HashMap, and solve the collision using separate chain. We will learn how to generate hash code for a string, and how to generate it efficiently using Horner's method.

# 3 Heap and Heap Sort (2 marks)

PriorityQueue is a Java class that is implemented using Heap data structure. We can implement HeapSort using PriorityQueue as follows, which is not efficient:

### 3.1 Implement Heap2540 class (1.5 marks)

Instead of using the PriorityQueue class provided in Java SDK, we will implement it, called Heap2540 by ourself. The heap sort code is also a little different as listed below. Instead of adding elements one by one, we construct the heap from an array all at once.

```
public static String[] heapSort2540(String[] a) {
    Heap2540 pq = new Heap2540(a);
    int n = a.length;
    String[] result = new String[n];
    for (int i = 0; i < n; i++) {
        result[i] = pq.removeMax();
    }
    return result;
}</pre>
```

We provided the starter code in our submission site. It is not runnable yet because there are a few lines are missing in three places:

swim(): Heapify the array bottom up.
 private void swim(int k) {
 while (k > 1 && less(k / 2, k)) {
 swap(k, k / 2);

swap(k, k / 2); k = k / 2; }

• sink(): Heapify the array top down.

```
 \begin{array}{ll} \mbox{private void sink(int k) } \{ & \mbox{while } (2 \ ^k \ ^c = n) \} \\ & \mbox{int } j = 2 \ ^k \ /' \ Left \ child \\ & \mbox{if } (j < n \ \&\& \ less(j,\ j+1)) \ j++; \ /' \ Right \ child \ is \ bigger \ if \ (lless(k,\ j)) \ break; \\ & \mbox{swap(k,\ j);} \\ & \mbox{k} = j; \\ & \mbox{\}} \\ \} \end{array}
```

• The Constructor Heat2540(String[] a): construct a heap from an array;

```
 \begin{array}{ll} \text{public Heap2540(String[\ ] a) \{} \\ n = a.\text{length; //length of array} \\ \text{heap} = \text{new String[h+1]; // create a new heap} \\ \text{for (int i = 0; i < n; +i+) {} \\ \text{heap[i+1]} = a[i]; // add elements from array to heap} \\ \text{for (int k = n / 2; k >= 1; k-) {} \\ \text{sink(k); // heapify} \\ \end{array}
```

You will get the marks only if your code can run and pass our test on our submission site. There are no partial marks.

#### 3.2 Complexity of Heap Sort (0.5 mark)

Write below the time complexity of the heap sort, supposing that the data size is n. Give your justification briefly.

# 4 Hashing

Hashing is the fast way to count word frequency. This time we will not use a sorting method. Instead, each time when we see a word, we will find the word and its frequency, and update its frequency. Instead of the slow sequential searching as we did in A1, we will use hashing to access the word directly. The overall logic is described below:

```
String maxWord="";
for (String k : map.keys())
        if (map.get(k) > max){
            max = map.get(k);
            maxWord=k;
        }
return new AbstractMap.SimpleEntry < String, Integer > (maxWord, max);
}
```

Your task is to implement HashMap2540, so that word counting can work. Note that you are not allowed to use existing implementations, such as the Hashtable class in Java.

In addition to HashMap2540, you will need a list for collision handling. It is provided as LinkedListForHash2540, and you do not need to change anything in this class. We use separate chaining to handle the collision. The collisions are stored in this class. It is a linked list, each element stores a (word, freq) pair.

### 4.1 Implement the put(key, value) method (1 marks)

The starter code for HashMap2540 is at the submission site. Your first task is to fix the put(key, value) method that is listed as below. There are three lines missing. Please fill in the three lines so that the program can run and get the correct counting. As before, your code should be able to run on our submission site.

Write the code below in the form for the convenience of marking. Note that you must get the code run correctly on our submission site.

```
public void put(Key key, Value val) {
    // double table size if average linked list size is 10. Note that the resize stratege is different from the Java implementation as discussed in the book.
    if (n >= 10 * m) resize(2 * m);
    // Put your code here.
    // 1) get the hash value of the key i.
    int i = myhash(key);
    // 2) then put (key, value) in the i-th linkedList implemented in LinkedListForHash254
    // 3) you need to handle the case whether n need to be increased depending on whether the key is already there.
    if (st[i]_get(key) == null) n++;
    st[i].put(key, val);
}
```

### 4.2 Improve the hashing method (1 marks)

In this implementation, you shall observe that the Hash method and Heap method have similar performances. It is against our knowledge –Hashing should be much faster than Heap sorting. A careful reading of the program reveals that the problem is in the myhash() method. It uses the polynomial method to calculate the hashcode of a string using the following formula:

```
hash = 31^{n-1}key[0] + 31^{n-2}key[1] + \dots + key[n-1]
```

The approach and the formula have no problem, but the corresponding code below is too slow:

This code is slow because of the invocation of the power function Math.pow(). Please rewrite the code using Horner's method, so that in each loop you only need to a multiplication once. Please refer to P.413 of the book for the detailed explanation. You will get the marks for this part if the mark program says that the speed improvement is good enough.

```
private int myhash(Key key) {
  int hash = 7;
  String k = (String) key; //here we assume keys are strings.
  int base=31;
  for (int i = 0; i < k.length(); i++)
     hash = hash * base + k.charAt(i);
  return Math.abs(hash) % m;
}</pre>
```

# 5 Bonus:Hash Hacking (1 mark)

If you run the hashing method on the hackedString200kwords.txt, you will find that it is extremely slow: my machine takes 4289ms using Hashing method, but only 115ms using HeapSort. The reason is that most of the words in the file have the same hashcode, hence the chain will be very long in the hashing method. Please rewrite the hashcode part so that it is more efficient. You need to submit your code on our submission site, and the top 6 students will get the bonus mark.