# Introduction to the Theory of Computation Solutions $$\operatorname{\textbf{Ryan}}$$ Dougherty

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#### 4.3

Let  $ALL_{DFA} = \{ \langle A \rangle | A \text{ is a DFA and } L(A) = \Sigma^* \}$ . Show that  $ALL_{DFA}$  is decidable. **Solution:** We will design a TM T that decides  $ALL_{DFA}$ :  $T = \text{``On input } \langle A \rangle$  where A is a DFA:

- 1. Construct a DFA B such that  $L(A) = \overline{L(B)}$ .
- 2. Run  $E_{DFA}$  on input  $\langle B \rangle$ . Output what  $E_{DFA}$  outputs.