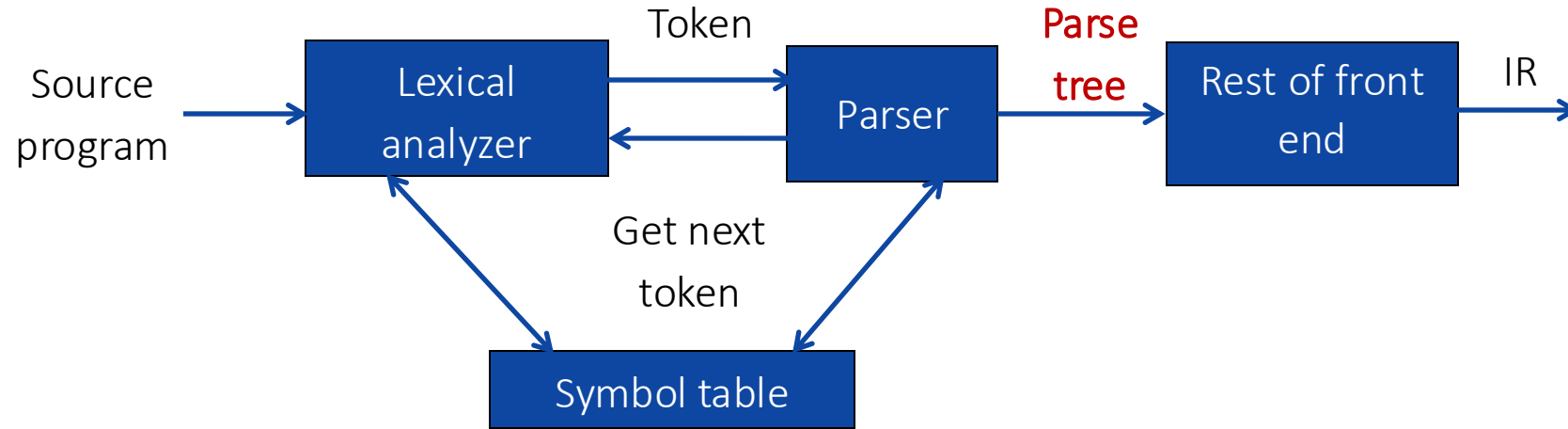


# Module 2 – Syntax Analysis

# Role of parser



- 
- Parser obtains a string of token from the lexical analyzer and reports **syntax error** if any otherwise generates **syntax tree**.
  - There are two types of parser:
    1. Top-down parser
    2. Bottom-up parser

# Context free grammar

- A context free grammar (CFG) is a 4-tuple  $G = (V, \Sigma, S, P)$  where,
    - $V$  is finite set of non terminals,
    - $\Sigma$  is disjoint finite set of terminals,
    - $S$  is an element of  $V$  and it's a start symbol,
    - $P$  is a finite set formulas of the form  $A \rightarrow \alpha$  where  $A \in V$  and  $\alpha \in (V \cup \Sigma)^*$
- 

## ► Nonterminal symbol:

- ➡ The name of syntax category of a language, e.g., noun, verb, etc.
- ➡ The It is written as a **single capital letter**, or as a **name enclosed between < ... >**, e.g., A or <Noun>

<Noun Phrase>  $\rightarrow$  <Article><Noun>

<Article>  $\rightarrow$  a | an | the

<Noun>  $\rightarrow$  boy | apple

# Context free grammar

- A context free grammar (CFG) is a 4-tuple  $G = (V, \Sigma, S, P)$  where,
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    - $P$  is a finite set formulas of the form  $A \rightarrow \alpha$  where  $A \in V$  and  $\alpha \in$
- 

▶  $(V \cup \Sigma)^*$  Terminal symbol:

- A symbol in the alphabet.
- It is denoted by lower case letter and punctuation marks used in language.

<Noun Phrase>  $\rightarrow$  <Article><Noun>

<Article>  $\rightarrow$  a | an | the

<Noun>  $\rightarrow$  boy | apple

# Context free grammar

- A context free grammar (CFG) is a 4-tuple  $G = (V, \Sigma, S, P)$  where,
    - $V$  is finite set of non terminals,
    - $\Sigma$  is disjoint finite set of terminals,
    - $S$  is an element of  $V$  and it's a **start symbol**,
    - $P$  is a finite set formulas of the form  $A \rightarrow \alpha$  where  $A \in V$  and  $\alpha \in (V \cup \Sigma)^*$
- 

## ► Start symbol:

→ First nonterminal symbol of the grammar is called start symbol.

**<Noun Phrase>**  $\rightarrow$  <Article><Noun>

<Article>  $\rightarrow$  a | an | the

<Noun>  $\rightarrow$  boy | apple

# Context free grammar

- A context free grammar (CFG) is a 4-tuple  $G = (V, \Sigma, S, P)$  where,
    - $V$  is finite set of non terminals,
    - $\Sigma$  is disjoint finite set of terminals,
    - $S$  is an element of  $V$  and it's a start symbol,
    - $P$  is a **finite set formulas** of the form  $A \rightarrow \alpha$  where  $A \in V$  and  $\alpha \in (V \cup \Sigma)^*$
- 

## ► Production:

↪ A production, also called a rewriting rule, is a rule of grammar. It has the form of

**A nonterminal symbol  $\rightarrow$  String of terminal and nonterminal symbols**

**$\langle \text{Noun Phrase} \rangle \rightarrow \langle \text{Article} \rangle \langle \text{Noun} \rangle$**

**$\langle \text{Article} \rangle \rightarrow a \mid an \mid the$**

**$\langle \text{Noun} \rangle \rightarrow boy \mid apple$**

# Example: Grammar

Write terminals, non terminals, start symbol, and productions for following grammar.

$$E \rightarrow E \ O \ E \mid (E) \mid -E \mid id$$
$$O \rightarrow + \mid - \mid * \mid / \mid \uparrow$$

**Terminals:**      $id \ + \ - \ * \ / \ \uparrow \ ( \ )$

**Non terminals:**  $E, O$

**Start symbol:**  $E$

**Productions:**  $E \rightarrow E \ O \ E \mid (E) \mid -E \mid id$

$$O \rightarrow + \mid - \mid * \mid / \mid \uparrow$$

# Derivation & Ambiguity



# Derivation

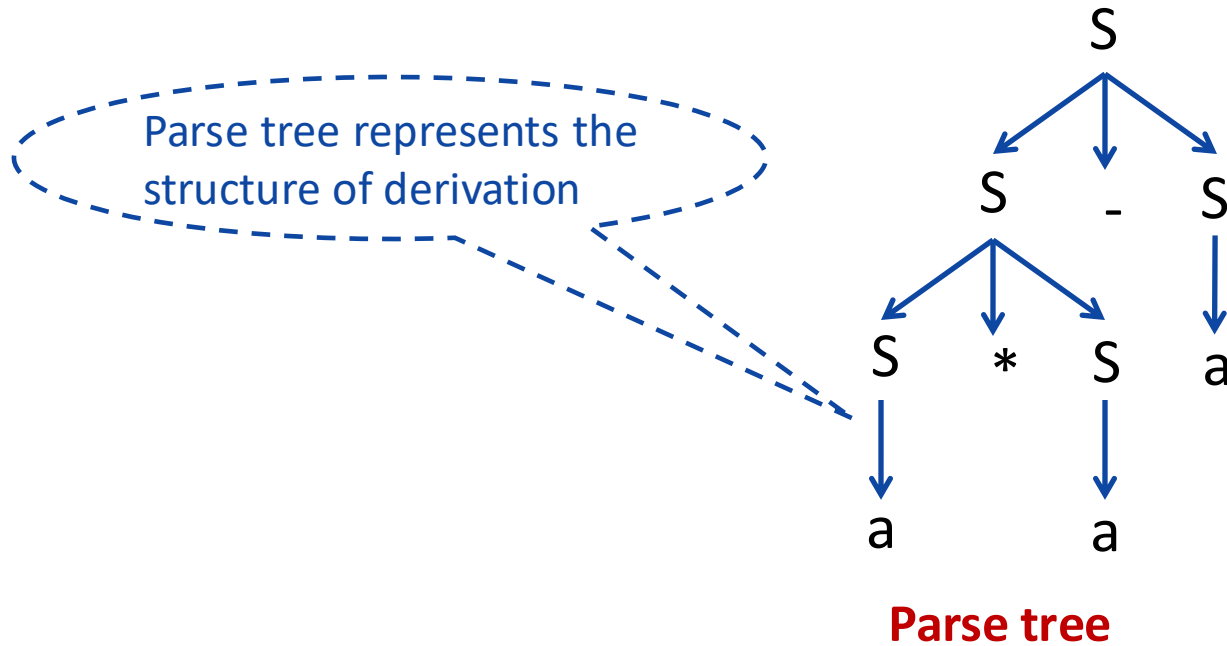
- Derivation is used to find whether the string belongs to a given grammar or not.
- Types of derivations are:
  1. Leftmost derivation
  2. Rightmost derivation

# Leftmost derivation

- A derivation of a string  $W$  in a grammar  $G$  is a left most derivation if at every step the **left most non terminal** is replaced.
- Grammar:  $S \rightarrow S+S \mid S-S \mid S*S \mid S/S \mid a$     Output string:  $a^*a-a$

$S$   
 $\rightarrow \underline{S}-S$   
 $\rightarrow S*\underline{S}-S$   
 $\rightarrow a^*\underline{S}-S$   
 $\rightarrow a^*a-S$   
 $\rightarrow a^*a-a$

**Leftmost Derivation**

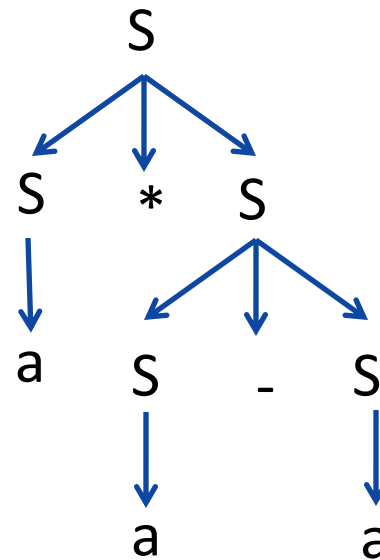


# Rightmost derivation

- A derivation of a string  $W$  in a grammar  $G$  is a right most derivation if at every step the right most non terminal is replaced.
- It is all called canonical derivation.
- Grammar:  $S \rightarrow S+S \mid S-S \mid S*S \mid S/S \mid a$  Output string:  $a*a-a$

$S$   
 $\rightarrow S*\underline{S}$   
 $\rightarrow S*\underline{S}-S$   
 $\rightarrow \underline{S}*S-a$   
 $\rightarrow S*a-a$   
 $\rightarrow a*a-a$

**Rightmost Derivation**



**Parse Tree**

# Exercise: Derivation

1. Perform leftmost derivation and draw parse tree.

$$S \rightarrow A1B$$

$$A \rightarrow 0A \mid \epsilon$$

$$B \rightarrow 0B \mid 1B \mid \epsilon$$

Output string: 1001

2. Perform leftmost derivation and draw parse tree.

$$S \rightarrow 0S1 \mid 01 \quad \text{Output string: 000111}$$

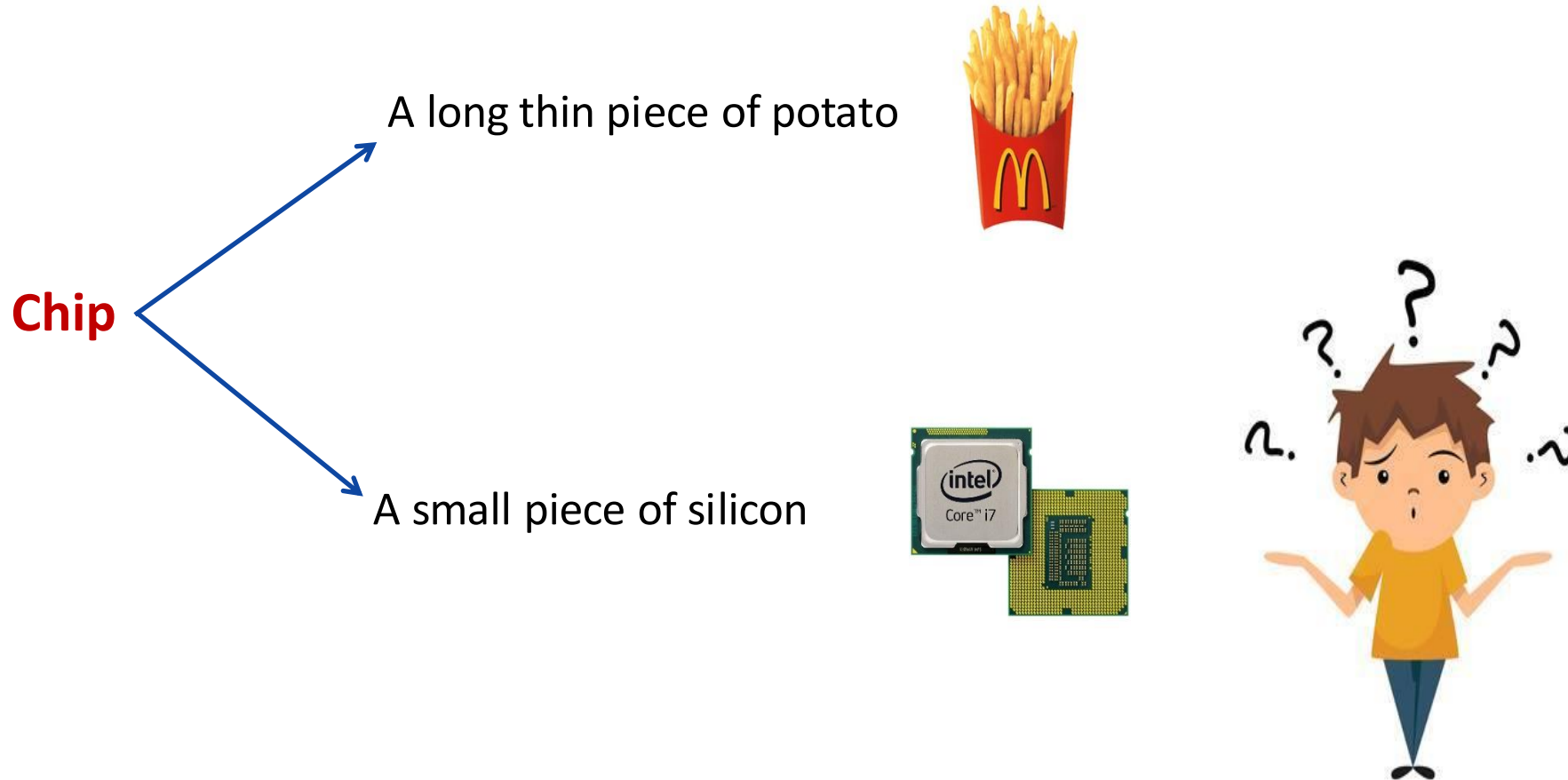
3. Perform rightmost derivation and draw parse tree.

$$E \rightarrow E+E \mid E * E \mid \text{id} \mid (E) \mid -E$$

Output string: id + id \* id

# Ambiguity

- Ambiguity, is a word, phrase, or statement which contains **more than one meaning**.



# Ambiguity

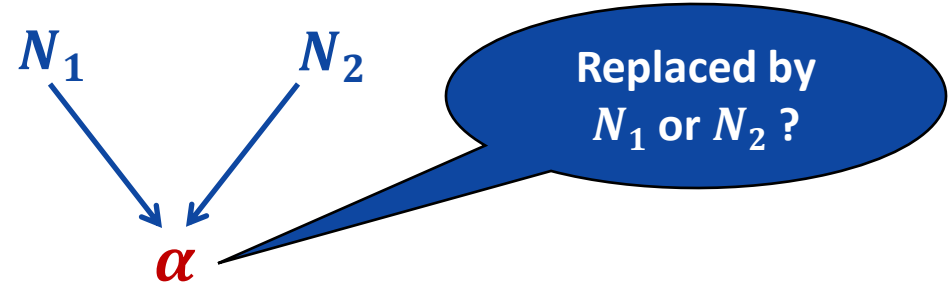
- In formal language grammar, ambiguity would arise if identical string can occur on the RHS of two or more productions.

- Grammar:

$N_1 \rightarrow \alpha$

$N_2 \rightarrow \alpha$

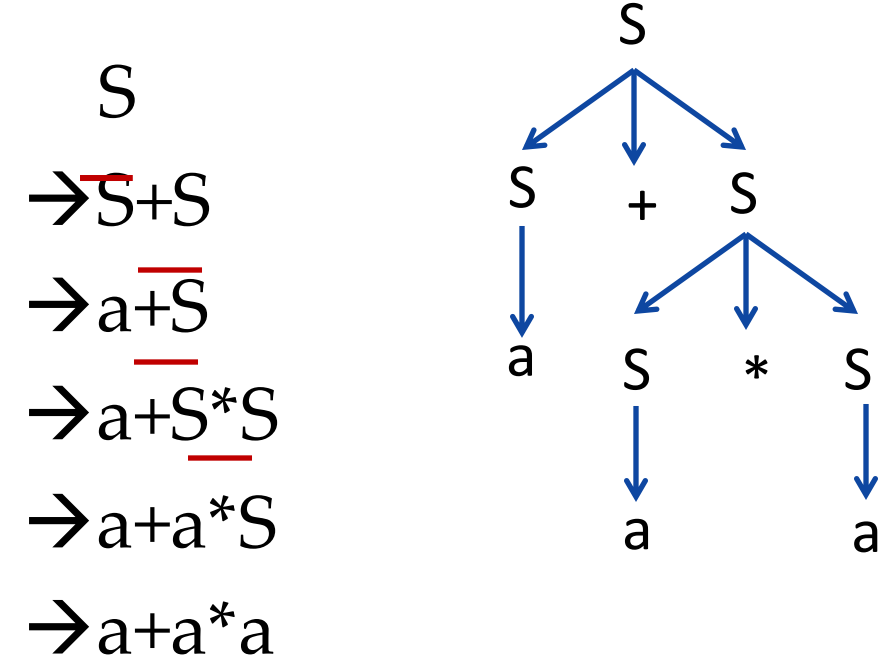
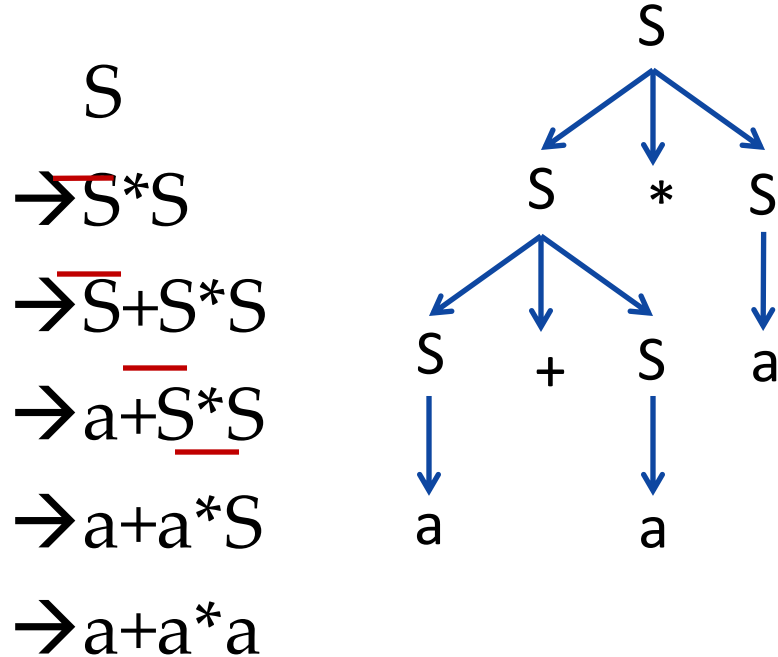
- $\alpha$  can be derived from either  $N_1$  or  $N_2$



# Ambiguous grammar

- Ambiguous grammar is one that produces more than one leftmost or more than one rightmost derivation for the same sentence.
- Grammar:  $S \rightarrow S+S \mid S*S \mid (S) \mid a$

Output string:  $a+a*a$



- Here, Two leftmost derivation for string  $a+a*a$  is possible hence, above grammar is ambiguous.

# Exercise: Ambiguous Grammar

Check Ambiguity in following grammars:

1.  $S \rightarrow aS \mid Sa \mid \epsilon$  (output string: aaaa)
2.  $S \rightarrow aSbS \mid bSaS \mid \epsilon$  (output string: abab)
3.  $S \rightarrow SS^+ \mid SS^* \mid a$  (output string: aa+a\*)
4.  $\langle \text{exp} \rangle \rightarrow \langle \text{exp} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle$   
 $\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle * \langle \text{letter} \rangle \mid \langle \text{letter} \rangle$   
 $\langle \text{letter} \rangle \rightarrow a \mid b \mid c \mid \dots \mid z$  (output string: a+b\*c)
5. Prove that the CFG with productions:  $S \rightarrow a \mid Sa \mid bSS \mid SSb \mid SbS$  is ambiguous (Hint: consider output string yourself)



# Left recursion & Left factoring

# Left recursion

- A grammar is said to be **left recursive** if it has a non terminal  $A$  such that there is a derivation  $A \rightarrow A\alpha$  for some string  $\alpha$ .

$$A \rightarrow A\alpha \mid \quad \longrightarrow \quad \begin{array}{l} A \rightarrow A' \\ A' \rightarrow \alpha A' \mid \epsilon \end{array}$$

# Examples: Left recursion elimination

$E \rightarrow E+T \mid T$

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \varepsilon$

$T \rightarrow T*F \mid F$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \varepsilon$

$X \rightarrow X\%Y \mid Z$

$X \rightarrow ZX'$

$X' \rightarrow \%YX' \mid \varepsilon$

# Exercise: Left recursion

1.  $A \rightarrow Abd \mid Aa \mid a$

$B \rightarrow Be \mid b$

2.  $A \rightarrow AB \mid AC \mid a \mid b$

3.  $S \rightarrow A \mid B$

$A \rightarrow ABC \mid Acd \mid a \mid aa$

$B \rightarrow Bee \mid b$

4.  $\text{Exp} \rightarrow \text{Exp} + \text{term} \mid \text{Exp} - \text{term} \mid \text{term}$

# Left factoring

Left factoring is a grammar transformation that is useful for producing a grammar suitable for predictive parsing.

$$S \rightarrow aAB \mid aCD$$

$$\begin{aligned} S &\rightarrow aS' \\ S' &\rightarrow AB \mid CD \end{aligned}$$

$$A \rightarrow xByA \mid xByAzA \mid a$$

$$\begin{aligned} A &\rightarrow xByAA' \mid a \\ A' &\rightarrow \epsilon \mid zA \end{aligned}$$

$$A \rightarrow aAB \mid aA \mid a$$

$$\begin{aligned} A &\rightarrow aA' \\ A' &\rightarrow AB \mid A \mid \epsilon \\ A' &\rightarrow AA'' \mid \epsilon \\ A'' &\rightarrow B \mid \epsilon \end{aligned}$$

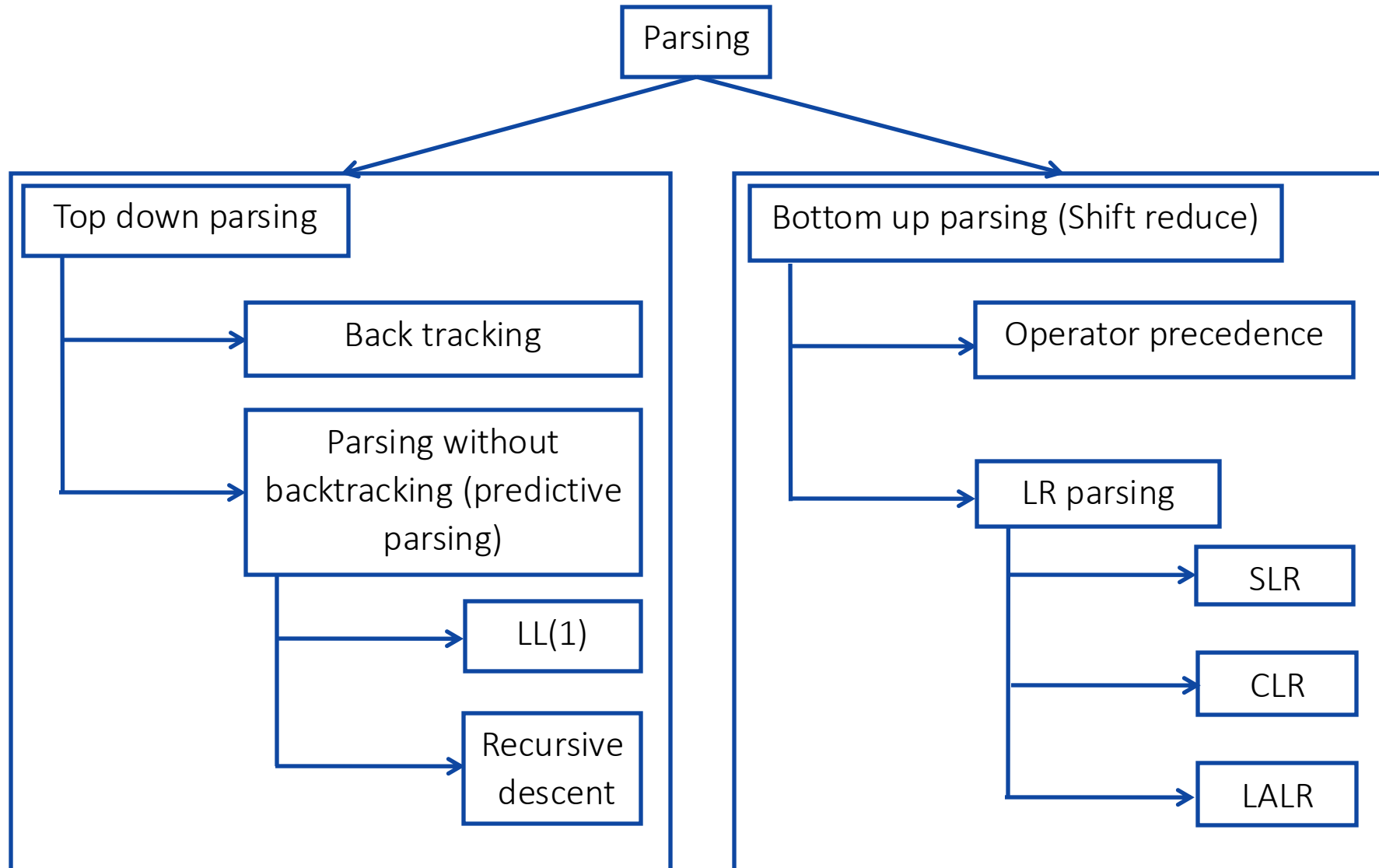
# Exercise

1.  $S \rightarrow iEtS \mid iEtSeS \mid a$
2.  $A \rightarrow ad \mid a \mid ab \mid abc \mid x$

# Parsing

- Parsing is a technique that takes input string and produces output either a **parse tree** if string is valid sentence of grammar, or an **error message** indicating that string is not a valid.
- Types of parsing are:
  1. **Top down parsing:** In top down parsing parser build parse tree from top to bottom.
  2. **Bottom up parsing:** Bottom up parser starts from leaves and work up to the root.

# Classification of parsing methods



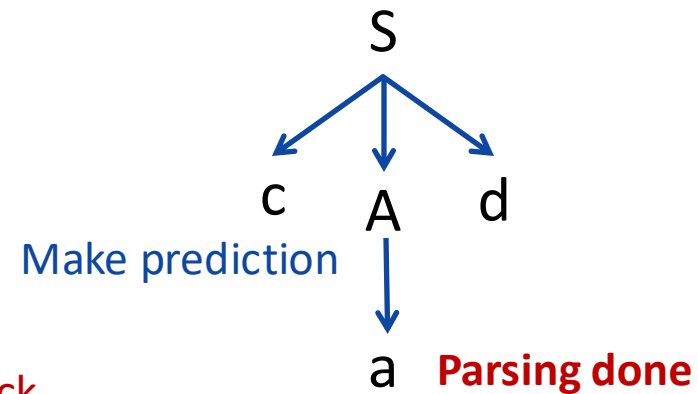
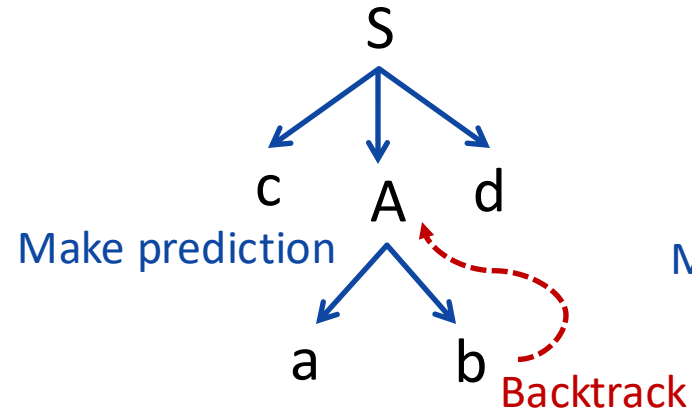
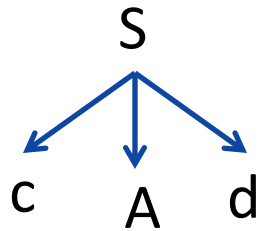


# Backtracking

- In backtracking, expansion of nonterminal symbol we choose one alternative and if any mismatch occurs then we try another alternative.

• Grammar:  $S \rightarrow cAd$   
 $A \rightarrow ab \mid a$

Input string: cad



# Exercise

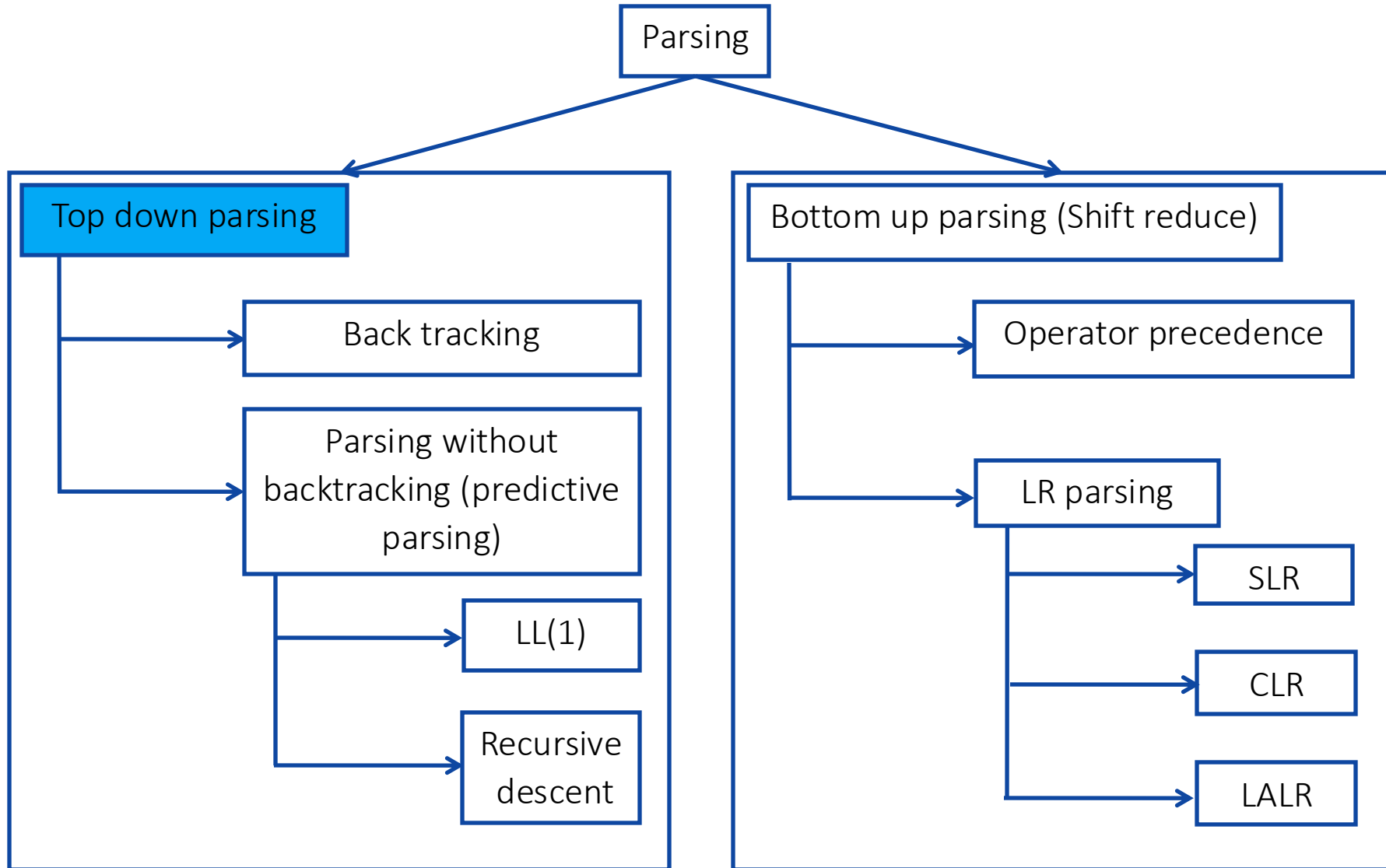
1.  $E \rightarrow 5+T \mid 3-T$

$$T \rightarrow V \mid V*V \mid V+V$$

$$V \rightarrow a \mid b$$

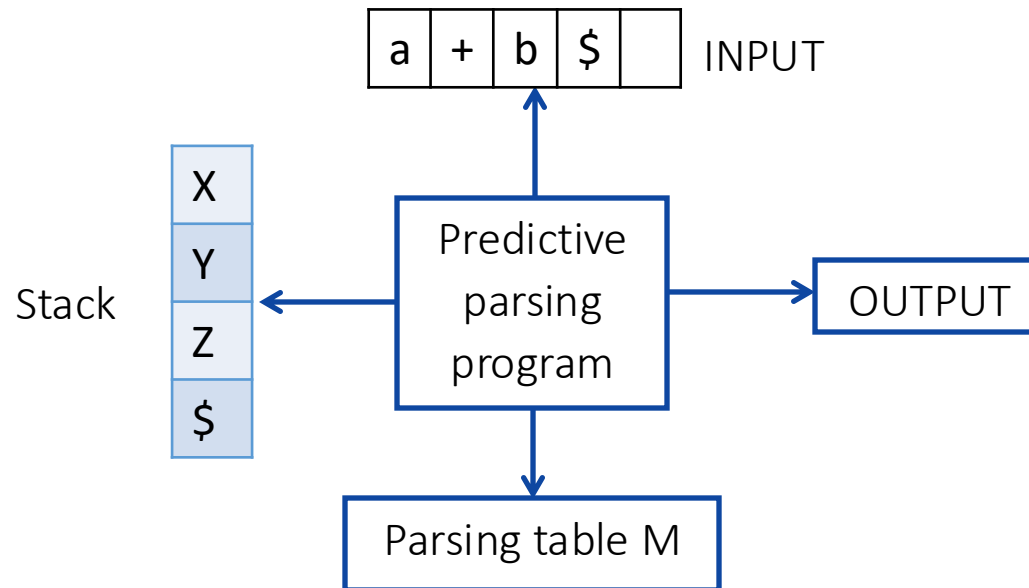
String: 3-a+b

# Parsing Methods



# LL(1) parser (predictive parser)

- LL(1) is non recursive top down parser.
  1. First **L** indicates input is scanned from left to right.
  2. The second **L** means it uses leftmost derivation for input string
  3. **1** means it uses only input symbol to predict the parsing process.



# LL(1) parsing (predictive parsing)

Steps to construct LL(1) parser

1. Remove left recursion / Perform left factoring (if any).
2. Compute FIRST and FOLLOW of non terminals.
3. Construct predictive parsing table.
4. Parse the input string using parsing table.

# Rules to compute first of non terminal

1. If  $A \rightarrow \alpha$  and  $\alpha$  is terminal, add  $\alpha$  to  $FIRST(A)$ .
2. If  $A \rightarrow \epsilon$ , add  $\epsilon$  to  $FIRST(A)$ .
3. If  $X$  is nonterminal and  $X \rightarrow Y_1 Y_2 \dots Y_k$  is a production, then place  $a$  in  $FIRST(X)$  if for some  $i$ ,  $a$  is in  $FIRST(Y_i)$ , and  $\epsilon$  is in all of  $FIRST(Y_1), \dots, FIRST(Y_{i-1})$ ; that is  $Y_1 \dots Y_{i-1} \Rightarrow \epsilon$ . If  $\epsilon$  is in  $FIRST(Y_j)$  for all  $j = 1, 2, \dots, k$  then add  $\epsilon$  to  $FIRST(X)$ .

Everything in  $FIRST(Y_1)$  is surely in  $FIRST(X)$  If  $Y_1$  does not derive  $\epsilon$ , then we do nothing more to  $FIRST(X)$ , but if  $Y_1 \Rightarrow \epsilon$ , then we add  $FIRST(Y_2)$  and so on.

# Rules to compute first of non terminal

## Simplification of Rule 3

If  $A \rightarrow Y_1 Y_2 \dots \dots Y_K$ ,

- If  $Y_1$  does not derive  $\epsilon$  then,  $FIRST(A) = FIRST(Y_1)$

- If  $Y_1$  derives  $\epsilon$  then,

$$FIRST(A) = FIRST(Y_1) - \epsilon \cup FIRST(Y_2)$$

- If  $Y_1$  &  $Y_2$  derives  $\epsilon$  then,

$$FIRST(A) = FIRST(Y_1) - \epsilon \cup FIRST(Y_2) - \epsilon \cup FIRST(Y_3)$$

- If  $Y_1, Y_2$  &  $Y_3$  derives  $\epsilon$  then,

$$FIRST(A) = FIRST(Y_1) - \epsilon \cup FIRST(Y_2) - \epsilon \cup FIRST(Y_3) - \epsilon \cup FIRST(Y_4)$$

- If  $Y_1, Y_2, Y_3 \dots Y_K$  all derives  $\epsilon$  then,

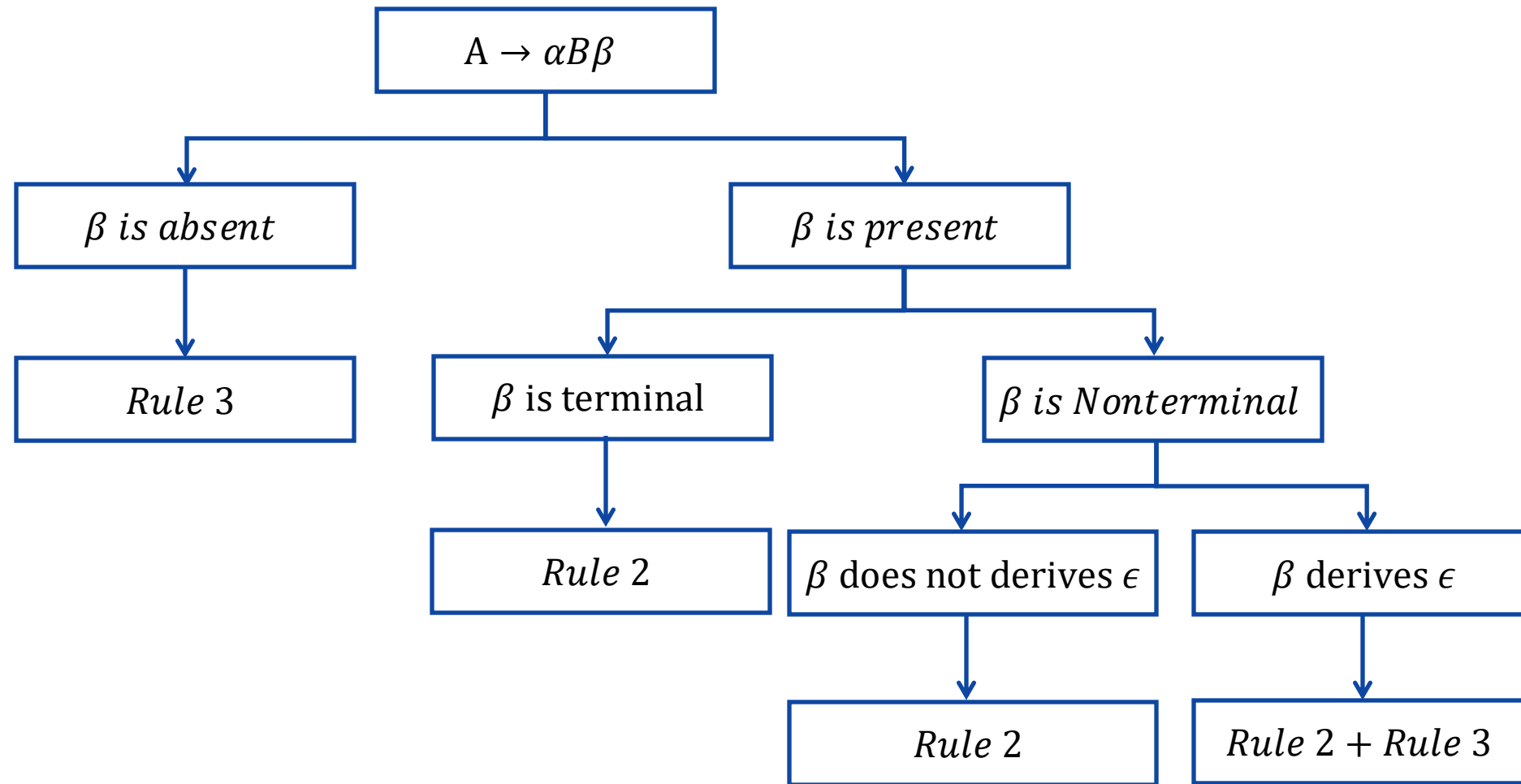
$$FIRST(A) = FIRST(Y_1) - \epsilon \cup FIRST(Y_2) - \epsilon \cup FIRST(Y_3) - \epsilon \cup FIRST(Y_4) - \epsilon \cup \dots \dots \dots FIRST(Y_K) \text{ (note: if all non terminals derives } \epsilon \text{ then add } \epsilon \text{ to } FIRST(A))$$

# Rules to compute FOLLOW of non terminal

1. Place \$ in  $follow(S)$ . (S is start symbol)
2. If  $A \rightarrow \alpha B \beta$ , then everything in  $FIRST(\beta)$  except for  $\epsilon$  is placed in  $FOLLOW(B)$
3. If there is a production  $A \rightarrow \alpha B$  or a production  $A \rightarrow \alpha B \beta$  where  $FIRST(\beta)$  contains  $\epsilon$  then everything in  $FOLLOW(A) = FOLLOW(B)$



# How to apply rules to find FOLLOW of non terminal?



# Rules to construct predictive parsing table

1. For each production  $A \rightarrow \alpha$  of the grammar, do steps 2 and 3.
2. For each terminal  $a$  in  $first(\alpha)$ , Add  $A \rightarrow \alpha$  to  $M[A, a]$ .
3. If  $\epsilon$  is in  $first(\alpha)$ , Add  $A \rightarrow \alpha$  to  $M[A, b]$  for each terminal  $b$  in  $FOLLOW(B)$ . If  $\epsilon$  is in  $first(\alpha)$ , and  $\$$  is in  $FOLLOW(A)$ , add  $A \rightarrow \alpha$  to  $M[A, \$]$ .
4. Make each undefined entry of  $M$  be error.

# Example-1: LL(1) parsing

$S \rightarrow aBa$

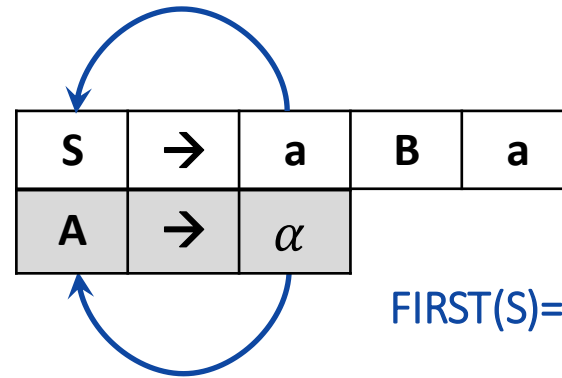
$B \rightarrow bB \mid \epsilon$

Step 1: Not required

Step 2: Compute FIRST

First(S)

$S \rightarrow aBa$

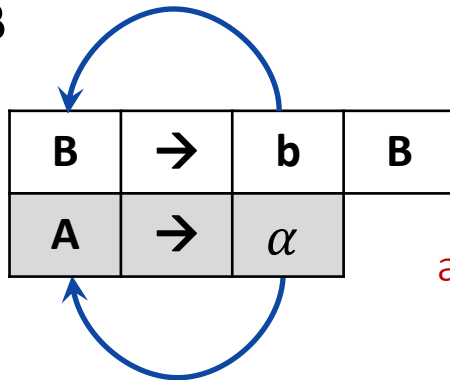


Rule 1  
add  $\alpha$  to  $FIRST(A)$

$FIRST(S) = \{ a \}$

First(B)

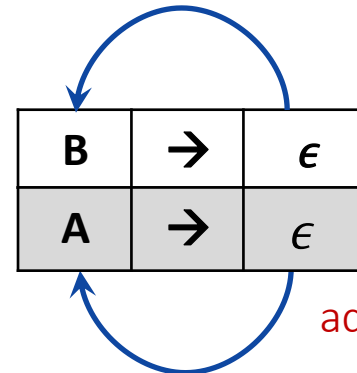
$B \rightarrow bB$



Rule 1  
add  $\alpha$  to  $FIRST(A)$

$FIRST(B) = \{ b, \epsilon \}$

$B \rightarrow \epsilon$



Rule 2  
add  $\epsilon$  to  $FIRST(A)$

NT	First
S	
B	

# Example-1: LL(1) parsing

$S \rightarrow aBa$

$B \rightarrow bB \mid \epsilon$

Step 2: Compute FOLLOW

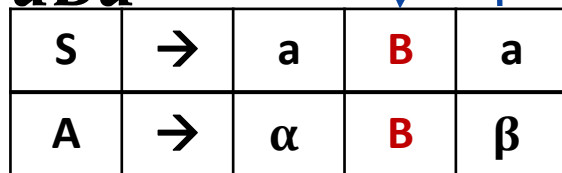
Follow(S)

Rule 1: Place \$ in FOLLOW(S)

$\text{Follow}(S) = \{ \$ \}$

Follow(B)

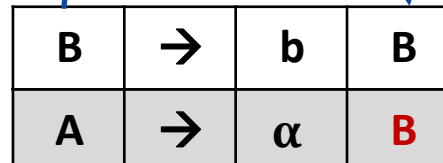
$S \rightarrow aBa$



S	→	a	B	a
A	→	$\alpha$	B	$\beta$

Rule 2  
 $\text{First}(\beta) = \epsilon$

$B \rightarrow bB$



B	→	b	B
A	→	$\alpha$	B

Rule 3  
 $\text{Follow}(A) = \text{follow}(B)$

$\text{Follow}(B) = \{ a \}$

NT	First	Follow
S	{a}	
B	{b, $\epsilon$ }	

# Example-1: LL(1) parsing

$S \rightarrow aBa$

$B \rightarrow bB \mid \epsilon$

Step 3: Prepare predictive parsing table

NT	First	Follow
S	{a}	{\$}
B	{b, $\epsilon$ }	{a}

NT	Input Symbol		
	a	b	\$
S			
B			

$S \rightarrow aBa$

$a = \text{FIRST}(aBa) = \{ a \}$

$M[S, a] = S \rightarrow aBa$

Rule: 2

$A \rightarrow \alpha$

$a = \text{first}(\alpha)$

$M[A, a] = A \rightarrow \alpha$

# Example-1: LL(1) parsing

$S \rightarrow aBa$

$B \rightarrow bB \mid \epsilon$

Step 3: Prepare predictive parsing table

NT	First	Follow
S	{a}	{\$}
B	{b, $\epsilon$ }	{a}

NT	Input Symbol		
	a	b	\$
S	$S \rightarrow aBa$		
B			

$B \rightarrow bB$

$a = \text{FIRST}(bB) = \{ b \}$

$M[B, b] = B \rightarrow bB$

Rule: 2

$A \rightarrow \alpha$

$a = \text{first}(\alpha)$

$M[A, a] = A \rightarrow \alpha$

# Example-1: LL(1) parsing

$S \rightarrow aBa$

$B \rightarrow bB \mid \epsilon$

Step 3: Prepare predictive parsing table

NT	First	Follow
S	{a}	{\$}
B	{b, $\epsilon$ }	{a}

NT	Input Symbol		
	a	b	\$
S	$S \rightarrow aBa$		
B		$B \rightarrow bB$	

$B \rightarrow \epsilon$

$b = \text{FOLLOW}(B) = \{ a \}$

$M[B, a] = B \rightarrow \epsilon$

Rule: 3

$A \rightarrow \alpha$

$b = \text{follow}(A)$

$M[A, b] = A \rightarrow \alpha$

# Example-2: LL(1) parsing

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

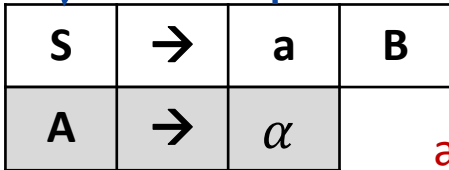
$C \rightarrow cS \mid \epsilon$

Step 1: Not required

Step 2: Compute FIRST

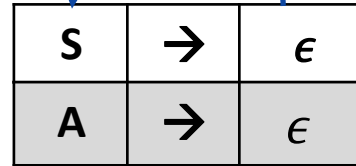
First(S)

$S \rightarrow aB$



Rule 1  
add  $\alpha$  to  $FIRST(A)$

$S \rightarrow \epsilon$



Rule 2  
add  $\epsilon$  to  $FIRST(A)$

$FIRST(S) = \{ a, \epsilon \}$

NT	First
S	
B	
C	



# Example-2: LL(1) parsing

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

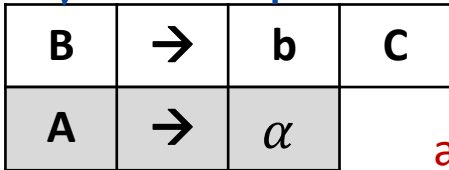
$C \rightarrow cS \mid \epsilon$

Step 1: Not required

Step 2: Compute FIRST

First(B)

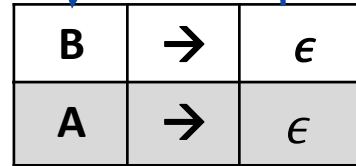
$B \rightarrow bC$



Rule 1  
add  $\alpha$  to  $FIRST(A)$

$FIRST(B) = \{ b, \epsilon \}$

$B \rightarrow \epsilon$



Rule 2  
add  $\epsilon$  to  $FIRST(A)$

NT	First
S	{ a, $\epsilon$ }
B	
C	

# Example-2: LL(1) parsing

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

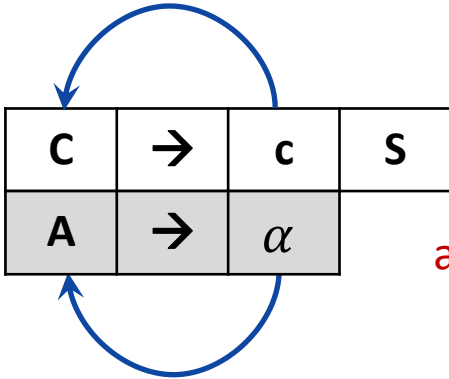
$C \rightarrow cS \mid \epsilon$

Step 1: Not required

Step 2: Compute FIRST

$\text{First}(C)$

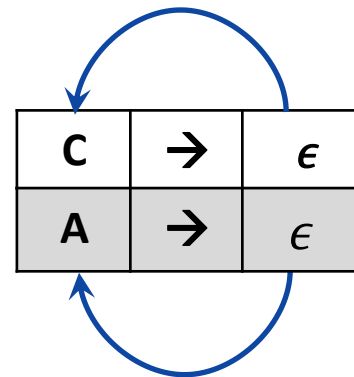
$C \rightarrow cS$



Rule 1  
add  $\alpha$  to  $\text{FIRST}(A)$

$\text{FIRST}(B) = \{ c, \epsilon \}$

$C \rightarrow \epsilon$



Rule 2  
add  $\epsilon$  to  $\text{FIRST}(A)$

NT	First
S	{ a, $\epsilon$ }
B	{ b, $\epsilon$ }
C	

# Example-2: LL(1) parsing

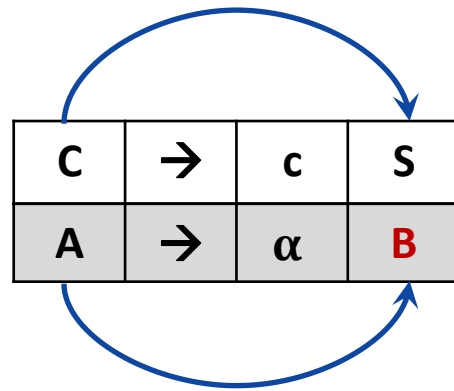
Step 2: Compute FOLLOW

Follow(S)

Rule 1: Place \$ in FOLLOW(S)

Follow(S)={ \$ }

$C \rightarrow cS$



Rule 3

Follow(A)=follow(B)

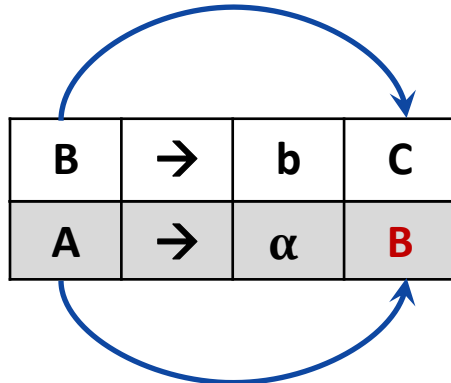
Follow(S)=Follow(C)={\$}

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

$C \rightarrow cS \mid \epsilon$

$B \rightarrow bC$

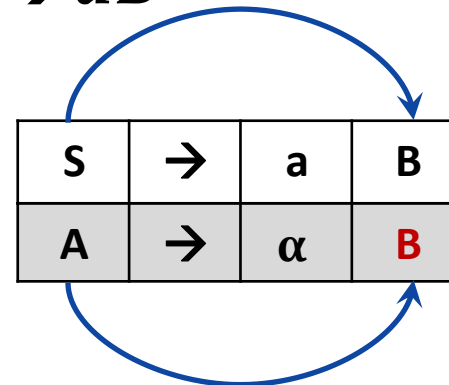


Rule 3

Follow(A)=follow(B)

Follow(C)=Follow(B)={\$}

$S \rightarrow aB$



Rule 3

Follow(A)=follow(B)

Follow(B)=Follow(S)={\$}

NT	First	Follow
S	{a,ε}	
B	{b,ε}	
C	{c,ε}	

# Example-2: LL(1) parsing

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

$C \rightarrow cS \mid \epsilon$

NT	First	Follow
S	{a, $\epsilon$ }	{ $\$$ }
B	{b, $\epsilon$ }	{ $\$$ }
C	{c, $\epsilon$ }	{ $\$$ }

Step 3: Prepare predictive parsing table

N T	Input Symbol			
	a	b	c	$\$$
S				
B				
C				

$S \rightarrow aB$

$a = \text{FIRST}(aB) = \{ a \}$

$M[S, a] = S \rightarrow aB$

Rule: 2

$A \rightarrow \alpha$

$a = \text{first}(\alpha)$

$M[A, a] = A \rightarrow \alpha$

# Example-2: LL(1) parsing

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

$C \rightarrow cS \mid \epsilon$

NT	First	Follow
S	{a}	{\$}
B	{b, $\epsilon$ }	{\$}
C	{c, $\epsilon$ }	{\$}

Step 3: Prepare predictive parsing table

N T	Input Symbol			
	a	b	c	\$
S	$S \rightarrow aB$			
B				
C				

$S \rightarrow \epsilon$

$b = \text{FOLLOW}(S) = \{ \$ \}$

$M[S, \$] = S \rightarrow \epsilon$

Rule: 3

$A \rightarrow \alpha$

$b = \text{follow}(A)$

$M[A, b] = A \rightarrow \alpha$

# Example-2: LL(1) parsing

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

$C \rightarrow cS \mid \epsilon$

NT	First	Follow
S	{a}	{\$}
B	{b, $\epsilon$ }	{\$}
C	{c, $\epsilon$ }	{\$}

Step 3: Prepare predictive parsing table

N T	Input Symbol			
	a	b	c	\$
S	$S \rightarrow aB$			$S \rightarrow \epsilon$
B				
C				

$B \rightarrow bC$

$a = \text{FIRST}(bC) = \{ b \}$

$M[B, b] = B \rightarrow bC$

Rule: 2

$A \rightarrow \alpha$

$a = \text{first}(\alpha)$

$M[A, a] = A \rightarrow \alpha$

# Example-2: LL(1) parsing

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

$C \rightarrow cS \mid \epsilon$

NT	First	Follow
S	{a}	{\$}
B	{b, $\epsilon$ }	{\$}
C	{c, $\epsilon$ }	{\$}

Step 3: Prepare predictive parsing table

N T	Input Symbol			
	a	b	c	\$
S	$S \rightarrow aB$			$S \rightarrow \epsilon$
B		$B \rightarrow bC$		
C				

$B \rightarrow \epsilon$

$b = \text{FOLLOW}(B) = \{ \$ \}$

$M[B, \$] = B \rightarrow \epsilon$

Rule: 3

$A \rightarrow \alpha$

$b = \text{follow}(A)$

$M[A, b] = A \rightarrow \alpha$

# Example-2: LL(1) parsing

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

$C \rightarrow cS \mid \epsilon$

NT	First	Follow
S	{a}	{\$}
B	{b, $\epsilon$ }	{\$}
C	{c, $\epsilon$ }	{\$}

Step 3: Prepare predictive parsing table

N T	Input Symbol			
	a	b	c	\$
S	$S \rightarrow aB$			$S \rightarrow \epsilon$
B		$B \rightarrow bC$		$B \rightarrow \epsilon$
C				

$C \rightarrow cS$

$a = \text{FIRST}(cS) = \{ c \}$

$M[C, c] = C \rightarrow cS$

Rule: 2

$A \rightarrow \alpha$

$a = \text{first}(\alpha)$

$M[A, a] = A \rightarrow \alpha$



# Example-2: LL(1) parsing

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

$C \rightarrow cS \mid \epsilon$

NT	First	Follow
S	{a}	{\$}
B	{b, $\epsilon$ }	{\$}
C	{c, $\epsilon$ }	{\$}

Step 3: Prepare predictive parsing table

N T	Input Symbol			
	a	b	c	\$
S	$S \rightarrow aB$			$S \rightarrow \epsilon$
B		$B \rightarrow bB$		$B \rightarrow \epsilon$
C			$C \rightarrow cS$	

$C \rightarrow \epsilon$

$b = \text{FOLLOW}(C) = \{ \$ \}$

$M[C, \$] = C \rightarrow \epsilon$

Rule: 3

$A \rightarrow \alpha$

$b = \text{follow}(A)$

$M[A, b] = A \rightarrow \alpha$

# Example-3: LL(1) parsing

$E \rightarrow E+T \mid T$

$T \rightarrow T*F \mid F$

$F \rightarrow (E) \mid \text{id}$

Step 1: Remove left recursion

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid \text{id}$

# Example-3: LL(1) parsing

Step 2: Compute FIRST

First(E)

$E \rightarrow TE'$

E	→	T	E'
A	→	Y <sub>1</sub>	Y <sub>2</sub>

Rule 3

$\text{First}(A) = \text{First}(Y_1)$

$\text{FIRST}(E) = \text{FIRST}(T) = \{ (, \text{id} \}$

First(T)

$T \rightarrow FT'$

T	→	F	T'
A	→	Y <sub>1</sub>	Y <sub>2</sub>

Rule 3

$\text{First}(A) = \text{First}(Y_1)$

$\text{FIRST}(T) = \text{FIRST}(F) = \{ (, \text{id} \}$

First(F)

$F \rightarrow (E)$

F	→	(	E	)
A	→	α		

Rule 1

add α to  $\text{FIRST}(A)$

$\text{FIRST}(F) = \{ (, \text{id} \}$

F	→	id
A	→	α

Rule 1

add α to  $\text{FIRST}(A)$

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid \text{id}$

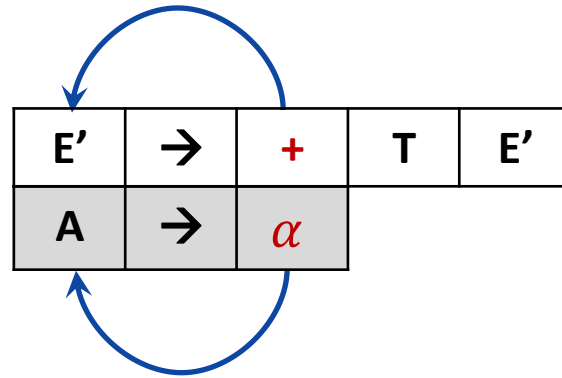
NT	First
E	
E'	
T	
T'	
F	

# Example-3: LL(1) parsing

Step 2: Compute FIRST

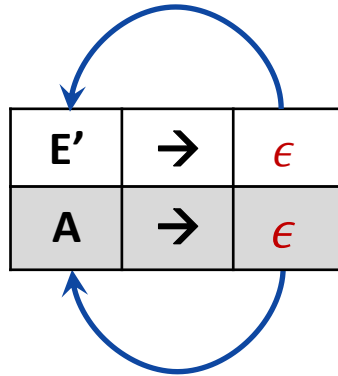
First( $E'$ )

$E' \rightarrow +TE'$



Rule 1  
add  $\alpha$  to  $FIRST(A)$

$E' \rightarrow \epsilon$



Rule 2  
add  $\epsilon$  to  $FIRST(A)$

$FIRST(E') = \{ +, \epsilon \}$

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

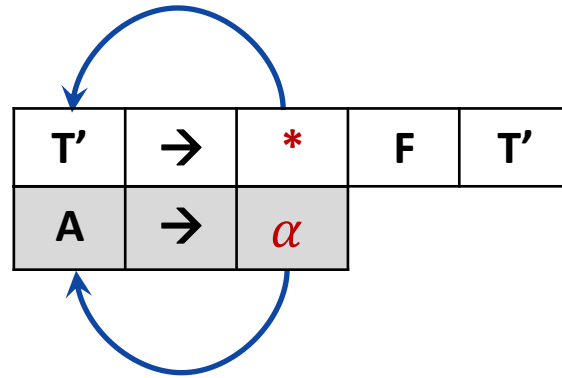
NT	First
E	{ (, id }
E'	
T	{ (, id }
T'	
F	{ (, id }

# Example-3: LL(1) parsing

Step 2: Compute FIRST

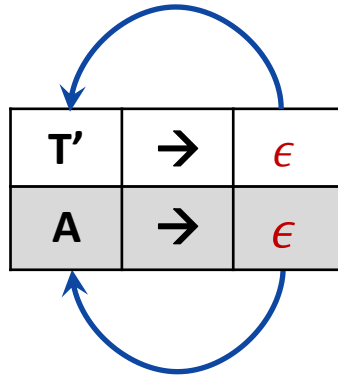
First( $T'$ )

$T' \rightarrow *FT'$



Rule 1  
add  $\alpha$  to  $FIRST(A)$

$T' \rightarrow \epsilon$



Rule 2  
add  $\epsilon$  to  $FIRST(A)$

$FIRST(T') = \{ *, \epsilon \}$

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

NT	First
E	{ (, id }
E'	{ +, $\epsilon$ }
T	{ (, id }
T'	
F	{ (, id }

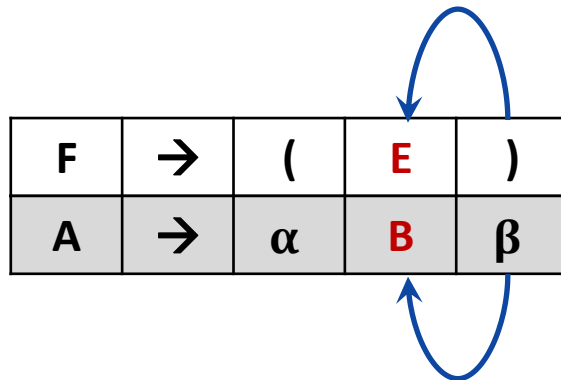
# Example-3: LL(1) parsing

Step 2: Compute FOLLOW

FOLLOW(E)

Rule 1: Place \$ in FOLLOW(E)

$F \rightarrow (E)$



Rule 2

$\text{FOLLOW}(E) = \{ \$, ) \}$

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid \text{id}$

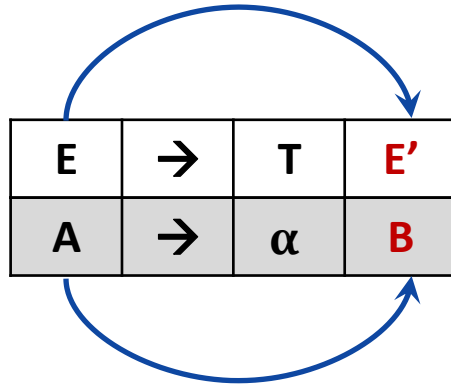
NT	First	Follow
E	{ (, id }	
E'	{ +, ε }	
T	{ (, id }	
T'	{ *, ε }	
F	{ (, id }	

# Example-3: LL(1) parsing

Step 2: Compute FOLLOW

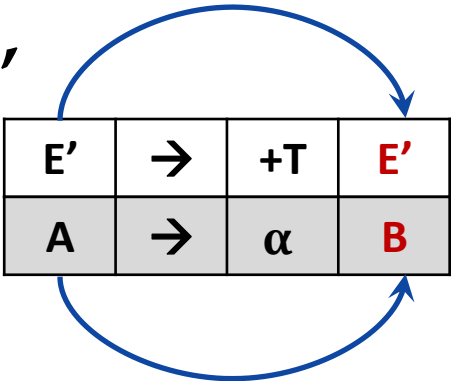
$\text{FOLLOW}(E')$

$E \rightarrow TE'$



Rule 3

$E' \rightarrow +TE'$



Rule 3

$\text{FOLLOW}(E') = \{ \$, ) \}$

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid \text{id}$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	
T	{ (, id }	
T'	{ *, $\epsilon$ }	
F	{ (, id }	

# Example-3: LL(1) parsing

Step 2: Compute FOLLOW

FOLLOW(T)

$E \rightarrow TE'$

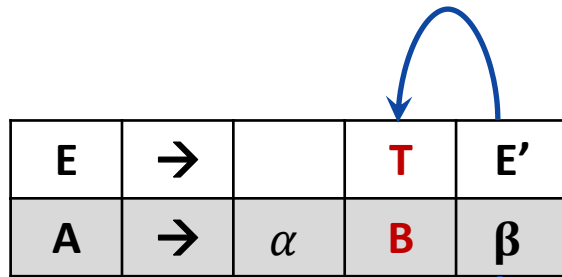
$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

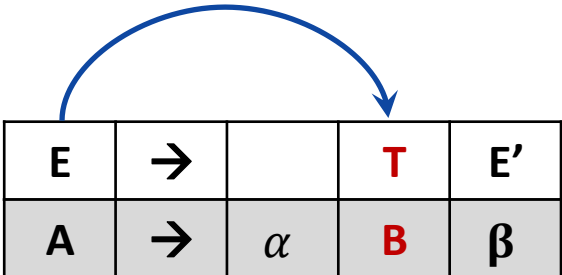
$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid id$



Rule 2



Rule 3

$\text{FOLLOW}(T) = \{ +, \$, ) \}$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	
T'	{ *, $\epsilon$ }	
F	{ (, id }	



# Example-3: LL(1) parsing

Step 2: Compute FOLLOW

FOLLOW(T)

$E' \rightarrow +TE'$

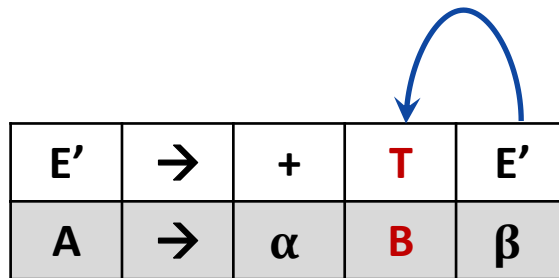
$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

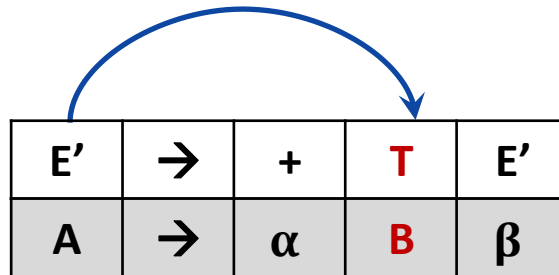
$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid id$



Rule 2



Rule 3

$FOLLOW(T) = \{ +, \$, ) \}$

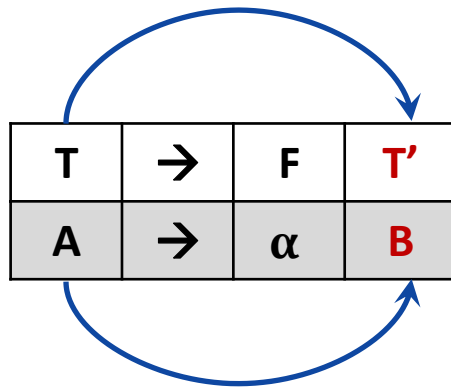
NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	
T'	{ *, $\epsilon$ }	
F	{ (, id }	

# Example-3: LL(1) parsing

Step 2: Compute FOLLOW

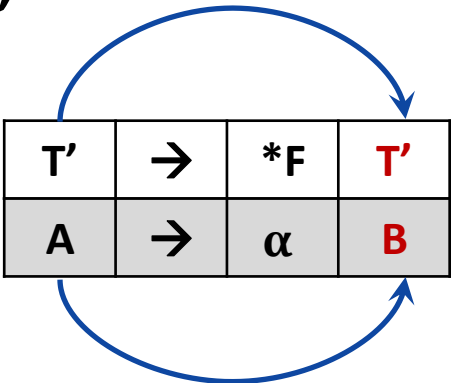
FOLLOW( $T'$ )

$T \rightarrow FT'$



Rule 3

$T' \rightarrow *FT'$



Rule 3

FOLLOW( $T'$ ) = {+, \$, )}

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid id$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, $\epsilon$ }	
F	{ (, id }	

# Example-3: LL(1) parsing

Step 2: Compute FOLLOW

FOLLOW(F)

$T \rightarrow FT'$

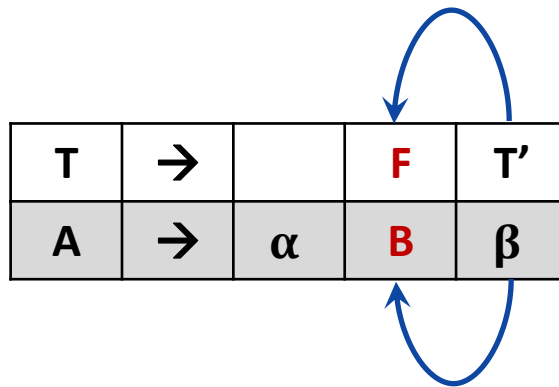
$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

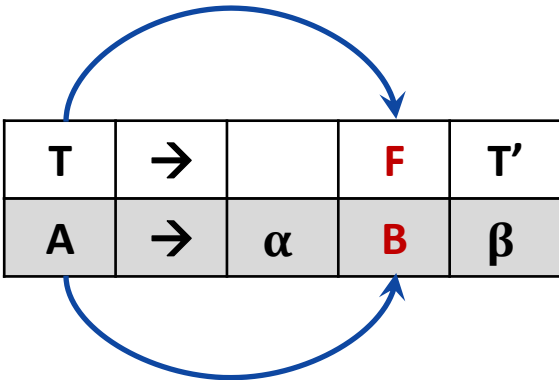
$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid id$



Rule 2



Rule 3

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, ε }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, ε }	{ +, \$, ) }
F	{ (, id }	

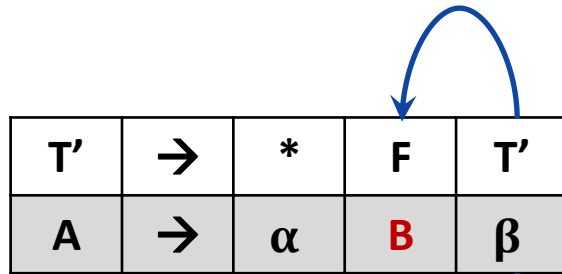
$\text{FOLLOW}(F) = \{ *, +, \$, ) \}$

# Example-3: LL(1) parsing

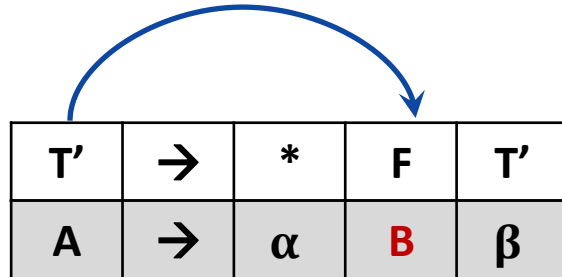
Step 2: Compute FOLLOW

FOLLOW(F)

$T' \rightarrow *FT'$



Rule 2



Rule 3

$\text{FOLLOW}(F) = \{ *, +, \$, ) \}$

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid \text{id}$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, $\epsilon$ }	{ +, \$, ) }
F	{ (, id }	

# Example-3: LL(1) parsing

Step 3: Construct predictive parsing table

NT	Input Symbol					
	id	+	*	(	)	\$
E						
E'						
T						
T'						
F						

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, $\epsilon$ }	{ +, \$, ) }
F	{ (, id }	{ *, +, \$, ) }

$E \rightarrow TE'$

$a = \text{FIRST}(TE') = \{ (, id \}$

$M[E, (] = E \rightarrow TE'$

$M[E, id] = E \rightarrow TE'$

Rule: 2

$A \rightarrow \alpha$

$a = \text{first}(\alpha)$

$M[A, a] = A \rightarrow \alpha$

# Example-3: LL(1) parsing

Step 3: Construct predictive parsing table

NT	Input Symbol					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'						
T						
T'						
F						

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, $\epsilon$ }	{ +, \$, ) }
F	{ (, id }	{ *, +, \$, ) }

$E' \rightarrow +TE'$

$a = \text{FIRST}(+TE') = \{ + \}$

$M[E', +] = E' \rightarrow +TE'$

Rule: 2

$A \rightarrow \alpha$

$a = \text{first}(\alpha)$

$M[A, a] = A \rightarrow \alpha$

# Example-3: LL(1) parsing

Step 3: Construct predictive parsing table

NT	Input Symbol					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$				
T						
T'						
F						

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, $\epsilon$ }	{ +, \$, ) }
F	{ (, id }	{ *, +, \$, ) }

$E' \rightarrow \epsilon$

$b = \text{FOLLOW}(E') = \{ \$, ) \}$

$M[E', \$] = E' \rightarrow \epsilon$

$M[E', )] = E' \rightarrow \epsilon$

Rule: 3

$A \rightarrow \alpha$

$b = \text{follow}(A)$

$M[A, b] = A \rightarrow \alpha$

# Example-3: LL(1) parsing

Step 3: Construct predictive parsing table

NT	Input Symbol					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T						
T'						
F						

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, $\epsilon$ }	{ +, \$, ) }
F	{ (, id }	{ *, +, \$, ) }

$T \rightarrow FT'$

$a = \text{FIRST}(FT') = \{ (, id \}$

$M[T, (] = T \rightarrow FT'$

$M[T, id] = T \rightarrow FT'$

Rule: 2

$A \rightarrow \alpha$

$a = \text{first}(\alpha)$

$M[A, a] = A \rightarrow \alpha$



# Example-3: LL(1) parsing

Step 3: Construct predictive parsing table

NT	Input Symbol					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'						
F						

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, $\epsilon$ }	{ +, \$, ) }
F	{ (, id }	{ *, +, \$, ) }

$T' \rightarrow *FT'$

$a = \text{FIRST}(*FT') = \{ * \}$

$M[T', *] = T' \rightarrow *FT'$

Rule: 2  
 $A \rightarrow \alpha$   
 $a = \text{first}(\alpha)$   
 $M[A, a] = A \rightarrow \alpha$

# Example-3: LL(1) parsing

Step 3: Construct predictive parsing table

NT	Input Symbol					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'			$T' \rightarrow *FT'$			
F						

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, $\epsilon$ }	{ +, \$, ) }
F	{ (, id }	{ *, +, \$, ) }

$T' \rightarrow \epsilon$

$b = \text{FOLLOW}(T') = \{ +, \$, ) \}$

$M[T', +] = T' \rightarrow \epsilon$

$M[T', \$] = T' \rightarrow \epsilon$

$M[T', )] = T' \rightarrow \epsilon$

Rule: 3

$A \rightarrow \alpha$

$b = \text{follow}(A)$

$M[A, b] = A \rightarrow \alpha$

# Example-3: LL(1) parsing

Step 3: Construct predictive parsing table

NT	Input Symbol					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F						

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, $\epsilon$ }	{ +, \$, ) }
F	{ (, id }	{ *, +, \$, ) }

$F \rightarrow (E)$

$a = \text{FIRST}((E)) = \{ ( \}$

$M[F, (] = F \rightarrow (E)$

Rule: 2  
 $A \rightarrow \alpha$   
 $a = \text{first}(\alpha)$   
 $M[A, a] = A \rightarrow \alpha$

# Example-3: LL(1) parsing

Step 3: Construct predictive parsing table

NT	Input Symbol					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F				$F \rightarrow (E)$		

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

NT	First	Follow
E	{ (, id }	{ \$, ) }
E'	{ +, $\epsilon$ }	{ \$, ) }
T	{ (, id }	{ +, \$, ) }
T'	{ *, $\epsilon$ }	{ +, \$, ) }
F	{ (, id }	{ *, +, \$, ) }

$F \rightarrow id$

$a = \text{FIRST}(id) = \{ id \}$

$M[F, id] = F \rightarrow id$

Rule: 2  
 $A \rightarrow \alpha$   
 $a = \text{first}(\alpha)$   
 $M[A, a] = A \rightarrow \alpha$

# Example-3: LL(1) parsing

- Step 4: Make each undefined entry of table be Error

NT	Input Symbol					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$	Error	Error	$E \rightarrow TE'$	Error	Error
E'	Error	$E' \rightarrow +TE'$	Error	Error	$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$	Error	Error	$T \rightarrow FT'$	Error	Error
T'	Error	$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$	Error	$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$	Error	Error	$F \rightarrow (E)$	Error	Error

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid id$

# Example-3: LL(1) parsing

Step 4: Parse the string :  $\text{id} + \text{id} * \text{id} \$$

STACK	INPUT	OUTPUT
E\$	id+id*id\$	

NT	Input Symbol					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$	Error	Error	$E \rightarrow TE'$	Error	Error
E'	Error	$E' \rightarrow +TE'$	Error	Error	$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$	Error	Error	$T \rightarrow FT'$	Error	Error
T'	Error	$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$	Error	$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow \text{id}$	Error	Error	$F \rightarrow (E)$	Error	Error


Q1: Find out whether the following grammar is LL(1):

$$S \rightarrow aSbS \mid bSaS \mid \epsilon$$

Sol. FIRST(S): {a, b,  $\epsilon$ }

FOLLOW(S): {\$, b, a}



Not LL(1) Grammar

	a	b	\$
S	<div><math>S \rightarrow aSbS</math> <math>S \rightarrow \epsilon</math></div>	<div><math>S \rightarrow bSaS</math> <math>S \rightarrow \epsilon</math></div>	$S \rightarrow \epsilon$

# Check whether the following Grammar is LL(1).

1.

$S \rightarrow aBa$

$B \rightarrow bB \mid \epsilon$

2.

$S \rightarrow aSbS \mid bSaS \mid \epsilon$

3.

$S \rightarrow (S) \mid \epsilon$

4.

$S \rightarrow iEtS \mid iEtSeS \mid a$

$E \rightarrow b$

5.

$S \rightarrow A$

$A \rightarrow Bb \mid Cd$

$B \rightarrow aB \mid \epsilon$

$C \rightarrow cC \mid \epsilon$

6.

$S \rightarrow (L) \mid a$

$L \rightarrow L,S \mid S$

Note: Ensure that each cell in the parsing table contains at most one production rule. If any cell contains more than one production rule, the grammar is not LL(1).



Q2: Find out whether the following grammar is LL(1):

$$S \rightarrow (S) \mid \varepsilon$$

Sol. FIRST(S):  $\{ (, \varepsilon \}$

FOLLOW(S):  $\{ \$, ) \}$

 LL(1) Grammar

	(	)	\$
S	$S \rightarrow (S)$	$S \rightarrow \varepsilon$	$S \rightarrow \varepsilon$

Q3: Find out whether the following grammar is LL(1):

$$S \rightarrow AaAb \mid BbBa$$

$$A \rightarrow \varepsilon$$

$$B \rightarrow \varepsilon$$

LL(1) Grammar

FIRST FOLLOW

Sol.

	FIRST	FOLLOW
$S \rightarrow AaAb \mid BbBa$	$\{a, b\}$	$\{\$ \}$
$A \rightarrow \varepsilon$	$\{\varepsilon\}$	$\{a, b\}$
$B \rightarrow \varepsilon$	$\{\varepsilon\}$	$\{b, a\}$

	a	b	\$
S	$S \rightarrow AaAb$	$S \rightarrow BbBa$	
A	$A \rightarrow \varepsilon$	$A \rightarrow \varepsilon$	
B	$B \rightarrow \varepsilon$	$B \rightarrow \varepsilon$	

Q4: Find out whether the following grammar is LL(1):

$$\left. \begin{array}{l} S \rightarrow A \mid a \\ A \rightarrow a \end{array} \right\}$$

Not LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow A \mid a$	{a}	{ \$ }
$A \rightarrow a$	{a}	{ \$ }

Q5: Find out whether the following grammar is LL(1):

$$S \rightarrow aB \mid \epsilon$$

$$B \rightarrow bC \mid \epsilon$$

$$C \rightarrow cS \mid \epsilon$$

LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow aB \mid \epsilon$	$\{a, \epsilon\}$	$\{\$, \}$
$B \rightarrow bC \mid \epsilon$	$\{b, \epsilon\}$	$\{\$, \}$
$C \rightarrow cS \mid \epsilon$	$\{c, \epsilon\}$	$\{\$, \}$

	a	b	c	\$
S	$S \rightarrow aB$			$S \rightarrow \epsilon$
B		$B \rightarrow bC$		$B \rightarrow \epsilon$
C			$C \rightarrow cS$	$C \rightarrow \epsilon$



Q1: Find out whether the following grammar is LL(1):

$$S \rightarrow AB$$

$$A \rightarrow a \mid \varepsilon$$

$$B \rightarrow b \mid \varepsilon$$

LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow AB$	$\{a, b, \varepsilon\}$	$\{\$ \}$
$A \rightarrow a \mid \varepsilon$	$\{a, \varepsilon\}$	$\{b, \$ \}$
$B \rightarrow b \mid \varepsilon$	$\{b, \varepsilon\}$	$\{\$ \}$

	a	b	\$
S	$S \rightarrow AB$	$S \rightarrow AB$	$S \rightarrow AB$
A	$A \rightarrow a$	$A \rightarrow \varepsilon$	$A \rightarrow \varepsilon$
B		$B \rightarrow b$	$B \rightarrow \varepsilon$

Q2: Find out whether the following grammar is LL(1):

$$S \rightarrow aSA \mid \varepsilon$$

$$A \rightarrow c \mid \varepsilon$$

Not LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow aSA \mid \varepsilon$	$\{a, \varepsilon\}$	$\{\$, c\}$
$A \rightarrow c \mid \varepsilon$	$\{c, \varepsilon\}$	$\{\$, c\}$

	a	c	\$
S	$S \rightarrow aSA$	$S \rightarrow \varepsilon$	$S \rightarrow \varepsilon$
A		$A \rightarrow c$ $A \rightarrow \varepsilon$	$A \rightarrow \varepsilon$

Q3: Find out whether the following grammar is LL(1):

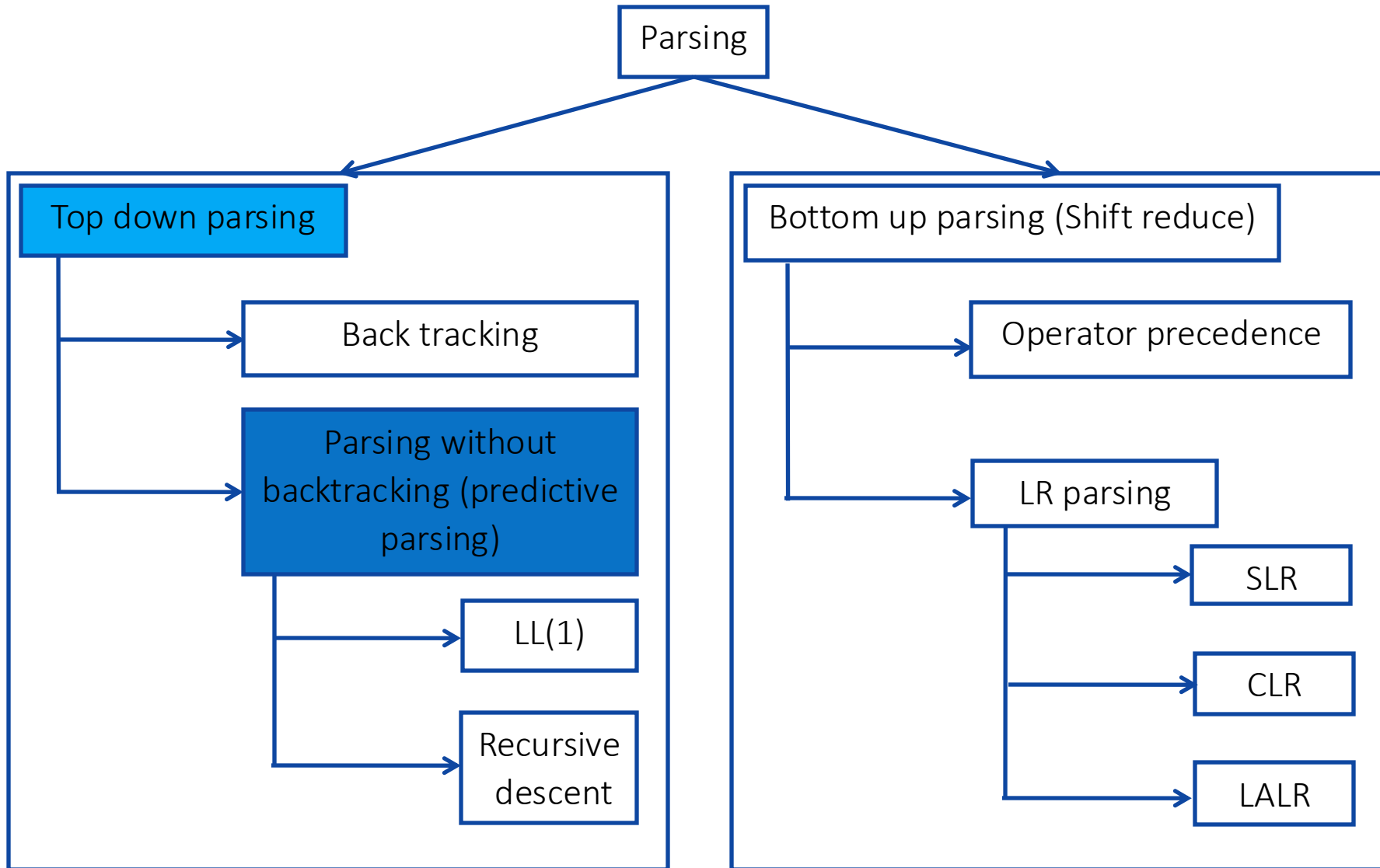
FIRST FOLLOW

Sol.

$S \rightarrow A$	$\{a, b, c, d\}$	$\{\$ \}$
$A \rightarrow Bb \mid Cd$	$\{a, b, c, d\}$	$\{\$ \}$
$B \rightarrow aB \mid \epsilon$	$\{a, \epsilon\}$	$\{b\}$
$C \rightarrow cC \mid \epsilon$	$\{c, \epsilon\}$	$\{d\}$

	a	b	c	d	\$
S	$S \rightarrow A$	$S \rightarrow A$	$S \rightarrow A$	$S \rightarrow A$	
A	$A \rightarrow Bb$	$A \rightarrow Bb$	$A \rightarrow Cd$	$A \rightarrow Cd$	
B	$B \rightarrow aB$	$B \rightarrow \epsilon$			
C			$C \rightarrow cC$	$C \rightarrow \epsilon$	

# Parsing methods





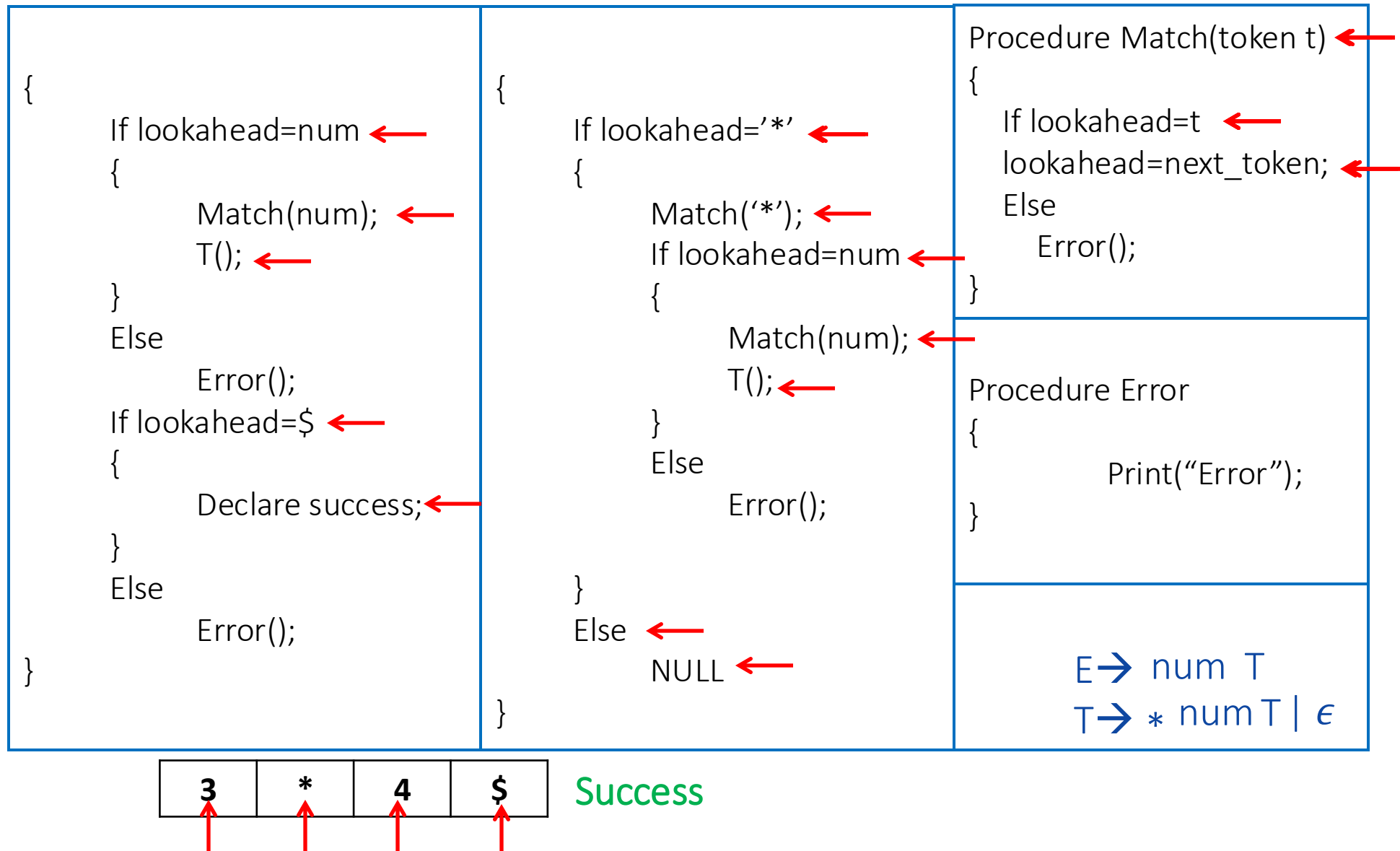
# Recursive descent parsing

- A top down parsing that executes a set of recursive procedure to process the input without backtracking is called recursive descent parser.
- There is a procedure for each non terminal in the grammar.
- Consider RHS of any production rule as definition of the procedure.
- As it reads expected input symbol, it advances input pointer to next position.

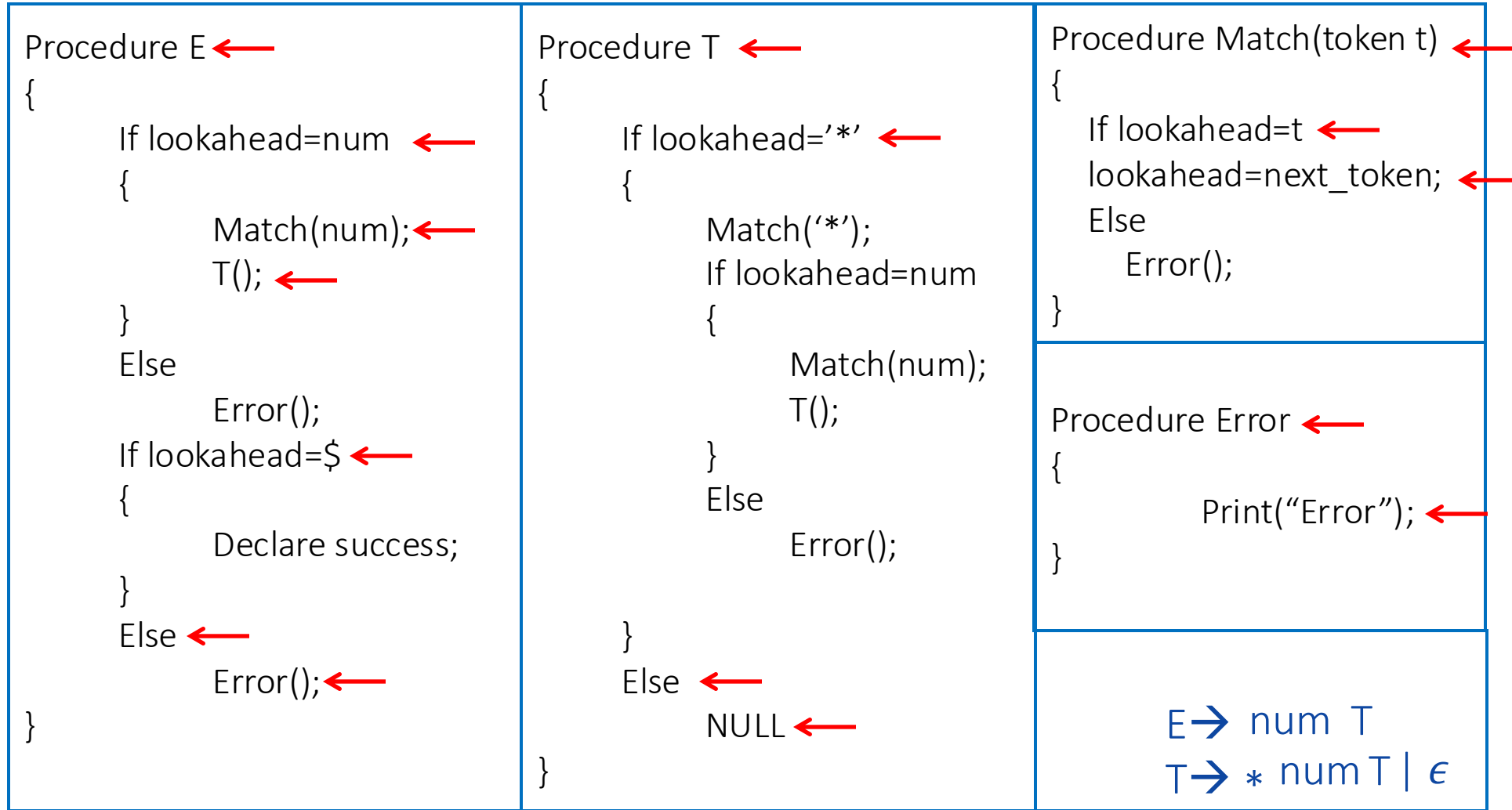
# Cont.,

```
void A() {  
    Choose an A-production,  $A \rightarrow X_1 X_2 \cdots X_k$ ;  
    for (  $i = 1$  to  $k$  ) {  
        if (  $X_i$  is a nonterminal )  
            call procedure  $X_i()$ ;  
        else if (  $X_i$  equals the current input symbol  $a$  )  
            advance the input to the next symbol;  
        else /* an error has occurred */;  
    }  
}
```

# Example: Recursive descent parsing



# Example: Recursive descent parsing



3	*	4	\$
---	---	---	----

Success

3	4	*	\$
---	---	---	----

Error

Consider the following grammar having rules,

$$E \rightarrow iE'$$

$$E' \rightarrow +iE' \mid \varepsilon$$

$E \rightarrow iE'$   
 $E' \rightarrow +iE' \mid \varepsilon$

## Recursive Descent Parser:

```
1.  E()  
2.  {  
3.      if(look_ahead=='i')  
4.      {  
5.          match('i');  
6.          E'();  
7.      }  
8.  }
```

$E \rightarrow iE'$   
 $E' \rightarrow +iE' \mid \varepsilon$

```
1.  E'()  
2.  {  
3.      if(look_ahead=='+')  
4.      {  
5.          match('+');  
6.          match('i');  
7.          E'();  
8.      }  
9.      else  
10.         return;  
11. }
```

## Recursive Descent Parser:

$E \rightarrow iE'$

$E' \rightarrow +iE' \mid \varepsilon$

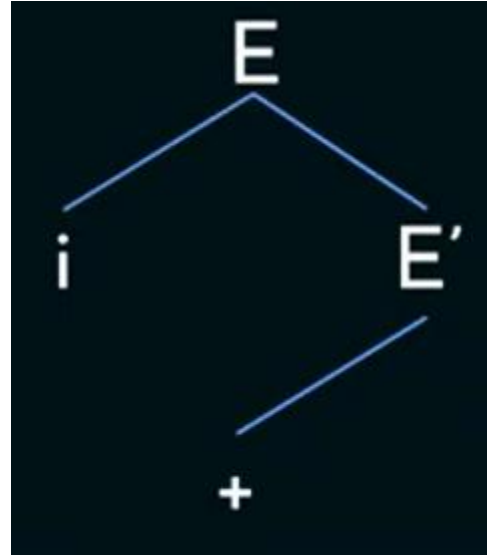
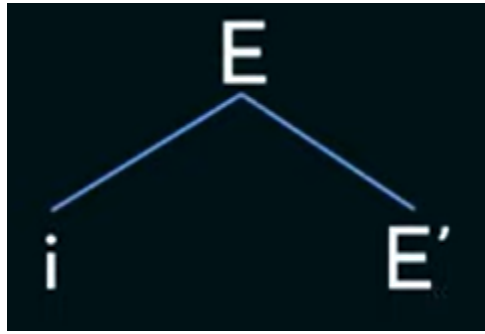
```
1. E()  
2. {  
3.     if(look_ahead=='i')  
4.     {  
5.         match('i');  
6.         E'();  
7.     }  
8. }
```

```
1. E'()  
2. {  
3.     if(look_ahead=='+')  
4.     {  
5.         match('+');  
6.         match('i');  
7.         E'();  
8.     }  
9.     else  
10.         return;  
11. }
```

```
1. match(char c)  
2. {  
3.     if(look_ahead==c)  
4.         look_ahead = getchar();  
5.     else  
6.         printf("ERROR!");  
7. }
```

```
1. main()  
2. {  
3.     E();  
4.     if(look_ahead=='$')  
5.         printf("Parsing Successful!");  
6. }
```





Input:  $i + i \$$

