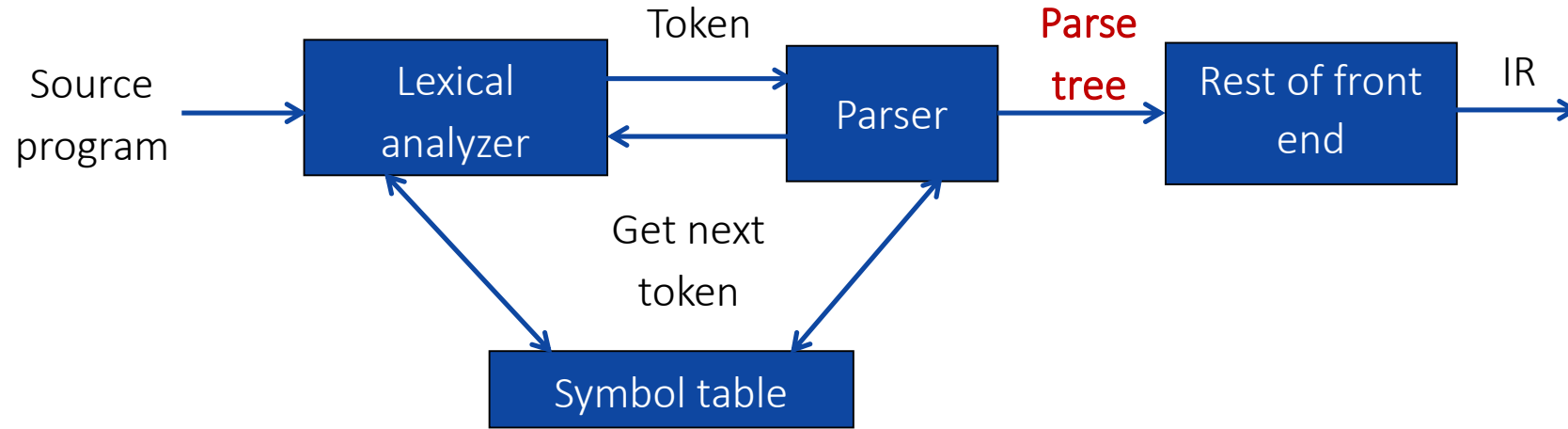


Module 2 – Syntax Analysis

Role of parser



-
- Parser obtains a string of token from the lexical analyzer and reports **syntax error** if any otherwise generates **syntax tree**.
 - There are two types of parser:
 1. Top-down parser
 2. Bottom-up parser

Context free grammar

- A context free grammar (CFG) is a 4-tuple $G = (V, \Sigma, S, P)$ where,
 - V is finite set of non terminals,
 - Σ is disjoint finite set of terminals,
 - S is an element of V and it's a start symbol,
 - P is a finite set formulas of the form $A \rightarrow \alpha$ where $A \in V$ and $\alpha \in (V \cup \Sigma)^*$
-

► Nonterminal symbol:

- ➡ The name of syntax category of a language, e.g., noun, verb, etc.
- ➡ The It is written as a **single capital letter**, or as a **name enclosed between < ... >**, e.g., A or <Noun>

<Noun Phrase> \rightarrow <Article><Noun>

<Article> \rightarrow a | an | the

<Noun> \rightarrow boy | apple

Context free grammar

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 - S is an element of V and it's a start symbol,
 - P is a finite set formulas of the form $A \rightarrow \alpha$ where $A \in V$ and $\alpha \in$
-

▶ $(V \cup \Sigma)^*$ Terminal symbol:

- A symbol in the alphabet.
- It is denoted by lower case letter and punctuation marks used in language.

<Noun Phrase> \rightarrow <Article><Noun>

<Article> \rightarrow a | an | the

<Noun> \rightarrow boy | apple

Context free grammar

- A context free grammar (CFG) is a 4-tuple $G = (V, \Sigma, S, P)$ where,
 - V is finite set of non terminals,
 - Σ is disjoint finite set of terminals,
 - S is an element of V and it's a **start symbol**,
 - P is a finite set formulas of the form $A \rightarrow \alpha$ where $A \in V$ and $\alpha \in (V \cup \Sigma)^*$
-

► Start symbol:

→ First nonterminal symbol of the grammar is called start symbol.

<Noun Phrase> \rightarrow <Article><Noun>

<Article> \rightarrow a | an | the

<Noun> \rightarrow boy | apple

Context free grammar

- A context free grammar (CFG) is a 4-tuple $G = (V, \Sigma, S, P)$ where,
 - V is finite set of non terminals,
 - Σ is disjoint finite set of terminals,
 - S is an element of V and it's a start symbol,
 - P is a **finite set formulas** of the form $A \rightarrow \alpha$ where $A \in V$ and $\alpha \in (V \cup \Sigma)^*$
-

► Production:

↪ A production, also called a rewriting rule, is a rule of grammar. It has the form of

A nonterminal symbol \rightarrow String of terminal and nonterminal symbols

$\langle \text{Noun Phrase} \rangle \rightarrow \langle \text{Article} \rangle \langle \text{Noun} \rangle$

$\langle \text{Article} \rangle \rightarrow a \mid an \mid the$

$\langle \text{Noun} \rangle \rightarrow boy \mid apple$

Example: Grammar

Write terminals, non terminals, start symbol, and productions for following grammar.

$$E \rightarrow E \ O \ E \mid (E) \mid -E \mid id$$
$$O \rightarrow + \mid - \mid * \mid / \mid \uparrow$$

Terminals: $id \ + \ - \ * \ / \ \uparrow \ (\)$

Non terminals: E, O

Start symbol: E

Productions: $E \rightarrow E \ O \ E \mid (E) \mid -E \mid id$

$$O \rightarrow + \mid - \mid * \mid / \mid \uparrow$$

Derivation & Ambiguity

Derivation

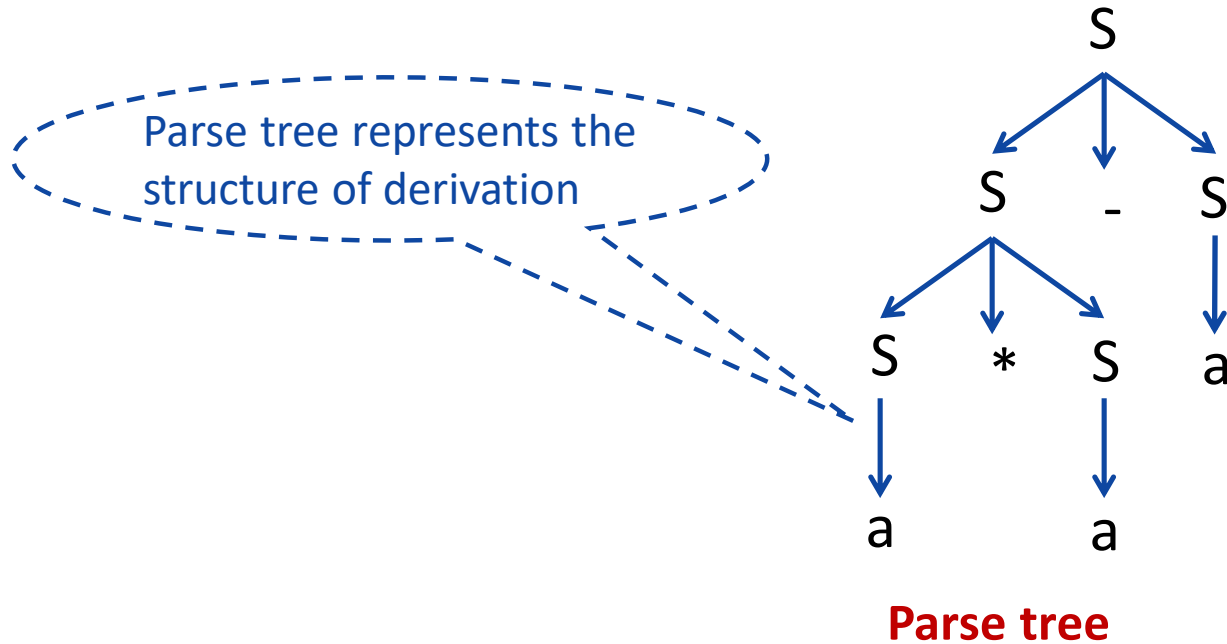
- Derivation is used to find whether the string belongs to a given grammar or not.
- Types of derivations are:
 1. Leftmost derivation
 2. Rightmost derivation

Leftmost derivation

- A derivation of a string W in a grammar G is a left most derivation if at every step the **left most non terminal** is replaced.
- Grammar: $S \rightarrow S+S \mid S-S \mid S*S \mid S/S \mid a$ Output string: a^*a-a

S
 $\rightarrow \underline{S}-S$
 $\rightarrow S*\underline{S}-S$
 $\rightarrow a^*S-\underline{S}$
 $\rightarrow a^*a-S$
 $\rightarrow a^*a-a$

Leftmost Derivation

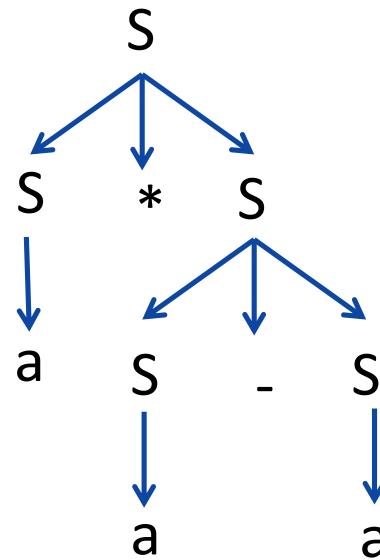


Rightmost derivation

- A derivation of a string W in a grammar G is a right most derivation if at every step the right most non terminal is replaced.
- It is all called canonical derivation.
- Grammar: $S \rightarrow S+S \mid S-S \mid S*S \mid S/S \mid a$ Output string: $a*a-a$

S
 $\rightarrow S*\underline{S}$
 $\rightarrow S*\underline{S}-S$
 $\rightarrow \underline{S}*S-a$
 $\rightarrow S*a-a$
 $\rightarrow a*a-a$

Rightmost Derivation



Parse Tree

Exercise: Derivation

1. Perform leftmost derivation and draw parse tree.

$$S \rightarrow A1B$$

$$A \rightarrow 0A \mid \epsilon$$

$$B \rightarrow 0B \mid 1B \mid \epsilon$$

Output string: 1001

2. Perform leftmost derivation and draw parse tree.

$$S \rightarrow 0S1 \mid 01 \quad \text{Output string: 000111}$$

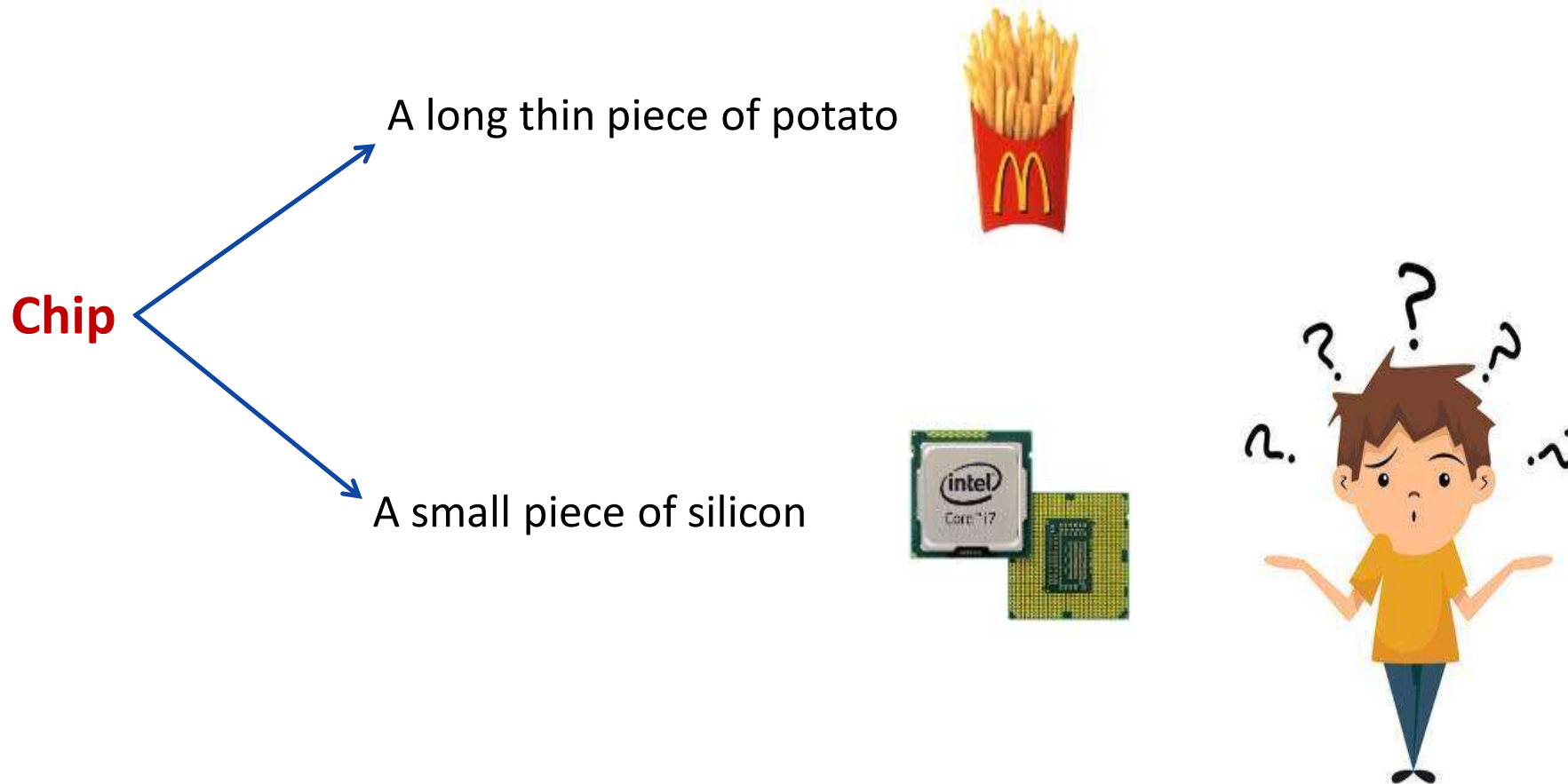
3. Perform rightmost derivation and draw parse tree.

$$E \rightarrow E+E \mid E * E \mid \text{id} \mid (E) \mid -E$$

Output string: id + id * id

Ambiguity

- Ambiguity, is a word, phrase, or statement which contains **more than one meaning**.



Ambiguity

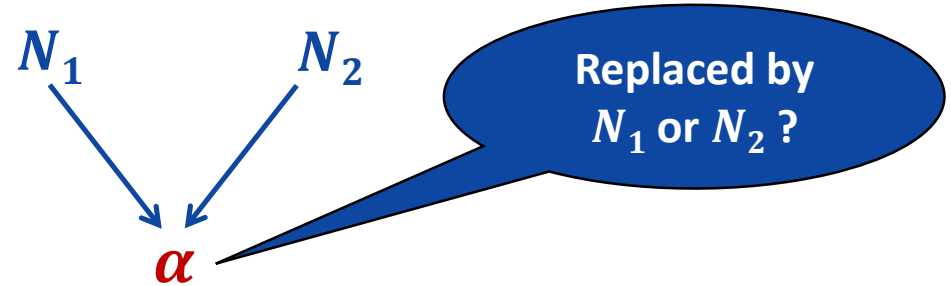
- In formal language grammar, ambiguity would arise if identical string can occur on the RHS of two or more productions.

- Grammar:

$$N_1 \rightarrow \alpha$$

$$N_2 \rightarrow \alpha$$

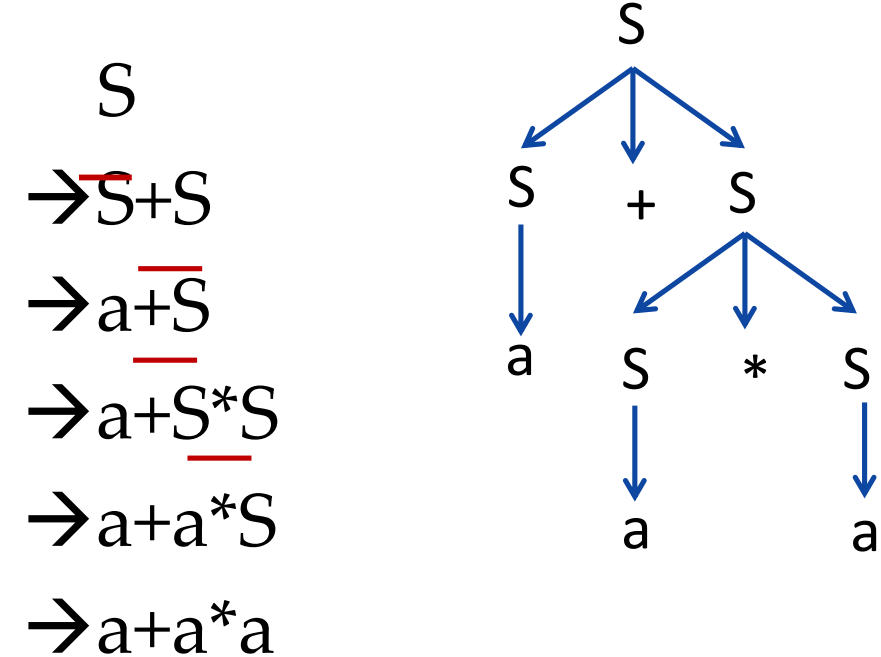
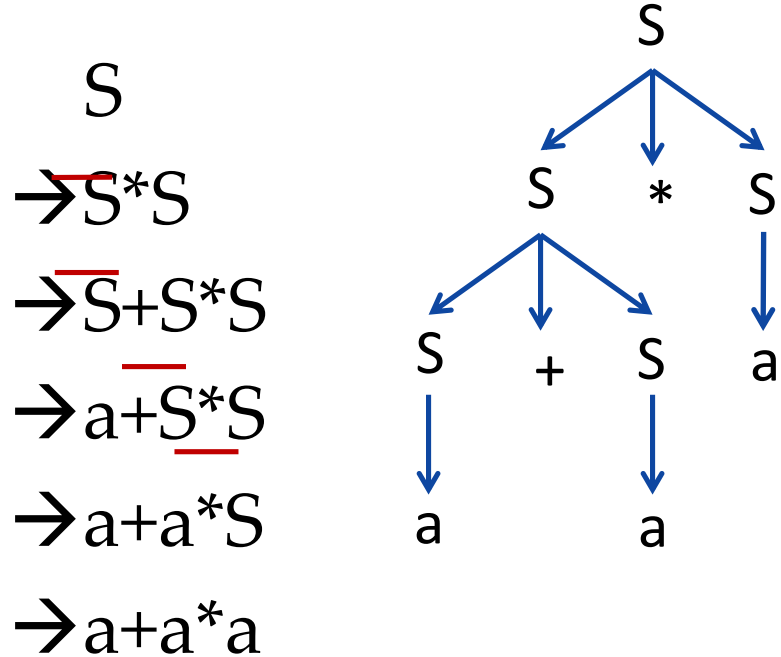
- α can be derived from either N_1 or N_2



Ambiguous grammar

- Ambiguous grammar is one that produces more than one leftmost or more than one rightmost derivation for the same sentence.
- Grammar: $S \rightarrow S+S \mid S*S \mid (S) \mid a$

Output string: $a+a*a$



- Here, Two leftmost derivation for string $a+a*a$ is possible hence, above grammar is ambiguous.

Exercise: Ambiguous Grammar

Check Ambiguity in following grammars:

1. $S \rightarrow aS \mid Sa \mid \epsilon$ (output string: aaaa)
2. $S \rightarrow aSbS \mid bSaS \mid \epsilon$ (output string: abab)
3. $S \rightarrow SS^+ \mid SS^* \mid a$ (output string: aa+a*)
4. $\langle \text{exp} \rangle \rightarrow \langle \text{exp} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle$
 $\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle * \langle \text{letter} \rangle \mid \langle \text{letter} \rangle$
 $\langle \text{letter} \rangle \rightarrow a \mid b \mid c \mid \dots \mid z$ (output string: a+b*c)
5. Prove that the CFG with productions: $S \rightarrow a \mid Sa \mid bSS \mid SSb \mid SbS$ is ambiguous (Hint: consider output string yourself)

Left recursion & Left factoring

Left recursion

- A grammar is said to be **left recursive** if it has a non terminal A such that there is a derivation $A \rightarrow A\alpha$ for some string α .

$$A \rightarrow A\alpha \mid \quad \longrightarrow \quad \begin{array}{l} A \rightarrow A' \\ A' \rightarrow \alpha A' \mid \epsilon \end{array}$$

Examples: Left recursion elimination

$E \rightarrow E+T \mid T$

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \varepsilon$

$T \rightarrow T*F \mid F$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \varepsilon$

$X \rightarrow X\%Y \mid Z$

$X \rightarrow ZX'$

$X' \rightarrow \%YX' \mid \varepsilon$

Exercise: Left recursion

1. $A \rightarrow Abd \mid Aa \mid a$

$B \rightarrow Be \mid b$

2. $A \rightarrow AB \mid AC \mid a \mid b$

3. $S \rightarrow A \mid B$

$A \rightarrow ABC \mid Acd \mid a \mid aa$

$B \rightarrow Bee \mid b$

4. $\text{Exp} \rightarrow \text{Exp} + \text{term} \mid \text{Exp} - \text{term} \mid \text{term}$

Left factoring

Left factoring is a grammar transformation that is useful for producing a grammar suitable for predictive parsing.

$$S \rightarrow aAB \mid aCD$$

$$\begin{aligned} S &\rightarrow aS' \\ S' &\rightarrow AB \mid CD \end{aligned}$$

$$A \rightarrow xByA \mid xByAzA \mid a$$

$$\begin{aligned} A &\rightarrow xByAA' \mid a \\ A' &\rightarrow \epsilon \mid zA \end{aligned}$$

$$A \rightarrow aAB \mid aA \mid a$$

$$\begin{aligned} A &\rightarrow aA' \\ A' &\rightarrow AB \mid A \mid \epsilon \\ A' &\rightarrow AA'' \mid \epsilon \\ A'' &\rightarrow B \mid \epsilon \end{aligned}$$

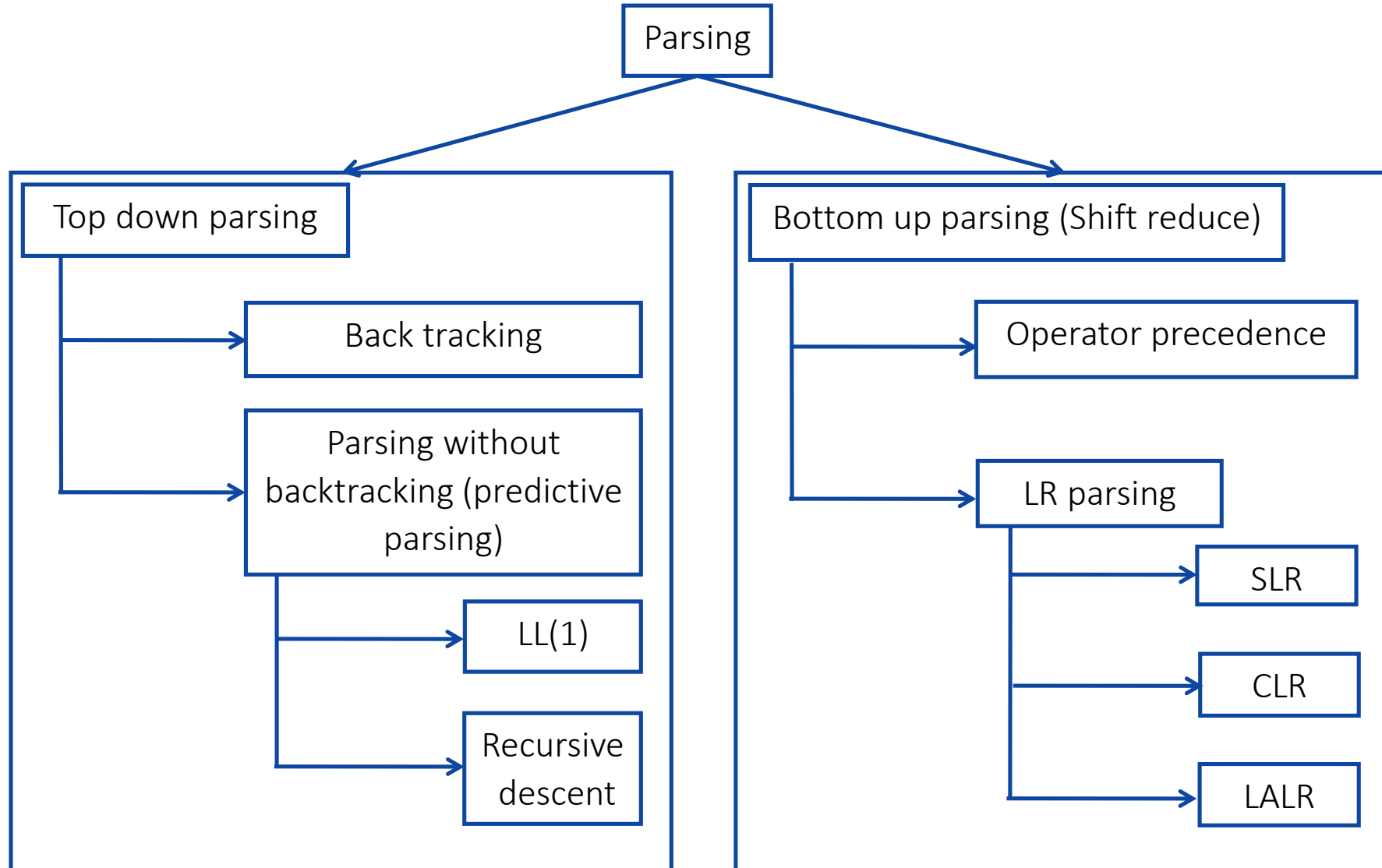
Exercise

1. $S \rightarrow iEtS \mid iEtSeS \mid a$
2. $A \rightarrow ad \mid a \mid ab \mid abc \mid x$

Parsing

- Parsing is a technique that takes input string and produces output either a **parse tree** if string is valid sentence of grammar, or an **error message** indicating that string is not a valid.
- Types of parsing are:
 1. **Top down parsing:** In top down parsing parser build parse tree from top to bottom.
 2. **Bottom up parsing:** Bottom up parser starts from leaves and work up to the root.

Classification of parsing methods

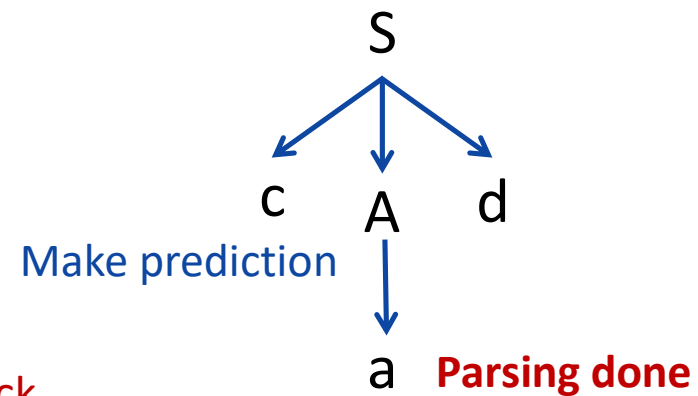
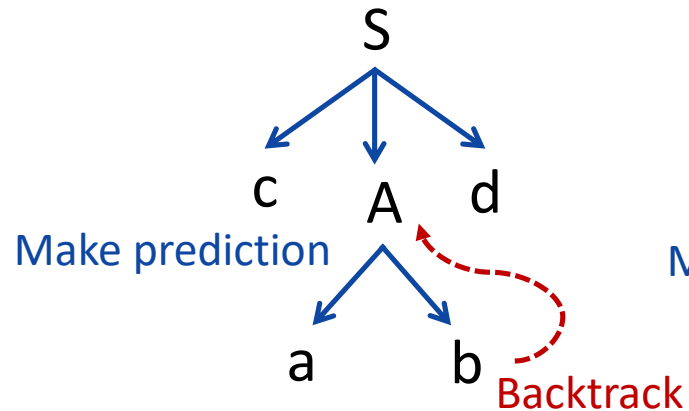
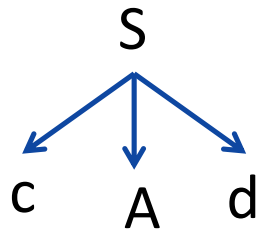


Backtracking

- In backtracking, expansion of nonterminal symbol we choose one alternative and if any mismatch occurs then we try another alternative.

• Grammar: $S \rightarrow cAd$
 $A \rightarrow ab \mid a$

Input string: cad



Exercise

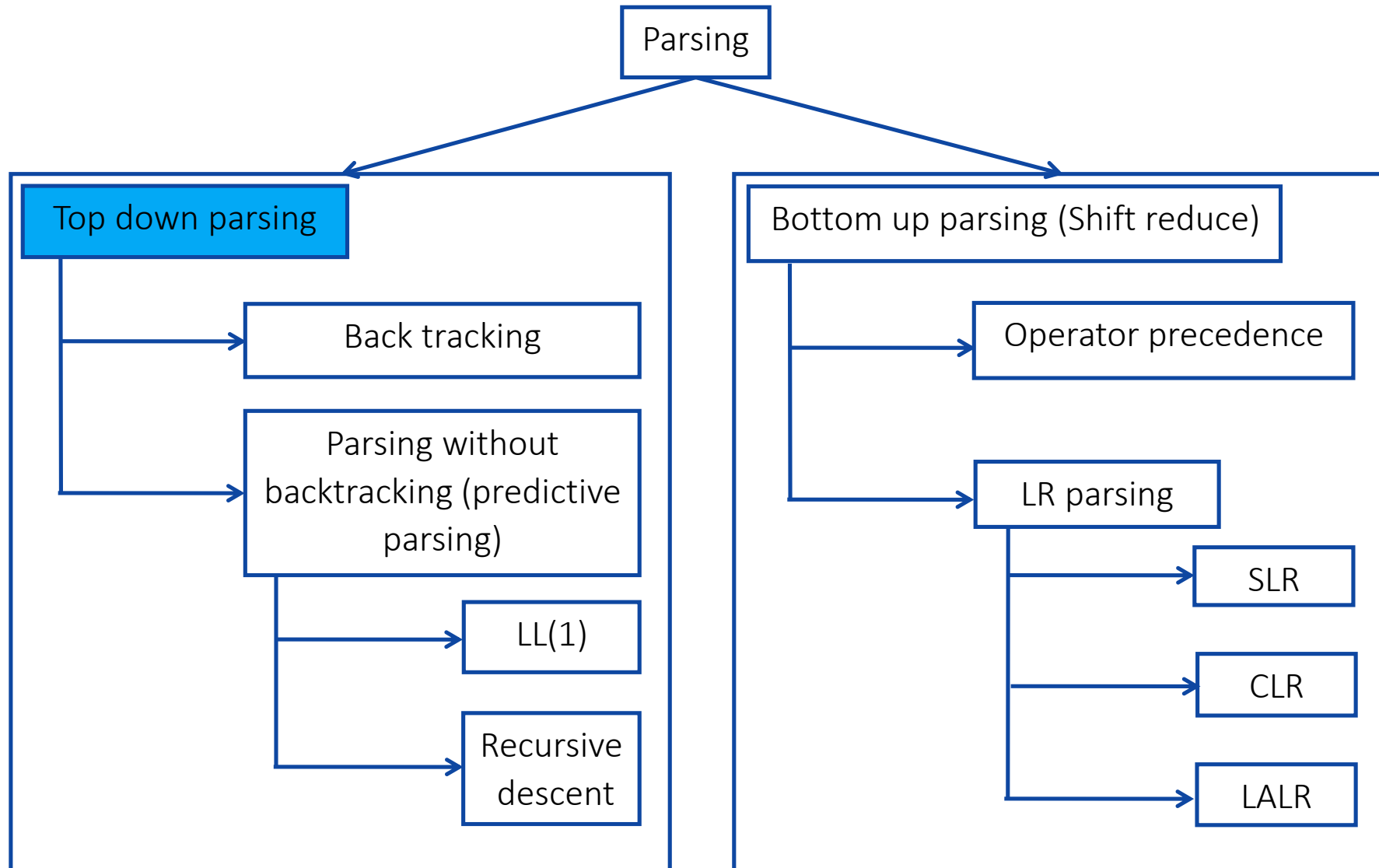
1. $E \rightarrow 5+T \mid 3-T$

$$T \rightarrow V \mid V*V \mid V+V$$

$$V \rightarrow a \mid b$$

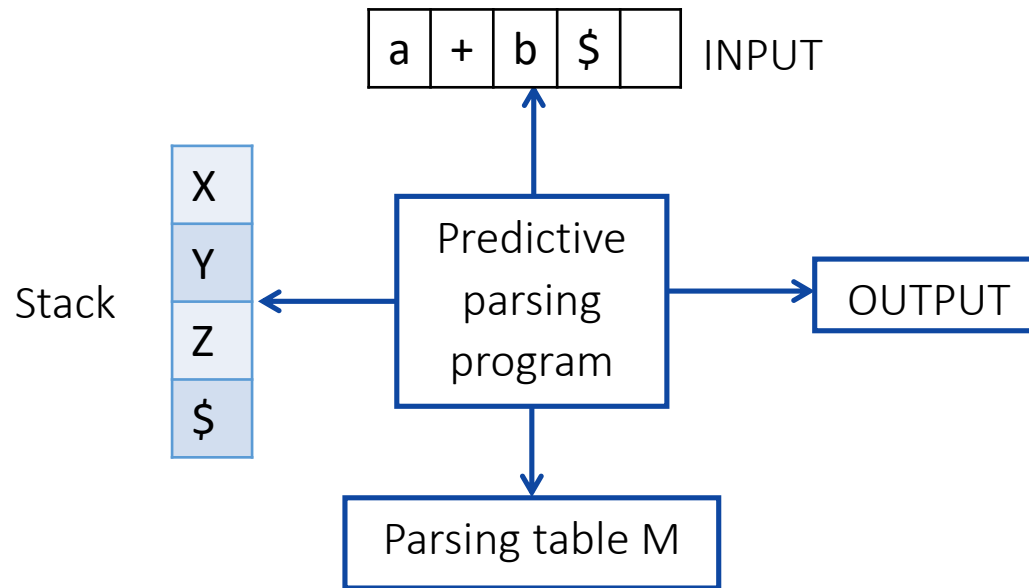
String: 3-a+b

Parsing Methods



LL(1) parser (predictive parser)

- LL(1) is non recursive top down parser.
 1. First **L** indicates input is scanned from left to right.
 2. The second **L** means it uses leftmost derivation for input string
 3. **1** means it uses only input symbol to predict the parsing process.



LL(1) parsing (predictive parsing)

Steps to construct LL(1) parser

1. Remove left recursion / Perform left factoring (if any).
2. Compute FIRST and FOLLOW of non terminals.
3. Construct predictive parsing table.
4. Parse the input string using parsing table.

Rules to compute first of non terminal

1. If $A \rightarrow \alpha$ and α is terminal, add α to $FIRST(A)$.
2. If $A \rightarrow \epsilon$, add ϵ to $FIRST(A)$.
3. If X is nonterminal and $X \rightarrow Y_1 Y_2 \dots Y_k$ is a production, then place a in $FIRST(X)$ if for some i , a is in $FIRST(Y_i)$, and ϵ is in all of $FIRST(Y_1), \dots, FIRST(Y_{i-1})$; that is $Y_1 \dots Y_{i-1} \Rightarrow \epsilon$. If ϵ is in $FIRST(Y_j)$ for all $j = 1, 2, \dots, k$ then add ϵ to $FIRST(X)$.

Everything in $FIRST(Y_1)$ is surely in $FIRST(X)$ If Y_1 does not derive ϵ , then we do nothing more to $FIRST(X)$, but if $Y_1 \Rightarrow \epsilon$, then we add $FIRST(Y_2)$ and so on.

Rules to compute first of non terminal

Simplification of Rule 3

If $A \rightarrow Y_1 Y_2 \dots Y_K$,

- If Y_1 does not derive ϵ then, $FIRST(A) = FIRST(Y_1)$

- If Y_1 derives ϵ then,

$$FIRST(A) = FIRST(Y_1) - \epsilon \cup FIRST(Y_2)$$

- If Y_1 & Y_2 derives ϵ then,

$$FIRST(A) = FIRST(Y_1) - \epsilon \cup FIRST(Y_2) - \epsilon \cup FIRST(Y_3)$$

- If Y_1, Y_2 & Y_3 derives ϵ then,

$$FIRST(A) = FIRST(Y_1) - \epsilon \cup FIRST(Y_2) - \epsilon \cup FIRST(Y_3) - \epsilon \cup FIRST(Y_4)$$

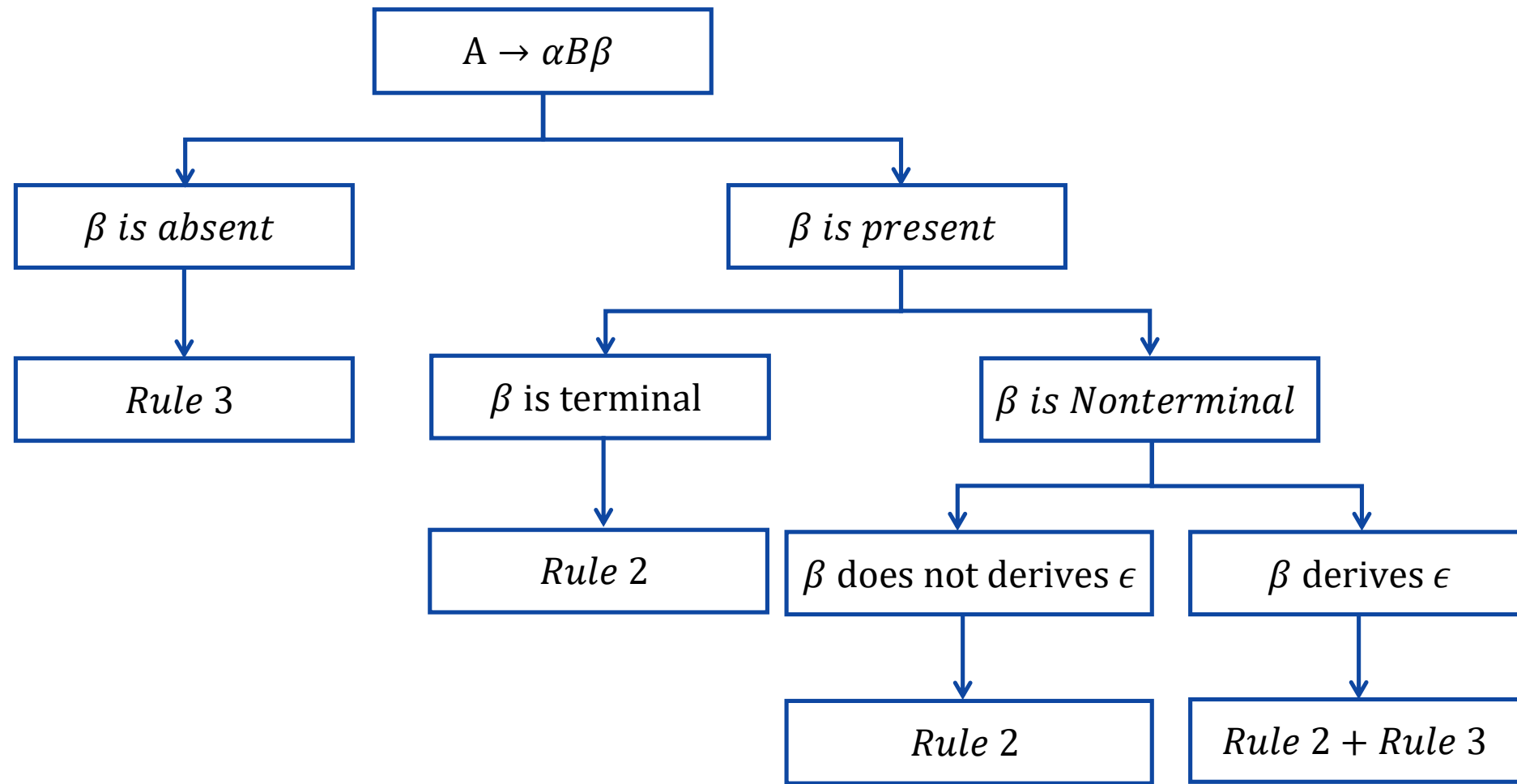
- If $Y_1, Y_2, Y_3 \dots Y_K$ all derives ϵ then,

$$FIRST(A) = FIRST(Y_1) - \epsilon \cup FIRST(Y_2) - \epsilon \cup FIRST(Y_3) - \epsilon \cup FIRST(Y_4) - \epsilon \cup \dots \dots \dots FIRST(Y_K) \text{ (note: if all non terminals derives } \epsilon \text{ then add } \epsilon \text{ to } FIRST(A))$$

Rules to compute FOLLOW of non terminal

1. Place \$ in $follow(S)$. (S is start symbol)
2. If $A \rightarrow \alpha B \beta$, then everything in $FIRST(\beta)$ except for ϵ is placed in $FOLLOW(B)$
3. If there is a production $A \rightarrow \alpha B$ or a production $A \rightarrow \alpha B \beta$ where $FIRST(\beta)$ contains ϵ then everything in $FOLLOW(A) = FOLLOW(B)$

How to apply rules to find FOLLOW of non terminal?



Rules to construct predictive parsing table

1. For each production $A \rightarrow \alpha$ of the grammar, do steps 2 and 3.
2. For each terminal a in $first(\alpha)$, Add $A \rightarrow \alpha$ to $M[A, a]$.
3. If ϵ is in $first(\alpha)$, Add $A \rightarrow \alpha$ to $M[A, b]$ for each terminal b in $FOLLOW(B)$. If ϵ is in $first(\alpha)$, and $\$$ is in $FOLLOW(A)$, add $A \rightarrow \alpha$ to $M[A, \$]$.
4. Make each undefined entry of M be error.

Example-1: LL(1) parsing

$S \rightarrow aBa$

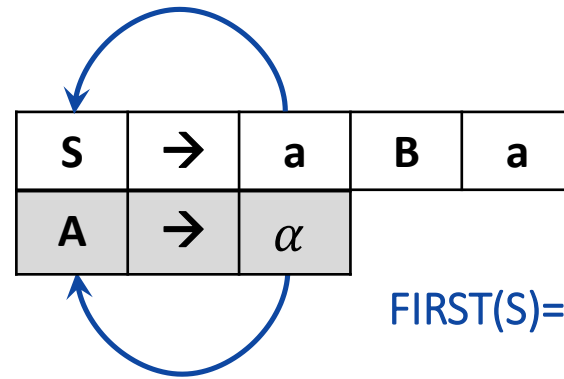
$B \rightarrow bB \mid \epsilon$

Step 1: Not required

Step 2: Compute FIRST

First(S)

$S \rightarrow aBa$

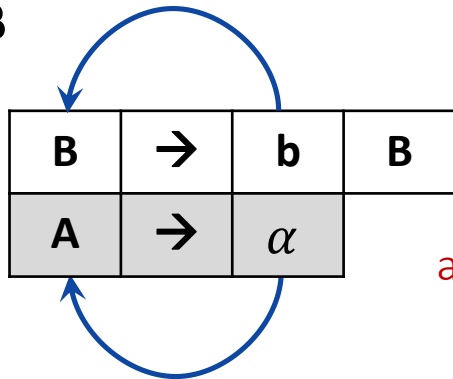


Rule 1
add α to $FIRST(A)$

$FIRST(S) = \{ a \}$

First(B)

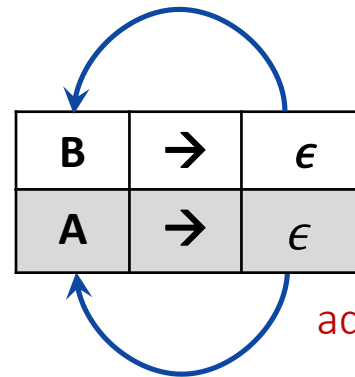
$B \rightarrow bB$



Rule 1
add α to $FIRST(A)$

$FIRST(B) = \{ b, \epsilon \}$

$B \rightarrow \epsilon$



Rule 2
add ϵ to $FIRST(A)$

NT	First
S	
B	

Example-1: LL(1) parsing

$S \rightarrow aBa$

$B \rightarrow bB \mid \epsilon$

Step 2: Compute FOLLOW

Follow(S)

Rule 1: Place \$ in FOLLOW(S)

$\text{Follow}(S) = \{ \$ \}$

NT	First	Follow
S	{a}	
B	{b, ϵ }	

Follow(B)

$S \rightarrow aBa$

S	→	a	B	a
A	→	α	B	β

Rule 2
 $\text{First}(\beta) = \epsilon$

$B \rightarrow bB$

B	→	b	B
A	→	α	B

Rule 3
 $\text{Follow}(A) = \text{follow}(B)$

$\text{Follow}(B) = \{ a \}$

Example-1: LL(1) parsing

$S \rightarrow aBa$

$B \rightarrow bB \mid \epsilon$

Step 3: Prepare predictive parsing table

NT	First	Follow
S	{a}	{\$}
B	{b, ϵ }	{a}

NT	Input Symbol		
	a	b	\$
S			
B			

$S \rightarrow aBa$

$a = \text{FIRST}(aBa) = \{ a \}$

$M[S, a] = S \rightarrow aBa$

Rule: 2

$A \rightarrow \alpha$

$a = \text{first}(\alpha)$

$M[A, a] = A \rightarrow \alpha$

Example-1: LL(1) parsing

$S \rightarrow aBa$

$B \rightarrow bB \mid \epsilon$

Step 3: Prepare predictive parsing table

NT	First	Follow
S	{a}	{\$}
B	{b, ϵ }	{a}

NT	Input Symbol		
	a	b	\$
S	$S \rightarrow aBa$		
B			

$B \rightarrow bB$

$a = \text{FIRST}(bB) = \{ b \}$

$M[B, b] = B \rightarrow bB$

Rule: 2

$A \rightarrow \alpha$

$a = \text{first}(\alpha)$

$M[A, a] = A \rightarrow \alpha$

Example-1: LL(1) parsing

$S \rightarrow aBa$

$B \rightarrow bB \mid \epsilon$

Step 3: Prepare predictive parsing table

NT	First	Follow
S	{a}	{\$}
B	{b, ϵ }	{a}

NT	Input Symbol		
	a	b	\$
S	$S \rightarrow aBa$		
B		$B \rightarrow bB$	

$B \rightarrow \epsilon$

$b = \text{FOLLOW}(B) = \{ a \}$

$M[B, a] = B \rightarrow \epsilon$

Rule: 3

$A \rightarrow \alpha$

$b = \text{follow}(A)$

$M[A, b] = A \rightarrow \alpha$

Exercise: LL(1) parsing

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

$C \rightarrow cS \mid \epsilon$

$E \rightarrow E+T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow (E) \mid \text{id}$

$, \epsilon \}$

Q1: Find out whether the following grammar is LL(1):

$$S \rightarrow aSbS \mid bSaS \mid \epsilon$$

Sol. FIRST(S): {a, b, ϵ }

FOLLOW(S): {\$, b, a}



Not LL(1) Grammar

	a	b	\$
S	<div>$S \rightarrow aSbS$ $S \rightarrow \epsilon$</div>	<div>$S \rightarrow bSaS$ $S \rightarrow \epsilon$</div>	$S \rightarrow \epsilon$

Check whether the following Grammar is LL(1).

1.

$S \rightarrow aBa$

$B \rightarrow bB \mid \epsilon$

2.

$S \rightarrow aSbS \mid bSaS \mid \epsilon$

3.

$S \rightarrow (S) \mid \epsilon$

4.

$S \rightarrow iEtS \mid iEtSeS \mid a$

$E \rightarrow b$

5.

$S \rightarrow A$

$A \rightarrow Bb \mid Cd$

$B \rightarrow aB \mid \epsilon$

$C \rightarrow cC \mid \epsilon$

6.

$S \rightarrow (L) \mid a$

$L \rightarrow L,S \mid S$

Note: Ensure that each cell in the parsing table contains at most one production rule. If any cell contains more than one production rule, the grammar is not LL(1).

Q2: Find out whether the following grammar is LL(1):

$$S \rightarrow (S) \mid \varepsilon$$

Sol. FIRST(S): $\{ (, \varepsilon \}$

FOLLOW(S): $\{ \$,) \}$

 LL(1) Grammar

	()	\$
S	$S \rightarrow (S)$	$S \rightarrow \varepsilon$	$S \rightarrow \varepsilon$

Q3: Find out whether the following grammar is LL(1):

$$S \rightarrow AaAb \mid BbBa$$

$$A \rightarrow \varepsilon$$

$$B \rightarrow \varepsilon$$

LL(1) Grammar

FIRST FOLLOW

Sol.

	FIRST	FOLLOW
$S \rightarrow AaAb \mid BbBa$	$\{a, b\}$	$\{\$ \}$
$A \rightarrow \varepsilon$	$\{\varepsilon\}$	$\{a, b\}$
$B \rightarrow \varepsilon$	$\{\varepsilon\}$	$\{b, a\}$

	a	b	\$
S	$S \rightarrow AaAb$	$S \rightarrow BbBa$	
A	$A \rightarrow \varepsilon$	$A \rightarrow \varepsilon$	
B	$B \rightarrow \varepsilon$	$B \rightarrow \varepsilon$	

Q4: Find out whether the following grammar is LL(1):

$$\left. \begin{array}{l} S \rightarrow A \mid a \\ A \rightarrow a \end{array} \right\}$$

Not LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow A \mid a$	{a}	{\$}
$A \rightarrow a$	{a}	{\$}

Q5: Find out whether the following grammar is LL(1):

$$S \rightarrow aB \mid \epsilon$$

$$B \rightarrow bC \mid \epsilon$$

$$C \rightarrow cS \mid \epsilon$$

LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow aB \mid \epsilon$	$\{a, \epsilon\}$	$\{\$, \epsilon\}$
$B \rightarrow bC \mid \epsilon$	$\{b, \epsilon\}$	$\{\$, \epsilon\}$
$C \rightarrow cS \mid \epsilon$	$\{c, \epsilon\}$	$\{\$, \epsilon\}$

	a	b	c	\$
S	$S \rightarrow aB$			$S \rightarrow \epsilon$
B		$B \rightarrow bC$		$B \rightarrow \epsilon$
C			$C \rightarrow cS$	$C \rightarrow \epsilon$

Q1: Find out whether the following grammar is LL(1):

$$S \rightarrow AB$$

$$A \rightarrow a \mid \varepsilon$$

$$B \rightarrow b \mid \varepsilon$$

LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow AB$	$\{a, b, \varepsilon\}$	$\{\$ \}$
$A \rightarrow a \mid \varepsilon$	$\{a, \varepsilon\}$	$\{b, \$ \}$
$B \rightarrow b \mid \varepsilon$	$\{b, \varepsilon\}$	$\{\$ \}$

	a	b	\$
S	$S \rightarrow AB$	$S \rightarrow AB$	$S \rightarrow AB$
A	$A \rightarrow a$	$A \rightarrow \varepsilon$	$A \rightarrow \varepsilon$
B		$B \rightarrow b$	$B \rightarrow \varepsilon$

Q2: Find out whether the following grammar is LL(1):

$$S \rightarrow aSA \mid \varepsilon$$

$$A \rightarrow c \mid \varepsilon$$

Not LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow aSA \mid \varepsilon$	$\{a, \varepsilon\}$	$\{\$, c\}$
$A \rightarrow c \mid \varepsilon$	$\{c, \varepsilon\}$	$\{\$, c\}$

	a	c	\$
S	$S \rightarrow aSA$	$S \rightarrow \varepsilon$	$S \rightarrow \varepsilon$
A		$A \rightarrow c$ $A \rightarrow \varepsilon$	$A \rightarrow \varepsilon$

Q3: Find out whether the following grammar is LL(1):

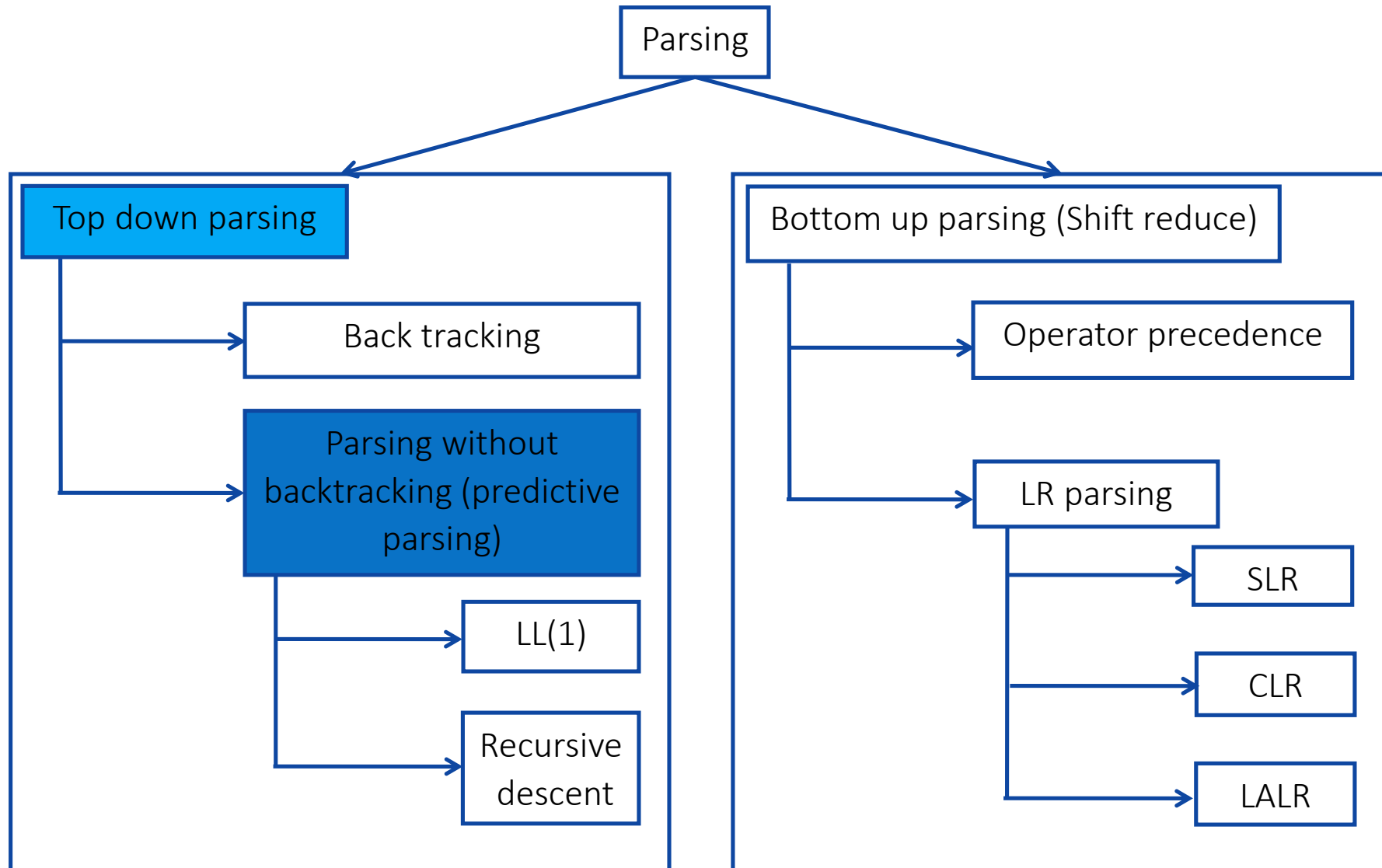
FIRST FOLLOW

Sol.

$S \rightarrow A$	$\{a, b, c, d\}$	$\{\$ \}$
$A \rightarrow Bb \mid Cd$	$\{a, b, c, d\}$	$\{\$ \}$
$B \rightarrow aB \mid \epsilon$	$\{a, \epsilon\}$	$\{b\}$
$C \rightarrow cC \mid \epsilon$	$\{c, \epsilon\}$	$\{d\}$

	a	b	c	d	\$
S	$S \rightarrow A$	$S \rightarrow A$	$S \rightarrow A$	$S \rightarrow A$	
A	$A \rightarrow Bb$	$A \rightarrow Bb$	$A \rightarrow Cd$	$A \rightarrow Cd$	
B	$B \rightarrow aB$	$B \rightarrow \epsilon$			
C			$C \rightarrow cC$	$C \rightarrow \epsilon$	

Parsing methods



Recursive descent parsing

- A top down parsing that executes a set of recursive procedure to process the input without backtracking is called recursive descent parser.
- There is a procedure for each non terminal in the grammar.
- Consider RHS of any production rule as definition of the procedure.
- As it reads expected input symbol, it advances input pointer to next position.

Consider the following grammar having rules,

$$E \rightarrow iE'$$

$$E' \rightarrow +iE' \mid \varepsilon$$

$E \rightarrow iE'$
 $E' \rightarrow +iE' \mid \varepsilon$

Recursive Descent Parser:

```
1.  E()  
2.  {  
3.      if(look_ahead=='i')  
4.      {  
5.          match('i');  
6.          E'();  
7.      }  
8.  }
```

$E \rightarrow iE'$
 $E' \rightarrow +iE' \mid \varepsilon$

```
1.  E'()  
2.  {  
3.      if(look_ahead=='+')  
4.      {  
5.          match('+');  
6.          match('i');  
7.          E'();  
8.      }  
9.      else  
10.         return;  
11. }
```

Recursive Descent Parser:

$E \rightarrow iE'$

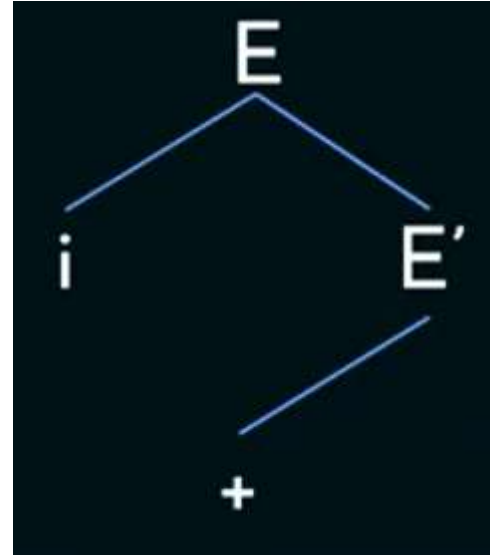
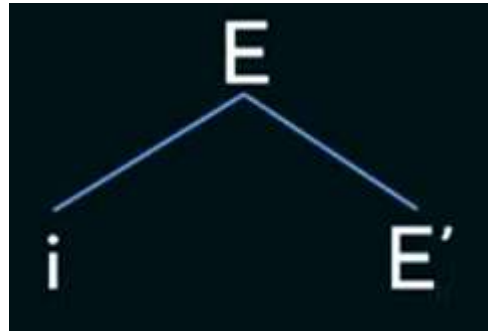
$E' \rightarrow +iE' \mid \varepsilon$

```
1. E()  
2. {  
3.     if(look_ahead=='i')  
4.     {  
5.         match('i');  
6.         E'();  
7.     }  
8. }
```

```
1. E'()  
2. {  
3.     if(look_ahead=='+')  
4.     {  
5.         match('+');  
6.         match('i');  
7.         E'();  
8.     }  
9.     else  
10.         return;  
11. }
```

```
1. match(char c)  
2. {  
3.     if(look_ahead==c)  
4.         look_ahead = getchar();  
5.     else  
6.         printf("ERROR!");  
7. }
```

```
1. main()  
2. {  
3.     E();  
4.     if(look_ahead=='$')  
5.         printf("Parsing Successful!");  
6. }
```



Input: $i + i \$$

