

Measuring Modes on Strings: Part 1

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April 27, 2021

1 Introduction

This report details an investigation into the phenomena observed on a vibrating string. Several experiments took place, using a guitar, as guitars feature strings under tension that can freely vibrate. The frequency and amplitude of vibrations can be easily and precisely adjusted on a well-intonated guitar by fretting the strings along the fingerboard. Results are tabulated and plotted on graphs using MATLAB.

2 Theory

A string vibrates with a fundamental, or in music theory tonic, frequency. This fundamental frequency is related to the length L of a vibrating string:

$$f_1 = \frac{c}{2L} \tag{1}$$

The mass of a string and its length can be used to find a mass per unit length M . This mass per unit length can then be formulated with it's tension T to find the speed of a transverse wave on a string:

$$c = \sqrt{\frac{T}{M}} \tag{2}$$

Equation 2 allows us to formulate:

$$f_1 = \frac{\sqrt{\frac{T}{M}}}{2L} \tag{3}$$

If the ends of a string under tension are fixed, the fundamental frequency will have a wavelength equal to half the string's length. The frequencies of higher harmonics of the fundamental frequency are integer multiples of the fundamental frequency:

$$f_n = \frac{c}{2L}n \quad (4)$$

3 Experiment One

3.1 Methodology

In experiment one, the relationship between resonant frequency and string length were investigated. Preliminary measurements of mass and length were taken in order to find a mass per unit length $M = 0.012618\text{kg m}^{-1}$. Then the low E string was played in an open position, thus at it's maximum string length and at a frequency of 83Hz. Using equation 4 the higher harmonics $n = 1, 2, 3...$ are predicted for the vibrating open E string. The sound of the vibrating string was captured using a microphone and passed into a Simulink frequency spectrum analyser. From this spectrum analyser the frequencies of the fundamental tone and it's higher harmonics could be ascertained.