

70051 rac101 2
t5 dg4217 v1



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dg4217

Exercise Information

Module: 70051 Introduction to Symbolic Artificial Intelligence (MSc AI)

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Exercise: 2 (CW)

Due: Tue - 03 Nov 2020

Title: Logic

Assessment: Individual

FAO: Craven, Robert (rac101)

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Student Declaration - Version 1

- I declare that this final submitted version is my unaided work.

Signed: (electronic signature) Date: 2020-11-03 18:36:46

For Markers only: (circle appropriate grade)

GALKINA, (dg4217)	Daria	01379079	t5	2020-11-03 18:36:46	A* A B C D E F
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i. p: Michel is either fulfilled or rich

q: Michel will live another 5 years

$$(\neg p \rightarrow \neg q)$$

ii. p: snowstorm arrives

q: Raheem will wear his boots

$$((p \rightarrow q) \wedge p)$$

iii. p: Arika is on set

q: Toshiro is on set

r: fuming will begin

s: caterers cleared out

$$((p \wedge q) \rightarrow r) \leftrightarrow s$$

iv. p: Irad arrived

q: Sarah arrived

$$((p \vee \neg q) \wedge (\neg(p \wedge \neg q)))$$

v. p: Herbert heard the performance

q: Anne-Sophie heard the performance

r: Anne-Sophie answered her phone call

$$(\neg r \rightarrow \neg(p \wedge q))$$

2. i. Satisfiability of a propositional formula A:

Propositional formula is satisfiable if there is some v , such that

$$h_v(A) = t$$

where v is the atomic evaluation function &

h_v is the propositional evaluation function based on v .

ii ~~What is~~ Logical Equivalence of two propositional formulas $A \& B$:

Two propositional formulas are logically equivalent, if for every v ,

$$h_v(A) = h_v(B), \text{ where } v \models h_v \text{ defined above.}$$

iii. $\neg A$ is satisfiable iff $\neg\neg A \neq T$

so if $\neg\neg A \equiv T \therefore h_v(\neg A) = t \rightarrow h_v(\neg\neg A) = f$. & will always be false

for $\neg A$ to be satisfiable $h_v(\neg A)$ it needs to be true in some cases

however if $\neg\neg A \equiv T$, then $h_v(\neg A)$ will always be false.

$\therefore \neg A$ is satisfiable iff $\neg\neg A \neq T$

$$\Leftrightarrow h_v(\neg A) = f \Rightarrow h_v(\neg\neg A) = t.$$

3. 2³

P	q	r	$(P \wedge \neg q \leftrightarrow \neg (\neg r \vee \neg p)) \rightarrow (\neg q \rightarrow r)$									
t	t	t	t	f	f	f	t	f	f	f	t	t
t	t	f	t	f	f	f	t	f	t	f	t	f
t	f	t	t	t	t	t	f	f	f	t	t	t
t	f	f	t	t	t	f	f	t	f	t	t	f
f	t	t	f	f	f	t	f	f	t	t	t	t
f	t	f	f	f	f	t	f	t	t	t	f	f
f	f	t	f	f	t	t	f	f	t	t	t	t
f	f	f	f	f	t	t	f	t	t	t	f	t

As there are two cases when truth table found false it is not valid,
 (however it is satisfactory)

4. i a. CNF

b. CNF

c. CNF

d. CNF

e. DNF

f. neither. $\neg p$ not literal (or DNF?)

g. CNF

h. DNF

ii. Property of Refutation-soundness \wedge -completeness of resolution derivation

Let S be in CNF. $S \text{ rescpl} \emptyset \text{ iff } S \models \perp$

It's important as based on that we can say S is satisfied iff $S \text{ H rescpl} \emptyset$
meaning that if you can't derive \emptyset from S by resolution derivation, then
 S is satisfiable: the property helps define the satisfiability for S .

iii. a. $\{\{p, s\}, \{q, r\}, \{\neg s, q\}, \{\neg p, \neg r, \neg s\}\}$

$\{\{p, s\}, \{\neg p, \neg r, \neg s\}\}$ [q was pure]

$\{\{p, s\}\}$ [$\neg r$ was pure]

(satisfiable)

b. $\{\{\neg p, q, r\}, \{\neg q\}, \{p, r, q\}, \{\neg r, q\}\}$

$\{\{\neg p, r\}, \{p, r\}, \{\neg r\}\}$ [unit propagation by unit clause $\{\neg q\}$]

$\{\{\neg p\}, \{p\}\}$ [unit propagation by unit clause $\{\neg r\}$]

$\{\{\}\}$ [unit propagation by unit clause $\{p\}$]

(unsatisfiable: \emptyset)

5. p: I'm going

q: You are going

r: Tara's going

$p \rightarrow \neg q, \neg q \rightarrow \neg r, r \vee \neg p, \neg p \rightarrow r$ therefore q.

CNF: $(p \rightarrow \neg q) \wedge (\neg q \rightarrow \neg r) \wedge (r \vee \neg p) \wedge (\neg p \rightarrow r) \wedge \{\neg q\}$

Set $\{\{\neg p, \neg q\}, \{q, \neg r\}, \{r, \neg p\}, \{\neg p, r\}, \{q\}\}$.

Let's check if the clauses where $\neg q$ is satisfiable \Rightarrow

$\{\{\neg p, \neg q\}, \{q, \neg r\}, \{r, \neg p\}, \{\neg p, r\}, \{\neg q\}\}$

$\{\{r, \neg q\}, \{q, \neg r\}, \{r\}, \{\neg q\}\}$ [resolve in all ways on p]

$\{\{q\}, \{\neg q\}\}$ [unit propagation by unit clause $\{r\}$]

$\{\}\}$ [unit propagation by unit clause $\{\neg q\}$]

\emptyset in set \therefore unsatisfiable suggesting the original argument is valid

extra

let's see: $\{\{\neg p, \neg q\}, \{q, \neg r\}, \{r, \neg p\}, \{\neg p, r\}, \{\neg q\}\}$

$\{\{r, \neg q\}, \{q, \neg r\}, \{r\}, \{\neg q\}\}$

$\{\{q\}, \{\neg q\}\}$

\therefore Satisfiable conclusion.

i. h_1 -signature:

$$C = \{\text{andrea}\}$$

$$P_1 = \{\text{aunt's agent}\} \quad \text{auntagent}(x) : \text{aunt's agent}$$

$$P_2 = \{\text{given cupcake}\} \quad \text{cupcake}(x, y) : \text{cupcake given by } x \text{ to } y$$

$$\forall X \forall Y (\text{auntagent}(X) \rightarrow \exists Z (\text{cupcake}(X, Z) \wedge Z = \text{andrea}))$$

ii. h_2 -signature

$$P_1 = \{\text{computer}\} \quad \text{computer}(x) : x \text{ is a computer}$$

$$P_2 = \{\text{connected}\} \quad \text{connected}(x, y) : \wedge (x = y) \quad \text{connect } x \text{ to } y$$

$$\exists X \forall Y (\text{computer}(X) \wedge \text{computer}(Y) \wedge \neg (\text{connected}(X, Y)) \rightarrow \text{connected}(X, Y))$$

If computer is known:

$$C = \{\text{computer}\}$$

$$P_1 = \{\text{computers}\}$$

$$P_2 = \{\text{connected}\}$$

$$\forall X (\text{computers}(X) \wedge \neg (\text{connected} \underset{x=\text{computer}}{\wedge} (X))) \wedge \neg (\text{connected}(X, X)) \rightarrow \text{connected}(\text{computer}, X)$$

iii. h_3 -signature

$$P_1 = \{\text{paint-K, paint-PL, room}\}$$

$$P_2 = \{\text{hang}\} \quad \text{hang}(x, y) : \text{hang painting } y \text{ in room } x.$$

$$\exists Y \forall Z ((\text{paint-K}(Y) \wedge \text{room}(Z) \wedge \text{hang}(Z, Y)) \rightarrow (\text{paint-PL}(X) \rightarrow \text{hang}(Z, X)))$$

If room is known then $C = \{\text{room}\}$

$$P_1 = \{\text{paint-K, paint-PL}\}$$

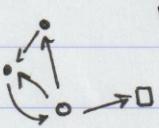
$$P_2 = \{\text{hung}\}$$

$$\forall Y (\text{paint-K}(Y) \wedge \text{hang}(\text{room}, Y)) \rightarrow \forall X (\text{paint-PL}(X) \rightarrow \text{hang}(\text{room}, X)).$$

IV. λ -signature:

$P_2 = \{ \text{loves} \}$ loves(x, y): x loves y .

$\exists X \exists Y \neg (\text{loves}(X, Y)) \rightarrow \neg (\forall X \exists Y (\text{loves}(X, Y)))$



7.

$$\text{i. } \forall X (a(X, X) \rightarrow \neg(X=j))$$

for any X that has a directed arrow pointing at it from k , X won't be j .

false: k only directs to j

$$\text{ii. } c(l) \rightarrow \exists X (b(X) \wedge c(X) \wedge a(l, X))$$

If l is a circular object than there is at least one X that's circular, filled & l

true: if k & l are both circular & filled & k points to l .

$$\text{iii. } \exists X \exists Y (\neg(X=Y) \wedge a(X, Y))$$

for any X , there is no Y such that X & Y are not one object and X points to Y .

false: there are objects that point at other but themselves.

$$\text{iv. } \forall X (\neg s(X) \rightarrow \exists Y (c(Y) \wedge b(Y) \wedge a(X, Y)))$$

If X is not square then it connects to some object that's circular & filled.

false: if connects only to l (or it isn't filled)

$$\text{v. } \forall X (\exists Y (\neg(X=Y) \wedge a(X, Y)) \rightarrow \exists Y (a(X, Y) \wedge a(Y, X)))$$

For all X , there is Y that's not X and X connects, if so,

for X there is some Y that X points to & it's not itself, and for those cases there is some y that either points to X , or X points to it & it's true for all X .

false: not the case for every case

true: if X connects to Y than it will connect to Y .

$$\text{vi. } \forall X \forall Y (a(X, j) \wedge a(Y, j) \rightarrow (a(X, Y) \vee a(Y, X)))$$

For all X & Y that connect to j , they have connection between each other.

true: if k connects to j & l connects to k .