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#### Department of Computing Academic Year **2019-2020**



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#### **Exercise Information**

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Reasoning in AI

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#### Student Declaration - Version 1

• I declare that this final submitted version is my unaided work.

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For Markers only: (circle appropriate grade)

SPOONER,	Jordan	01201572	c4	2020-02-17 18:32:23	<b>A</b> *	$\mathbf{A}$	${f B}$	$\mathbf{C}$	$\mathbf{D}$	${f E}$	$\mathbf{F}$
(js4416)											

Q1. (a) For a model M, path TT and LTL formulas P and Y:

 $(M,TT) \models \varphi R \psi$  iff there is some  $i \geq 0$  such that  $(M,TT[i..\infty]) \models \varphi$  and for all  $0 \leq j \leq i$  we have  $(M,TT[j..\infty]) \models \psi$ , or for all  $k \geq 0$ ,  $(M,TT[k..\infty]) \models \psi$ .

(b)  $\varphi R \psi \equiv (\tau(T \cup \tau \psi)) V(\psi \cup (\psi \wedge \varphi))$   $\psi \text{ holds forever or } \psi \text{ until and invluding } \psi \text{ holds}$ 

Solution could have been simplified futher. However, the explanation given is very strong

(c)  $(M,\Pi) \models (\neg (TU\neg \Psi)) \lor (\Psi \cup (\Psi \wedge \Psi))$ (defined) iff  $(M,\Pi) \models \neg (TU\neg \Psi)$  or  $(M,\Pi) \models \Psi \cup (\Psi \wedge \Psi)$ (by 1.4) iff  $\neg [(M,\Pi [k..\infty]) \models \neg \Psi)$  for some  $k \geqslant 0$ , or  $(M,\Pi) \models \Psi \cup (\Psi \wedge \Psi)$ (by 1.4) iff  $\neg [(M,\Pi [k..\infty]) \models \neg \Psi)$  for some  $k \geqslant 0$ , or  $(M,\Pi) \models \Psi \cup (\Psi \wedge \Psi)$ (by 1.4) iff  $\neg [(M,\Pi [k..\infty]) \models \neg \Psi)$  for some  $k \geqslant 0$ , or  $(M,\Pi) \models \Psi \cup (\Psi \wedge \Psi)$ (by 1.4) iff  $\neg [(M,\Pi [k..\infty]) \models \neg \Psi)$  for some  $k \geqslant 0$ , or  $(M,\Pi) \models \Psi \cup (\Psi \wedge \Psi)$ (by 1.4) iff  $\neg [(M,\Pi [k..\infty]) \models \neg \Psi)$  for some  $k \geqslant 0$ , or  $(M,\Pi) \models \Psi \cup (\Psi \wedge \Psi)$ (by 1.4) iff  $\neg [(M,\Pi [k..\infty]) \models \Psi)$  for some  $(M,\Pi) \models \Psi$  or  $(M,\Pi) \models \Psi \cup (\Psi \wedge \Psi)$ (by 1.4) iff  $\neg [(M,\Pi) [k..\infty]) \models \Psi$  for some  $(M,\Pi) \models \Psi$  or  $(M,\Pi) \models \Psi \cup (\Psi \wedge \Psi)$ (by 1.4) iff  $\neg [(M,\Pi) [k..\infty]) \models \Psi$  for some  $(M,\Pi) \models \Psi$  or  $(M,\Pi) \models \Psi$ 

(restricting) iss (MoTT)= YU(YAY) if ( or (MJT[1.0]) = (414) for some 130 and (M,TT[j.o])= 4 for all 0 < j < i (1.4) '&f ⊕ or (M, TT[i..∞]) = 4 and (MoTT[i. 00]) = 4 for some 1 > 0 and (MoTT [j....) = 4 for all 0 ≤ j < i. (reinte) 'If (MoTT[i.....) F (P for Some i > 0 and (MoTT[j..00]) ≠ 4 for all O≤j≤io or for all \$30 (MoTT [k.. 0]) = y. which is the condition provided in part (a). LRY = (つ(TUつか)) V(ヤロ(ヤハ上)) = (7 ドラヤ) V (4 U(411)) (form parts (a) to (c)) = G4 V (4 U(4 N+)) ( by defn F) = GYV (YUL) (by defn G) = GYVI by defn 1.4, (Since XNT = X) this would require = GY A[i.. 0] = L for some ( Fince X VI = X) 170 to hold for Some path J. Clearly no such I exists, So it is equivalent to 1

Q2.(1) (M,2) = EF \$\phi\$ iff (M,2) F E (TU p) (grien) iff for some path & starting from q, - $(M,\lambda) \models T \cup \phi$ (defn 1.7) ist for some path I starting from q, (MolEi]) = O for some j > 0 and (M, A[R]) FT for all O < R < j if for some path & starting from q, for some j>0 (M, A[j]) = p. ( since (M, s) ET) (ii) (M,2) = AF p iff (Moa) = A (TUP) ( guen) iff for every path & starting from 9,  $(M_0\lambda) \neq T \cup \phi$ iff for every path & starting from 90 for some j 70 (M, 161) = p. (by the same reasoning as in (B))

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(III) (Mog) FEGO
      ESF (Mog) = 7 AF 7 $ (gien)
       iff (M,2) = 7A(TU-P) (given)
      iff (Mog) # A(TU 7 D) (debn 1.7)
      iff it is not the case that for all paths I
           Starting from 90 (Mox) = TUT $ (1.7)
      iff for some path & starting from 9, (M3/1) # TU7 $ (M3/1) # TU7 $
      iff for some path of starting from 2,
           it is not the case that (Mol[i]) = 70
          for some 170 and (M, )(k)) +T for all O < k < j.
      iff for some path I starting from q , it is not
          the case that (M, &[i]) + 7 $ for some j70
      iff for some path & starting from 9,
                                              ((M,s)FT)
          for all j > 0 (M) A[j] \ n \ D
                                            (YFK = XEL)
     If for some path I starting from 9
                                             ( 1.7 ( and 77 X = X)
        for all i 20 (M, x [i]) = 0
(IV) (M,2) = AGO
     iff (M, 7) FTEFTD (gien)
     iff (M,9) = 7E(TU7D) (gien)
     *FF (M29) \ E(TU70) (1.7)
     iff there is some path of starting from 2 s.t. (M:X)=TU-D
     iff for all paths 1 starting from Q, (Mox) # TU-D (1.7)
                                           ( Switch quantitiers)
     iff for all paths I starting from q.
           for all in (Mon [j]) = p.
                                         ( by the same
                                         reasoning as
```

### (23. (a)

Consider an arbitrary CTL formula P According to the definition in lecture 5, P can take seven forms:

 $\Phi ::= \alpha | \neg \phi_1 | \phi_1 \wedge \phi_2 | E \times \phi_1 | A \times \phi_1 |$   $E(\phi_1 \cup \phi_2) | A(\phi_1 \cup \phi_3)$ 

where  $\phi_1$  and  $\phi_2$  are CTL formulas.

We show by induction that  $\Phi$  is a formula CTL\*.

Specifically, our inductrie hypothesis is that any CTL formula is a CTL\* (State) formula.

D'Ease case: Die an atom a

By definition 1, an atom a is a (state) formula of CTL\* as required.

2) Inductie case 1: 0 is 7 \$1

By our I. H. , assume \$\phi\_1\$ is a (state) formula CTLK.

By defn 1 (line 1), 7 \$\phi\_1\$ is therefore also a (state) formula in CTLX.

- 3 Inductive case 2: \$\Phi\$ is \$\phi\_1 \lambda \phi\_2\$

  By the IH passume \$\Phi\_1\$ and \$\phi\_2\$ are (state) formulas

  By defin 1, \$\Phi\_1 \lambda \phi\_2\$ is then a (state) formula in CTLX as required.
- D'Inductive case 3: \$\Phi\$ is \pi\(\phi\),

  By the IH, a secure \$\Phi\$, is a (state) formula of CTLK.
  - Ey defn 1 (line 2)  $\phi$ , is a path formula also.

    By defn 1 (line 2),  $X\phi_i$  is a path formula also.

    By defn 1 (line 1),  $EX\phi_i$  is a (state) formula of CTL\* as required.
- By the IH, assume Φ, is a (state) formula of CTLA.

  By B = XΦ; is a path formula of CTLA on

  By defin 1 (lie 1), AXΦ, is a (state) formula of CTLA.

  Traductie case 5: Φ is E(Φ, UΦ2)
- By the IH, assume Φ, and Φ, are state formulas of CTLK.

  By defn 1, they are also path formulas of CTLK.

  By defn 1, Φ, υΦ, is a path formula of CTLK.

  By defn 1, E (Φ, υΦ, is a state formula of CTLK.

  By defn 1, E (Φ, υΦ, is a state formula of CTLK.

#### F Inductie case b: p is A(p, Upa)

By D, we get  $\Phi, U\Phi_2$  is a path formula of CTLX.

By defn 1, A  $(\Phi, U\Phi_2)$  is a (state) formula of CTLX.

CTLX as required.

Hence every formula p of CTL is a (state)

# (b) Consider the CTLX formula Ea

This is a formula of CTLX, deried as follows:  $\phi \to E \psi \to E \phi \to E a$ 

It is not a formula of CTL since E4 can only be accepted if 4 is of the forme XD or DUD; and 'a' is dearly

Hence there exists a formula of CTLK that does not belong to CTL. 2

Q4. We denote entailment in CTL as  $\neq$  and entailment in CTL\* as  $\neq$ \*.

We must show that every construction in CTL (i.e. those seen in the previous question) have the same semanties in CTLK.

Once again, we will show this by induction.

het M be an arbitrary model, 9 be an arbitrary state, and be an arbitrary CTL\* (state) formula which is also a (state) formula in CTL.

Our inductive hypothesis is that (Mog) = \$\phi\$ iff (Mog) = \$\phi\$.

We will use  $\phi$ ; to denote CTL\* (state) formulas which are also (state) formulas of CTL.

```
Inductive case 3
                     of takes the form EXD,
   (M_2) = * E \times \phi_1
          iff for some path & starting from 2,
            (M_3\lambda) \models * x \downarrow, (defn 2)
         iff for some path I storting from q,
           (M, \lambda[1..\infty]) \models^* \phi, \quad (defin 2)
  (F) iff for some path I starting from 9,
          (M, A[I]) + + , (defn 2, since p, is a state formula)
         iff for some path & starting from 9,
              (M, A[I]) = 0, (I.H., since
A[I] is a state)
         iff for some path I starting from q.
           (M_3A) \neq X\Phi, (defn 1.8)
        iff (M, λ) = EXΦ, (defn 1.7)
                                           as required.
Inductie case 4 $ takes the form AXD,
   (Mog) = * Ax 0,
         iff for all paths & starting from 9 3
             (M_3 \wedge) \models^* \times \phi_1
                                      (defn 2)
        iff for all paths & starting from 9,
           (M_3A) \models X\emptyset, (Same as \mathbb{D})
        iff (M, \lambda) \models A \times \phi, (defn 1.7)
                                as required.
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#### Base case P is an atom a

$$(M \circ Q) \models^* a \text{ iff } Q \in V(a)$$
 (defn 2)  
iff  $(M \circ Q) \models a$  (defn 1.7)  
as required.

Inductive case 1  $\phi$  is of the form  $7\phi$ ,  $(M_0q) \models^* 7\phi$ , iff  $(M_0q) \not\models^* \phi$ , (defn 2)iff  $(M_0q) \not\models \phi$ , (by I.H.)iff  $(M_0q) \models 7\phi$ , (by defn 1.7)as required.

Inductive case 2  $\phi$  takes the form  $\phi, \Lambda \phi_2$   $(M_0q) \models^* \phi, \Lambda \phi_2$ iff  $(M_0q) \not\models^* \phi$ , and  $(M_0q) \not\models^* \phi_2$  (defining iff  $(M_0q) \not\models \phi_1$  and  $(M_0q) \not\models \phi_2$  (by to H.) iff  $(M_0q) \not\models \phi, \Lambda \phi_2$  (by defining) as required.

#### Inductive case 5 P takes the form E(p, Upz) (M22) = \* E(D, UD2) iff for some path & starting from q. (defn 2) (M) A) = \* P,UP2 iff for some path I starting from 9, (M, A[i..∞]) = \*p, for some i>0, and (Mo A [j. 00]) = \* po for all O\(\defn2\) (defn2) iff for some path & stating from q (Molij) + p, for some 120 and (defn 2, (MoALi] = De for all OSj <1 since of and are state formules) iff for some path & Starting from q (Mol[i]) = p, for some 1>0 and (M, A[j]) + pr for all O < j < i (I. H., since A[i] and A[j] are states) iff for some path & staring from q $(M_0)$ $\neq \phi_1 \cup \phi_2$ iff (Mog) = E (p, up) as required. (defn 1.8) (defn 1.7) Inductive case 6 \$\phi\$ takes the form A(\$\phi, U\$\P2) $(M_3q) = *A(p_1 U p_2)$ iff for all paths & starting from 90 (defn 2) (M, 1) = \* 0, U 02 iff for all paths & starting from 2, $(M_0 \lambda) \models \phi_1 \cup \phi_2$ (same as (1)) iff (Moa) = A(O,UD) (defn 1-7)

as required.

Note that we have shown the I.H. holds over all formulas of CTL, as per the definition on slide | 42. Also this is a strict subset of the formulas of CTLX > by the previous question. Hence the formulas of CTLX that are also formulas of CTL have the same semantics in both logies, as required.

Q5. (a)

Consider an arbitrary formula \$ of CTL; an arbitrary model M and an arbitrary state 5.

By question 3(a),  $\phi' = \phi$  a formula of CTL\*.

By question 4. (Mos) = \$\phi\$ iff (Mos) = \$\phi'\_3\$
as required.

Hence CTL\* is more expressive than CTL.

(b) Congider the formula of CTLX:  $\Phi = A \left( T U \left( a \Lambda X a \right) \right)$   $= A F \left( a \Lambda X a \right) \left( by defn & F_3 \\ slide & 142 \right)$   $\Phi \text{ is equivalent to the LTh formula}$   $F(a \Lambda X a) \qquad (slide 126)$ 

Dis not expressible in CTL (slide 208)

Hence we have that CTLX is strictly more expressive than CTL, as required.

Qb. We do induction over defn 2.

Given models  $M = (St_3 \rightarrow_3 V)$  and  $M' = (St'_3 \rightarrow_3' V')$ , States test and t'est' arbitrary paths  $TTE(St_3)$  and  $TE(St_3)$ , arbitrary state formula  $\phi$  and arbitrary path formula  $\phi$ , Such that  $(M:t) \approx (M'_3 t')$  and  $(M_3 TT) \approx (M'_3 TT')$ , our T. H. is that:  $\Phi$   $(M,t) \neq \phi$  iff  $(M',t') \neq \phi$ and  $(M_3 TT) \neq \psi$  iff  $(M'_3 TT') \neq 2\psi$ 

Base case & takes the form p.

 $(M,t) \neq p$  is  $t \in V(p)$  (defin 2) iff  $t' \in V'(p)$  (defin 3a) iff  $(M',t') \neq p$  (defin 2) as required

Inductive case 1  $\phi$  takes the form  $\neg \phi_1$   $(M \rightarrow t) \models \neg \phi_1$  if  $f(M_3 t') \not\models \phi_1$  (define) iff  $f(M_3 t') \not\models \neg \phi_1$  (tefne) as required

#### Inductive case 2 \$\phi\$ takes the form \$\Phi\_1 \Ap2

 $(M_3t) \models \Phi, \Lambda \Phi_2$ iff  $(M_3t) \models \Phi_1$  and  $(M_3t) \models \Phi_2$  (defn 2) iff  $(M'_3t') \models \Phi_1$  and  $(M'_3t') \models \Phi_2$  (I.o.H.) iff  $(M'_3t') \models \Phi_1 \Lambda \Phi_2$  (defn 2)

as required.

For the next inductive cases, we first prove the following: Lemma 1 Given a path  $\lambda$  in M: starting at some state  $\lambda[o]$ , and a model M' such that  $(M_{\circ}\lambda[o]) \approx (M'_{\circ}\lambda'[o])$ ;  $(M_{\circ}\lambda) \approx (M'_{\circ}\lambda')$ , and rice versa.

#### Proof O Formards:

We must show that there exists a  $\lambda'$  s.t.  $(M, \lambda[i]) \approx (M, \lambda'[i])$  for all  $i \ge 0$ .

We must show that there exists a bisimulation B between M and M's.t. B(A[i],A[i]) for all i>0.

By B. we know there exists a bisimulation B between M and M' s.t. B (A[o], A'[o]). We now show by induction over IN that B(A[i], A'[i]) for all i>0.

Our I.H. is that B(1[k], Y[k]).

Base case B(A[O], A'[O]) holds as stated earlier.

Inductive case Assume  $B(A[k], \lambda'[k])$ we know that  $\lambda[k] \in St$  and  $\lambda[k] \rightarrow \lambda[k+l]$ By defn 3(b) (forth), there exists some state,
call it  $\lambda'[k+l] \in St'$  s.t.  $B(\lambda[k], \lambda'[k+l])$ ,
as required.

Dedewards: the proof is symmetrical, it relies on defn 3(c) (back) instead of 3(b) (forth).

### Inductive case 3 \$\phi\$ takes the form E4, (Mot) FEY iff for some path & starting from to (M , 2) = 4 (defn 2) Now we note that (Mot) & (M', t') by (D) and that A [0] = t. If we have & '[0] = t's we can therefore apply hemma 1 to get that (MoA) & (M's 2') and vice versa. Hence, this is equivalent to the condition that: for some path I' starting from t's (M, 1) = 4 (by the IOHO) iff (M; 1/2) = E7 (defn 2) as regimed Inductive case 4 \$ takes the form AY, $(M,t) \models AY$

 $(M,t) \models A \psi$ ,  $(M \circ A) \models \psi$ , (defn 2)  $(M \circ A) \models \psi$ , (defn 2)  $(M' \circ A') \models \psi$ , (same reasoning as above) $(M' \circ A') \models A \psi$ , (defn 2).

## Inductive case 5 4 takes the form p,

 $(M_0 T) \neq \emptyset,$ iff  $(M_0 T) \neq \emptyset,$  (defn 2)

Note that (MoTT) & (M'STT') by (E). Hence by the definition of bisimilar paths, (MoTT[0]) & (M'STT'[0]), so this condition is equivalent to:

 $(M_3'T'[O]) \models \phi,$  (by the I. H.) iff  $(M'_3T') \models \phi,$  (defn 2)

Inductive case 6 4 takes the form 74,

 $(M_0TT) \models \neg \psi,$   $iff (M_0TT) \not\models \psi,$  (define)  $iff (M',T') \not\models \psi,$  (I.H.)  $iff (M',T') \models \neg \psi,$  (define) as required.

### Inductie case 7 4 takes the form 4, 142

(MoTT) = 4, 142

iff (MoTT) = Y, and (MoTT) = Y2 (defor 2)

iff (MoTT) = Y, and (MoTT) = Y2 (I. H2)

iff (MoTT) = Y, MY2 (defor 2)

as required.

Inductive case 8  $\psi$  takes the form  $\chi \psi$ ,  $(M_0TT) \models \chi \psi$ ,  $iff (M_0TT[1..\infty]) \models \psi$ , (defn 2)

Note that (MoTT) & (MoTT) by (D). Hence by
the definition of a bisimilar path, (MoTT[i]) ~

(MoTT[i]) for all i > 0. Again, by defin, we
therefore has that (MoTT[1.00]) ~ (MoTT[1.00])
Hence this condition is equivalent to

(MoTT[1.00]) = 4,

(I.H.)

iff (MoTT) = X 4, as required (defn 2)

## Inductive case 9 4 takes the form 4, U42

(MoTD = 4, UVa iff (MoT[i...∞]) = Y, for some i≥0 and (MoTT[j..0]) = 42 for all O < j < i (defn2) By a similar argument as before  $(M_3TT[k..\infty]) \approx (M'_3TT'[k..\infty])$  for any  $k \ge 0$ 

Hence this is equivalent to the condition

(MoTT[i... 2]) = 4, for some 120 and (M, TT'[j...oo]) = V2 for all OSj <i iff (M'sTI) = 4, U 42 (defn2) as required

Hence we have shaon that for all CTL\* formulas, ほ (Mot) ~ (M'st'):

That is, the touth of CTLX formulas is presend by bisimulations.

ASsume tEM and t'EM' are CTL-equivalent. Q7. We must show that (Mot) and (M', E) are bisinilar.

He must show that there exists a bisimulation B from M to M' and that B(t, t').

Specifically, ne show that the CTL-equivalence relection (which he denote a km) is such a bisimulation.

- O his is a pisimulation from M to M'
  Consider any states u Est and U'ESt'
  Such that u his u'. B
  - To all atoms p, we must show  $u \in V(p)$  iff  $u' \in V(p)$  iff  $(M, u) \neq p$  (defn 2) iff  $(M' > u') \neq p$  ( $(M' > u') \neq p$ ) iff  $(M' > u') \neq p$  ( $(M > u') \neq p$ ) iff  $(M' > u') \neq p$  ( $(M > u') \neq p$ ) as required
  - (b) We must show that if VESt and u >V, then there is V'ESt' such that u' >V' and V KNOV!
    - · Assume there exists a VESt s.t. u >V. (1)
    - \* Assume for the purpose of contradiction that there is no V'ESt's.t. u'->'v' and VENSV'.(2)
    - · Let S'= \{w'\in \st' \| u' \righta' \w'\righta',

      Note that (M,u) \= EXT (since u \rightarrow V(1))

      and u \( \since \) \( \since \)

- By (2), for every  $\omega_i' \in S'$  there exists a CTL formula  $\phi_i$  such that  $(M,v) \models \phi_i$  but  $(M', \omega_i') \not\models \phi_i$ .
- It follows that  $(M_0 u) \models E \times (\phi_1 \wedge \dots \wedge \phi_n)$ and that  $(M'_0 u') \not\models E \times (\phi_1 \wedge \dots \wedge \phi_n)$ .
- · But that contradicts that uses w (8).
- . Hence the forth condition holds.
- (2) The back condition can be shown similarly.
- (2) We must show that B(t,t').

  This holds directly from the definition of
  B and that t and t' are CTh-equivalent.

5

## Q8. We show that CTL and CTL+ have the same distinguishing power.

## Formards: Assume (M,t) and (M,t') satisfy the same formulas of CTL.

- · That is, for any CTL formula \$\phi\$; (Mot) \= \$\phi\$ iff (Mot') \= \$\phi\$.
- · That is, tEM and t'EM' are CTL-equivalent.
- · By Q7, (M,t) ~ (M',t').
- · By Qb, truth of CTL\* formulas is preserved by bisimulations. That is, (Mst) FΦ\* iff (Mst') F\* Φ\* for any CTL\* formula Φ\*.
- · Hence (Mot) and (Mot!) satisfy the same formulas of CTLX, as required.

## Backwards: Assume (Mot) and (M's t') Satisfy the Same formulas of CTLK.

- · That is, for any CTL\* formula  $\phi^*$  (Mot)  $F^*\phi^*$  is (Mot)  $F^*\phi^*$ .
- · By Q.5a, for every CTL formula  $\Phi$  there exists a CTLK formula  $\Phi'$  such that  $\Phi$  and  $\Phi'$  are equivalent:  $(M_5t) \models \Phi$  iff  $(M_5t') \models^*\Phi'$  and  $(M'_5t) \not\models \Phi$  iff  $(M'_5t') \not\models^*\Phi'$ .
- By the previous two points, we conclude that  $(M_3t) \neq \emptyset$  if  $(M'_3t) \neq \emptyset$  for every CTL formula  $\emptyset$ .
- · That is (Mot) and (Mit') satisfy the same CTL formulas, as required.

Distinguishing power is determined by a logic's ability to discern between particular models. Whilst expressioness refers to the definability of certain properties by formulas of a logic.

Since CTLK is strictly more expressive than CTL, but has the same distinguishing power, this means that although CTLK can express properties which CTL cannot (such as AF (alxi) - in all paths, there are two consecutive modes satisfying a), it is always possible to write a CTL formula which is satisfied in the same finite models as those satisfied by a CTLK formula. Specifically, any non-bisimilar models (as per defn 3) can be distinguished, and so any set of non-bisimilar models could simply be distinguished by a disjunction of CTL formulas.

		Out of	49			
10			1 (2)	1/0		
a/ <b>2</b>		b/ <b>2</b>	c/ <b>3</b>	d/3 Solution correct and well explained, though the		
				explanation for steps could have been presented in a		
		Solution could have simplified futher. How	ever,	stronger manner. However since the main explanation		
		the explanation give very strong	en is Solution correct and extremely well explained	is the truth condition, the solution is adequate		
	2	1	3	3		
			2			
a/2 b/2		b/ <b>2</b>	c <b>/2</b>	d <b>/2</b>		
2 2			2	2		
a/ <b>3</b>			3 b/ <b>2</b>			
	3		2			
			4			
/5						
	5					
a/ <b>2</b>			5 b/ <b>2</b>			
a1 <b>2</b>				well justified		
	2		2			
		6	7	8		
	/6	/6	/5			

Correct methodology but

to prove the back relation

5

no actual attempt is seen

All correct but no

attempt to resolve the

contradiction

4