

# Questions

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## Question 1

0.0/1.0 point (graded)

For a discrete Markov chain:

The sum of the elements of a row of the transition matrix is always equal to 1:

☐ True

☐ False

The sum of the elements of a column of the transition matrix is always equal to 1:

☐ True

☐ False

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## Question 2

0.0/2.0 points (graded)

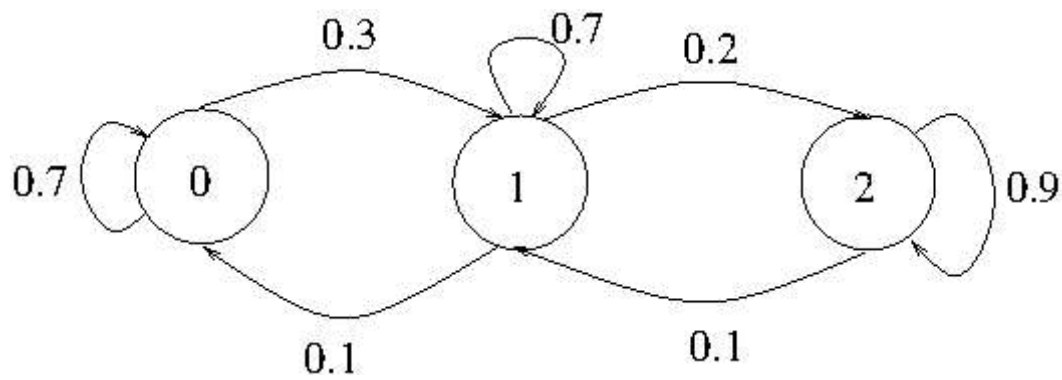


Figure 1

Which of the following balance equations are correct for the Markov chain in Figure 1?

☐ Case 1:

$$\begin{cases} \pi(0)0.3 = \pi(1)0.1 \\ \pi(1)0.2 = \pi(2)0.1 \end{cases}$$

☐ Case 2:

$$\begin{cases} \pi(0)0.3 = \pi(1)0.1 \\ \pi(1)(0.1 + 0.2) = \pi(0)0.3 + \pi(2)0.1 \end{cases}$$

☐ Case 3:

$$\begin{cases} \pi(1)0.3 = \pi(0)0.1 \\ \pi(2)0.2 = \pi(1)0.1 \end{cases}$$

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### Question 3

0.0/1.0 point (graded)

Consider again the Markov chain of question 2.

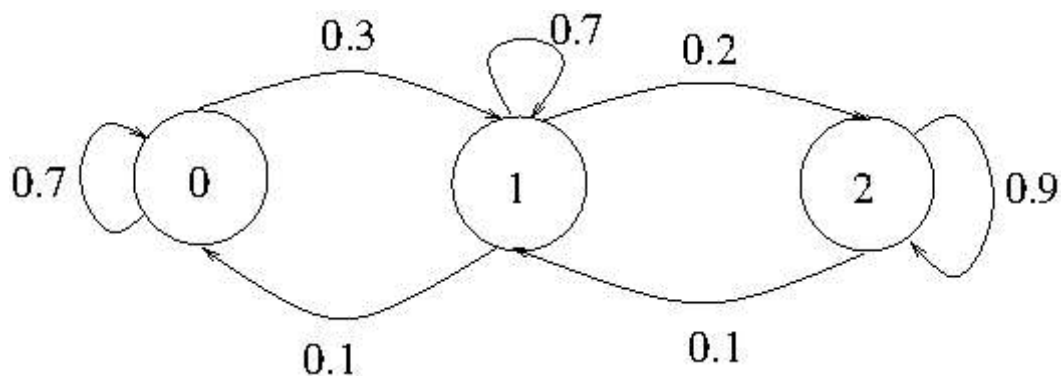


Figure 1

Denote by  $P$  its transition matrix.  $P_{ij}$  is the element in the  $j^{th}$  column of line  $i$  ( $i=0..2, j=0..2$ ). What are the values of  $P_{0,0}$ ,  $P_{0,1}$  and  $P_{0,2}$ ?

$P_{0,0} =$

$P_{0,1} =$

$P_{0,2} =$

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## Question 4

3 points possible (graded)

What is the steady state distribution (if it exists) of the Markov chain presented in the previous questions?

$\pi(0)=$

$\pi(1)=$

$\pi(2)=$

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## Question 5

0.0/1.0 point (graded)

Give the steady state distribution (if it exists) of the Markov chain presented in Figure 2.

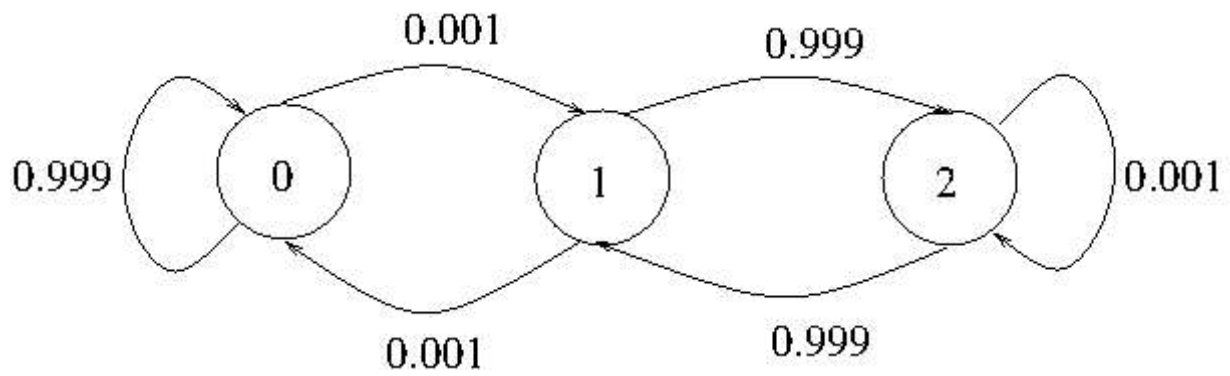


Figure 2

$\pi(0) =$

$\pi(1) =$

$\pi(2) =$

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## Question 6

1 point possible (graded)

Assume the following Markov chain (cf. Figure 3):

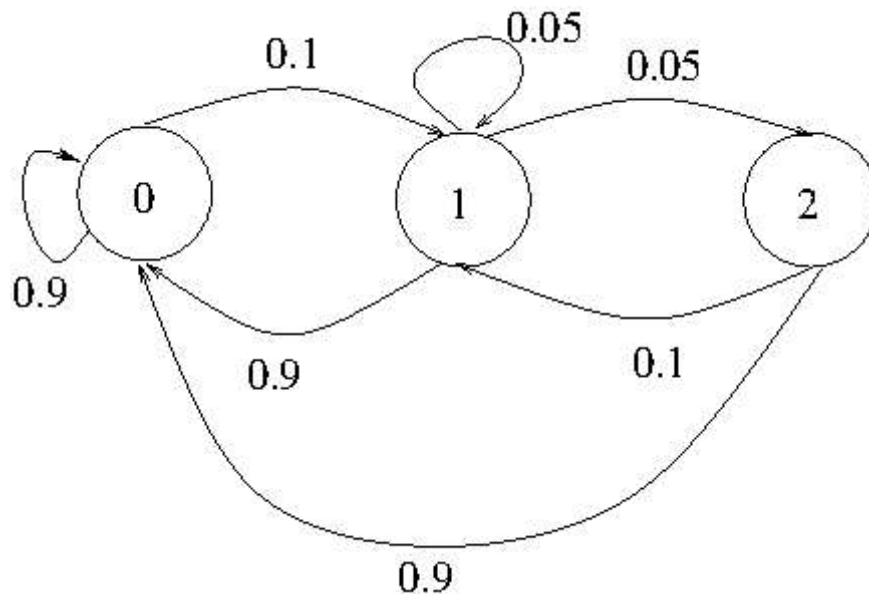


Figure 3

Is the steady state probability of being in state 0 higher when the process is in state 0 at time 0 with probability 0.99 than when it is in state 0 at time 0 with probability  $10^{-6}$  ?

☐ Yes

☐ No

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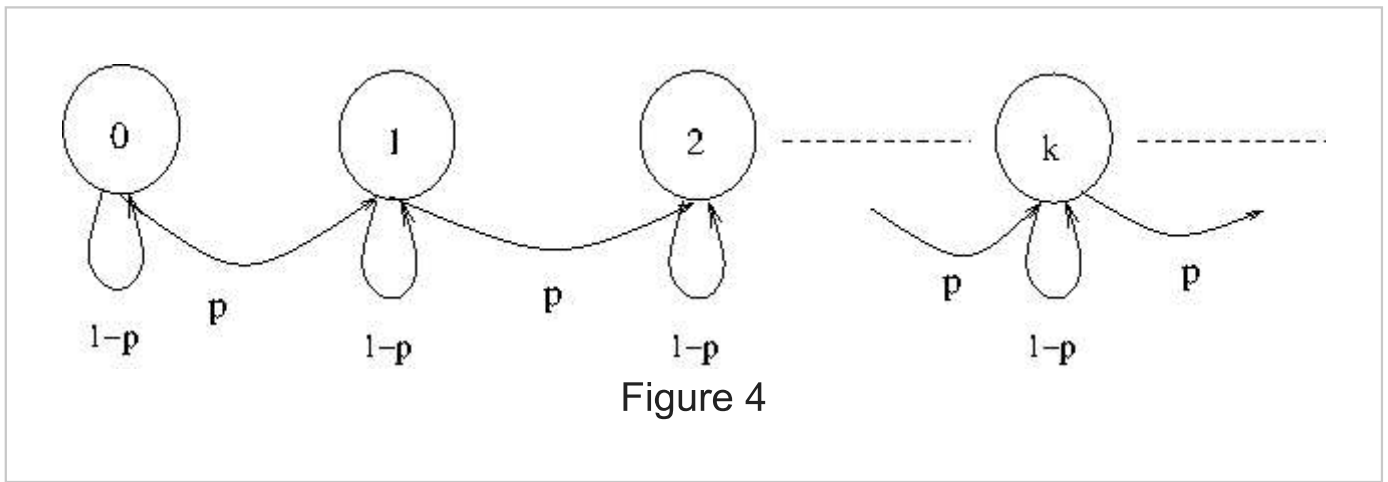
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## Question 7

1 point possible (graded)

Consider the following infinite state Markov chain (cf. Figure 4):



There is a steady state and it does not depend on the initial state.

☐ True

☐ False

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## Question 8

1 point possible (graded)

Consider the following finite state Markov chain (cf. Figure 5):

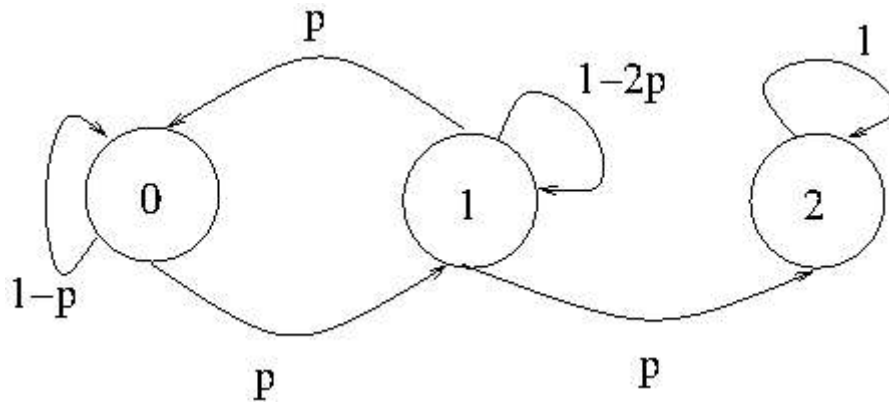


Figure 5

There is a steady state and it does not depend on the initial state.

☐ True

☐ False

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## Question 9

1 point possible (graded)

Consider the following Markov chain (cf. Figure 6):



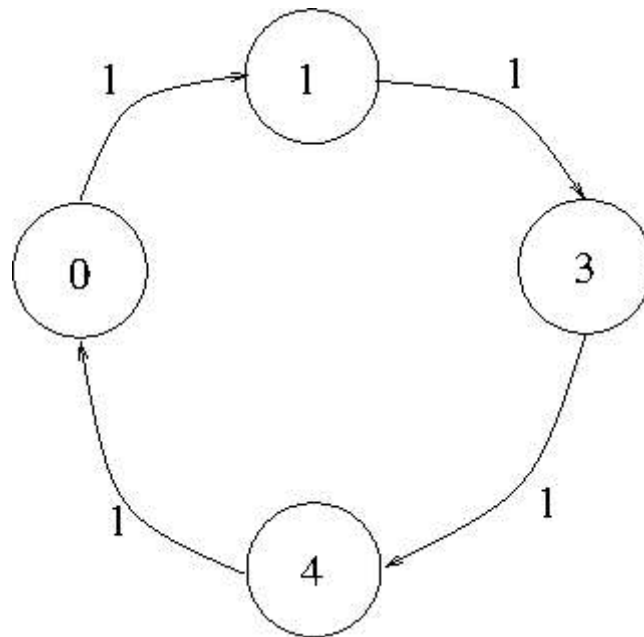


Figure 6

There is a steady state and it does not depend on the initial state.

☐ True

☐ False

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## Question 10

1 point possible (graded)

Consider the following finite state Markov chain (cf. Figure 7):

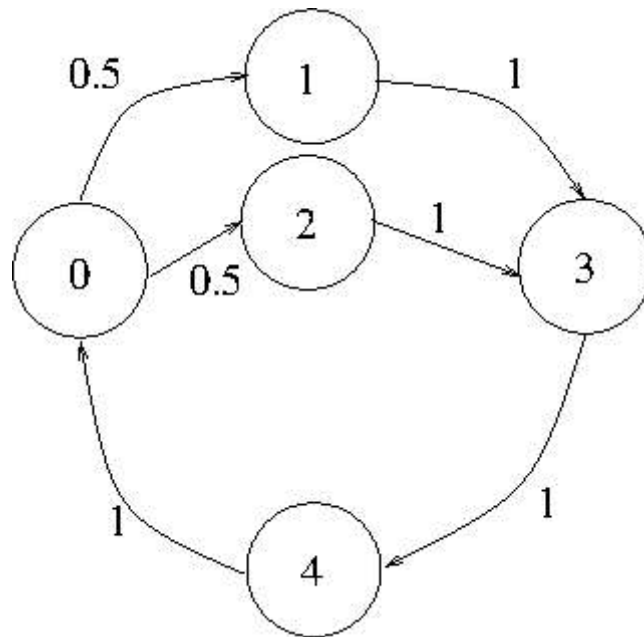


Figure 7

There is a steady state and it does not depend on the initial state.

☐ True

☐ False

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## Question 11

1 point possible (graded)

If  $P$  denotes the transition matrix of a discrete time Markov chain, the probability of arriving in state  $j$  from state  $i$  in  $n$  time units is:

☐  $(P^n)_{i,j}$

☐  $(P_{i,j})^n$

☐  $n \times P_{i,j}$

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## Question 12

1 point possible (graded)

Consider an infinite FIFO queue in discrete time with one single server. At each time, there is a single packet arrival with probability  $p_1$ , two packet arrivals with probability  $p_2$  and no arrival with probability  $1 - p_1 - p_2$ . The service time is constant, equal to 1 time unit. The number of clients at time  $n$ , denoted  $N(n)$  is a discrete time Markov Chain:

☐ True

☐ False

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## Question 13

1 point possible (graded)

Consider the following meteorological model:

- If the weather is bad at day  $n$ , then it remains bad at day  $n + 1$  with probability 0.5;
- If the weather is beautiful at day  $n$ , then it remains beautiful at day  $n + 1$  with probability 0.8 if it was beautiful at day  $n - 1$ ;
- If the weather is beautiful at day  $n$ , then it remains beautiful at day  $n + 1$  with probability 0.3 if it was bad at day  $n - 1$ .

Let us denote by  $X(n)$  the weather at day  $n$ .  $X(n)$  takes values in  $\{Be, Ba\}$  (for "Beautiful" or "Bad"). Is  $X(n)$  a Markov chain?

☐ Yes

☐ No

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