

YAKEEN NEET 2.0

2026

Basic Maths and Calculus (Mathematical Tools)

Physics

Lecture - 03

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30 chapters
12 TOPIC (Avg)
360 TOPIC





Topics to be covered

1

PhD on Trigonometry

2

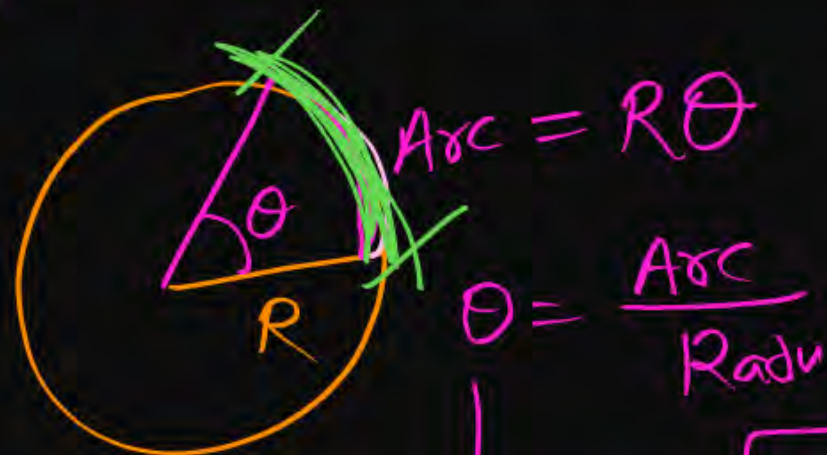
3

4



Recap of previous lecture

1



2

unit Radian / degree / mint / sec.
SI

3

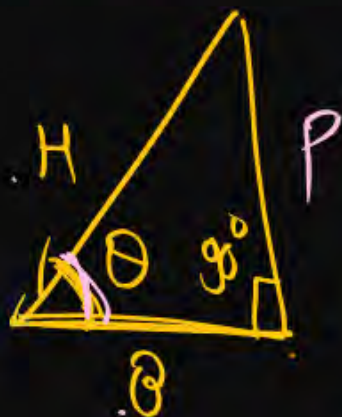
$$1 \text{ rad} = 180^\circ$$

4

$$1^\circ = 60 \text{ mint} = 60'$$

$$\text{Arc} = R \theta$$

$$\text{metre} = \text{metre} \times \text{radian}$$



$$\sin \theta = \frac{P}{H} = \frac{1}{\csc \theta}$$

$$\cos \theta = \frac{B}{H} = \frac{1}{\sec \theta}$$

$$\tan \theta = \frac{P}{B} \quad \csc \theta = \frac{H}{P}$$

$$L^1 = L^1 M^0 L^0 T^0 \leftarrow \text{dimension}$$

Sangrouh Assignment

electric charge & field
5% chapt 2

Question

H/w → ***
PhD. on.

H/w भेजना है



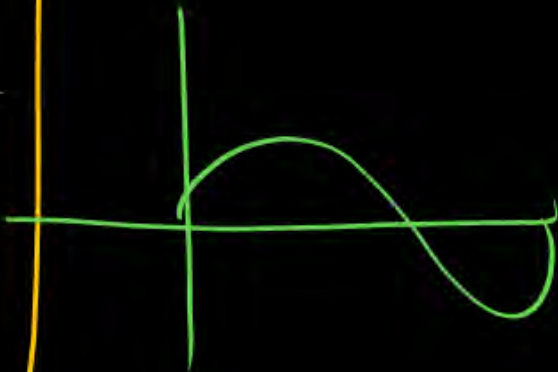
A vertical pole of height $h = 10$ m stands on ground that slopes upwards at a constant angle $\alpha = 30^\circ$ with the horizontal. If the sun's angle of elevation above the horizontal is $\theta = 60^\circ$, what is the length of the shadow cast by the pole on the sloping ground?

↳ Inclined plane

- 1 5 m
- 2 10 m
- 3 $10\sqrt{3}$ m
- 4 $\frac{10}{\sqrt{3}-1}$ m



	0°	30°	45°	60°	90°	120°	135°	150°	180°
$\sin \theta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{1}{\sqrt{2}}$	$-\frac{\sqrt{3}}{2}$	-1
$\tan \theta$									





@MRPHYSICSS

#

Parallel line
 $\theta = 0^\circ$

orthogonal line
 (perpendicular)
 90°

Antiparallel line
 $\theta = 180^\circ$

#

Acute Angle
 $\theta < 90^\circ$

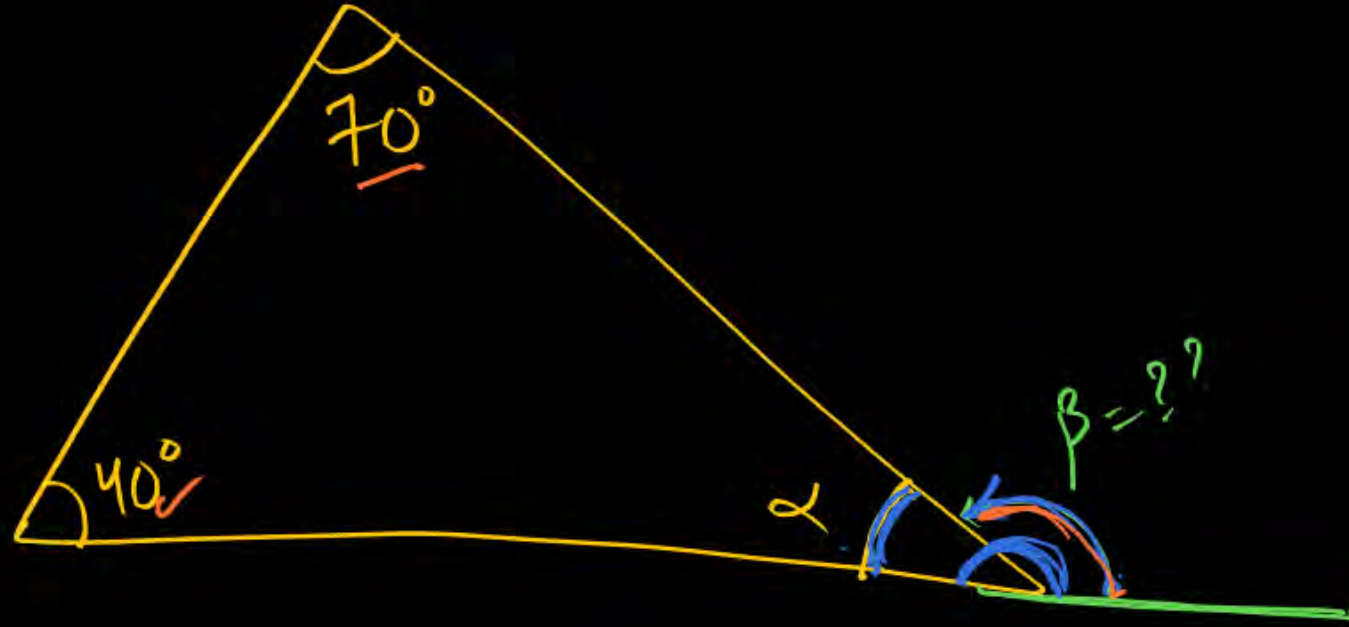
Obtuse angle
 $\theta > 90^\circ$

Alternate Angle

$\alpha + \beta = \text{exterior Angle}$

$$\alpha + \beta + \gamma = 180$$

$$\gamma = 180 - (\alpha + \beta)$$



find α Angle & β angle

$$40 + 70 + \alpha = 180$$

$$\alpha = 180 - 110$$

$$\boxed{\alpha = 70^\circ} \text{ Ans}$$

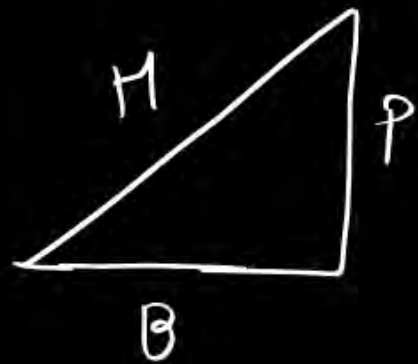
we know that

$$\alpha + \beta = 180^\circ$$

$$\beta = 180 - \alpha$$
$$= 180 - 70$$

$$\boxed{\beta = 110} \checkmark$$

Some important Pythagorean relation



$$H = \sqrt{P^2 + B^2}$$



$$\Rightarrow P=1, B=2 \quad H=\sqrt{5} \quad (1, 2, \sqrt{5})$$

$$\Rightarrow P=4, B=3 \quad H=5 \quad (3, 4, 5)$$

$$\Rightarrow P=12, B=5 \quad H=13 \quad (12, 5, 13)$$

$$\Rightarrow P=7, B=24 \quad H=25 \quad (7, 24, 25)$$

$$\Rightarrow P=6, B=8 \quad H=10 \quad (6, 8, 10)$$

#

$$H = \sqrt{P^2 + B^2} = \sqrt{144 + 25} = \sqrt{169} = 13$$

$$\begin{array}{r} 24 \\ 24 \\ \hline 96 \\ 48 \\ \hline 576 \end{array}$$

$$25^2 = 625$$

#

$$p^2 + b^2 = H^2$$

→ divided by H^2 Both side

$$\frac{p^2}{H^2} + \frac{b^2}{H^2} = \frac{H^2}{H^2} \cdot 1$$

#

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\cos^2 \theta = 1 - \sin^2 \theta$$

⊕

$$\cos \theta = \sqrt{1 - \sin^2 \theta}$$

⊕

$$\sin \theta = \sqrt{1 - \cos^2 \theta}$$

divide by p^2 both side

$$\frac{p^2}{p^2} + \frac{b^2}{p^2} = \frac{H^2}{p^2}$$

$$1 + \cot^2 \theta = \operatorname{cosec}^2 \theta$$

divide by b^2 both side

$$\frac{p^2}{b^2} + \frac{b^2}{b^2} = \frac{H^2}{b^2}$$

$$\tan^2 \theta + 1 = \sec^2 \theta$$

$$\textcircled{\#} \sin(A+B) = \sin A \cdot \cos B + \sin B \cdot \cos A$$

$$\sin(A-B) = \sin A \cdot \cos B - \sin B \cdot \cos A$$

$$\cos(A+B) = \cos A \cdot \cos B - \sin A \cdot \sin B$$

$$\cos(A-B) = \cos A \cdot \cos B + \sin A \cdot \sin B$$

$$\checkmark \tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \cdot \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \cdot \tan B}$$

$$\Rightarrow \text{If } A=B=\theta$$

$$\sin(2\theta) = \underbrace{\sin \theta \cdot \cos \theta} + \underbrace{\sin \theta \cdot \cos \theta}$$

$$\textcircled{\#} \boxed{\sin(2\theta) = 2 \sin \theta \cdot \cos \theta}$$

$$\cos(A+B) = \cos A \cdot \cos B - \sin A \cdot \sin B$$

$$\boxed{\cos(2\theta) = \cos^2 \theta - \sin^2 \theta} \checkmark \textcircled{\#}$$

$$\cos(2\theta) = 1 - \sin^2 \theta - \sin^2 \theta$$

$$\boxed{\cos(2\theta) = 1 - 2 \sin^2 \theta} \textcircled{\#}$$

$$\sin(2\theta) = 2 \sin \theta \cdot \cos \theta$$

→ If $2\theta = \alpha$
 $\theta = \alpha/2$

$$\sin \alpha = 2 \sin \frac{\alpha}{2} \cdot \cos(\frac{\alpha}{2})$$

→ Half Angle
Formula

$$\cos(2\theta) = \cos^2 \theta - \sin^2 \theta$$

$$\cos \alpha = \cos^2 \frac{\alpha}{2} - \sin^2 \frac{\alpha}{2}$$

Half Angle Formula

$$\textcircled{\#} \sin(105^\circ) = \overset{A+D}{\sin(60+45^\circ)} = \sin 60^\circ \cdot \cos 45^\circ + \sin 45^\circ \cdot \cos 60^\circ$$

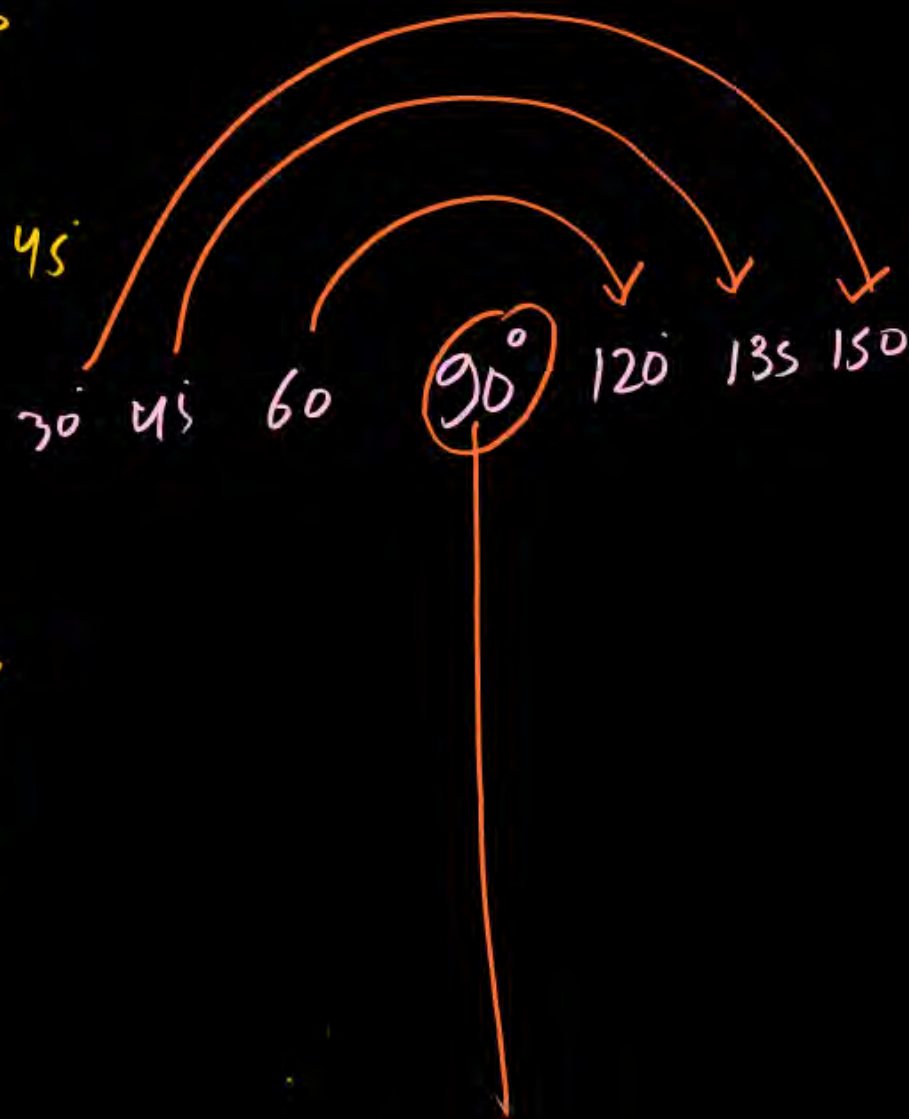
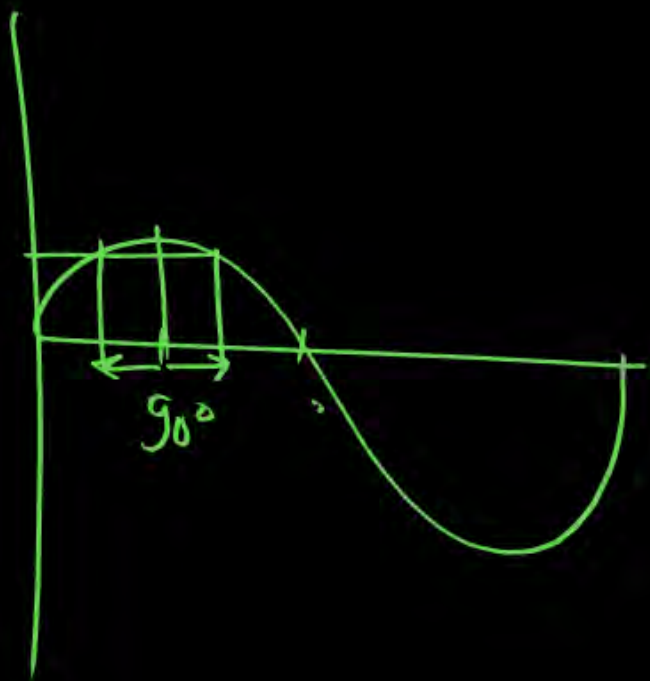
$$= \frac{\sqrt{3}}{2} \times \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} \times \frac{1}{2}$$

$$= \frac{\sqrt{3} + 1}{2\sqrt{2}} \}$$

$$\textcircled{\#} \sin(75^\circ) = \sin(45^\circ + 30^\circ) = \sin 45^\circ \cdot \cos 30^\circ + \sin 30^\circ \cos 45^\circ$$

$$= \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} + \frac{1}{2} \times \frac{1}{\sqrt{2}}$$

$$= \frac{\sqrt{3} + 1}{2\sqrt{2}} \}$$



$$\checkmark \# \cos(15^\circ) = \cos(45^\circ - 30^\circ) = \cos 45^\circ \cos 30^\circ + \sin 45^\circ \sin 30^\circ$$

$$= \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \times \frac{1}{2}$$

$$\checkmark \# \tan(105^\circ) = \tan(60^\circ + 45^\circ) = \frac{\tan 60^\circ + \tan 45^\circ}{1 - \tan 60^\circ \tan 45^\circ} = \frac{\sqrt{3} + 1}{2\sqrt{2}}$$

$$\sin 2\theta = 2\sin\theta \cdot \cos\theta$$

$$\cos(2\theta) = \cos^2\theta - \sin^2\theta$$

$$\cos(2\theta) = 1 - 2\sin^2\theta$$

$$2\sin^2\theta = 1 - \cos(2\theta)$$

$$\sin\theta = \sqrt{\frac{1 - \cos(2\theta)}{2}}$$

No need to solve find value of $\sin 22.5^\circ$

$$\sin 22.5^\circ = \sqrt{\frac{1 - \cos(2 \times 22.5)}{2}}$$

$$= \sqrt{\frac{1 - \frac{1}{\sqrt{2}}}{2}}$$

$$= \sqrt{\frac{\frac{\sqrt{2}-1}{\sqrt{2}}}{2}} = \sqrt{\frac{\sqrt{2}-1}{2\sqrt{2}}}$$

Not for us.

Small Angle approximation

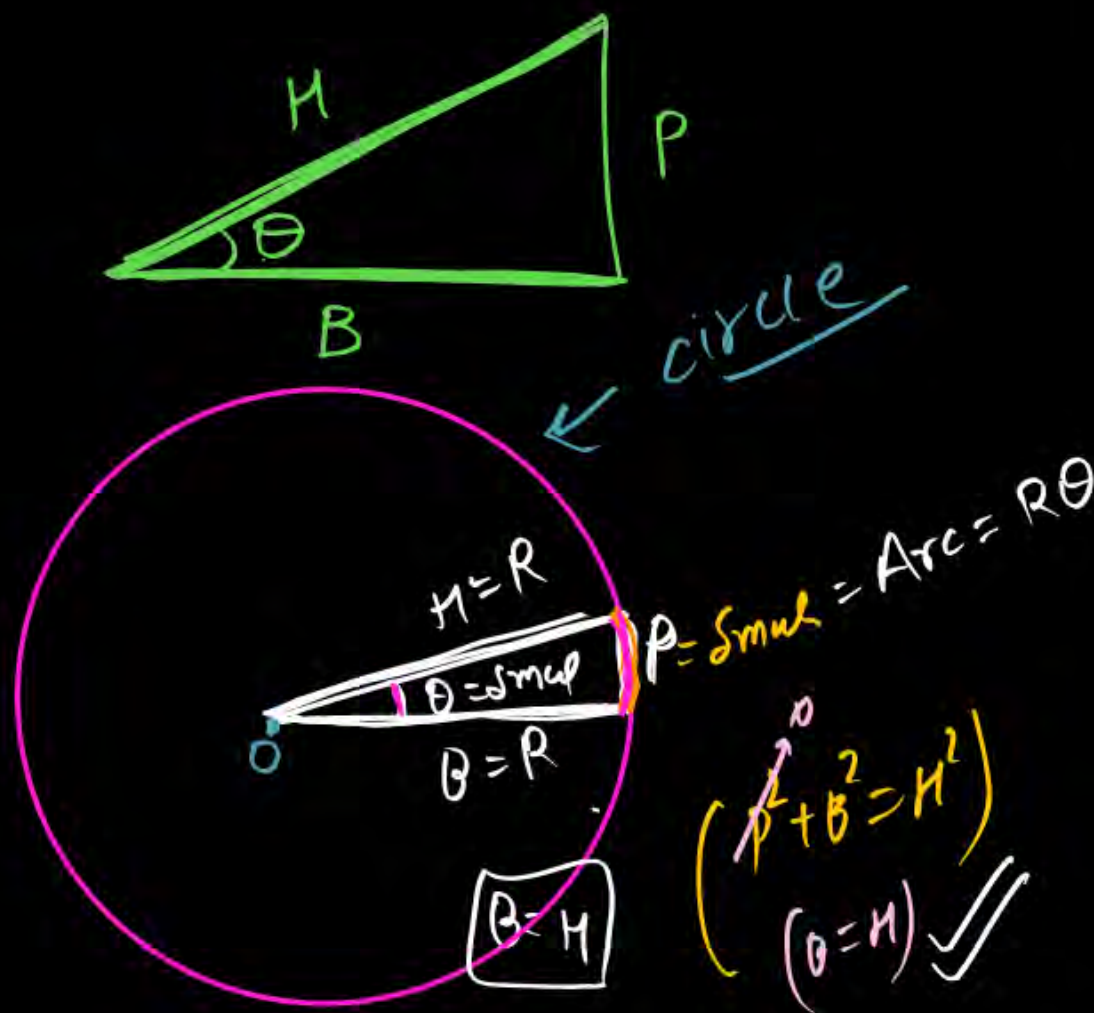
$$\cos \theta = \frac{B}{H}$$

$\theta \rightarrow$ small

$$\cos \theta = \frac{\cancel{B}}{\cancel{B}} = 1$$

$$\boxed{\cos \theta = 1}$$

small



$$\sin \theta = \frac{P}{H} = \frac{\cancel{R}\theta}{\cancel{R}}$$

$$\boxed{\sin \theta = \theta} \checkmark$$

$$\tan \theta = \frac{P}{B} = \frac{\cancel{R}\theta}{\cancel{R}} = \theta$$

for small angle $\theta \leq 5^\circ$

$$\cos \theta = 1$$

$$\boxed{\sin \theta = \tan \theta = \theta} \checkmark$$

for small angle

$$\cos 3^\circ = 1$$

$$\cos 4^\circ = 1$$

$$\cos 2^\circ = 1$$

$$\cos 1^\circ = 1$$

$$\sin \theta = \theta$$

$$\sin 2^\circ = 2^\circ \text{ wrong}$$

$$\sin 2^\circ = 2^\circ = \frac{2 \times \pi \text{ rad}}{180}$$

$$\# \sin 2^\circ = \frac{\pi}{90} \text{ rad}$$

$$180^\circ = \pi \text{ rad}$$

$$\sin 3^\circ = 3^\circ = \frac{3 \times \pi \text{ rad}}{180} = \left(\frac{\pi}{60} \right) \text{ rad}$$

$$\tan 4^\circ = 4^\circ = \left[\frac{4 \times \pi \text{ rad}}{180} \right] \text{ rad}$$

Question



Which of the following option is correct for the value of $\tan(2^\circ)$ $= 2^\circ = 2 \frac{\pi \text{ rad}}{180^\circ} = \frac{\pi}{90} \text{ rad}$

1 2° ✗

2 $\pi/90$ ✓
93%

3 $\pi/30$ ✗

4 2 rad ✗

$\tan 2^\circ = 2^\circ$

7% >>>>>> 93%
~~_____~~

ASTC Rule

$$\sin 30^\circ = \frac{1}{2}$$

$$\sin(-30^\circ) = -\frac{1}{2}$$

$$\tan(60^\circ) = \sqrt{3}$$

$$\cos(-30^\circ) = +\frac{\sqrt{3}}{2}$$

$$2^{\text{nd}} [\sin(150^\circ) = +$$

$$3^{\text{rd}} [\sin(240^\circ) = -$$

$$4^{\text{th}} \begin{cases} \sin(300^\circ) = - \\ \sin(-60^\circ) = - \end{cases}$$

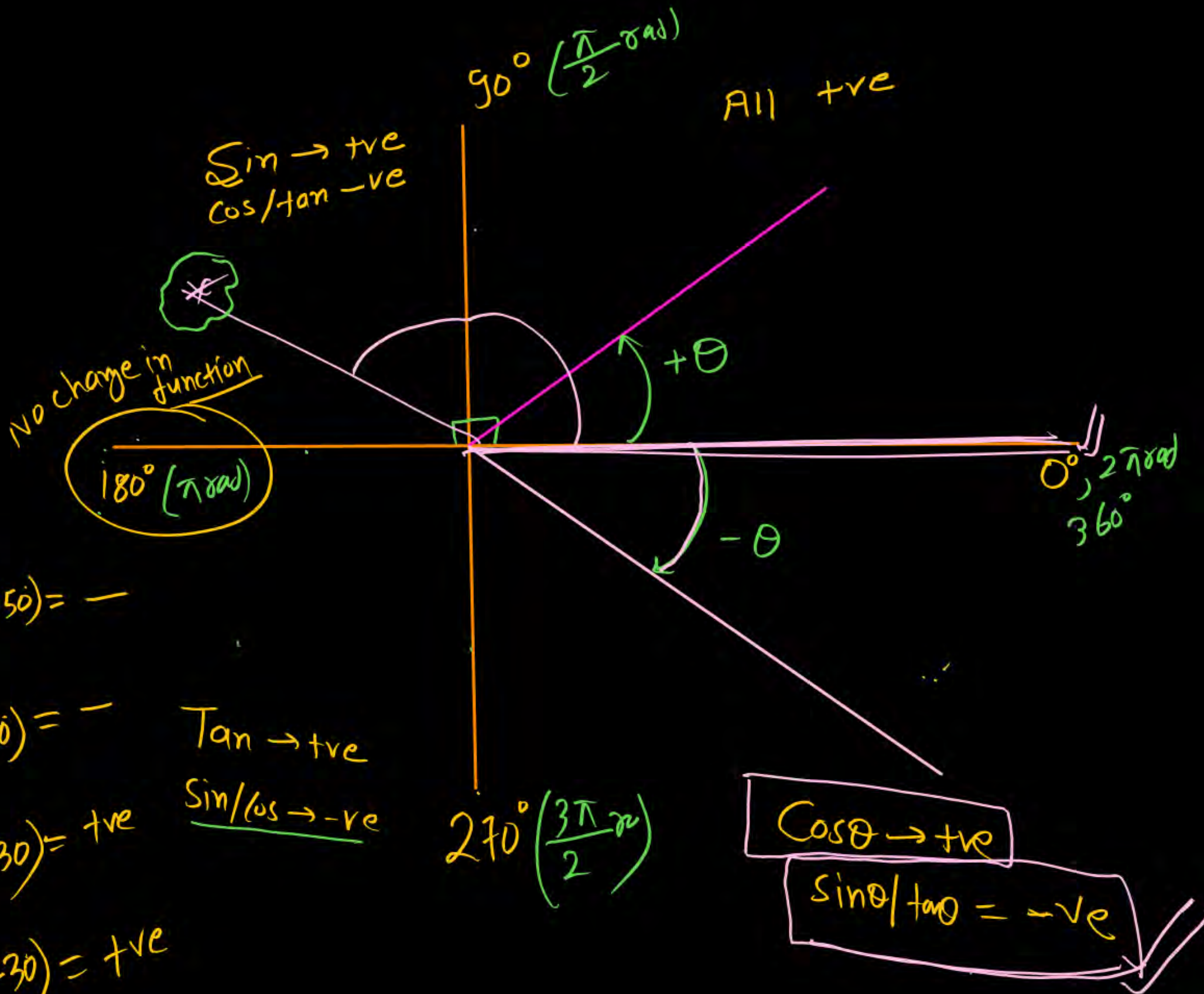
$$2^{\text{nd}} [\cos(150^\circ) = -$$

$$3^{\text{rd}} [\cos(240^\circ) = -$$

$$4^{\text{th}} \begin{cases} \cos(330^\circ) = +ve \\ \cos(-30^\circ) = +ve \end{cases}$$

Tan \rightarrow +ve

Sin/cos \rightarrow -ve



$$\overset{A}{\sin}(180-\overset{B}{\theta}) = \cancel{\sin 180}^0 \cos \theta - \sin \theta \cos 180^\circ$$

$$= 0 - \sin \theta (-1)$$

$$\sin(180-\theta) = \sin \theta$$

$$\# \cos(180-\theta) = -\cos \theta$$

$$\# \cos(180+\theta) = -\cos \theta$$

$$\sin(180+\theta) = -\sin \theta$$

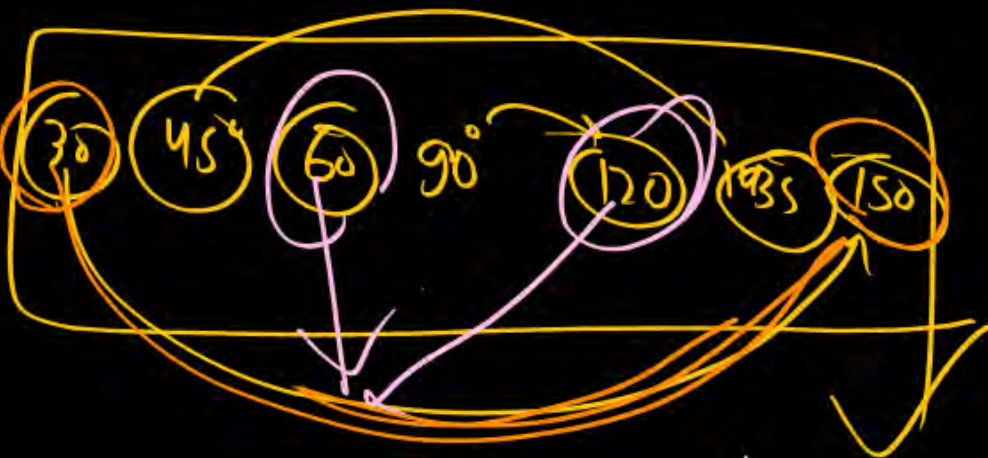
$$\text{Ex } \sin(120^\circ) = \sin(\underline{180}-60) = \sin 60 = \frac{\sqrt{3}}{2}$$

$$\# \sin(150^\circ) = \sin(180-30) = \sin 30 = \frac{1}{2}$$

$$\# \sin(240^\circ) = \sin(180+60) = -\sin 60 = -\frac{\sqrt{3}}{2}$$

MP* Concept

Pho



$$\begin{aligned}
 \checkmark \quad \sin(180 - \theta) &= \sin \theta \\
 \sin(180 + \theta) &= -\sin \theta \\
 \cos(180 - \theta) &= -\cos \theta \\
 \cos(180 + \theta) &= -\cos \theta
 \end{aligned}$$

1st

$$\begin{aligned}
 \sin(360 + \theta) &= \sin \theta \\
 \cos(360 + \theta) &= \cos \theta
 \end{aligned}$$

4th

$$\begin{aligned}
 \sin(360 - \theta) &= -\sin \theta \\
 \cos(360 - \theta) &= +\cos \theta
 \end{aligned}$$

$$\checkmark \quad \sin(90 + \theta) = +\cos \theta$$

$$\checkmark \quad \cos(90 - \theta) = \sin \theta$$

$$\checkmark \quad \cos(90 + \theta) = -\sin \theta$$



$$\# \sin(90+\theta) = \overset{1}{\cancel{\sin 90}} \cos\theta + \sin\theta \overset{0}{\cancel{\cos 90}}$$

$$\# \boxed{\sin(90+\theta) = \cos\theta}$$

→ Iska sign dekna hai 2nd quadrant me

$$\# \boxed{\sin(90-\theta) = \cos\theta}$$

Question



If $y = \frac{\sin \theta}{\theta}$ then find value of y if $\theta = 30^\circ$.

$$y = \frac{\sin \theta}{\theta}$$

$$y_{\theta=30^\circ} = \frac{\sin 30^\circ}{\pi/6} = \frac{\frac{1}{2}}{\pi/6} = \frac{6 \times 1}{2 \times \pi} = \frac{3}{\pi} \text{ Ans}$$

$$y_{\theta=30^\circ} = \frac{\sin 30^\circ}{30} \quad \text{X}$$

$$30^\circ = \frac{\pi}{6} \text{ rad}$$

Suggest suitable match between function given in the first column and its description given in the second column.

- 1 $A \rightarrow PT, B \rightarrow QT, C \rightarrow QT, D \rightarrow PS$
- 2 $A \rightarrow PT, B \rightarrow QS, C \rightarrow QT, D \rightarrow PS$
- 3 $A \rightarrow QT, B \rightarrow QS, C \rightarrow PT, D \rightarrow PS$
- 4 $A \rightarrow QS, B \rightarrow PT, C \rightarrow QT, D \rightarrow PS$

Column-I	Column-II
(A) $\sin (390^\circ)$	(P) Positive
(B) $\sin (-30^\circ)$	(Q) Negative
(C) $\cos 120^\circ$	(R) Zero
(D) $\tan (-120^\circ)$	(S) Modulus is greater than one
	(T) Modulus is less than one

Question



Find value:

(i) $\sin 2^\circ$

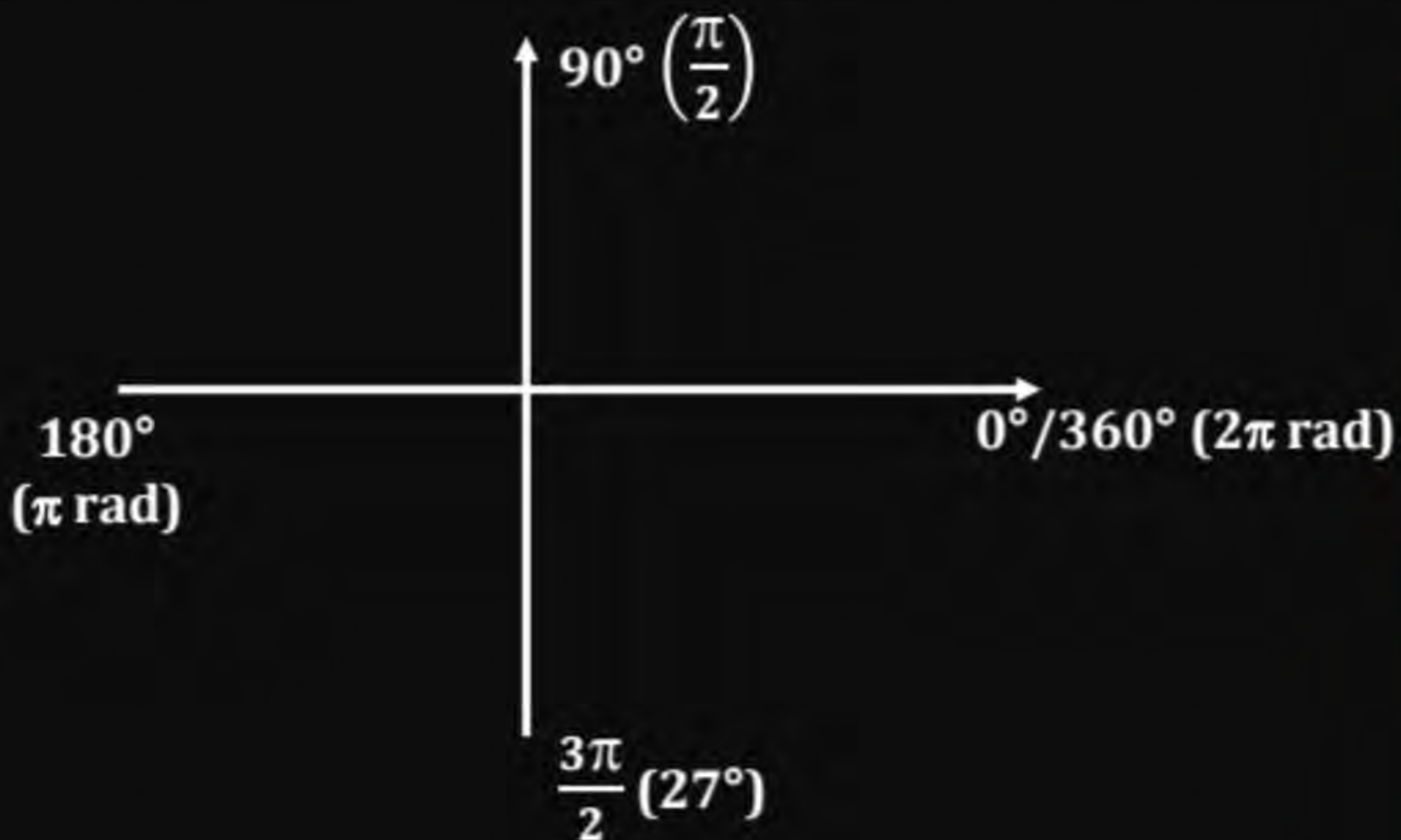
(ii) $\tan 3^\circ$

(iii) $\cos 3^\circ$

(iv) $\sin (88.5^\circ)$



TRIGONOMETRY FUNCTION CHARGE



HW *page*

$$\sin (90^\circ - \theta) =$$

$$\cos (90^\circ - \theta) =$$

$$\sin (90^\circ + \theta) =$$

$$\cos (90^\circ + \theta) =$$

$$\sin (180^\circ - \theta) =$$

$$\cos (180^\circ - \theta) =$$

Question

17/10



Find value of

(i) $\sin(-30^\circ)$

(ii) $\cos(-60^\circ)$

(iii) $\sin(120^\circ)$

(iv) $\sin(390^\circ)$

H/W



$$\sin (360^\circ) =$$

$$\checkmark \sin (450^\circ) = \sin (\underline{360} + 90) = \sin 90 = 1$$

$$\sin (-90^\circ) =$$

$$\sin (120^\circ) =$$

$$\sin (-150^\circ) =$$

$$\cos (300^\circ) =$$

$$\cos (330^\circ) =$$

$$\tan (240^\circ) =$$

$$\cos (-30^\circ) =$$

$$\tan (-60^\circ) =$$

$$\cot (-45^\circ) =$$

Question

$$y = 4 \sin(2\theta)$$

Find maximum value of y and also find angle at which y will be maximum?

$$|\cos(7\theta)|_{\max} = 1$$

$$\sin\theta_{\max} = 1$$

$$\sin(2\theta)_{\max} = 1$$

$$\sin\left(\frac{3\theta}{2}\right)_{\max} = 1$$



max kaha mila ki nahi mila

$$y = 4 \sin 2\theta$$

$$y_{\max} = 4 |\sin(2\theta)|_{\max}$$

$$y_{\max} = 4$$

$$\sin(2\theta)_{\max} = 1$$

$$\text{at } 2\theta = 90^\circ$$

$$\boxed{\theta = 45^\circ}$$
 feel

$$R = \frac{u^2 \sin 2\theta}{g}$$

$$R_{\max} = \frac{u^2}{g} |\sin 2\theta|_{\max}$$

$$R_{\max} = \frac{u^2}{g}$$

$$\sin 2\theta = 1$$

$$2\theta = 90^\circ$$

$$\text{at } \boxed{\theta = 45^\circ}$$

 R_{\max}

② at which angle $\sin(3\theta)$ will have maxⁿ valⁿ

$$\sin(3\theta)_{\text{max}} = 1$$

$$3\theta = 90^\circ$$

$$\theta = \frac{90}{3} = \underline{\underline{30^\circ}}$$

Question

H/W



If $y = 3 \cos (3\theta)$, then find angle at which y will be zero.

$\phi = \text{initial phase}$

$y = A \sin(\omega t + kx + \phi)$

Diagram illustrating the components of the SHM wave equation:

- 1 points to ϕ (Initial phase)
- 2 points to $\omega t + kx$ (Angular displacement)
- 3 points to the entire argument $(\omega t + kx + \phi)$

Kisko phase kahteha?

(a) 1 50% ✓✓

(b) 2

✓✓ (c) 3 32% ✓

(d) Hamko nahi aaw

gharchi on top

SHM
Wave
Veer
war o?h
EM wave

THANK
YOU