

End-to-Beginning (Sequence/array A):

$n = \text{sizeof}(A) // 1$

$H[n] // 1$

For($i=0; i < n; i++$) $// n$

$H[i] = 0 // 1$

For($i=n-2; !(i < 0); i--$) $// n-2$

For($j=i+1; j < n; j++$) $// n - (i+1) + 1 \Rightarrow \sum_{i=0}^{n-2} (n-i)$

if($A[i] < A[j]$ && $H[i] \leq H[j]$) $// 3$

$H[i] = H[j] + 1 // 2$

$\text{max} = \text{max element of } (H) + 1 // 2$

$R[\text{max}] // 1$

$r = 0 // 1$

$\text{Less} = \text{max} - 1 // 2$

For($i=0; i < n$ && $r! = \text{max}; i++$) $// n$ } $4n$

if($H[i] == \text{Less}$) $// 1 + \text{max}(3, 0) = 4$

$R[r] = A[i] // 1$

$r++ // 1$

$\text{Less}-- // 1$

return $R // 1$

$$T(n) = 1 + \left(\frac{1}{2}n^2 - \frac{1}{2}n - 1\right) \cdot 5 + 4n + 9$$

$$T(n) = n + \frac{5}{2}n^2 - \frac{5}{2}n - 5 + 4n + 9$$

$$T(n) = \frac{5}{2}n^2 + \frac{5}{2}n + 4$$

Where $f(n) = n^2$ Prove $T(n) = O(n^2)$ by limit THM. AS $L > 0$ AND $L < \infty$.

$$\lim_{n \rightarrow \infty} \frac{T(n)}{f(n)} = \frac{\frac{d}{dn} \left(\frac{5}{2}n^2 + \frac{5}{2}n + 4 \right)}{\frac{d}{dn} (n^2)} \rightarrow \lim_{n \rightarrow \infty} \frac{5n + \frac{5}{2}}{2n} = \frac{\infty}{\infty}$$

$$\lim_{n \rightarrow \infty} \frac{\frac{d}{dn} (5n + \frac{5}{2})}{\frac{d}{dn} (2n)} = \frac{5}{2} > 0 \text{ AND } \frac{5}{2} < \infty$$

$$\therefore \frac{5}{2}n^2 + \frac{5}{2}n + 4 = O(n^2)$$

$$2^2 = 4$$

KB	0	1
00	0	1
10	0	1
01	0	1
11	0	1

$$\frac{2^n}{2}$$

The idea of creating ^(generating) every possible subsequences from a sequence

	a	b	c		0	8	4	12		# of index searching through
\emptyset	0	0	0	1	0	0	0	0	\emptyset	
a	1	0	0	2	1	0	0	0	0	
b	0	1	0	3	0	1	0	0	8	
a-b	1	1	0	4	1	1	0	0	08	
c	0	0	1	5	0	0	1	0	4	
a-c	1	0	1	6	1	0	1	0	04	
b-c	0	1	1	7	0	1	1	0	84	8(4)
abc	1	1	1	8	1	1	1	0	084	
				9	0	0	0	1	12	$\frac{16}{2} (4)$
				10	1	0	0	1	012	
				11	0	1	0	1	812	8(4)
				12	1	1	0	1	0812	
				13	0	0	1	1	412	
				14	1	0	1	1	0412	
				15	0	1	1	1	8412	
				16	1	1	1	1	08412	

$\frac{n!}{2}$
~~48~~(3) indices searched
~~8~~n

$$\frac{2^n}{2} (n)$$

n=3 #sub seq = 8 n=4 #sub seq = 16 AND n=2 #sub seq = 4

So the pattern he is 2^n of subsequences of a sequence.

AND searching through ^{steps} each index takes $T(n) = 2^{n-1} \cdot n$

PSEUDOCODE FOR
LONGEST INCREASING SUBSEQUENCE
generates
(subsequences)

this pseudo code is the

$S = \langle \text{subsets of a sequence} \rangle$ // to generate per last page takes about 2^n time
 $\text{best} = \emptyset$, $\text{is_best} = \text{TRUE}$ // 2
 For i in S : // 2^n
 if ($i.\text{size}() > \text{best}.\text{size}()$): // 1
 For ($j=1$; $j < i.\text{size}()$; $j++$): // n
 if ($i[j-1] > i[j]$): // $1 + \max(2, 0) = 3$
 $\text{is_best} = \text{FALSE}$ // 1
 break // 1

 if ($\text{is_best} == \text{FALSE}$): // $1 + \max(2, 0) = 3$
 $\text{best} = i$ // 1
 $\text{is_best} = \text{TRUE}$ // 1

$$T(n) = 2 + 2^n \cdot 1 \cdot n \cdot 3 + 3 = 3 \cdot 2^n \cdot n + 5$$

To prove $T(n) = O(f(n))$ when $f(n) = 2^n \cdot n$

$$\lim_{n \rightarrow \infty} \frac{T'(n)}{f'(n)} = \frac{\frac{d}{dn}(3 \cdot 2^n \cdot n + 5)}{\frac{d}{dn}(2^n \cdot n)} \xrightarrow{n \rightarrow \infty} \frac{3 \cdot 2^n \ln(2) \cdot n + 3 \cdot 2^n}{2^n \cdot \ln(2) \cdot n + 2^n} = \frac{3(2^n \ln(2) \cdot n + 2^n)}{(2^n \ln(2) \cdot n + 2^n)} = 3$$

$$\therefore 3 \cdot 2^n \cdot n + 5 = O(2^n \cdot n)$$