Discrete Math Homework 3 Due Wednesday, February 1 at the beginning of class

General instructions:

- Use standard size paper (8.5 by 11).
- Answer each question in order using a single column.
- Be neat. If we cannot read your solution it is wrong.
- Show your work. If you just write an answer, you will get minimal credit even if the answer is correct.

Question A) Rosen 1.1 Exercise 28 (p. 15)

Question B) Rosen 1.1 Exercise 30 (p. 15).

Rosen section 1.3.

Question C) Use a truth table to verify the logical equivalence

$$(p \rightarrow q) \lor r \equiv p \rightarrow (q \lor r)$$

Question D) Use the logical equivalences in Table 6 and $p \rightarrow q \equiv \neg p \lor q$ to show that the following is true

$$(p \rightarrow q) \lor r \equiv p \rightarrow (q \lor r)$$

Question E) Use the logical equivalences in Table 6 and $p \rightarrow q \equiv \neg p \lor q$ to show that the following is true

$$(T \rightarrow (q \lor \neg r)) \land \neg (p \rightarrow F) \equiv (r \rightarrow q) \land p$$

Question F) Rosen 1.3 Exercise 8 c, d (p. 35).

Question G) Rosen 1.3 Exercise 10 a, d (p. 35).

Rosen section 1.4.

Question H) Rosen 1.4 Exercise 8 a, b (p. 53)

Question I) Rosen 1.4 Exercise 2 (p. 53)

Question J) Rosen 1.4 Exercise 6 a, e, f (p. 53)

You may choose to solve one (and only one) of the following Extra Credit Problems. If you submit more than one, only the first will be graded.

Extra Credit 1) Prove or disprove that the following two compound propositions are logically equivalent.

$$(p \to (q \lor \neg r)) \land q$$
$$(q \land s) \lor ((p \leftrightarrow q) \oplus \neg p)$$

Extra Credit 2) Rosen 1.2 Exercise 46 (p. 16) - Hint: See problem 45 for the meaning of Not in this particular Fuzzy Logic system.

Extra Credit 3) Rosen 1.3 Exercise 50 (p. 36) – Hint: Use the result of question 45 to show part c.