

Translating from English to Logic:

- 1) What is my domain?
- 2) What are my quantifiers?
- 3) What are my predicates?
- 4) Build it up

$P(x)$ is "x is happy" $Q(x)$ is "x sleeps 8 hours"

$\forall x.[P(x) \rightarrow Q(x)]$ Every person that is happy sleeps 8 hours

$P(a) = T, Q(a) = T$	
$P(a) = T, Q(a) = F$	This possibility is ruled out
$P(a) = F, Q(a) = T$	
$P(a) = F, Q(a) = F$	

$\forall x.[P(x) \wedge Q(x)] \equiv \forall x.P(x) \wedge \forall x'.Q(x')$ Every person is happy and sleeps 8 hours

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$\forall x.[P(x) \vee Q(x)]$ Every person is happy or sleeps 8 hours

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Example:

Translate "Some happy people do not sleep 8 hours a night." into predicate logic

- 1) people
- 2) Some
- 3) $P(x)$ is "x is happy" $Q(x)$ is "x sleeps 8 hours"
- 4) $\exists x.P(x) \wedge \neg Q(x)$ where x is a person