

(a) De Morgan's theorem: $\overline{a \cdot b} = \bar{a} + \bar{b}$

$$\overline{a + b} = \bar{a} \cdot \bar{b}$$

Context: Boolean algebra
(Lecture 2)

Logic minimisation
(Lecture 3)

(b) A minterm of n Boolean variables is the conjunction of all variables in either their complemented or uncomplemented form

A prime implicant is a term which cannot be further combined.

An essential term is a prime implicant ~~that no other~~ which covers a minterm that no other prime implicant covers.

(c) K-map for $f = (a \cdot b) \oplus (c + d)$:

| | | | | |
|---|----------|---|----------|---|
| | <u>a</u> | | <u>b</u> | |
| | 0 | 0 | 1 | 0 |
| c | 1 | 1 | 0 | 1 |
| d | 1 | 1 | 0 | 1 |
| | 1 | 1 | 0 | 1 |

$$f = \bar{a} \cdot c + \bar{b} \cdot c + \bar{a} \cdot d + \bar{b} \cdot d + ab\bar{c}\bar{d}$$

All terms are prime & essential terms

(d) K-map for f above with don't cares for $a \cdot b$

| | | | | |
|---|-----------------|---|---|---|
| | <u>a b</u> | | | |
| | 0 | 0 | X | 0 |
| c | 1 | 1 | X | 1 |
| d | 1 | 1 | X | 1 |
| | 1 | 1 | X | 1 |

$$f \text{ is now } = c + d$$