

1999

p6q7  
wfc  
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## Prolog Question 2. WFC

A trinary tree is constructed from 3-ary compound terms  $n(a,b,c)$  called nodes, where components  $a, b$  and  $c$  are either nodes or integers. Suppose integer components are restricted to the values 0 and 1.

(a) Write a Prolog program to return a list of all the 0's and a list of all the 1's in a given tree. For example, the goal `enum(n(n(0,1,0),1,0), X, Y)` should instantiate  $X$  to  $[0, 0, 0]$  and  $Y$  to  $[1, 1]$ . The program will be expected to use difference lists.  
[10 marks].

(b) A terminal node of the trinary tree is said to be of *odd parity* if the number of its 1 components is an odd number. For example,  $n(1,1,1)$  is of odd parity, and  $n(1,0,1)$  is not of odd parity. Write a Prolog program to count the number of terminal nodes in a tree that have odd parity. For example, the goal `odd(n(n(0,1,0),1,0), X)` should instantiate  $X$  to 1.  
[10 marks].

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## Suggested Solution.

(a) This is similar in structure to the problem in Worksheet 29 in the notes:

```
enum(n(A, B, C), X1-X4, Y1-Y4) :-
    enum(A, X1-X2, Y1-Y2),
    enum(B, X2-X3, Y2-Y3),
    enum(C, X3-X4, Y3-Y4).
enum(0, [0|X]-X, Y-Y).
enum(1, X-X, [1|Y]-Y).
```

(b)

```
odd(n(A, B, C), Z) :- odd(A, An), odd(B, Bn), odd(C, Cn), Z is An+Bn+Cn.
odd(n(0,0,1), 1).
odd(n(0, 1,0), 1).
odd(n(1, 0, 0), 1).
odd(n(1,1,1), 1).
odd(n(_, _, _), 0).
```

There is no doubt a tail recursive formulation as well.