

maximum is 2^{n-1}

$$Z = Y \times X$$

y_1, y_0	x_1, x_0	z_3	z_2	z_1	z_0
0 0	0 0	0	0	0	0
0 0	0 1	0	0	0	0
0 0	1 0	0	0	0	0
0 0	1 1	0	0	0	0
0 1	0 0	0	0	0	0
0 1	0 1	0	0	0	1
0 1	1 0	0	0	1	0
0 1	1 1	0	0	1	1
1 0	0 0	0	0	0	0
1 0	0 1	0	0	1	0
1 0	1 0	0	1	0	0
1 0	1 1	0	1	1	0
1 1	0 0	0	0	0	0
1 1	0 1	0	0	1	0
1 1	1 0	0	0	1	1
1 1	1 1	0	1	1	0
1 1	1 1	1	0	0	1

$$Z_3 = y_1 y_0 x_1 x_0$$

$$Z_2 = y_1 \bar{y}_0 x_1 + y_1 x_1 \bar{x}_0$$

Z_1

$\neg x_0$

y_1	$1x1$	$1x3$	$1x2$	$1x0$
y_1	$3x1$	$3x3$	$3x2$	$3x0$
y_1	$2x1$	$2x3$	$2x2$	$2x0$
y_1	$0x1$	$0x3$	$0x2$	$0x0$

x_1

~~$$Z = y_0 \bar{y}_1 x_1 + y_1 y_0 \bar{x}_1 + y_1 \bar{y}_0 x_0$$~~

$$Z_1 = \bar{y}_1 y_0 x_1 + y_1 \bar{y}_0 x_0 + x_1 \bar{x}_0 y_0 + \bar{x}_1 x_0 y_1$$

Z_0

$\neg x_0$

y_0	1	1		
y_0	1	1		
y_0				
y_0				

x_1

$$Z_0 = x_0 y_0$$

8 bit multiplier \Rightarrow 16 eqns in 16 variables
 $\sim 2^{15}$ complexity

Another way is with two bit multipliers and adders

Another way is with shift and add.