

Question 1      Notes

This is closely based on 93 P11 q11.  
It worked fairly well then. I don't think  
the prior set matters.

Solution      Definitions

- i) REFL, ANTI-SYMM + TRANSITIVE. (3)
- ii) + "TRICHOTOMY" (1)
- iii) ~~ALL~~  $\infty$  DESCENDING CHAINS (2)  
are ultimately constant.

Examples

	over $\mathbb{N}$	over $\mathbb{Z}$
a) $\mathbb{P}_1$		
(4) i)	✓	✓
ii)	✓	✓
iii)	✓	×
minimal	○	—
maximal	—	—

# Mathematics for Computation Theory

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## Question 1 solution ctd)

### Examples

b)  $R_2$

over  $N$

over  $Z$

(5)

i)	✓	✗ pre-order (2)
ii)	✗	✗
iii)	✓ (1)	✗ (2)
minimal	1	— (2)
maximal	0	0

(1) under my definition — need to be flexible.

(2)  $1 = -1 \cdot -1$  ,  $-1 = -1 \cdot 1$

c)  $R_3$

(5)

i)	✗ (3)	✗ (3)
ii)	✗	✗
iii)	✓	✓
minimal	1	1, -1
maximal	0	0

(3) NOT transitive, hence not partial order,