Solution notes

Foundations of Computer Science 2005 – Paper 1 Question 6 (LCP)

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(a) (Lecture 7, datatypes and exceptions.)
fun sum [] = 0 : int
  | sum (k::ks) = k + sum ks;
exception Fail;
fun find_path p t =
  let fun find vs (Twig v) = if p (v + sum vs) then rev (v::vs)
                               else raise Fail
    \mid find vs (Br(v,t1,t2)) =
        find (v::vs) t1
        handle Fail => find (v::vs) t2
  in find [] t
  end;
(b) (Lectures 4–5, lists, and 10, functions as values.)
fun all_paths p t =
  let fun find vs (Twig v) = if p (v + sum vs) then [rev (v::vs)] else []
    \mid find vs (Br(v,t1,t2)) =
        (find (v::vs) t1) @ (find (v::vs) t2)
  in find [] t
  end;
(c) (Lecture 13, lazy lists.)
The accumulating argument has to be a function in order for laziness to work.
fun all_pathq p t =
  let fun find vs (Twig v) xf =
           if p (v + sum vs) then Cons(rev (v::vs), xf) else xf()
    | find vs (Br(v,t1,t2)) xf =
        find (v::vs) t1 (fn () => find (v::vs) t2 xf)
  in find [] t (fn () => Nil)
  end;
```