

Solution notes

Specification and Verification I 2005 – Paper 8 Question 13 (MJCG)

- (b) What is partial about partial correctness? [2 marks]

Partial correctness only considers properties of the form “if a program terminates then ...”. It is partial because it does not specify termination; it deals with safety but not liveness.

- (b) What is the difference between a variant and an invariant? [2 marks]

A variant is an expressions whose value strictly decreases on each iteration of a loop. An invariant is a statement that remains true after each iteration. Thus a variant changes value, but an invariant doesn't change its truth-value. Invariants are for partial correctness and variants are to prove termination.

- (c) Why are annotations needed for mechanising program verification? [2 marks]

Annotations are needed because there is no algorithm that will generate invariants or variants (program correctness is undecidable, at least when arithmetic is present).

- (d) What additional annotations are needed for total correctness? [2 marks]

For total correctness one must provide a variant as an additional annotation beyond those needed for partial correctness.

- (e) How do refinement and *post hoc* verification differ? [2 marks]

*Refinement is a correct-by-construction method of writing code; with *post hoc* verification one first writes code, then proves it correct.*

- (f) Give an example of a higher-order formula that is not first-order. [2 marks]

$$\forall e_0. g. \exists f. f(0) = e_0 \wedge f(n+1) = g(f(n))$$

- (g) Why is higher-order logic typed? [2 marks]

Higher order logic is typed to avoid Russell's Paradox:

$$(\lambda P. \neg(P(P)))(\lambda P. \neg(P(P))) = \neg((\lambda P. \neg(P(P)))(\lambda P. \neg(P(P))))$$

- (h) How are $\{P\}C\{Q\}$ and $\text{wlp}(C, Q)$ related? [2 marks]

$$\{P\}C\{Q\} = P \Rightarrow \text{wlp}(C, Q)$$

- (i) How can $[c]q$ and $\langle c \rangle q$ be defined in higher-order logic? [2 marks]

$$[c]q = \lambda s. \forall s'. c(s, s') \Rightarrow q(s') \text{ and } \langle c \rangle q = \neg([c](\neg q))$$

- (j) Explain the difference between soundness and completeness? [2 marks]

A deductive system is sound if everything that can be deduced is true; it is complete if everything that is true can be deduced.

Context

This question covers the whole course.

Marking Scheme

For each section:

2 marks : complete and correct answer;

1 marks : partial answer lacking some key material or minor inaccuracies;