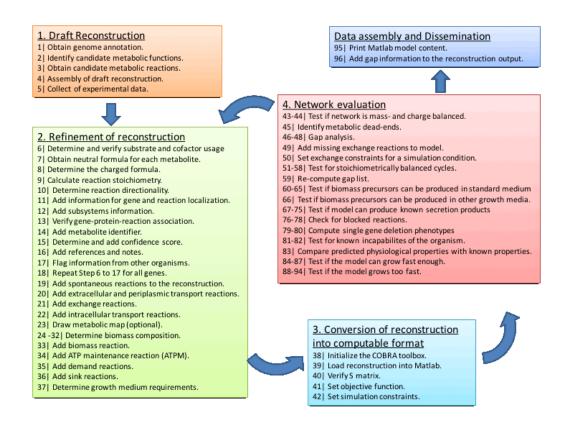
Example use of functions listed in the Standard operating procedure for metabolic reconstruction.

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INTRODUCTION

This tutorial has been adapted and expanded from the protocol for generating metabolic network reconstruction [1].



This tutorial will illustrate the example input for The COBRA Toolbox functions applied in the <u>steps 38 to 96</u> of the protocol workflow, using the E. coli core reconstruction [2] as the model of choice.

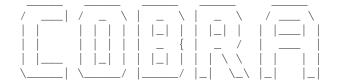
When Matlab/Toolbox commands are following by a ';' the output is not printed. Omitting the ';' invokes printing of the variable content.

EQUIPMENT SETUP

Step 38. Initialize The COBRA Toolbox.

Initialize The COBRA Toolbox using the initCobraToolbox function.

initCobraToolbox(false) % false, as we don't want to update



COnstraint-Based Reconstruction and Analysis The COBRA Toolbox - 2017

Documentation:

http://opencobra.github.io/cobratoolbox

- > Checking if git is installed ... Done.
- > Checking if the repository is tracked using git ... Done.
- > Checking if curl is installed ... Done.
- > Checking if remote can be reached ... Done.
- > Initializing and updating submodules ... Done.
- > Adding all the files of The COBRA Toolbox ... Done.
- > Define CB map output... set to svg.
- > Retrieving models ... Done.
- > TranslateSBML is installed and working properly.
- > Configuring solver environment variables ...
 - [---*] ILOG_CPLEX_PATH: C:\Program Files\IBM\ILOG\CPLEX_Studio1263\cplex\matlab\x64_win64
 - [---] GUROBI_PATH: --> set this path manually after installing the solver (see instructions)
 - [---*] TOMLAB_PATH: C:\Program Files\tomlab\
 - [----] $MOSEK_PATH$: --> set this path manually after installing the solver (see instructions) Done.
- > Checking available solvers and solver interfaces ... Done.
- > Setting default solvers ... Done.
- > Saving the MATLAB path ... Done.
 - The MATLAB path was saved in the default location.
- > Summary of available solvers and solver interfaces

	Support	LP	MILP	QP	MIQP	NLP
cplex_direct	full	0	0	0	0	_
dqqMinos	full	0	_	_	_	-
glpk	full	1	1	_	-	_
gurobi	full	1	1	1	1	_
ibm_cplex	full	0	0	0	-	_
matlab	full	1	-	_	-	1
mosek	full	0	0	0	-	-
pdco	full	1	-	1	-	-
quadMinos	full	0	-	-	-	0
tomlab_cplex	full	1	1	1	1	-
qpng	experimental	-	-	1	-	-
tomlab_snopt	experimental	-	_	_	_	1
gurobi_mex	legacy	0	0	0	0	_
lindo_old	legacy	0	_	-	_	_
lindo_legacy	legacy	0	_	_	_	_
lp_solve	legacy	1	_	_	_	_
opti	legacy	0	0	0	0	0
Total		6	3	4	2	2

⁺ Legend: - = not applicable, 0 = solver not compatible or not installed, 1 = solver installed.

- > You can solve LP problems using: 'glpk' 'gurobi' 'matlab' 'pdco' 'tomlab_cplex' 'lp_solve'
- > You can solve MILP problems using: 'glpk' 'gurobi' 'tomlab_cplex'
- > You can solve QP problems using: 'gurobi' 'pdco' 'tomlab_cplex' 'qpng'
- > You can solve MIQP problems using: 'gurobi' 'tomlab_cplex'
- > You can solve NLP problems using: 'matlab' 'tomlab_snopt'
- > Checking for available updates ...
- --> You cannot update your fork using updateCobraToolbox(). [f4a806 @ TutorialReview-SOP]. Please use the MATLAB.devTools (https://github.com/opencobra/MATLAB.devTools).

Setting the optimization solver.

This tutorial will be run with the 'glpk' package, which is a linear programming ('LP') solver. The 'glpk' package does not require additional instalation and configuration.

```
solverName = 'glpk';
solverType = 'LP';
changeCobraSolver(solverName, solverType);
```

However, for the analysis of large models, such as Recon 3, it is not recommended to use the 'glpk' package but rather an industrial strength solver, such as the 'gurobi' package.

A solver package may offer different types of optimization programmes to solve a problem. The above example used a LP optimization, other types of optimization programmes include; mixed-integer linear programming ('MILP'), quadratic programming ('QP'), and mixed-integer quadratic programming ('MIQP').

```
warning off MATLAB:subscripting:noSubscriptsSpecified
```

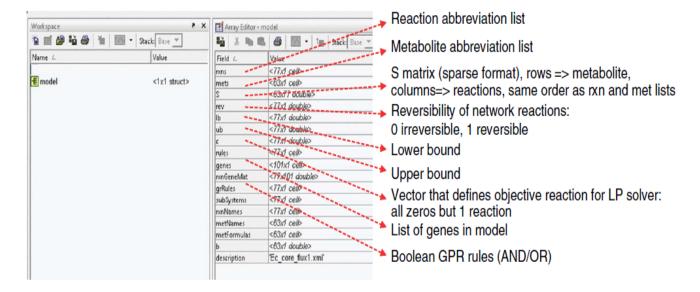
PROCEDURE

Step 39. Load reconstruction into Matlab.

The metabolic network reconstruction, containing a reaction and metabolite list, is contained by the file 'Ecoli_core_model.mat'.

```
modelFileName = 'ecoli_core_model.mat';
modelDirectory = getDistributedModelFolder(modelFileName); %Look up the folder for the
modelFileName= [modelDirectory filesep modelFileName]; % Get the full path. Necessary
model = readCbModel(modelFileName);
modelEcore = model;
```

The reconstruction is contained in the resulting model structure.



The figure above shows the data contained in the different structure fields. We will use this model structure for all consequent computation if not noted differently.

Use the command open to view the model structure in Matlab.

```
if usejava('desktop') % This line of code is to avoid execution of example in non gui-e
    open modelEcore
end
```

The content of the structure can be assessed as follows:

• You wish to see the abbreviation of the 8th metabolite in the model:

```
modelEcore.mets{8}

ans =
acald[c]
```

You wish to see the abbreviation of the 1st reaction in the model:

```
modelEcore.rxns{1}
ans =
ACALD
```

 You wish to see the entry of the stoichiometric matrix of the 1st reaction (column) and 8th metabolite (row):

```
modelEcore.S(8,1)
ans =
  (1,1)     -1
```

Print the reaction formula of the 1st reaction in the model:

```
printRxnFormula(modelEcore, modelEcore.rxns(1))

ACALD acald[c] + coa[c] + nad[c] <=> accoa[c] + h[c] + nadh[c]
ans =
   'acald[c] + coa[c] + nad[c] <=> accoa[c] + h[c] + nadh[c] '
```

 You want to change the lower bound (lb) of the 5th reaction to 10 mmol/gDW/h (without using any COBRA Toolbox functions):

```
rules: {95×1 cell}
  genes: {137×1 cell}
rxnGeneMat: [95×137 double]
  grRules: {95×1 cell}
subSystems: {95×1 cell}
  rxnNames: {95×1 cell}
  metNames: {72×1 cell}
metFormulas: {72×1 cell}
  b: [72×1 double]
description: 'Ecoli_core_model'
```

You want to add a field to the model structure.

A note:

```
modelEcore.newField = 'ABC - a note'
modelEcore =
           rxns: {95×1 cell}
           mets: \{72\times1\text{ cell}\}
             S: [72×95 double]
            rev: [95×1 double]
             lb: [95×1 double]
             ub: [95×1 double]
             c: [95×1 double]
          rules: {95×1 cell}
          genes: {137×1 cell}
     rxnGeneMat: [95×137 double]
       grRules: {95×1 cell}
     subSystems: {95×1 cell}
      rxnNames: {95×1 cell}
       metNames: {72×1 cell}
    metFormulas: {72×1 cell}
         b: [72×1 double]
    description: 'Ecoli_core_model'
       newField: 'ABC - a note'
```

An array $B = [1 \ 2 \ 3]$

```
B = [1 2 3];
modelEcore.newField = B
```

```
modelEcore =
           rxns: {95×1 cell}
           mets: \{72\times1\text{ cell}\}
             S: [72×95 double]
            rev: [95×1 double]
             lb: [95×1 double]
             ub: [95×1 double]
             c: [95×1 double]
          rules: {95×1 cell}
          genes: {137×1 cell}
     rxnGeneMat: [95×137 double]
       grRules: {95×1 cell}
     subSystems: {95×1 cell}
      rxnNames: {95×1 cell}
       metNames: {72×1 cell}
    metFormulas: {72×1 cell}
         b: [72×1 double]
    description: 'Ecoli_core_model'
      newField: [1 2 3]
```

• Create a list of strings:

• Create a list of numbers:

• Transpose a list:

```
ListTranspose = ListNumbers'
ListTranspose =

1
2
2
```

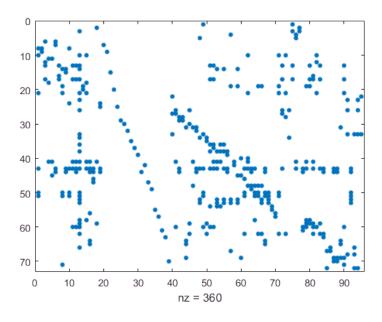
• Find the index of a reaction, e.g., 'ATPM', in the model

```
rxnList = 'ATPM';
rxnID = findRxnIDs(modelEcore, rxnList)
rxnID = 11
```

Step 40. Verify S matrix.

Remember that in the S matrix the rows and the columns correspond to the metabolites and the reactions of the model, respectively. The number of non-zero (nz) entries in the S matrix is visualized graphically below using a spy image.

```
spy(modelEcore.S)
```



To put this number into perspective, we can calculate the percentage of non-zero entries of S.

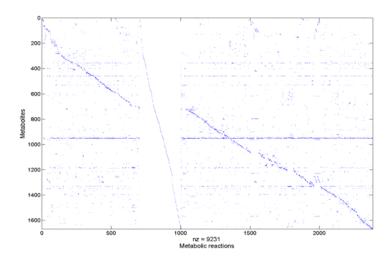
```
[a, b] = size(modelEcore.S);
nz = nnz(modelEcore.S);
Perc_nz = nz*100/(a*b)
```

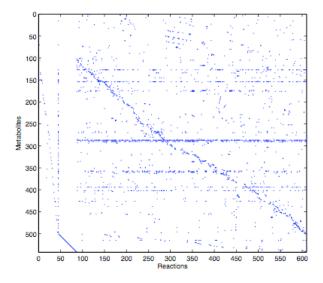
 $Perc_nz = 5.2632$

- Many large scale models have less than 1% of non-zero entries in the S matrix.
- Looking at the S matrix is a quick way to see whether there is something obviously wrong with the model and the S matrix.

Here are two further examples of S matrices visualized using a spy image:

E. coli - AF1260 [3]





Consider to also use the tutorial on 'Numerical properties of a reconstruction' to investigate the propeties of the S matrix.

Step 41. Set objective function.

We will set the biomass reaction (Biomass_Ecoli_core_w_GAM) of the *E. coli* core model as objective function:

```
modelEcore = changeObjective(modelEcore, 'Biomass_Ecoli_core_w_GAM');
```

If you wish to check which reaction(s) make up the objective function and its components, use the following function:

objectiveAbbr = checkObjective(modelEcore)

maryT = Coefficient	Metabolite	metID	Reaction	RxnID
-1.496	3pg[c]	3	Biomass_Ecoli_core_w_GAM	13
-3.7478	accoa[c]	10	Biomass_Ecoli_core_w_GAM	13
59.81	adp[c]	13	Biomass_Ecoli_core_w_GAM	13
4.1182	akg[c]	14	Biomass_Ecoli_core_w_GAM	13
-59.81	atp[c]	17	Biomass_Ecoli_core_w_GAM	13
3.7478	coa[c]	21	Biomass_Ecoli_core_w_GAM	13
-0.361	e4p[c]	23	Biomass_Ecoli_core_w_GAM	13
-0.0709	f6p[c]	26	Biomass_Ecoli_core_w_GAM	13
-0.129	g3p[c]	33	Biomass_Ecoli_core_w_GAM	13
-0.205	g6p[c]	34	Biomass_Ecoli_core_w_GAM	13
-0.2557	gln-L[c]	36	Biomass_Ecoli_core_w_GAM	13
-4.9414	glu-L[c]	38	Biomass_Ecoli_core_w_GAM	13
-59.81	h2o[c]	41	Biomass_Ecoli_core_w_GAM	13
59.81	h[c]	43	Biomass_Ecoli_core_w_GAM	13
-3.547	nad[c]	50	Biomass_Ecoli_core_w_GAM	13
3.547	nadh[c]	51	Biomass_Ecoli_core_w_GAM	13
13.028	nadp[c]	52	Biomass_Ecoli_core_w_GAM	13

```
-13.028
                  nadph[c]
                                53
                                         Biomass_Ecoli_core_w_GAM
                                                                      13
   -1.7867
                  oaa[c]
                                58
                                         Biomass_Ecoli_core_w_GAM
                                                                      13
    -0.5191
                                59
                                         Biomass_Ecoli_core_w_GAM
                                                                      13
                  pep[c]
     59.81
                 pi[c]
                                60
                                         Biomass_Ecoli_core_w_GAM
                                                                      13
                                62
                                         Biomass_Ecoli_core_w_GAM
                                                                      13
    -2.8328
                  pyr[c]
   -0.8977
                  r5p[c]
                                66
                                         Biomass Ecoli core w GAM
                                                                     13
objectiveAbbr =
    'Biomass_Ecoli_core_w_GAM'
```

Step 42. Set simulation constraints.

EX_glc(e) -10
maxConstraints:

A first step when using and debugging a model should be to identify the constraints that have been applied.

```
minInf = -1000;
maxInf = 1000;
printConstraints(modelEcore, minInf, maxInf)

MinConstraints:
ACONTD    10
ATPM    8.39
```

- As you can see, only three reactions are constrained in this model. The glucose exchange reaction (EX_glc(e)), the aconitase reaction (ACONTb) and the ATP non-growth associated maintenance reaction (ATPM). Note that in all three cases, a lower bound has been set only but no upper bound.
- The 'minInf' and 'maxInf' were set to -1000 and 1000, respectively, as these values represent the infinity of the E. coli core model. Other models may have different infinities.
- Note also that the printConstraints function returns only those constraints that are greater than -1000 but are smaller than 1000.

To know which medium constraints are applied to the model, we can use the following function:

```
printUptakeBound(modelEcore);
EX_co2(e) -1000
EX_glc(e) -10
EX_h(e) -1000
EX_h2o(e) -1000
EX_nh4(e) -1000
EX_nb4(e) -1000
EX_pi(e) -1000
EX_pi(e) -1000
```

• As you can see, the model is set to a minimal medium (EX_glc(e) set to -10 mmol/gDW/h) with the presence of oxygen.

Let's assume that you would like to set the lower bound of the ATP maintenance reaction ('ATPM') to 8.39 mmol/gDW/h:

```
modelEcore = changeRxnBounds(modelEcore, 'ATPM', 8.39, '1');
```

and the upper bound of the 'ATPM' reaction to 8.39 mmol/gDW/h:

```
modelEcore = changeRxnBounds(modelEcore, 'ATPM', 8.39, 'u');
```

To change both the lower and upper bound in the same command use:

```
modelEcore = changeRxnBounds(modelEcore, 'ATPM', 8.39, 'b');
```

Let's assume that you would like to set the lower bound of the 'ATPM' reaction to 8.39 mmol/gDW/h and the ATP synthetase ('ATPS4r') to an upper bound of 100 mmol/gDW/h:

```
modelEcore = changeRxnBounds(modelEcore, 'ATPM', 8.39, 'l' );
modelEcore = changeRxnBounds(modelEcore, 'ATPS4r', 100, 'u');
```

The set constraints can be checked using the following function:

```
printConstraints(modelEcore, -1000,1000)

MinConstraints:
ACONTD   10
ATPM   8.39
EX_glc(e)   -10
maxConstraints:
ATPM   8.39
ATPS4r   100
```

Steps 43 - 44. Test if network is mass- and charge balanced.

Check mass- and charge balance for the entire network of the model:

```
[massImbalance, imBalancedMass, imBalancedCharge, imBalancedRxnBool, Elements, missingF
```

Step 45. Identify metabolic dead-ends

Detect deadend metabolites:

```
outputMets = detectDeadEnds(modelEcore)

outputMets =
   30
   32
   37
   49
```

Print the corresponding metabolite names:

```
DeadEnds = modelEcore.mets(outputMets)

DeadEnds =
    'fru[e]'
    'fum[e]'
    'gln-L[e]'
    'mal-L[e]'
```

• These metabolites are only produced or consumed in the network and the associated reactions are blocked reactions.

Identify associated reactions:

[rxnList, rxnFormulaList] = findRxnsFromMets(modelEcore, DeadEnds)

```
rxnList =
   'EX_fru(e)'
    'EX_fum(e)'
    'EX_gln_L(e)'
    'EX_mal_L(e)'
    'FRUpts2'
    'FUMt2_2'
    'GLNabc'
    'MALt2_2'
rxnFormulaList =
   'fru[e] -> '
    'fum[e] -> '
    'gln-L[e] -> '
    'mal-L[e] -> '
    'fru[e] + pep[c] -> f6p[c] + pyr[c] '
    'fum[e] + 2 h[e] -> fum[c] + 2 h[c] '
    'atp[c] + gln-L[e] + h2o[c] -> adp[c] + gln-L[c] + h[c] + pi[c] '
    '2 h[e] + mal-L[e] -> 2 h[c] + mal-L[c] '
```

 As you can see, these metabolites have each two reactions associated. Why are they then detected as deadend metabolites?

Let's have a look at the lower and upper bounds of these reactions:

```
ans = 1000
1000
1000
1000
1000
1000
1000
```

• In this particular case, these four metabolites are deadend metabolites as the associated exchange reactions are set to lb=0 (i.e., no uptake is permitted). As we are interested in dead-end metabolites that are generally only consumed or produced by the network, irrespective of the applied constraints, we will set the lower bound of all exchange reaction to -1000 and the upper bound to 1000.

```
modelEcore_New = modelEcore;
modelEcore_New.lb(strmatch('EX_', modelEcore_New.rxns)) = -1000;
modelEcore_New.ub(strmatch('EX_', modelEcore_New.rxns)) = 1000;
```

Now we repeat the identification of deadend metabolites:

- And indeed no deadend metabolites remain. This example also illustrates how such issues can be fixed one option is to revert the directionality of the associated reactions.
- Note that changing the directionality must be carefully evaluated in each case, to ensure that the
 resulting model is biologically accurate. For instance, changing the directionality of the 'FRUpts_2'
 reaction would have not been biologically meaningful, as the Phosphotransferase system is known to
 be unidirectional under physiologically relevant conditions.

Steps 46 - 49. Refer to 'gap analysis' tutorial.

Step 50. Set exchange constraints for a simulation condition.

The COBRA Toolbox function, changeRxnBounds, is used to set constraints on a reaction which is demonstrated in step 67 of this tutorial.

Steps 51 - 59. Test for stoichiometrically balanced cycles (SBCs).

SBCs or Type III pathways, are formed by internal network reactions and can carry fluxes despite closed exchange reactions (closed system). Therefore, use the following testForTypeIIIPathways function. The function is only available for windows systems and requires the X3 program from the UCSD Systems Biology Research Group homepage:

- The indices of the exchange reactions ('EX_') are input as a list.
- The output filename can be specified with 'test', it receives automatically the extension '.expa'. The filename is optional, the default name is: 'ModelTestTypeIII'

```
selExc = findExcRxns(modelEcore);
listExch = find(selExc);
```

```
try
    testForTypeIIIPathways(modelEcore, listExch, 'test');
catch ME
    getReport(ME)
end
```

No Type III pathways can be found in model.rm: cannot remove 'test_myT3_Sprs.txttest_myT3.txttest_myRxnMet /bin/bash: del: command not found

This error message is returned from X3.exe since there are no SBCs in the E. coli core network.

Steps 60 - 66. Test if biomass precursors can be produced in standard medium

%TODO steps 64 to 66 are not referenced in this section.

60. Obtain a list of biomass components:

```
BiomassComponents = modelEcore.mets(find(modelEcore.S(:, strmatch('Biomass', modelEcore
BiomassComponents =
   '3pg[c]'
    'accoa[c]'
    'adp[c]'
    'akg[c]'
    'atp[c]'
    'coa[c]'
    'e4p[c]'
    'f6p[c]'
    'g3p[c]'
    'g6p[c]'
    'gln-L[c]'
    'glu-L[c]'
    'h2o[c]'
    'h[c]'
    'nad[c]'
    'nadh[c]'
    'nadp[c]'
    'nadph[c]'
    'oaa[c]'
    'pep[c]'
    'pi[c]'
    'pyr[c]'
    'r5p[c]'
```

61. Add a demand function for each biomass precursor:

```
[modelEcore_NEW, rxnNames] = addDemandReaction(modelEcore, BiomassComponents);
DM_3pg[c]
           3pg[c]
                     ->
DM_accoa[c]
            accoa[c]
                         ->
DM_adp[c]
         adp[c]
                     ->
DM_akg[c]
         akg[c]
                     ->
         atp[c]
DM_atp[c]
                     ->
         coa[c]
DM_coa[c]
                     ->
           e4p[c]
DM_e4p[c]
                     ->
DM_f6p[c] f6p[c]
                     ->
```

```
DM_g3p[c]
          g3p[c]
DM_g6p[c] g6p[c]
DM_gln-L[c] gln-L[c]
DM_glu-L[c] glu-L[c]
DM_h2o[c] h2o[c]
              glu-L[c]
20[c]
DM_h[c] h[c]
DM_nad[c] nad[c]
                      ->
DM_nadh[c] nadh[c]
                        ->
DM_nadp[c] nadp[c]
DM_nadph[c] nadph[c]
DM_oaa[c] oaa[c] ->
DM_pep[c] pep[c]
                       ->
DM_pi[c] pi[c]
DM_pyr[c] pyr[c]
DM_r5p[c] r5p[c]
```

For each biomass component i, perform the following test:

```
for i = 1 : length(BiomassComponents)
```

62. Change objective function to the demand function:

```
modelEcore_NEW = changeObjective(modelEcore_NEW, rxnNames(i));
```

63. Maximize ('max') for new objective function (Demand function)

```
FBAsolution = optimizeCbModel(modelEcore_NEW, 'max');
```

- FBAsolution is a structure containing the result of the optimization. FBAsolution.f gives the maximal value of the objective reaction (i.e., 'DM_pep[c]'), which is greater than 0 mmol/gDW/h. This means that our *E. coli* core model can produce pep[c].
- Store each solution in a vector:

```
BiomassComponentsValue(i,1) = FBAsolution.f;
end
```

Print each BiomassComponent and the corresponding value:

```
[BiomassComponents num2cell(BiomassComponentsValue)]
```

```
ans =
              [
                   10.0000]
   '3pg[c]'
   'accoa[c]'
              [-1.1313e-16]
              [-1.7764e-15]
   'adp[c]'
              [ 10.0000]
   'akg[c]'
   'atp[c]'
              [
                        0]
   'coa[c]'
              [ 3.4642e-15]
   'e4p[c]'
              [
                   7.5000]
   'f6p[c]'
              [
                   5.0000]
   'g3p[c]'
              [
                    10]
   'g6p[c]'
              [
                   5.0000]
   'gln-L[c]' [
                       10]
```

```
'glu-L[c]' [
'h2o[c]' [
                 10.0000]
'h2o[c]'
                   1000]
'h[c]'
            [
                    1000]
'nad[c]'
            [ 8.3105e-16]
'nadh[c]'
            [ 2.9009e-27]
            [ 9.1312e-29]
'nadp[c]'
'nadph[c]'
            [-1.1583e-16]
            [ 10.0000]
'oaa[c]'
'pep[c]'
                 10.0000]
            [
'pi[c]'
            [ 1.0000e+03]
           [ 10.0000]
'pyr[c]'
                  6.0000]
'r5p[c]'
            [
```

- As we can see, not all biomass components (or rather their corresponding demand reaction) can have a non-zero flux. Why is that?
- Just to remember us, the model constraints are:

```
printConstraints(modelEcore_NEW, -1000,1000)
```

```
MinConstraints:
ACONTb 10
ATPM 8.39
EX_glc(e) -10
maxConstraints:
ATPM 8.39
ATPS4r 100
```

- Note that only those constraints will be printed that are smaller greater than -1000 and smaller than 1000.
- Let's revisit how the biomass reaction is formulated in this model:

modelEcore = changeObjective(modelEcore, modelEcore.rxns(strmatch('Biomass', modelEcore)
[objectiveAbbr] = checkObjective(modelEcore)

maryT = Coefficient	Metabolite	metID	Reaction	RxnII
-1.496	3pg[c]	3	Biomass_Ecoli_core_w_GAM	13
-3.7478	accoa[c]	10	Biomass_Ecoli_core_w_GAM	13
59.81	adp[c]	13	Biomass_Ecoli_core_w_GAM	13
4.1182	akg[c]	14	Biomass_Ecoli_core_w_GAM	13
-59.81	atp[c]	17	Biomass_Ecoli_core_w_GAM	13
3.7478	coa[c]	21	Biomass_Ecoli_core_w_GAM	13
-0.361	e4p[c]	23	Biomass_Ecoli_core_w_GAM	13
-0.0709	f6p[c]	26	Biomass_Ecoli_core_w_GAM	13
-0.129	g3p[c]	33	Biomass_Ecoli_core_w_GAM	13
-0.205	g6p[c]	34	Biomass_Ecoli_core_w_GAM	13
-0.2557	gln-L[c]	36	Biomass_Ecoli_core_w_GAM	13
-4.9414	glu-L[c]	38	Biomass_Ecoli_core_w_GAM	13
-59.81	h2o[c]	41	Biomass_Ecoli_core_w_GAM	13
59.81	h[c]	43	Biomass_Ecoli_core_w_GAM	13
-3.547	nad[c]	50	Biomass_Ecoli_core_w_GAM	13
3.547	nadh[c]	51	Biomass_Ecoli_core_w_GAM	13
13.028	nadp[c]	52	Biomass_Ecoli_core_w_GAM	13
-13.028	nadph[c]	53	Biomass_Ecoli_core_w_GAM	13
-1.7867	oaa[c]	58	Biomass_Ecoli_core_w_GAM	13
-0.5191	pep[c]	59	Biomass_Ecoli_core_w_GAM	13
59.81	pi[c]	60	Biomass_Ecoli_core_w_GAM	13

```
-2.8328 pyr[c] 62 Biomass_Ecoli_core_w_GAM 13
-0.8977 r5p[c] 66 Biomass_Ecoli_core_w_GAM 13
objectiveAbbr =
    'Biomass_Ecoli_core_w_GAM'
```

- As you can see, there are numerous metabolites that have a positive coefficient in the biomass equation, meaning that they are produced by the biomass reaction and thus we need to test whether these metabolites can be removed, rather than produced by the model. Hence, we need to add sink reactions (rather than demand reactions) and minimize them:
- **64.** Identify reactions that are mainly responsible for synthesizing the biomass component.
 - Let's get all biomass components with a positive coefficient in the biomass reaction:

```
BiomassComponentsPos = modelEcore.mets(find(modelEcore.S(:, strmatch('Biomass', modelEcore.S()))
BiomassComponentsPos =
    'adp[c]'
    'akg[c]'
    'coa[c]'
    'h[c]'
    'nadh[c]'
    'nadp[c]'
    'pi[c]'
BiomassComponentsNeg = modelEcore.mets(find(modelEcore.S(:, strmatch('Biomass', modelEcore.S()))
BiomassComponentsNeg =
   '3pg[c]'
    'accoa[c]'
    'atp[c]'
    'e4p[c]'
    'f6p[c]'
    'g3p[c]'
    'g6p[c]'
    'gln-L[c]'
    'glu-L[c]'
    'h2o[c]'
    'nad[c]'
    'nadph[c]'
    'oaa[c]'
    'pep[c]'
    'pyr[c]'
    'r5p[c]'
```

65. For each of these metabolites, we add sink reactions for components with a positive coefficient and demand reactions for components with a negative coefficient.

```
[modelEcore_NEW] = addSinkReactions(modelEcore, BiomassComponentsPos);
sink_adp[c]
            adp[c]
                      <=>
sink_akg[c] akg[c]
                     <=>
sink_coa[c]
           coa[c]
                     <=>
sink_h[c] h[c]
                 <=>
sink_nadh[c] nadh[c]
                      <=>
sink_nadp[c] nadp[c]
sink_pi[c] pi[c]
                  <=>
```

```
[modelEcore_NEW, rxnNames] = addDemandReaction(modelEcore_NEW, BiomassComponentsNeg);
         3pg[c]
DM 3pq[c]
DM_accoa[c] accoa[c]
                       ->
DM_atp[c] atp[c]
                    ->
DM_e4p[c] e4p[c]
                    ->
DM_f6p[c] f6p[c]
                    ->
DM_g3p[c] g3p[c]
                    ->
DM_g6p[c] g6p[c]
                    ->
DM_gln-L[c] gln-L[c]
DM_glu-L[c]
           glu-L[c]
DM_h2o[c] h2o[c]
                   ->
DM_nad[c] nad[c]
DM_nadph[c] nadph[c]
DM_oaa[c] oaa[c]
                   ->
        pep[c]
DM_pep[c]
                    ->
DM_pyr[c]
          pyr[c]
                    ->
DM_r5p[c]
          r5p[c]
                    ->
```

• Note that we added both the sink and the demand reactions to the model simultanously. The reason for this is that metabolites such as coa and accoa, or nadh and nad, are not produced or consumed in this model but only recycled. Hence, for obtaining a non-zero flux for any of the associated sink or demand reactions one needs to add the reaction pair. In larger networks (than the *E. coli* core model) this will be less of a problem as they capture the biosynthetic pathways for these metabolites.

Now lets repeat the analysis (note that we minimize the objective):

```
for i = 1 : length(BiomassComponentsPos)
    modelEcore_NEW = changeObjective(modelEcore_NEW, strcat('sink_', BiomassComponents
    FBAsolution = optimizeCbModel(modelEcore_NEW, 'min');
    BiomassComponentsValuePos(i, 1) = FBAsolution.f;
end
[BiomassComponentsPos num2cell(BiomassComponentsValuePos)]
ans =
   'adp[c]'
             Γ
                  -1000]
   'akg[c]'
             [
                  -1000]
   'coa[c]'
              [-663.3333]
   'h[c]'
              Γ
                  -10001
              [
   'nadh[c]'
                  -1000]
```

• All these metabolites can be removed by the model.

-1000]

-1000]

[

[

'nadp[c]'

'pi[c]'

ans =

We repeat the same analysis for all negative biomass components.

Now lets repeat the analysis (note that we maximize the objective):

```
for i = 1 : length(BiomassComponentsNeg)
    modelEcore_NEW = changeObjective(modelEcore_NEW, strcat('DM_', BiomassComponentsNeg
    FBAsolution = optimizeCbModel(modelEcore_NEW, 'max');
    BiomassComponentsValueNeg(i, 1) = FBAsolution.f;
end
[BiomassComponentsNeg num2cell(BiomassComponentsValueNeg)]
```

```
'3pg[c]'
           [ 555.8050]
'accoa[c]'
            [ 663.3333]
            [ 1000]
[ 280.4025]
'atp[c]'
'e4p[c]'
            [ 186.9350]
'f6p[c]'
           [ 370.5367]
'g3p[c]'
'q6p[c]'
           [ 186.9350]
'gln-L[c]'
           [
                    500]
'glu-L[c]' [1.0000e+03]
'h2o[c]'
                  1000]
           [
           [1.0000e+03]
'nad[c]'
'nadph[c]' [
                  1000]
'oaa[c]'
           [ 990.1464]
'pep[c]'
           [ 555.8050]
'pyr[c]'
           [ 992.5000]
'r5p[c]'
            [ 224.3220]
```

• All these biomass precursors can be produced by the model. Hence a non-zero, positive flux through the biomass reaction should be possible:

```
FBAsolution = optimizeCbModel(modelEcore, 'max');
FBAsolution.f
```

ans = 0.7082

FBAsolution.x contains the flux value for each reaction in the network. To view the flux values use:

```
printFluxVector(modelEcore, FBAsolution.x, 'true')

ACONTa 10
```

```
ACONTb
        10
ADK1
      9.68291
ATPM
      8.39
ATPS4r 61.4747
Biomass_Ecoli_core_w_GAM 0.708235
CO2t -29.8607
CS 10
CYTBD 58.0838
ENO 17.0578
EX_co2(e) 29.8607
EX_glc(e) -10
EX_h(e) 14.2072
EX_h2o(e) 35.0198
EX nh4(e) -3.86187
EX o2(e) -29.0419
EX_pi(e) -2.60539
FBA 9.29552
    9.23588
FUM
GAPD
      18.1173
       10
GLCpts
GLNS 0.181096
GLUDy
       -3.68077
H2Ot
      -35.0198
ICDHyr
        0.764115
    9.23588
ICL
MALS 9.23588
MDH
     -5.10764
    23.5794
ME2
NADH16 48.8479
NADTRHD 11.4359
NH4t 3.86187
```

```
29.0419
O2t
      21.8902
PDH
PFK
      9.29552
PGI
      9.85481
      -18.1173
PGK
PGM
      -17.0578
PIt2r
        2.60539
     16.373
PPC
    9.68291
PPS
RPE
      -0.50908
      -0.50908
RPI
SUCDi
       9.23588
TALA
       -0.126703
TKT1
       -0.126703
TKT2
       -0.382376
TPI 9.29552
```

- To see which network reactions participate in the optimal solution. Keep in mind that there may be more than one optimal solution (so-called alternate optimal solutions, which have the same optimal value for the objective function but the internal flux distribution may be different).
- Compare this solution with a sparse FBA solution, which returns an optimal flux distribution with the least number of active model reactions. Note that the underlying algorithm is an approximation to the exact sparsest solution and also that there may be alternative optimal solutions with equal numbers of active reactions.

```
FBAsolution = optimizeCbModel(modelEcore, 'max', 'zero');
FBAsolution.f
ans = 0.7082
printFluxVector(modelEcore, FBAsolution.x, 'true')
ACONTa
        10
ACONTb
        10
AKGDH 3.69917
ATPM
      8.39
ATPS4r 31.7196
Biomass_Ecoli_core_w_GAM 0.708235
CO2t -11.6696
CS 10
CYTBD 39.8928
ENO 17.0578
EX co2(e) 11.6696
EX_for(e) 18.191
EX_glc(e) -10
        32.3982
EX_h(e)
EX_h2o(e)
         16.8287
           -3.86187
EX_nh4(e)
EX_o2(e)
         -19.9464
EX_pi(e)
         -2.60539
    9.29552
FBA
FORti
       18.191
     9.23588
FUM
GAPD
      18.1173
GLCpts
       10
GLNS 0.181096
GLUDy -3.68077
      -16.8287
H2Ot
ICDHyr 4.46328
```

```
ICL
      5.53672
MALS
       5.53672
      11.2654
MDH
ME2
      3.5072
         30.6569
NADH16
NH4t
       3.86187
O2t
      19.9464
      9.29552
PFK
      18.191
PFL
      9.85481
PGT
      -18.1173
PGK
PGM
      -17.0578
PIt2r
        2.60539
    6.69013
      -0.50908
      -0.50908
SUCDi
       9.23588
         -3.69917
SUCOAS
TALA
       -0.126703
THD2
       4.93711
TKT1
       -0.126703
       -0.382376
TKT2
      9.29552
TPI
```

66. To test whether the biomass precursors can be produced in other growth media, repeat steps 60-65.

Steps 67 - 70. Test if model can produce known secretion products.

67. Collect a list of known secretion products and medium conditions.

For this example, acetate secretion ('EX_ac(e)') was chosen and let's require that secretion flux is at least 2 mmol/gDW/h (i.e. the lower bound is constrained to 2).

```
modelEcore_New = changeRxnBounds(modelEcore, 'EX_ac(e)', 2, '1');
```

68. Set the constraints to the desired medium condition (e.g., minimal medium + carbon source). For changing the constraints use the following function:

```
modelEcore_New = changeRxnBounds(modelEcore, {'EX_glc(e)' 'EX_o2(e)'}, [-10 -18.5],
```

• If the model is required to grow in addition to producing the by-product, set the lower bound of the biomass reaction to the corresponding value required for growth.

Note: If the model is required to grow in addition to producing the by-product, set the lower bound of the biomass reaction to the corresponding value required for growth. We determine the value based on the following FBA solution.

• Optimize for growth:

```
modelEcore_New = changeObjective(modelEcore_New, 'Biomass_Ecoli_core_w_GAM');
FBAsolution = optimizeCbModel(modelEcore_New, 'max')

FBAsolution =
    full: [95×1 double]
    obj: 0.6411
```

```
rcost: [95×1 double]
  dual: [72×1 double]
  solver: 'glpk'
algorithm: 'default'
  stat: 1
origStat: 5
  time: 0.0260
  basis: []
    x: [95×1 double]
    f: 0.6411
    y: [72×1 double]
    w: [95×1 double]
    v: [95×1 double]
    v: [95×1 double]
```

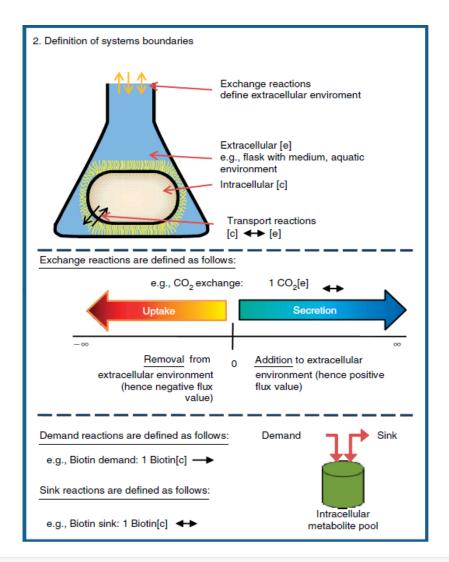
• Set the lower bound of the biomass reaction to the value of the FBA solution:

```
modelEcore_New = changeRxnBounds(modelEcore_New, 'Biomass_Ecoli_core_w_GAM', 0.64, '1'
```

- Note that the maximally possible biomass reaction flux decreased substantially, with these additional constraints.
- **69.** Change the objective function to the exchange reaction of your secretion product (i.e., acetate):

```
modelEcore_New = changeObjective(modelEcore_New, 'EX_ac(e)');
```

70. Maximize ('max') for the new objective function (as a secretion is expected to have a positive flux value, see Figure):



```
FBAsolution = optimizeCbModel (modelEcore_New, 'max')
```

```
FBAsolution =
         full: [95×1 double]
          obj: 0.0448
        rcost: [95×1 double]
         dual: [72×1 double]
       solver: 'glpk'
    algorithm: 'default'
         stat: 1
     origStat: 5
         time: 0.0260
        basis: []
            x: [95 \times 1 \text{ double}]
            f: 0.0448
            y: [72×1 double]
            w: [95×1 double]
            v: [95×1 double]
```

• It seems that the model can produce 3.5x mmol/gDW/h of acetate with the following constraints:

```
printConstraints(modelEcore_New, -1000,1000)
```

MinConstraints: ACONTb 10

```
ATPM 8.39
Biomass_Ecoli_core_w_GAM 0.64
EX_glc(e) -10
EX_o2(e) -18.5
maxConstraints:
ATPM 8.39
ATPS4r 100
```

Steps 71 - 75. Test if model can produce a certain ratio of two secretion products.

Acetate and Formate secretion are the two secretion products used in this example.

- **71.** Set the constraints to the desired medium condition (e.g., minimal medium + carbon source). As shown above in step 68.
- 72. Let's verify that both metabolites can be secreted independently. Repeat steps 69 and 70.

```
modelEcoreAc = changeObjective(modelEcore, 'EX_ac(e)');
FBAsolution = optimizeCbModel(modelEcoreAc, 'max')
FBAsolution =
        full: [95×1 double]
         obj: 10.0000
       rcost: [95×1 double]
        dual: [72×1 double]
      solver: 'glpk'
   algorithm: 'default'
        stat: 1
    origStat: 5
        time: 0.0270
       basis: []
           x: [95 \times 1 \text{ double}]
           f: 10.0000
           y: [72×1 double]
           w: [95×1 double]
           v: [95×1 double]
modelEcoreFor = changeObjective(modelEcore, 'EX_for(e)');
FBAsolution = optimizeCbModel(modelEcoreFor, 'max')
FBAsolution =
        full: [95×1 double]
         obj: 40.0000
       rcost: [95×1 double]
        dual: [72×1 double]
      solver: 'glpk'
   algorithm: 'default'
        stat: 1
    origStat: 5
        time: 0.0260
       basis: []
           x: [95 \times 1 \text{ double}]
           f: 40.0000
           y: [72×1 double]
           w: [95×1 double]
           v: [95×1 double]
```

73. Add a row to the S matrix to couple the by-product secretion reactions:

```
modelEcore_NEW = addRatioReaction(modelEcore, {'EX_ac(e)' 'EX_for(e)'}, [1 1]);
```

• Acetate and Formate secretion are coupled to a ratio of 1:1.

Also, let's require that the acetate secretion flux is at least 1 mmol/gDW/h (i.e. the lower bound is constrained to 1).

```
modelEcore_NEW = changeRxnBounds(modelEcore_NEW, 'EX_ac(e)', 1, 'l');
```

Note: If the model is required to grow in addition to producing the by-product, set the lower bound of the biomass reaction to the corresponding value required for growth. We determine the value based on the following FBA solution.

• Optimize for growth:

```
modelEcore_NEW = changeObjective(modelEcore_NEW, 'Biomass_Ecoli_core_w_GAM');
FBAsolution = optimizeCbModel(modelEcore_NEW, 'max')
FBAsolution =
        full: [95×1 double]
         obj: 0.6374
       rcost: [95×1 double]
        dual: [73×1 double]
      solver: 'qlpk'
   algorithm: 'default'
        stat: 1
     origStat: 5
        time: 0.0260
       basis: []
           x: [95 \times 1 \text{ double}]
           f: 0.6374
           y: [73×1 double]
           w: [95×1 double]
           v: [95×1 double]
```

- Note that the maximally possible biomass reaction flux decreased due to the additional constraints.
- Set the lower bound of the biomass reaction to the value of the FBA solution:

```
modelEcore_NEW = changeRxnBounds(modelEcore_NEW, 'Biomass_Ecoli_core_w_GAM', 0.63, 'Decore_NEW | Decore_w_GAM'
```

What is the flux through the two secretion reactions:

```
FBAsolution.x(find(ismember(modelEcore_NEW.rxns, 'EX_for(e)')))
ans = 1

FBAsolution.x(find(ismember(modelEcore_NEW.rxns, 'EX_ac(e)')))
ans = 1
```

- Keep in mind that the optimizeCbModel only returns one of the possible flux distributions with maximal biomass yield.
- 74. Change the objective function to the exchange reaction of one of your secretion products:

```
modelEcore_NEW = changeObjective(modelEcore_NEW, 'EX_ac(e)');
```

75. Maximize for the new objective function (as a secretion is expected to have a positive flux value):

```
FBAsolution = optimizeCbModel (modelEcore_NEW, 'max')
FBAsolution =
        full: [95×1 double]
         obj: 1.1047
       rcost: [95x1 double]
        dual: [73×1 double]
      solver: 'glpk'
   algorithm: 'default'
        stat: 1
     origStat: 5
        time: 0.0260
       basis: []
           x: [95 \times 1 \text{ double}]
           f: 1.1047
           y: [73×1 double]
            w: [95×1 double]
            v: [95×1 double]
```

• Check that the second secretion product can be produced in the defined ratio:

```
FBAsolution.x(find(ismember(modelEcore_NEW.rxns, 'EX_for(e)')))
ans = 1.1047
```

Steps 76 - 77. Check for blocked reactions.

- **76.** Change simulation conditions to rich medium or open all exchange reactions.
 - Identify the exchange reactions and set the reaction values to infinity (e.g., 1,000) and + infinity (e.g., + 1,000):

```
selExc = findExcRxns(modelEcore);
ExR = modelEcore.rxns(selExc);
modelEcore_Open = changeRxnBounds(modelEcore, ExR, -1000, 'l');
modelEcore_Open = changeRxnBounds(modelEcore_Open, ExR, 1000, 'u');
```

Verify the constraints on the model:

```
printConstraints(modelEcore_Open, -1000, 1000)
```

```
MinConstraints:
ACONTD 10
ATPM 8.39
maxConstraints:
ATPM 8.39
ATPS4r 100
```

printUptakeBound(modelEcore_Open);

```
EX_ac(e)
          -1000
EX_acald(e)
           -1000
EX_akg(e)
           -1000
EX_co2(e)
           -1000
EX_etoh(e)
            -1000
EX_for(e)
           -1000
           -1000
EX fru(e)
EX_fum(e)
           -1000
           -1000
EX_glc(e)
EX_gln_L(e) -1000
EX_glu_L(e)
            -1000
EX_h(e) -1000
EX_h2o(e) -1000
EX_lac_D(e) -1000
            -1000
EX_mal_L(e)
           -1000
EX_nh4(e)
EX_02(e) -1000
EX_pi(e)
         -1000
           -1000
EX_pyr(e)
            -1000
EX_succ(e)
```

77. Run analysis for blocked reactions. The findBlockedReaction function returns a list of blocked reactions ('BlockedReactions').

```
BlockedReactions = findBlockedReaction(modelEcore_Open)

Starting parallel pool (parpool) using the 'local' profile ... connected to 4 workers.

BlockedReactions = {''}
```

- The answer is an empty array since the *E. coli* core network has no blocked reactions.
- If the model contains blocked reactions, please refer to the tutorial for 'gap filling' on how to proceed.

Steps 79 - 80. Compute single gene deletion phenotypes

79. Use The Cobra Toolbox function, singleGeneDeletion, to simulate gene deletion:

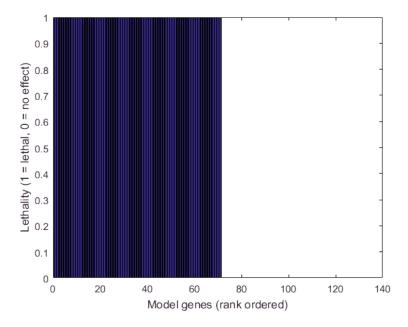
```
[grRatio, grRateKO, grRateWT, hasEffect] = singleGeneDeletion(modelEcore);
Single gene deletion analysis in progress ...
```

• The variable 'hasEffect' is returned, and an entry of 1 in the vector indicate that a gene deletion had an affect on the objective function (here, growth rate).

Let's visualize hasEffect:

```
bar(sort(hasEffect, 'descend'))
xlabel('Model genes (rank ordered)');
```

```
ylabel('Lethality (1 = lethal, 0 = no effect)')
```



How many genes are in my model?

```
length(modelEcore.genes)
```

ans = 137

How many genes have an effect and which ones?

```
length(find(hasEffect))
```

ans = 71

Which gene deletions had an affect?

modelEcore.genes(find(hasEffect))

```
ans =
    'b0114'
    'b0115'
    'b0116'
    'b0474'
    'b0720'
    'b0721'
    'b0722'
    'b0723'
    'b0724'
    'b0726'
    'b0727'
    'b0728'
    'b0729'
    'b0767'
    'b0809'
    'b0810'
    'b0811'
    'b1136'
    'b1479'
    'b1602'
```

```
'b1603'
'b1702'
'b1761'
'b1779'
'b1817'
'b1818'
'b1819'
'b1852'
'b2029'
'b2276'
'b2277'
'b2278'
'b2279'
'b2280'
'b2281'
'b2282'
'b2283'
'b2284'
'b2285'
'b2286'
'b2287'
'b2288'
'b2415'
'b2416'
'b2463'
'b2587'
'b2779'
'b2926'
'b3212'
'b3213'
'b3236'
'b3403'
'b3528'
'b3731'
'b3732'
'b3733'
'b3734'
'b3735'
'b3736'
'b3737'
'b3738'
'b3919'
'b3956'
'b4015'
'b4025'
'b4077'
'b4151'
'b4152'
'b4153'
'b4154'
's0001'
```

Which gene deletions are lethal?

• We define all growth rates lower than 0.001 1/hr as no growth.

```
tol = 1e-3;
LethalGenes = modelEcore.genes(find(grRateKO < tol))</pre>
```

```
LethalGenes = 'b0721' 'b0722'
```

```
'b0723'
'b0724'
'b1136'
'b3919'
```

length(LethalGenes)

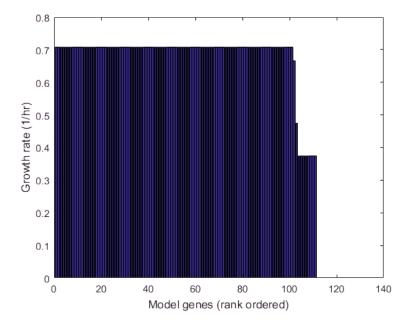
```
ans = 6
```

• Plot the effect of gene deletions on growth rate:

Some entries in 'grRateKO' maybe NaN. This is because the model is infeasible for those knockouts due to the lower bound on the 'ATPM'. We will replace those instances by zero.

```
grRateKO(isnan(grRateKO)) = 0;

bar(sort(grRateKO, 'descend'));
xlabel('Model genes (rank ordered)');
ylabel('Growth rate (1/hr)')
```



- 80. Compare with experimental data.
 - Are those genes known to be lethal in the organism (in vivo)?

Steps 81-82. Test for known incapabilities of the organism.

- **81.** Set simulation condition for comparisons with known incapabilities.
 - Change the objective function. Test for incapability by maximizing for the objective function.
 - If incapable, no solution or zero flux should be returned.

```
modelIncapable = changeRxnBounds(modelEcore, 'EX_glc(e)', 0, 'l');
modelIncapable = changeRxnBounds(modelIncapable, 'EX_ac(e)', -10, 'l');
```

FBAsolution = optimizeCbModel(modelIncapable, 'max', false)

```
FBAsolution =
         full: [95×1 double]
          obj: 5.2916e-16
        rcost: [95x1 double]
         dual: [72×1 double]
       solver: 'glpk'
    algorithm: 'default'
         stat: 1
     origStat: 5
         time: 0.0380
        basis: []
            x: [95 \times 1 \text{ double}]
            f: 5.2916e-16
            y: [72×1 double]
            w: [95×1 double]
            v: [95×1 double]
```

- E. coli cannot grow in vitro on acetate as a sole carbon source, and the in silco model is also incapable of that
- **82.** If the *in silico* model is capable of a function that the organism is incapable of *in vitro*, use single-reaction deletion to identify candidate reactions that enable the model's capability despite known incapability (see step 79).
 - Such reactions need to be manually evaluated.

Step 83. Compare predicted physiological properties with known properties.

Use previous steps of the tutorial and compare known physiological, phenotypic, or genetic properties with the model capabilities.

Steps 84-87. Test if the model can grow fast enough.

- 84. Optimize for biomass reaction in different medium conditions and compare with experimental data.
 - If the model does not grow, check boundary constraints, simulation conditions, and network completeness.
 - If the model grows too slowly, there are multiple possible issues. Start by checking boundary constraints and reaction directionality.
- **85.** Test if any of the medium components are growth limiting.
 - If yes, increase uptake rate of one substrate at a time and maximize biomass (step 86).
- 86. Maximize for biomass.
 - If the biomass flux is higher, the substrate is growth limiting. Such substrates can give information about possible gaps in the network.
- 87. Determine reduced costs when maximizing biomass (see steps 88-89).

- Find reactions with low reduced cost values.
- Increasing flux through identified reactions will lead to higher biomass flux.

Steps 88 - 89. Test if the model grows too fast.

When optimization results for a biomass reaction in different medium conditions are compared with experimental data, one can evaluate if the model grows too fast. Analysis of modeling constraints, reduced cost and single gene deletion, are helpful in the evaluation of growth conditions.

88. Determine the reduced cost associated with network reactions when optimizing for an objective function:

```
FBAsolution = optimizeCbModel(modelEcore, 'max', false)
```

```
FBAsolution =
        full: [95×1 double]
         obj: 0.7082
       rcost: [95x1 double]
        dual: [72×1 double]
       solver: 'glpk'
    algorithm: 'default'
        stat: 1
     origStat: 5
        time: 0.0310
        basis: []
            x: [95 \times 1 \text{ double}]
            f: 0.7082
            y: [72×1 double]
            w: [95×1 double]
            v: [95×1 double]
```

 FBAsolution.y contains the shadow price for each metabolite and FBAsolution.w contains the reduced cost for each network reaction.

Shadow price:
$$\pi_i = -\frac{\partial Z}{\partial b_i} \left[\frac{\partial \text{ growth}}{\partial \text{ nutrient}} \right] + \text{or } -$$

- 1. $\Pi_i=0$; not a governing constraint
- 2. $\Pi_i < 0$; more 'i' the higher Z becomes
- 3. $\Pi_i > 0$; more 'i' the lower Z becomes

Reduced cost: $\rho_i = \frac{\partial Z}{\partial v_i}$

Amount by which the objective function will change with the flux level through an internal flux that is not in the basis solution

- We find the reduced cost particularly informative to identify constraints that limit the maximal value of the objective function.
- Note that by definition the reduced cost has a negative sign. Meaning that a reaction A with a reduced
 cost of 35 would lead to an increase in the objective value by 35 if the flux through this reaction would be
 increased by 1 flux unit.

Print those reactions that have the smallest reduced cost associated:

```
[a,b] = sort(FBAsolution.w, 'descend');
modelEcore.rxns(b(1:10))
ans =
    'EX_fru(e)'
    'EX_glc(e)'
    'EX_succ(e)'
    'EX_ac(e)'
    'EX_acald(e)'
    'EX_etoh(e)'
    'EX_fum(e)'
    'EX_mal_L(e)'
    'EX_akg(e)'
    'EX_glu_L(e)'
a(1:10)
ans =
    0.1416
   0.1416
   0.0708
   0.0708
   0.0708
   0.0708
   0.0708
   0.0708
    0.0708
   0.0708
```

- Generally, we are looking for exchange reactions that may be limiting the objective value (e.g., growth yield) as those ones are easy to adjust *in silico* (and *in vitro*).
- The uptake of glucose is limiting and the associated reduced cost is 0.1416, i.e., if we were to increase the flux through this reaction by 1 unit we would increase the objective by 0.1416.
- Let's test this by repeating step 88 with an increase to the flux through EX_glc(e) by one unit.
- **89.** Beforehand we proceed, let's verify the constraints are set as intended:

```
printConstraints(modelEcore, -1000, 1000);
```

```
MinConstraints:
ACONTD 10
ATPM 8.39
EX_glc(e) -10
maxConstraints:
ATPM 8.39
ATPS4r 100
```

printUptakeBound(modelEcore);

```
EX_co2(e) -1000

EX_glc(e) -10

EX_h(e) -1000

EX_h2o(e) -1000

EX_nh4(e) -1000

EX_o2(e) -1000

EX pi(e) -1000
```

Increase the flux through EX_glc(e) by one unit (keep in mind that uptake is defined as a negative flux through exchange reactions):

```
modelEcore_New = changeRxnBounds(modelEcore, 'EX_glc(e)', -11, 'l');
FBAsolution = optimizeCbModel(modelEcore_New, 'max', false)
```

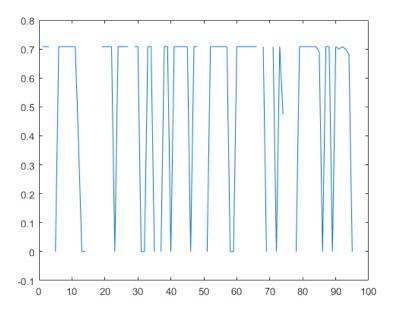
```
FBAsolution =
         full: [95×1 double]
          obj: 0.8499
        rcost: [95×1 double]
        dual: [72×1 double]
       solver: 'glpk'
    algorithm: 'default'
         stat: 1
     origStat: 5
         time: 0.0330
        basis: []
            x: [95 \times 1 \text{ double}]
            f: 0.8499
            y: [72×1 double]
            w: [95×1 double]
            v: [95×1 double]
```

- And indeed the biomass flux rate increased accordingly.
- For more systematic analysis of the effect of reduced costs and limiting variable, please also refer to the tutorial on robustness and phase plane analysis.

93. Use single-reaction deletion to identify single reactions that may enable the model to grow too fast.

Which gene deletion would lead to a lower growth rate?

plot(grRateKO)



94. Reduced cost.

The reduced cost analysis can be used to identify those reactions that can reduce the growth rate (positive cost value). Reduced cost demonstrated as as part of step 89.

95. Print Matlab model content.

• Add a field if missing:

```
if ~isfield(modelEcore, 'osense')
    modelEcore.osense = -1;
end
if ~isfield(modelEcore, 'csense')
    modelEcore.csense(1:length(modelEcore.mets), 1) = 'E';
end
```

• Write a SBML file:

```
writeCbModel(modelEcore, 'sbml', 'EColiCore.xml')
Document written
```

```
ans =

constraint: [1×0 struct]
functionDefinition: [1×0 struct]
event: [1×0 struct]
rule: [1×0 struct]
unitDefinition: [1×1 struct]
initialAssignment: [1×0 struct]
SBML_level: 3
SBML_version: 1
annotation: ''
```

```
areaUnits: ''
   avogadro_symbol: ''
  conversionFactor: ''
      delay_symbol: ''
       extentUnits: ''
fbc activeObjective: 'obj'
       fbc_version: 2
                id: 'COBRAModel'
       lengthUnits: ''
            metaid: 'COBRAModel'
              name: ''
             notes: ''
            sboTerm: -1
     substanceUnits: ''
         timeUnits: ''
       time_symbol: ''
          typecode: 'SBML_MODEL'
       volumeUnits: ''
           species: [1x72 struct]
       compartment: [1x2 struct]
         parameter: [1x7 struct]
          reaction: [1×95 struct]
     fbc_fluxBound: [1x2 struct]
   fbc_geneProduct: [1x137 struct]
      fbc_objective: [1x1 struct]
         namespaces: [1x2 struct]
         fbc_strict: 1
```

TIMING

The tutorial runs as given in a few seconds to minutes. However, if you use this tutorial for debugging and generating your own model, please consider the timing of the steps, as they have been given in the original protocol [1].

The timing of the entire reconstruction process depends on the properties of the target organism (prokaryote vs. eukaryote, genome size), the quality of the genome annotation, and the availability of experimental data.

The timing listed below represents an average and can be used to plan the different stages.

Step 1 - 4 (Stage 1, draft reconstruction): days to a week.

Step 5 (Stage 1, collection of experimental data): ongoing throughout the reconstruction process

Step 6 - 23 (Stage 2, reconstruction refinement): months to a year (if debugging and gap filling is done along the way)

Step 24 - 32 (Stage 2, biomass determination): days to weeks, depending on data availability

Step 34 - 36 (Stage 2, biomass determination): days to a week.

Step 37 (Stage 2, growth requirements): days to weeks, depending on data availability

Step 38 - 42 (Stage 3, conversion): days to a week.

Step 43 - 94 (Stage 4, network evaluation/debugging): week to months.

Step 95 - 96 (Data assembly): days to weeks, depending how much and in which format data was collected.

TROUBLESHOOTING

As given in original protocol [1].

Step 38 See installation instructions of the COBRA Toolbox for details on how to install and setup Matlab, SBML and COBRA Toolbox.

Step 51 Make sure that you are working in the directory were the X3.exe script was copied to. The .expa file produced by the function must be in the same directory as X3.exe.

ANTICIPATED RESULTS

As given in original protocol [1].

This protocol will result in a reconstruction that covers most of the known metabolic information of the target organism and represents a knowledge database. This reconstruction can be used as a resource for information (query tool), high-throughput data mapping (context for content), and a starting point for mathematical models.

References

- [1] Thiele I, Palsson BO: A protocol for generating a high-quality genome-scale metabolic reconstruction. Nat Protoc 2010, 5:93-121.
- [2] Orth JD, Fleming RM, Palsson BO: Reconstruction and Use of Microbial Metabolic Networks: the Core Escherichia coli Metabolic Model as an Educational Guide. EcoSal Plus 2010, 4.
- [3] Feist AM, Henry CS, Reed JL, Krummenacker M, Joyce AR, Karp PD, Broadbelt LJ, Hatzimanikatis V, Palsson BO: A genome-scale metabolic reconstruction for Escherichia coli K-12 MG1655 that accounts for 1260 ORFs and thermodynamic information. Molecular systems biology 2007, 3:121.
- [4] Geobacter sulfurreducans