# **SPARK 2014 User's Guide**

Release 2019

AdaCore and Altran UK Ltd

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### **GETTING STARTED WITH SPARK**

We begin with a very simple guide aimed at getting new users up and running with the SPARK tools. A small SPARK example program will be used for illustration.

**Note:** The online version of this User's Guide applies to the latest development version of the SPARK toolset. If you're using an official release, some of the described features may not apply. Refer to the version of the SPARK 2014 User's Guide shipping with your release, available through  $Help \rightarrow SPARK$  in GPS and GNATbench IDEs, or under share/doc/spark in your SPARK installation.

As a prerequisite, it is assumed that the SPARK tools have already been installed. As a minimum you should install:

- · SPARK Pro, SPARK Discovery or SPARK Community
- GPS or the GNATbench plug-in of Eclipse

SPARK Pro is the most complete toolset for SPARK. SPARK Discovery is a reduced toolset that still allows to perform all analyses presented in this User's Guide, but is less powerful than SPARK Pro. Compared to SPARK Pro, SPARK Discovery:

- only comes with one automatic prover instead of three
- does not include the static analyzer CodePeer
- · does not generate counterexamples for failed proofs
- · has limited proof support for programs using modular arithmetic or floating-point arithmetic
- comes without a lemma library for more difficult proofs

SPARK Community is a version packaged for free software developers, hobbyists, and students, which retains most of the capabilities of SPARK Pro. SPARK Community does not include the static analyzer CodePeer.

Note that GPS is not strictly required for SPARK as all the commands can be invoked from the command line, or from Eclipse using the GNATbench plug-in, but the instructions in this section assume that GPS is being used. If you are a supported user, you can get more information on how to install the tools in "AdaCore Installation Procedures" under the "Download" tab in GNAT Tracker, or by contacting AdaCore for further advice.

The key tools that we will use in this example are GNATprove and GPS. To begin with, launch GPS with a new default project and check that the *SPARK* menu is present in the menu bar.

**Note:** For SPARK 2005 users, this menu will appear under the name *SPARK 2014*, to avoid any confusion with the existing *SPARK* menu for SPARK 2005 toolset.

Now open a new file in GPS and type the following short program into it. Save this file as diff.adb.

```
procedure Diff (X, Y : in Natural; Z : out Natural) with

SPARK_Mode,
Depends => (Z => (X, Y))

is
begin
    Z := X - X;
end Diff;
```

The program is intended to calculate the difference between X and Y and store the result in Z. This is reflected in the aspect Depends which states that the output value of Z depends on the input values of X and Y, but, as you may have noticed, there is a bug in the code. Note the use of aspect SPARK\_Mode to identify this as SPARK code to be analysed with the SPARK tools. To analyze this program, select  $SPARK \rightarrow Examine\ File$  from the menu in GPS. GNATprove executes in flow analysis mode and reports:

```
diff.adb:1:20: warning: unused variable "Y"
diff.adb:1:36: info: initialization of "Z" proved
diff.adb:3:03: medium: missing dependency "null => Y"
diff.adb:3:24: medium: incorrect dependency "Z => Y"
```

These warnings are informing us that there is a discrepancy between the program's contract (which says that the value of Z is obtained from the values of X and Y) and its implementation (in which the value of Z is derived only from the value of X, and Y is unused). In this case the contract is correct and the code is wrong, so fix the code by changing the assignment statement to Z := X - Y; and re-run the analysis. This time it should report no warnings or errors.

Having established that the program is free from flow errors, now let's run the tools in proof mode to check for runtime errors. Select  $SPARK \rightarrow Prove\ File$  from the menu in GPS, and click on Execute in the resulting dialog box. GNAT prove now attempts to show, using formal verification, that the program is free from run-time errors. But it finds a problem and highlights the assignment statement in red, reporting:

This means that the tools are unable to show that the result of subtracting one Natural number from another will be within the range of the type Natural, which is hopefully not too surprising! There are various ways in which this could be addressed depending on what the requirements are for this subprogram, but for now let's change the type of parameter Z from Natural to Integer. If the analysis is re-run with this change in place then GNATprove will report no errors or warnings. All checks are proved so we can be confident that no exceptions will be raised by the execution of this code.

This short example was intended to give a flavor of the types of analysis that can be performed with the SPARK tools. A more in-depth example is presented later in *SPARK Tutorial*.

### INTRODUCTION

SPARK 2014 is a programming language and a set of verification tools designed to meet the needs of high-assurance software development. SPARK 2014 is based on Ada 2012, both subsetting the language to remove features that defy verification, but also extending the system of contracts and aspects to support modular, formal verification.

The new aspects support abstraction and refinement and facilitate deep static analysis to be performed including flow analysis and formal verification of an implementation against a specification.

SPARK 2014 is a much larger and more flexible language than its predecessor SPARK 2005. The language can be configured to suit a number of application domains and standards, from server-class high-assurance systems (such as air-traffic management applications), to embedded, hard real-time, critical systems (such as avionic systems complying with DO-178C Level A).

A major feature of SPARK 2014 is the support for a mixture of proof and other verification methods such as testing, which facilitates in particular the use of unit proof in place of unit testing; an approach now formalized in DO-178C and the DO-333 formal methods supplement. Certain units may be formally proven and other units validated through testing.

SPARK 2014 is supported by various tools in the GNAT toolsuite:

- the GNAT compiler
- the GPS integrated development environment
- the GNATtest tool for unit testing harness generation
- the GNAT prove tool for formal program verification

In the rest of this document, we'll simply say SPARK to refer to SPARK 2014.

The remainder of this document is structured as follows:

- Installation of GNAT prove goes through the installation steps on different platforms.
- *Identifying SPARK Code* describes the various means to identify the part of the program in SPARK that should be analyzed.
- Overview of SPARK Language provides an overview of the SPARK language.
- SPARK Tutorial gives an introduction to writing, testing and proving SPARK programs.
- Formal Verification with GNATprove describes the use of the GNATprove formal verification tool.
- Applying SPARK in Practice lists the main objectives and project scenarios for using SPARK.

**CHAPTER** 

THREE

### INSTALLATION OF GNATPROVE

In general, you will need to install a recent version of GNAT toolchain (that supports Ada 2012 syntax) to compile SPARK programs. You will need to install one toolchain for each platform that you target, for example one toolchain for native compilation on your machine and one toolchain for cross compilation to an embedded platform.

For analyzing SPARK programs, we recommend to first install GPS and then install GNATprove under the same location. Alternatively, you can install the GNATbench plug-in for Eclipse instead of GPS, using the Eclipse installation mechanism. The same version of GPS or GNATbench can support both native and cross compilations, as well as SPARK analysis.

If you choose to install GNATprove in a different location, you should also modify the environment variables GPR\_PROJECT\_PATH (if you installed GNAT). On Windows, edit the value of GPR\_PROJECT\_PATH under the Environnement Variables panel, and add to it the value of <GNAT install dir>/lib/gnat and <GNAT install dir>/share/gpr (so that SPARK can find library projects installed with GNAT) and <SPARK install dir>/lib/gnat (so that GNAT can find the SPARK lemma library project installed with SPARK, for details see *Manual Proof Using SPARK Lemma Library*). On Linux/Mac with Bourne shell, use:

#### or on Linux/Mac with C shell:

```
setenv GPR_PROJECT_PATH <GNAT install dir>/lib/gnat:<GNAT install dir>/share/gpr:

--<SPARK install dir>/lib/gnat:$GPR_PROJECT_PATH
```

See below for detailed installation instructions of GPS and GNATprove.

# 3.1 System Requirements

Formal verification is complex and time consuming, so GNATprove will benefit from all the speed (CPU) and memory (RAM) that can be made available. A minimum of 2 GB of RAM per core is recommended. More complex analyses will require more memory. A recommended configuration for running GNATprove on large systems is an x86-64 machine running Linux 64bits or Windows 64bits with at least 8 cores and 16 GB of RAM. Slower machines can be used to analyze small subsystems, but a minimum of 2.8Ghz CPU and 2 GB of RAM is required.

In addition, if you want to use the integration of CodePeer static analysis in GNATprove (switch --codepeer=on) you will need approximately 1 GB of RAM per 10K SLOC of code. In other words, in order to analyze 300K SLOC of code with CodePeer, you will need a 64bits configuration with at least 30 GB of RAM. Note that these numbers will vary depending on the complexity of your code. If your code is very simple, you will need less memory. On the other hand if your code is very complex, then you will likely need more memory.

### 3.2 Installation under Windows

If not already done, first run the GPS installer by e.g. double clicking on *gps-<version>-i686-pc-mingw32.exe* and follow the instructions.

**Note:** If you're using GNAT GPL instead of GNAT Pro, you should run instead the GNAT GPL installer, which installs GPS.

Then similarly run the GNATprove installer, by e.g. double clicking on spark-<version>-x86-windows-bin.exe.

You should have sufficient rights for installing the package (administrator or normal rights depending on whether it is installed for all users or a single user).

### 3.3 Installation under Linux/Mac

If not already done, you need to extract and install the GPS compressed tarball and then run the install, e.g.:

```
$ gzip -dc gps-<version>-<platform>-bin.tar.gz | tar xf -
$ cd gps-<version>-<platform>-bin
$ ./doinstall
```

Then follow the instructions displayed.

**Note:** If you're using GNAT GPL instead of GNAT Pro, you should install instead the GNAT GPL package, which installs GPS.

Then do the same with the SPARK tarball, e.g.:

```
$ gzip -dc spark-<version>-<platform>-bin.tar.gz | tar xf -
$ cd spark-<version>-<platform>-bin
$ ./doinstall
```

Note that you need to have sufficient rights for installing the package at the chosen location (e.g. root rights for installing under /opt/spark).

**CHAPTER** 

**FOUR** 

### IDENTIFYING SPARK CODE

In general a program can have some parts that are in SPARK (and follow all the rules in the SPARK Reference Manual), and some parts that are full Ada 2012. Pragma or aspect SPARK\_Mode is used to identify which parts are in SPARK (by default programs are in full Ada).

This section contains a simple description of pragma and aspect SPARK\_Mode. See *Pragma SPARK\_Mode* for the complete description.

Note that GNATprove only analyzes parts of the code that are identified as being in SPARK using pragma or aspect SPARK Mode.

# 4.1 Mixing SPARK Code and Ada Code

An Ada program unit or other construct is said to be "in SPARK" if it complies with the restrictions required to permit formal verification given in the SPARK Reference Manual. Conversely, an Ada program unit or other construct is "not in SPARK" if it does not meet these requirements, and so is not amenable to formal verification.

Within a single Ada unit, constructs which are "in" and "not in" SPARK may be mixed at a fine level in accordance with the following two general principles:

- SPARK code shall only reference SPARK declarations, but a SPARK declaration which requires a completion may have a non-SPARK completion.
- SPARK code may enclose non-SPARK code.
- non-SPARK code may enclose SPARK code only at library level. A subprogram body which is not in SPARK cannot contain SPARK code.

More specifically, non-SPARK completions of SPARK declarations are allowed for subprogram declarations, package declarations, task type declarations, protected type declarations, private type declarations, private extension declarations, and deferred constant declarations. [Strictly speaking, the private part of a package, a task type or a protected type is considered to be part of its completion for purposes of the above rules; this is described in more detail below].

When a non-SPARK completion is provided for a SPARK declaration, the user has an obligation to ensure that the non-SPARK completion is consistent (with respect to the semantics of SPARK) with its SPARK declaration. For example, SPARK requires that a function call has no side effects. If the body of a given function is in SPARK, then this rule is enforced via various language rules; otherwise, it is the responsibility of the user to ensure that the function body does not violate this rule. As with other such constructs (notably pragma Assume), failure to meet this obligation can invalidate any or all analysis (proofs and/or flow analysis) associated with the SPARK portion of a program. A non-SPARK completion meets this obligation if it is semantically equivalent (with respect to dynamic semantics) to some notional completion that could have been written in SPARK.

When a non-SPARK package declaration or body is included in a SPARK subprogram or package, the user has an obligation to ensure that the non-SPARK declaration is consistent (with respect to the semantics of SPARK) with

a hypothetical equivalent SPARK declaration. For example, SPARK requires that package elaboration code cannot modify variables defined outside of the package.

The SPARK semantics (specifically including flow analysis and proof) of a "mixed" program which meets the aforementioned requirement are well defined - they are the semantics of the equivalent 100% SPARK program. For the semantics of other "mixed" programs refer to the Ada Reference Manual.

In the case of a package, a task type, or a protected type, the specification/completion division described above is a simplification of the true situation. For instance, a package is divided into 4 sections, not just 2: its visible part, its private part, the declarations of its body, and the statement list of its body. For a given package and any number N in the range 0 .. 4, the first N sections of the package might be in SPARK while the remainder is not.

For example, the following combinations may be typical:

- Package specification in SPARK. Package body not in SPARK.
- Visible part of package specification in SPARK. Private part and body not in SPARK.
- Package specification in SPARK. Package body almost entirely in SPARK, with a small number of subprogram bodies not in SPARK.
- Package specification in SPARK, with all subprogram bodies imported from another language.
- Package specification contains a mixture of declarations which are in SPARK and not in SPARK. The latter declarations are only visible and usable from client units which are not in SPARK.

Task types and protected types are similar to packages but only have 3 sections instead of 4. The statement list section of the body is missing.

Another typical use is to exempt part of a subprogram from analysis by isolating it in a local subprogram whose body is not in SPARK.

Such patterns are intended to allow for application of formal verification to a subset of a program, and the combination of formal verification with more traditional testing (see *Applying SPARK in Practice*).

# 4.2 Project File Setup

The project file is used to identify coarsely which parts of a program are in SPARK. To get more details on project file setup, see section *Setting Up a Project File*.

# 4.2.1 Setting the Default SPARK\_Mode

There are two possible defaults:

- 1. No value of SPARK\_Mode is specified as a configuration pragma. In that case, only the parts of the program explicitly marked with SPARK\_Mode => On are in SPARK. This default is recommended if only a small number of units or subprograms are in SPARK.
- 2. A value of SPARK\_Mode => On is specified as a configuration pragma. In that case, all the program should be in SPARK, except for those parts explicitly marked with SPARK\_Mode => Off. This mode is recommended if most of the program is in SPARK.

Here is how to specify a value of SPARK\_Mode => On as a configuration pragma:

```
project My_Project is
    package Builder is
    for Global_Configuration_Pragmas use "spark.adc";
    end Builder;
end My_Project;
```

where spark.adc is a configuration file containing at least the following line:

```
pragma SPARK_Mode (On);
```

# 4.2.2 Specifying Files To Analyze

By default, all files from a project are analyzed by GNATprove. It may be useful to restrict the set of files to analyze to speedup analysis if only a subset of the files contain SPARK code.

The set of files to analyze can be identified by specifying a different value of various project attributes in the mode used for formal verification:

- Source\_Dirs: list of source directory names
- Source\_Files: list of source file names
- Source\_List\_File: name of a file listing source file names

#### For example:

```
type Modes is ("Compile", "Analyze");
Mode : Modes := External ("MODE", "Compile");

case Mode is
    when "Compile" =>
        for Source_Dirs use (...);
    when "Analyze" =>
        for Source_Dirs use ("dir1", "dir2");
        for Source_Files use ("file1.ads", "file2.ads", "file1.adb", "file2.adb");
end case;
```

Then, GNATprove should be called by specifying the value of the MODE external variable as follows:

```
gnatprove -P my_project -XMODE=Analyze
```

### 4.2.3 Excluding Files From Analysis

When choosing a default value of SPARK\_Mode => On, it may be needed to exclude some files from analysis (for example, because they contain non-SPARK code, or code that does not need to be formally analyzed).

The set of files to exclude can be identified by specifying a different value of various project attributes in the mode used for formal verification:

- Excluded\_Source\_Dirs: list of excluded source directory names
- Excluded\_Source\_Files: list of excluded source file names
- Excluded\_Source\_List\_File: name of a file listing excluded source file names

#### For example:

```
project My_Project is
    package Builder is
    for Global_Configuration_Pragmas use "spark.adc";
```

```
end Builder;

type Modes is ("Compile", "Analyze");
Mode : Modes := External ("MODE", "Compile");

case Mode is
   when "Compile" =>
        null;
   when "Analyze" =>
        for Excluded_Source_Files use ("file1.ads", "file1.adb", "file2.adb");
end case;
end My_Project;
```

Then, GNATprove should be called by specifying the value of the MODE external variable as follows:

```
gnatprove -P my_project -XMODE=Analyze
```

### 4.2.4 Using Multiple Projects

Sometimes, it is more convenient to analyze a subset of the source files with the default SPARK\_Mode => On and the rest of the source files with no setting for SPARK\_Mode. In that case, one can use two project files with different defaults, with each source file in one of the projects only. Files in one project can still refer to files in the other project by using a limited with clause between projects, as follows:

```
limited with "project_b"
project My_Project_A is
   package Compiler is
      for Local_Configuration_Pragmas use "spark.adc";
   end Compiler;
   for Source_Files use ("file1.ads", "file2.ads", "file1.adb", "file2.adb");
end My_Project_A;
```

```
limited with "project_a"
project My_Project_B is
   for Source_Files use ("file3.ads", "file4.ads", "file3.adb", "file4.adb");
end My_Project_B;
```

where spark.adc is a configuration file containing at least the following line:

```
pragma SPARK_Mode (On);
```

# 4.3 Using SPARK\_Mode in Code

The pragma or aspect SPARK\_Mode can be used in the code to identify precisely which parts of a program are in SPARK.

### 4.3.1 Basic Usage

The form of a pragma SPARK\_Mode is as follows:

```
pragma SPARK_Mode [ (On | Off) ]
```

For example:

```
pragma SPARK_Mode (On);
package P is
```

The form of an aspect SPARK\_Mode is as follows:

```
with SPARK_Mode => [ On | Off ]
```

For example:

```
package P with
   SPARK_Mode => On
is
```

A default argument of On is assumed for any SPARK\_Mode pragma or aspect for which no argument is explicitly specified.

For example:

```
package P is
   pragma SPARK_Mode; -- On is implicit here
```

or

```
package P with
   SPARK_Mode -- On is implicit here
is
```

We say that a package or a subprogram is library-level if it is either top-level or defined in a library-level package. The SPARK\_Mode pragma can be used in the following places in the code:

- immediately within or before a library-level package spec
- immediately within a library-level package body
- immediately following the private keyword of a library-level package spec
- immediately following the begin keyword of a library-level package body
- immediately following a library-level subprogram spec
- immediately within a library-level subprogram body
- immediately within a library-level task spec
- · immediately within a library-level task body
- immediately following the private keyword of a library-level task spec
- immediately within a library-level protected spec
- · immediately within a library-level protected body
- immediately following the private keyword of a library-level protected spec

The SPARK\_Mode aspect can be used in the following places in the code:

- on a library-level package spec or body
- on a library-level subprogram spec or body

- on a library-level task spec or body
- on a library-level protected spec or body

If a SPARK\_Mode pragma or aspect is not specified for a subprogram, package, task or protected spec/body, then its value is inherited from the current mode that is active at the point where the declaration occurs.

Note that a generic package instance is considered to be declared at its instantiation point. For example, a generic package cannot be both marked SPARK Mode and instantiated in a subprogram body.

### 4.3.2 Consistency Rules

The basic rule is that you cannot turn SPARK\_Mode back On, once you have explicitly turned if Off. So the following rules apply:

If a subprogram spec has SPARK\_Mode Off, then the body cannot have SPARK\_Mode On.

For a package, we have four parts:

- 1. the package public declarations
- 2. the package private part
- 3. the body of the package
- 4. the elaboration code after begin

For a package, the rule is that if you explicitly turn SPARK\_Mode Off for any part, then all the following parts cannot have SPARK\_Mode On. Note that this may require repeating a pragma SPARK\_Mode (Off) in the body. For example, if we have a configuration pragma SPARK\_Mode (On) that turns the mode On by default everywhere, and one particular package spec has pragma SPARK\_Mode (Off), then that pragma will need to be repeated in the package body.

Task types and protected types are handled similarly. If SPARK\_Mode is set to Off on one part, it cannot be set to On on the following parts, among the three parts:

- 1. the spec
- 2. the private part
- 3. the body

There is an exception to this rule, when SPARK\_Mode occurs in the code of a generic instantiated in code where SPARK Mode is Off. In that case, occurrences of SPARK Mode in the generic are ignored for this instance.

### 4.3.3 Examples of Use

### **Verifying Selected Subprograms**

If only a few selected subprograms are in SPARK, then it makes sense to set no default for SPARK\_Mode, and instead set SPARK\_Mode => On directly on the subprograms of interest. For example:

```
package Selected_Subprograms is

procedure Critical_Action with

SPARK_Mode => On;

procedure Sub_Action (X : out Boolean) with

Post => X = True;
```

```
procedure Non_Critical_Action;

end Selected_Subprograms;
```

Note that, although the bodies of procedure Sub\_Action and Non\_Critical\_Action are not analyzed, it is valid to call Sub\_Action in the body of procedure Critical\_Action, even without specifying SPARK\_Mode => On on the spec of Sub\_Action. Indeed, GNATprove checks in that case that the spec of Sub\_Action is in SPARK.

```
package body Selected_Subprograms is
      procedure Critical_Action with
        SPARK_Mode => On
4
          -- this procedure body is analyzed
6
         X : Boolean;
      begin
8
         Sub_Action (X);
         pragma Assert (X = True);
10
      end Critical_Action;
11
12
      procedure Sub_Action (X : out Boolean) is
13
15
         -- this procedure body is not analyzed
         X := True;
16
      end Sub_Action;
17
18
      procedure Non_Critical_Action is
19
      begin
20
         -- this procedure body is not analyzed
21
22
      end Non_Critical_Action;
23
24
   end Selected_Subprograms;
```

### Verifying Selected Units

If only a few selected units are in SPARK, then it makes sense to set no default for SPARK\_Mode, and instead set SPARK\_Mode => On directly on the units of interest. For example:

```
package Selected_Units with
SPARK_Mode => On

is

procedure Critical_Action;

procedure Sub_Action (X : out Boolean) with
Post => X = True;

procedure Non_Critical_Action with
SPARK_Mode => Off;

end Selected_Units;
```

Note that procedure Sub\_Action can be called inside SPARK code, because its spec is in SPARK, even though its body is marked SPARK\_Mode => Off. On the contrary, procedure Non\_Critical\_Action whose spec is

marked SPARK\_Mode => Off cannot be called inside SPARK code.

```
package body Selected_Units with
     SPARK_Mode => On
2
   is
3
      procedure Critical_Action is
5
         -- this procedure body is analyzed
         X : Boolean;
      begin
         Sub_Action (X);
         pragma Assert (X = True);
10
      end Critical_Action;
11
12
      procedure Sub_Action (X : out Boolean) with
13
        SPARK_Mode => Off
      is
15
      begin
16
         -- this procedure body is not analyzed
17
         X := True;
18
      end Sub_Action;
19
20
      procedure Non_Critical_Action with
21
        SPARK_Mode => Off
22
      is
23
      begin
24
         -- this procedure body is not analyzed
25
         null;
26
      end Non_Critical_Action;
27
28
   end Selected_Units;
```

### **Excluding Selected Unit Bodies**

If a unit spec is in SPARK, but its body is not in SPARK, the spec can be marked with SPARK\_Mode => On and the body with SPARK\_Mode => Off. This allows client code in SPARK to use this unit. If SPARK\_Mode is On by default, then it need not be repeated on the unit spec.

```
package Exclude_Unit_Body with
     SPARK_Mode => On
2
   is
      type T is private;
6
      function Get_Value return Integer;
      procedure Set_Value (V : Integer) with
        Post => Get_Value = V;
10
11
   private
12
      pragma SPARK_Mode (Off);
13
14
      -- the private part of the package spec is not analyzed
15
17
      type T is access Integer;
   end Exclude_Unit_Body;
```

Note that the private part of the spec (which is physically in the spec file, but is logically part of the implementation) can be excluded as well, by using a pragma SPARK\_Mode (Off) at the start of the private part.

```
package body Exclude_Unit_Body with
     SPARK_Mode => Off
2
   is
      -- this package body is not analyzed
      Value : T := new Integer;
6
      function Get_Value return Integer is
      begin
         return Value.all;
      end Get_Value;
12
      procedure Set_Value (V : Integer) is
13
      begin
14
         Value.all := V;
15
      end Set_Value;
16
   end Exclude_Unit_Body;
```

This scheme also works on generic units, which can then be instantiated both in code where SPARK\_Mode is On, in which case only the body of the instantiated generic is excluded, or in code where SPARK\_Mode is Off, in which case both the spec and the body of the instantiated generic are excluded.

```
generic
type T is private;
package Exclude_Generic_Unit_Body with

SPARK_Mode => On

is
procedure Process (X : in out T);
end Exclude_Generic_Unit_Body;
```

```
package body Exclude_Generic_Unit_Body with

SPARK_Mode => Off

is

-- this package body is not analyzed

procedure Process (X : in out T) is

begin

null;
end Process;
end Exclude_Generic_Unit_Body;
```

```
with Exclude_Generic_Unit_Body;
   pragma Elaborate_All (Exclude_Generic_Unit_Body);
2
4
   package Use_Generic with
5
     SPARK_Mode => On
6
       -- the spec of this generic instance is analyzed
7
      package G1 is new Exclude_Generic_Unit_Body (Integer);
8
      procedure Do_Nothing;
10
11
   end Use_Generic;
```

```
package body Use_Generic with
1
     SPARK_Mode => Off
2
3
   is
      type T is access Integer;
4
      -- this generic instance is not analyzed
      package G2 is new Exclude_Generic_Unit_Body (T);
      procedure Do_Nothing is
9
      begin
10
         null;
11
      end Do_Nothing;
12
13
   end Use_Generic;
```

### **Excluding Selected Parts of a Unit**

If most units are in SPARK except from some subprograms and packages, it makes sense to set the default to SPARK\_Mode (On), and set SPARK\_Mode => Off on non-SPARK declarations. We assume here that a value of SPARK\_Mode => On is specified as a configuration pragma.

```
package Exclude_Selected_Parts is
2
      procedure Critical_Action;
      procedure Non_Critical_Action;
6
      package Non_Critical_Data with
        SPARK_Mode => Off
10
         type T is access Integer;
         X : T;
11
         function Get_X return Integer;
12
      end Non_Critical_Data;
13
14
   end Exclude_Selected_Parts;
```

Note that procedure Non\_Critical\_Action can be called inside SPARK code, because its spec is in SPARK, even though its body is marked SPARK\_Mode => Off.

Note also that the local package Non\_Critical\_Data can contain any non-SPARK types, variables and subprograms, as it is marked SPARK\_Mode => Off. It may be convenient to define such a local package to gather non-SPARK declarations, which allows to mark globally the unit Exclude\_Selected\_Parts with SPARK\_Mode => On.

```
12
         -- this procedure body is not analyzed
13
         null;
14
      end Non_Critical_Action;
15
      package body Non_Critical_Data with
17
        SPARK_Mode => Off
18
19
          -- this package body is not analyzed
20
         function Get_X return Integer is
21
         begin
22
23
            return X.all;
         end Get_X;
24
      end Non_Critical_Data;
25
26
   end Exclude_Selected_Parts;
27
```

### OVERVIEW OF SPARK LANGUAGE

This chapter provides an overview of the SPARK language, detailing for each feature its consequences in terms of execution and formal verification. This is not a reference manual for the SPARK language, which can be found in:

- the Ada Reference Manual (for Ada features), and
- the SPARK 2014 Reference Manual (for SPARK-specific features)

More details on how GNAT compiles SPARK code can be found in the GNAT Reference Manual.

SPARK can be seen as a large subset of Ada with additional aspects/pragmas/attributes. It includes in particular:

- rich types (subtypes with bounds not known statically, discriminant records, subtype predicates, access types)
- flexible features to structure programs (function and operator overloading, early returns and exits, raise statements)
- code sharing features (generics, expression functions)
- object oriented features (tagged types, dispatching)
- concurrency features (tasks, protected objects)

In the rest of this chapter, the marker [Ada 2005] (resp. [Ada 2012]) is used to denote that a feature defined in Ada 2005 (resp. Ada 2012) is supported in SPARK, and the marker [Ravenscar] is used to denote that a concurrency feature from Ada which belongs to the Ravenscar profile is supported in SPARK. The marker [SPARK] is used to denote that a feature is specific to SPARK. Both the GNAT compiler and GNAT prove analyzer support all features listed here.

Some code snippets presented in this section are available in the example called gnatprove\_by\_example distributed with the SPARK toolset. It can be found in the share/examples/spark directory below the directory where the toolset is installed, and can be accessed from the IDE (either GPS or GNATBench) via the  $Help \rightarrow SPARK \rightarrow Examples$  menu item.

# 5.1 Language Restrictions

### 5.1.1 Excluded Ada Features

To facilitate formal verification, SPARK enforces a number of global simplifications to Ada. The most notable simplifications are:

- Uses of access types and allocators must follow an ownership policy, so that only one access object has readwrite permission to some allocated memory at any given time, or only read-only permission for that allocated memory is granted to possibly multiple access objects. See *Memory Ownership Policy*.
- All expressions (including function calls) are free of side-effects. Functions with side-effects are more complex
  to treat logically and may lead to non-deterministic evaluation due to conflicting side-effects in sub-expressions
  of an enclosing expression. Functions with side-effects should be written as procedures in SPARK.

- Aliasing of names is not permitted. Aliasing may lead to unexpected interferences, in which the value denoted
  locally by a given name changes as the result of an update to another locally named variable. Formal verification
  of programs with aliasing is less precise and requires more manual work. See *Absence of Interferences*.
- The goto statement is not permitted. Gotos can be used to create loops, which require a specific treatment in formal verification, and thus should be precisely identified. See *Loop Invariants* and *Loop Variants*.
- The use of controlled types is not permitted. Controlled types lead to the insertion of implicit calls by the compiler. Formal verification of implicit calls makes it harder for users to interact with formal verification tools, as there is no source code on which information can be reported.
- Handling of exceptions is not permitted. Exception handling gives raise to numerous interprocedural controlflow paths. Formal verification of programs with exception handlers requires tracking properties along all those paths, which is not doable precisely without a lot of manual work. But raising exceptions is allowed (see *Raising Exceptions and Other Error Signaling Mechanisms*).

The features listed above are excluded from SPARK because, currently, they defy formal verification. As formal verification technology advances the list will be revisited and it may be possible to relax some of these restrictions. There are other features which are technically feasible to formally verify but which are currently not supported in SPARK, such as access-to-subprogram types.

Uses of these features in SPARK code are detected by GNATprove and reported as errors. Formal verification is not possible on subprograms using these features. But these features can be used in subprograms in Ada not identified as SPARK code, see *Identifying SPARK Code*.

### 5.1.2 Partially Analyzed Ada Features

SPARK reinforces the strong typing of Ada with a stricter initialization policy (see *Data Initialization Policy*), and thus provides no means currently of specifying that some input data may be invalid. As a result, the following features are allowed in SPARK, but only partially analyzed by GNATprove:

- The result of a call to Unchecked\_Conversion is assumed to be a valid value of the resulting type.
- The evaluation of attribute Valid is assumed to always return True.

This is illustrated in the following example:

```
package Validity with
SPARK_Mode
is

procedure Convert (X : Integer; Y : out Float);
end Validity;
```

```
with Ada. Unchecked_Conversion;
2
   package body Validity with
3
     SPARK_Mode
4
   is
6
      function Int_To_Float is new Ada.Unchecked_Conversion (Integer, Float);
7
8
      procedure Convert (X : Integer; Y : out Float) is
9
      begin
10
         pragma Assert (X'Valid);
11
         Y := Int_To_Float (X);
12
         pragma Assert (Y'Valid);
```

```
end Convert;

end Validity;
```

GNAT prove proves both assertions, but issues warnings about its assumptions that the evaluation of attribute Valid on both input parameter X and the result of the call to Unchecked Conversion return True:

```
validity.adb:11:22: info: assertion proved validity.adb:11:22: warning: attribute Valid is assumed to return True validity.adb:13:22: info: assertion proved validity.adb:13:22: warning: attribute Valid is assumed to return True validity.ads:5:36: info: initialization of "Y" proved
```

### 5.1.3 Data Initialization Policy

Modes on parameters and data dependency contracts (see *Data Dependencies*) in SPARK have a stricter meaning than in Ada:

- Parameter mode in (resp. global mode Input) indicates that the object denoted in the parameter (resp. data dependencies) should be completely initialized before calling the subprogram. It should not be written in the subprogram.
- Parameter mode out (resp. global mode Output) indicates that the object denoted in the parameter (resp. data dependencies) should be completely initialized before returning from the subprogram. It should not be read in the program prior to initialization.
- Parameter mode in out (resp. global mode In\_Out) indicates that the object denoted in the parameter (resp. data dependencies) should be completely initialized before calling the subprogram. It can be written in the subprogram.
- Global mode Proof\_In indicates that the object denoted in the data dependencies should be completely initialized before calling the subprogram. It should not be written in the subprogram, and only read in contracts and assertions.

Hence, all inputs should be completely initialized at subprogram entry, and all outputs should be completely initialized at subprogram output. Similarly, all objects should be completely initialized when read (e.g. inside subprograms), at the exception of record subcomponents (but not array subcomponents) provided the subcomponents that are read are initialized.

A consequence of the rules above is that a parameter (resp. global variable) that is partially written in a subprogram should be marked as in out (resp. In\_Out), because the input value of the parameter (resp. global variable) is *read* when returning from the subprogram.

GNAT prove will issue check messages if a subprogram does not respect the aforementioned data initialization policy. For example, consider a procedure Proc which has a parameter and a global item of each mode:

```
package Data_Initialization with

SPARK_Mode

is

type Data is record

Val : Float;
Num : Natural;
end record;

G1, G2, G3 : Data;

procedure Proc
```

```
(P1 : in
                       Data:
12
         P2 :
                  out Data;
13
         P3 : in out Data)
14
15
      with
        Global => (Input => G1,
                     Output => G2,
                     In_Out => G3);
18
19
      procedure Call_Proc with
20
        Global => (Output => (G1, G2, G3));
21
22
   end Data_Initialization;
```

Procedure Proc should completely initialize its outputs P2 and G2, but it only initializes them partially. Similarly, procedure Call\_Proc which calls Proc should completely initialize all of Proc's inputs prior to the call, but it only initializes G1 completely.

```
package body Data_Initialization with
2
     SPARK_Mode
3
   is
      procedure Proc
5
         (P1 : in
                      Data;
6
                 out Data;
         P2:
7
         P3 : in out Data) is
      begin
         P2.Val := 0.0;
         G2.Num := 0;
          -- fail to completely initialize P2 and G2 before exit
12
      end Proc;
13
14
15
      procedure Call_Proc is
16
          X1, X2, X3 : Data;
17
      begin
          X1.Val := 0.0;
18
         X3.Num := 0;
19
         G1.Val := 0.0;
20
         G1.Num := 0;
21
          -- fail to completely initialize X1, X3 and G3 before call
22
          Proc (X1, X2, X3);
23
      end Call_Proc;
25
   end Data_Initialization;
```

On this program, GNATprove issues 6 high check messages, corresponding to the violations of the data initialization policy:

```
data_initialization.adb:23:07: high: "G3.Num" is not an input in the Global contract_
of subprogram "Call_Proc" at data_initialization.ads:20
data_initialization.adb:23:07: high: "G3.Num" is not initialized
data_initialization.adb:23:07: high: "G3.Val" is not an input in the Global contract_
of subprogram "Call_Proc" at data_initialization.ads:20
data_initialization.adb:23:07: high: "G3.Val" is not initialized
data_initialization.adb:23:07: high: either make "G3.Num" an input in the Global_
ocontract or initialize it before use
data_initialization.adb:23:07: high: either make "G3.Val" an input in the Global_
ocontract or initialize it before use
data_initialization.adb:23:13: high: "X1.Num" is not initialized
```

```
data_initialization.adb:23:17: warning: unused assignment to "X2"
data_initialization.adb:23:21: high: "X3.Val" is not initialized
data_initialization.adb:23:21: warning: unused assignment to "X3"
data_initialization.ads:12:07: warning: unused variable "P1"
data_initialization.ads:13:07: high: "P2.Num" is not initialized in "Proc"
data initialization.ads:14:07: warning: "P3" is not modified, could be IN
data_initialization.ads:14:07: warning: unused variable "P3"
data_initialization.ads:16:06: info: data dependencies proved
data_initialization.ads:16:27: low: unused global "G1"
data_initialization.ads:17:27: high: "G2.Val" is not an input in the Global contract,
→of subprogram "Proc" at line 11
data_initialization.ads:17:27: high: "G2.Val" is not initialized
data_initialization.ads:17:27: high: either make "G2.Val" an input in the Global...
→contract or initialize it before use
data_initialization.ads:18:27: low: unused global "G3"
data_initialization.ads:18:27: warning: "G3" is not modified, could be INPUT
data_initialization.ads:21:06: info: data dependencies proved
data_initialization.ads:21:28: info: initialization of "G1" proved
data_initialization.ads:21:32: info: initialization of "G2" proved
```

While a user can justify individually such messages with pragma Annotate (see section *Justifying Check Messages*), it is under her responsibility to then ensure correct initialization of subcomponents that are read, as GNAT prove relies during proof on the property that data is properly initialized before being read.

Note also the various warnings that GNATprove issues on unused parameters, global items and assignments, also based on the stricter SPARK interpretation of parameter and global modes.

### 5.1.4 Memory Ownership Policy

In SPARK, access values (a.k.a. pointers) are only allowed to alias in known ways, so that formal verification can be applied *as if* allocated memory pointed to by access values was a component of the access value seen as a record object.

In particular, assignment between access objects operates a transfer of ownership, where the source object loses its permission to read or write the underlying allocated memory.

For example, in the following example:

```
procedure Ownership_Transfer with
     SPARK_Mode
2
   is
3
      type Int_Ptr is access Integer;
4
5
      X : Int_Ptr;
6
          : Int_Ptr;
      Tmp : Integer;
7
   begin
      X := new Integer'(1);
9
      X.all := X.all + 1;
10
      Y := X;
      Y.all := Y.all + 1;
12
      X.all := X.all + 1;
                           -- illegal
13
      X.all := 1;
                            -- illegal
14
      Tmp := X.all;
                            -- illegal
15
   end Ownership_Transfer;
```

GNAT prove correctly detects that X.all can neither be read nor written after the assignment of X to Y and issues corresponding messages:

```
ownership_transfer.adb:13:06: insufficient permission on dereference from "X" ownership_transfer.adb:13:06: object was moved at line 11 ownership_transfer.adb:13:15: insufficient permission on dereference from "X" ownership_transfer.adb:13:15: object was moved at line 11 ownership_transfer.adb:14:06: insufficient permission on dereference from "X" ownership_transfer.adb:14:06: object was moved at line 11 ownership_transfer.adb:15:15: insufficient permission on dereference from "X" ownership_transfer.adb:15:15: object was moved at line 11
```

At call site, ownership is similarly transferred to the callee's parameters for the duration of the call, and returned to the actual parameters (a.k.a. arguments) when returning from the call.

For example, in the following example:

```
procedure Ownership_Transfer_At_Call with
     SPARK Mode
2
   is
3
      type Int_Ptr is access Integer;
4
      X : Int_Ptr;
5
6
7
      procedure Proc (Y : in out Int_Ptr)
        with Global => (In Out => X)
8
      is
Q
      begin
10
         Y.all := Y.all + 1;
11
         X.all := X.all + 1;
12
      end Proc;
13
14
   begin
15
16
      X := new Integer'(1);
      X.all := X.all + 1;
17
      Proc (X); -- illegal
   end Ownership_Transfer_At_Call;
```

GNATprove correctly detects that the call to Proc cannot take X in argument as X is already accessed as a global variable by Proc.

```
ownership_transfer_at_call.adb:5:04: info: initialization of "X" proved ownership_transfer_at_call.adb:8:11: info: data dependencies proved ownership_transfer_at_call.adb:18:10: high: formal parameter "Y" and global "X" are_ →aliased (SPARK RM 6.4.2)
```

Only pool-specific access types are allowed in SPARK, so it is not possible to declare access types with the qualifiers all or const, as these define general access types. This ensures in particular that access values in SPARK always point to dynamically-allocated memory, and thus can be freed when not null.

#### 5.1.5 Absence of Interferences

In SPARK, an assignment to a variable cannot change the value of another variable. This is enforced by restricting the use of access types (pointers) in SPARK, and by restricting aliasing between parameters and global variables so that only benign aliasing is accepted (i.e. aliasing that does not cause interference).

The precise rules detailed in SPARK RM 6.4.2 can be summarized as follows:

- Two mutable parameters should never be aliased.
- An immutable and a mutable parameters should not be aliased, unless the immutable parameter is always passed by copy.

- A mutable parameter should never be aliased with a global variable referenced by the subprogram.
- An immutable parameter should not be aliased with a global variable referenced by the subprogram, unless the immutable parameter is always passed by copy.

An immutable parameter is either an input parameter that is not of an access type, or an anonymous access-to-constant parameter. Except for parameters of access types, the immutable/mutable distinction is the same as the input/output one.

These rules extend the existing rules in Ada RM 6.4.1 for restricting aliasing, which already make it illegal to call a procedure with problematic (non-benign) aliasing between parameters of scalar type that are *known to denote the same object* (a notion formally defined in Ada RM).

For example, in the following example:

```
package Aliasing with
    SPARK_Mode

is
    Glob : Integer;

procedure Whatever (In_1, In_2 : Integer; Out_1, Out_2 : out Integer) with
    Global => Glob;

end Aliasing;
```

Procedure Whatever can only be called on arguments that satisfy the following constraints:

- 1. Arguments for Out\_1 and Out\_2 should not be aliased.
- 2. Variable Glob should not be passed in argument for Out\_1 and Out\_2.

Note that there are no constraints on input parameters In\_1 and In\_2, as these are always passed by copy (being of a scalar type). This would not be the case if these input parameters were of a record or array type.

For example, here are examples of correct and illegal (according to Ada and SPARK rules) calls to procedure Whatever:

```
with Aliasing; use Aliasing;
2
   procedure Check_Param_Aliasing with
3
    SPARK Mode
4
5
   is
      X, Y, Z : Integer := 0;
  begin
      Whatever (In_1 => X, In_2 => X, Out_1 => X, Out_2 => X); -- illegal
      Whatever (In_1 => X, In_2 => X, Out_1 => X, Out_2 => Y); -- correct
      Whatever (In_1 => X, In_2 => X, Out_1 => Y, Out_2 => X); -- correct
10
      Whatever (In_1 => Y, In_2 => Z, Out_1 => X, Out_2 => X); -- illegal
11
   end Check_Param_Aliasing;
```

GNATprove (like GNAT compiler, since these are also Ada rules) correctly detects the two illegal calls and issues errors:

```
check_param_aliasing.adb:8:45: writable actual for "Out_1" overlaps with actual for 
→"Out_2"
check_param_aliasing.adb:11:45: writable actual for "Out_1" overlaps with actual for
→"Out_2"
```

Here are other examples of correct and incorrect calls (according to SPARK rules) to procedure Whatever:

```
with Aliasing; use Aliasing;

procedure Check_Aliasing with

SPARK_Mode

is

X, Y, Z : Integer := 0;

begin

Whatever (In_1 => X, In_2 => X, Out_1 => X, Out_2 => Glob); -- incorrect

Whatever (In_1 => X, In_2 => Y, Out_1 => Z, Out_2 => Glob); -- incorrect

Whatever (In_1 => Glob, In_2 => Glob, Out_1 => X, Out_2 => Y); -- correct

end Check_Aliasing;
```

GNAT prove correctly detects the two incorrect calls and issues high check messages:

```
check_aliasing.adb:8:57: high: formal parameter "Out_2" and global "Glob" are aliased_

→ (SPARK RM 6.4.2)

check_aliasing.adb:9:57: high: formal parameter "Out_2" and global "Glob" are aliased_

→ (SPARK RM 6.4.2)
```

### 5.1.6 Raising Exceptions and Other Error Signaling Mechanisms

Raising an exception is allowed in SPARK to signal an error, but handling the exception raised to perform recovery or mitigation actions is outside of the SPARK subset. Typically, such exception handling code should be added to top-level subprograms in full Ada, or to a last chance handler called by the runtime when an exception is raised, none of which is analyzed by GNATprove.

GNAT prove treats raising an exception specially:

- in flow analysis, the program paths that lead to a raise\_statement are not considered when checking the contract of the subprogram, which is only concerned with executions that terminate normally; and
- in proof, a check is generated for each raise\_statement, to prove that no such program point is reachable.

Multiple error signaling mechanisms are treated the same way:

- · raising an exception
- pragma Assert (X) where X is an expression statically equivalent to False
- calling a procedure with an aspect or pragma No\_Return that has no outputs (unless the call is itself inside such a procedure, in which case the check is only generated on the call to the enclosing error-signaling procedure)

For example, consider the artificial subprogram  $Check\_OK$  which raises an exception when parameter OK is False:

```
package Abnormal_Terminations with

SPARK_Mode

is

G1, G2 : Integer := 0;

procedure Check_OK (OK : Boolean) with

Global => (Output => G1),

Pre => OK;

end Abnormal_Terminations;
```

```
package body Abnormal_Terminations with
SPARK_Mode
```

```
3
4
      procedure Check_OK (OK : Boolean) is
5
      begin
          if OK then
             G1 := 1;
          else
             G2 := 1;
10
             raise Program_Error;
11
          end if;
12
      end Check_OK;
13
   end Abnormal_Terminations;
```

Note that, although G2 is assigned in Check\_OK, its assignment is directly followed by a raise\_statement, so G2 is never assigned on an execution of Check\_OK that terminates normally. As a result, G2 is not mentioned in the data dependencies of Check\_OK. During flow analysis, GNATprove verifies that the body of Check\_OK implements its declared data dependencies.

During proof, GNATprove generates a check that the raise\_statement on line 11 is never reached. Here, it is proved thanks to the precondition of Check\_OK which states that parameter OK should always be True on entry:

```
abnormal_terminations.adb:11:10: info: raise statement proved unreachable abnormal_terminations.ads:8:06: info: data dependencies proved abnormal_terminations.ads:8:27: info: initialization of "G1" proved
```

GNATprove also checks that procedures that are marked with aspect or pragma No\_Return do not return: they should either raise an exception or loop forever on any input.

# **5.2 Subprogram Contracts**

The most important feature to specify the intended behavior of a SPARK program is the ability to attach a contract to subprograms. In this document, a *subprogram* can be a procedure, a function or a protected entry. This contract is made up of various optional parts:

- The *precondition* introduced by aspect Pre specifies constraints on callers of the subprogram.
- The *postcondition* introduced by aspect Post specifies (partly or completely) the functional behavior of the subprogram.
- The *contract cases* introduced by aspect Contract\_Cases is a way to partition the behavior of a subprogram. It can replace or complement a precondition and a postcondition.
- The *data dependencies* introduced by aspect Global specify the global data read and written by the subprogram.
- The *flow dependencies* introduced by aspect Depends specify how subprogram outputs depend on subprogram inputs.

Which contracts to write for a given verification objective, and how GNATprove generates default contracts, is detailed in *How to Write Subprogram Contracts*.

The contract on a subprogram describes the behavior of successful calls. Executions that end up by signalling an error, as described in *Raising Exceptions and Other Error Signaling Mechanisms*, are not covered by the subprogram's contract. A call to a subprogram is successful if execution terminates normally, or if execution loops without errors for a subprogram marked with aspect No\_Return that has some outputs (this is typically the case of a non-terminating subprogram implementing the main loop of a controller).

## 5.2.1 Preconditions

[Ada 2012]

The precondition of a subprogram specifies constraints on callers of the subprogram. Typically, preconditions are written as conjunctions of constraints that fall in one of the following categories:

- exclusion of forbidden values of parameter, for example X /= 0 or Y not in Active\_States
- specification of allowed parameter values, for example X in 1 .. 10 or Y in Idle\_States
- relations that should hold between parameter values, for example (if Y in Active\_State then Z /= Null\_State)
- expected values of global variables denoting the state of the computation, for example Current\_State in Active\_States
- invariants about the global state that should hold when calling this subprogram, for example Is\_Complete (State\_Mapping)
- relations involving the global state and input parameters that should hold when calling this subprogram, for example X in Next\_States (Global\_Map, Y)

When the program is compiled with assertions (for example with switch -gnata in GNAT), the precondition of a subprogram is checked at run time every time the subprogram is called. An exception is raised if the precondition fails. Not all assertions need to be enabled though. For example, a common idiom is to enable only preconditions (and not other assertions) in the production binary, by setting pragma Assertion\_Policy as follows:

```
pragma Assertion_Policy (Pre => Check);
```

When a subprogram is analyzed with GNATprove, its precondition is used to restrict the contexts in which it may be executed, which is required in general to prove that the subprogram's implementation:

- is free from run-time errors (see Writing Contracts for Program Integrity); and
- ensures that the postcondition of the subprogram always holds (see *Writing Contracts for Functional Correctness*).

In particular, the default precondition of True used by GNATprove when no explicit one is given may not be precise enough, unless it can be analyzed in the context of its callers by GNATprove (see *Contextual Analysis of Subprograms Without Contracts*). When a caller is analyzed with GNATprove, it checks that the precondition of the called subprogram holds at the point of call. And even when the implementation of the subprogram is not analyzed with GNATprove, it may be necessary to add a precondition to the subprogram for analyzing its callers (see *Writing Contracts on Imported Subprograms*).

For example, consider the procedure Add\_To\_Total which increments global counter Total by the value given in parameter Incr. To ensure that there are no integer overflows in the implementation, Incr should not be too large, which a user can express with the following precondition:

```
procedure Add_To_Total (Incr : in Integer) with
Pre => Incr >= 0 and then Total <= Integer'Last - Incr;</pre>
```

To ensure that the value of Total remains non-negative, one should also add the condition Total >= 0 to the precondition:

```
procedure Add_To_Total (Incr : in Integer) with
Pre => Incr >= 0 and then Total in 0 .. Integer'Last - Incr;
```

Finally, GNATprove also analyzes preconditions to ensure that they are free from run-time errors in all contexts. This may require writing the precondition in a special way. For example, the precondition of Add\_To\_Total above uses the shorcut boolean operator and then instead of and, so that calling the procedure in a context where Incr is

negative does not result in an overflow when evaluating Integer'Last - Incr. Instead, the use of and then ensures that a precondition failure will occur before the expression Integer'Last - Incr is evaluated.

**Note:** It is good practice to use the shortcut boolean operator and then instead of and in preconditions. This is required in some cases by GNAT prove to prove absence of run-time errors inside preconditions.

### 5.2.2 Postconditions

[Ada 2012]

The postcondition of a subprogram specifies partly or completely the functional behavior of the subprogram. Typically, postconditions are written as conjunctions of properties that fall in one of the following categories:

- possible values returned by a function, using the special attribute Result (see *Attribute Result*), for example Get'Result in Active\_States
- possible values of output parameters, for example Y in Active\_States
- expected relations between output parameter values, for example if Success then Y /= Null\_State
- expected relations between input and output parameter values, possibly using the special attribute Old (see *Attribute Old*), for example if Success then Y /= Y'Old
- expected values of global variables denoting updates to the state of the computation, for example Current\_State in Active\_States
- invariants about the global state that should hold when returning from this subprogram, for example Is\_Complete (State\_Mapping)
- relations involving the global state and output parameters that should hold when returning from this subprogram, for example X in Next\_States (Global\_Map, Y)

When the program is compiled with assertions (for example with switch -gnata in GNAT), the postcondition of a subprogram is checked at run time every time the subprogram returns. An exception is raised if the postcondition fails. Usually, postconditions are enabled during tests, as they provide dynamically checkable oracles of the intended behavior of the program, and disabled in the production binary for efficiency.

When a subprogram is analyzed with GNATprove, it checks that the postcondition of a subprogram cannot fail. This verification is modular: GNATprove considers all calling contexts in which the precondition of the subprogram holds for the analysis of a subprogram. GNATprove also analyzes postconditions to ensure that they are free from run-time errors, like any other assertion.

For example, consider the procedure Add\_To\_Total which increments global counter Total with the value given in parameter Incr. This intended behavior can be expressed in its postcondition:

```
procedure Add_To_Total (Incr : in Integer) with
  Post => Total = Total'Old + Incr;
```

The postcondition of a subprogram is used to analyze calls to the subprograms. In particular, the default postcondition of True used by GNATprove when no explicit one is given may not be precise enough to prove properties of its callers, unless it analyzes the subprogram's implementation in the context of its callers (see *Contextual Analysis of Subprograms Without Contracts*).

Recursive subprograms and mutually recursive subprograms are treated in this respect exactly like non-recursive ones. Provided the execution of these subprograms always terminates (a property that is not verified by GNATprove), then GNATprove correctly checks that their postcondition is respected by using this postcondition for recursive calls.

Special care should be exercized for functions that return a boolean, as a common mistake is to write the expected boolean result as the postcondition:

```
function Total_Above_Threshold (Threshold : in Integer) return Boolean with
  Post => Total > Threshold;
```

while the correct postcondition uses Attribute Result:

```
function Total_Above_Threshold (Threshold : in Integer) return Boolean with
Post => Total_Above_Threshold'Result = Total > Threshold;
```

Both GNAT compiler and GNAT prove issue a warning on the semantically correct but likely functionally wrong postcondition.

## 5.2.3 Contract Cases

### [SPARK]

When a subprogram has a fixed set of different functional behaviors, it may be more convenient to specify these behaviors as contract cases rather than a postcondition. For example, consider a variant of procedure Add\_To\_Total which either increments global counter Total by the given parameter value when possible, or saturates at a given threshold. Each of these behaviors can be defined in a contract case as follows:

Each contract case consists in a guard and a consequence separated by the symbol =>. When the guard evaluates to True on subprogram entry, the corresponding consequence should also evaluate to True on subprogram exit. We say that this contract case was enabled for the call. Exactly one contract case should be enabled for each call, or said equivalently, the contract cases should be disjoint and complete.

For example, the contract cases of Add\_To\_Total express that the subprogram should be called in two distinct cases only:

- on inputs that can be added to Total to obtain a value strictly less than a given threshold, in which case Add\_To\_Total adds the input to Total.
- on inputs whose addition to Total exceeds the given threshold, in which case Add\_To\_Total sets Total to the threshold value.

When the program is compiled with assertions (for example with switch -gnata in GNAT), all guards are evaluated on entry to the subprogram, and there is a run-time check that exactly one of them is True. For this enabled contract case, there is another run-time check when returning from the subprogram that the corresponding consequence evaluates to True.

When a subprogram is analyzed with GNATprove, it checks that there is always exactly one contract case enabled, and that the consequence of the contract case enabled cannot fail. If the subprogram also has a precondition, GNATprove performs these checks only for inputs that satisfy the precondition, otherwise for all inputs.

In the simple example presented above, there are various ways to express an equivalent postcondition, in particular using *Conditional Expressions*:

In general, an equivalent postcondition may be cumbersome to write and less readable. Contract cases also provide a way to automatically verify that the input space is partitioned in the specified cases, which may not be obvious with a single expression in a postcondition when there are many cases.

The guard of the last case may be others, to denote all cases not captured by previous contract cases. For example, the contract of Add\_To\_Total may be written:

When others is used as a guard, there is no need for verification (both at run-time and using GNATprove) that the set of contract cases covers all possible inputs. Only disjointness of contract cases is checked in that case.

# 5.2.4 Data Dependencies

### [SPARK]

The data dependencies of a subprogram specify the global data that a subprogram is allowed to read and write. Together with the parameters, they completely specify the inputs and outputs of a subprogram. Like parameters, the global variables mentioned in data dependencies have a mode: Input for inputs, Output for outputs and In\_Out for global variables that are both inputs and outputs. A last mode of Proof\_In is defined for inputs that are only read in contracts and assertions. For example, data dependencies can be specified for procedure Add\_To\_Total which increments global counter Total as follows:

```
procedure Add_To_Total (Incr : in Integer) with
Global => (In_Out => Total);
```

For protected subprograms, the protected object is considered as an implicit parameter of the subprogram:

- it is an implicit parameter of mode in of a protected function; and
- it is an implicit parameter of mode in out of a protected procedure or a protected entry.

Data dependencies have no impact on compilation and the run-time behavior of a program. When a subprogram is analyzed with GNATprove, it checks that the implementation of the subprogram:

- · only reads global inputs mentioned in its data dependencies,
- only writes global outputs mentioned in its data dependencies, and
- always completely initializes global outputs that are not also inputs.

See *Data Initialization Policy* for more details on this analysis of GNATprove. During its analysis, GNATprove uses the specified data dependencies of callees to analyze callers, if present, otherwise a default data dependency contract is generated (see *Generation of Dependency Contracts*) for callees.

There are various benefits when specifying data dependencies on a subprogram, which gives various reasons for users to add such contracts:

- GNATprove verifies automatically that the subprogram implementation respects the specified accesses to global data.
- GNATprove uses the specified contract during flow analysis, to analyze the data and flow dependencies of the subprogram's callers, which may result in a more precise analysis (less false alarms) than with the generated data dependencies.
- GNATprove uses the specified contract during proof, to check absence of run-time errors and the functional contract of the subprogram's callers, which may also result in a more precise analysis (less false alarms) than with the generated data dependencies.

When data dependencies are specified on a subprogram, they should mention all global data read and written in the subprogram. When a subprogram has neither global inputs nor global outputs, it can be specified using the null data dependencies:

```
function Get (X : T) return Integer with
  Global => null;
```

When a subprogram has only global inputs but no global outputs, it can be specified either using the Input mode:

```
function Get_Sum return Integer with
Global => (Input => (X, Y, Z));
```

or equivalently without any mode:

```
function Get_Sum return Integer with
Global => (X, Y, Z);
```

Note the use of parentheses around a list of global inputs or outputs for a given mode.

Global data that is both read and written should be mentioned with the In\_Out mode, and not as both input and output. For example, the following data dependencies on Add\_To\_Total are illegal and rejected by GNATprove:

```
procedure Add_To_Total (Incr : in Integer) with
Global => (Input => Total,
Output => Total); -- INCORRECT
```

Global data that is partially written in the subprogram should also be mentioned with the In\_Out mode, and not as an output. See *Data Initialization Policy*.

# 5.2.5 Flow Dependencies

## [SPARK]

The flow dependencies of a subprogram specify how its outputs (both output parameters and global outputs) depend on its inputs (both input parameters and global inputs). For example, flow dependencies can be specified for procedure Add\_To\_Total which increments global counter Total as follows:

```
procedure Add_To_Total (Incr : in Integer) with
  Depends => (Total => (Total, Incr));
```

The above flow dependencies can be read as "the output value of global variable Total depends on the input values of global variable Total and parameter Incr".

Outputs (both parameters and global variables) may have an implicit input part depending on their type:

- an unconstrained array A has implicit input bounds A'First and A'Last
- a discriminated record R has implicit input discriminants, for example R.Discr

Thus, an output array A and an output discriminated record R may appear in input position inside a flow-dependency contract, to denote the input value of the bounds (for the array) or the discriminants (for the record).

For protected subprograms, the protected object is considered as an implicit parameter of the subprogram which may be mentioned in the flow dependencies, under the name of the protected unit (type or object) being declared:

- as an implicit parameter of mode in of a protected function, it can be mentioned on the right-hand side of flow dependencies; and
- as an implicit parameter of mode in out of a protected procedure or a protected entry, it can be mentioned on both sides of flow dependencies.

Flow dependencies have no impact on compilation and the run-time behavior of a program. When a subprogram is analyzed with GNATprove, it checks that, in the implementation of the subprogram, outputs depend on inputs as specified in the flow dependencies. During its analysis, GNATprove uses the specified flow dependencies of callees to analyze callers, if present, otherwise a default flow dependency contract is generated for callees (see *Generation of Dependency Contracts*).

When flow dependencies are specified on a subprogram, they should mention all flows from inputs to outputs. In particular, the output value of a parameter or global variable that is partially written by a subprogram depends on its input value (see *Data Initialization Policy*).

When the output value of a parameter or global variable depends on its input value, the corresponding flow dependency can use the shorthand symbol + to denote that a variable's output value depends on the variable's input value plus any other input listed. For example, the flow dependencies of Add\_To\_Total above can be specified equivalently:

```
procedure Add_To_Total (Incr : in Integer) with
  Depends => (Total =>+ Incr);
```

When an output value depends on no input value, meaning that it is completely (re)initialized with constants that do not depend on variables, the corresponding flow dependency should use the null input list:

```
procedure Init_Total with
  Depends => (Total => null);
```

### 5.2.6 State Abstraction and Contracts

### [SPARK]

The subprogram contracts mentioned so far always used directly global variables. In many cases, this is not possible because the global variables are defined in another unit and not directly visible (because they are defined in the private part of a package specification, or in a package implementation). The notion of abstract state in SPARK can be used in that case (see *State Abstraction*) to name in contracts global data that is not visible.

### **State Abstraction and Dependencies**

Suppose the global variable Total incremented by procedure Add\_To\_Total is defined in the package implementation, and a procedure Cash\_Tickets in a client package calls Add\_To\_Total. Package Account which defines Total can define an abstract state State that represents Total, as seen in *State Abstraction*, which allows using it in Cash\_Tickets's data and flow dependencies:

```
procedure Cash_Tickets (Tickets : Ticket_Array) with
Global => (Output => Account.State),
Depends => (Account.State => Tickets);
```

As global variable Total is not visible from clients of unit Account, it is not visible either in the visible part of Account's specification. Hence, externally visible subprograms in Account must also use abstract state State in their data and flow dependencies, for example:

```
procedure Init_Total with
  Global => (Output => State),
  Depends => (State => null);

procedure Add_To_Total (Incr : in Integer) with
  Global => (In_Out => State),
  Depends => (State =>+ Incr);
```

Then, the implementations of Init\_Total and Add\_To\_Total can define refined data and flow dependencies introduced respectively by Refined\_Global and Refined\_Depends, which give the precise dependencies for these subprograms in terms of concrete variables:

```
procedure Init_Total with
   Refined_Global => (Output => Total),
   Refined_Depends => (Total => null)
is
begin
   Total := 0;
end Init_Total;

procedure Add_To_Total (Incr : in Integer) with
   Refined_Global => (In_Out => Total),
   Refined_Depends => (Total =>+ Incr)
is
begin
   Total := Total + Incr;
end Add_To_Total;
```

Here, the refined dependencies are the same as the abstract ones where State has been replaced by Total, but that's not always the case, in particular when the abstract state is refined into multiple concrete variables (see *State Abstraction*). GNATprove checks that:

- · each abstract global input has at least one of its constituents mentioned by the concrete global inputs
- each abstract global in\_out has at least one of its constituents mentioned with mode input and one with mode output (or at least one constituent with mode in\_out)
- each abstract global output has to have all its constituents mentioned by the concrete global outputs
- the concrete flow dependencies are a subset of the abstract flow dependencies

GNATprove uses the abstract contract (data and flow dependencies) of Init\_Total and Add\_To\_Total when analyzing calls outside package Account and the more precise refined contract (refined data and flow dependencies) of Init\_Total and Add\_To\_Total when analyzing calls inside package Account.

Refined dependencies can be specified on both subprograms and tasks for which data and/or flow dependencies that are specified include abstract states which are refined in the current unit.

### **State Abstraction and Functional Contracts**

If global variables are not visible for data dependencies, they are not visible either for functional contracts. For example, in the case of procedure Add\_To\_Total, if global variable Total is not visible, we cannot express anymore the precondition and postcondition of Add\_To\_Total as in *Preconditions* and *Postconditions*. Instead, we define accessor functions to retrieve properties of the state that we need to express, and we use these in contracts. For example here:

```
function Get_Total return Integer;

procedure Add_To_Total (Incr : in Integer) with
   Pre => Incr >= 0 and then Get_Total in 0 .. Integer'Last - Incr,
   Post => Get_Total = Get_Total'Old + Incr;
```

Function Get\_Total may be defined either in the private part of package Account or in its implementation. It may take the form of a regular function or an expression function (see *Expression Functions*), for example:

```
Total : Integer;
function Get_Total return Integer is (Total);
```

Although no refined preconditions and postconditions are required on the implementation of Add\_To\_Total, it is possible to provide a refined postcondition introduced by Refined\_Post in that case, which specifies a more precise functional behavior of the subprogram. For example, procedure Add\_To\_Total may also increment the value of a counter Call\_Count at each call, which can be expressed in the refined postcondition:

```
procedure Add_To_Total (Incr : in Integer) with
   Refined_Post => Total = Total'Old + Incr and Call_Count = Call_Count'Old + 1
is
   ...
end Add_To_Total;
```

A refined postcondition can be given on a subprogram implementation even when the unit does not use state abstraction, and even when the default postcondition of True is used implicitly on the subprogram declaration.

GNATprove uses the abstract contract (precondition and postcondition) of Add\_To\_Total when analyzing calls outside package Account and the more precise refined contract (precondition and refined postcondition) of Add\_To\_Total when analyzing calls inside package Account.

# **5.3 Package Contracts**

Subprograms are not the only entities to bear contracts in SPARK. Package contracts are made up of various optional parts:

- The *state abstraction* specifies how global variables defined in the package are referred to abstractly where they are not visible. Aspect Abstract\_State introduces abstract names and aspect Refined\_State specifies the mapping between these names and global variables.
- The *package initialization* introduced by aspect Initializes specifies which global data (global variables and abstract state) defined in the package is initialized at package startup.
- The *package initial condition* introduced by aspect Initial\_Condition specifies the properties holding after package startup.

Package startup (a.k.a. package *elaboration* in Ada RM) consists in the evaluation of all declarations in the package specification and implementation, in particular the evaluation of constant declarations and those variable declarations which contain an initialization expression, as well as the statements sometimes given at the end of a package body that are precisely executed at package startup.

## 5.3.1 State Abstraction

[SPARK]

The state abstraction of a package specifies a mapping between abstract names and concrete global variables defined in the package. State abstraction allows to define *Subprogram Contracts* at an abstract level that does not depend on a particular choice of implementation (see *State Abstraction and Contracts*), which is better both for maintenance (no need to change contracts) and scalability of analysis (contracts can be much smaller).

#### **Basic State Abstraction**

One abstract name may be mapped to more than one concrete variable, but no two abstract names can be mapped to the same concrete variable. When state abstraction is specified on a package, all non-visible global variables defined in the private part of the package specification and in its implementation should be mapped to abstract names. Thus, abstract names correspond to a partitioning of the non-visible global variables defined in the package.

The simplest use of state abstraction is to define a single abstract name (conventionally called State) to denote all non-visible global variables defined in the package. For example, consider package Account defining a global variable Total in its implementation, which is abstracted as State:

```
package Account with
   Abstract_State => State
is
    ...
end Account;

package body Account with
   Refined_State => (State => Total)
is
    Total : Integer;
    ...
end Account;
```

The aspect Refined\_State maps each abstract name to a list of concrete global variables defined in the package. The list can be simply null to serve as placeholder for future definitions of global variables. Instead of concrete global variables, one can also use abstract names for the state of nested packages and private child packages, whose state is considered to be also defined in the parent package.

If global variable Total is defined in the private part of Account's package specification, then the declaration of Total must use the special aspect Part\_Of to declare its membership in abstract state State:

```
package Account with
  Abstract_State => State
is
    ...
private
  Total : Integer with Part_Of => State;
    ...
end Account;
```

This ensures that Account's package specification can be checked by GNATprove even if its implementation is not in SPARK, or not available for analysis, or not yet developed.

A package with state abstraction must have a package body that states how abstract states are refined in aspect Refined\_State, unless the package body is not in SPARK. If there is no other reason for the package to have a body, then one should use pragma Elaborate\_Body in the package spec to make it legal for the package to have a body on which to express state refinement.

In general, an abstract name corresponds to multiple global variables defined in the package. For example, we can imagine adding global variables to log values passed in argument to procedure Add\_To\_Total, that are also mapped to abstract name State:

```
package Account with
   Abstract_State => State
is
    ...
end Account;

package body Account with
   Refined_State => (State => (Total, Log, Log_Size))
is
    Total : Integer;
   Log : Integer_Array;
   Log_Size : Natural;
    ...
end Account;
```

We can also imagine defining different abstract names for the total and the log:

The abstract names defined in a package are visible everywhere the package name itself is visible:

- in the scope where the package is declared, for a locally defined package
- in units that have a clause with <package>;
- in units that have a clause limited with <package>;

The last case allows subprograms in two packages to mutually reference the abstract state of the other package in their data and flow dependencies.

### **Special Cases of State Abstraction**

Global constants with a statically known value are not part of a package's state. On the contrary, constant with variable inputs are constants whose value depends on the value of either a variable or a subprogram parameter. Since they participate in the flow of information between variables, constants with variable inputs are treated like variables: they are part of a package's state, and they must be listed in its state refinement whenever they are not visible. For example, constant Total\_Min is not part of the state refinement of package Account below, while constant with variable inputs Total\_Max is part of it:

```
package body Account with
   Refined_State => (State => (Total, Total_Max))
is
   Total : Integer;
   Total_Min : constant Integer := 0;
```

```
Total_Max : constant Integer := Compute_Total_Max(...);
...
end Account;
```

Global variables are not always the only constituents of a package's state. For example, if a package P contains a nested package N, then N's state is part of P's state. As a consequence, if N is hidden, then its state must be listed in P's refinement. For example, we can nest Account in the body of the Account\_Manager package as follows:

```
package Account_Manager with
   Abstract_State => State
is
   ...
end Account_Manager;

package body Account_Manager with
   Refined_State => (State => Account.State)
is
   package Account with
    Abstract_State => State
   is
    ...
   end Account;
   ...
end Account_Manager;
```

#### State In The Private Part

Global variables and nested packages which themselves contain state may be declared in the private part of a package. For each such global variable and nested package state, it is mandatory to identify, using aspect Part\_Of, the abstract state of the enclosing package of which it is a constituent:

```
package Account_Manager with
   Abstract_State => (Totals, Details)
is
   ...
private
   Total_Accounts : Integer with Part_Of => Totals;

   package Account with
        Abstract_State => (State with Part_Of => Details)
   is
        Total : Integer with Part_Of => Totals;
        ...
   end Account;
   ...
end Account_Manager;
```

The purpose of using Part\_Of is to enforce that each constituent of an abstract state is known at the declaration of the constituent (not having to look at the package body), which is useful for both code understanding and tool analysis (including compilation).

As the state of a private child package is logically part of its parent package, aspect Part\_Of must also be specified in that case:

```
private package Account_Manager.Account with
  Abstract_State => (State with Part_Of => Details)
```

```
is
   Total : Integer with Part_Of => Totals;
   ...
end Account_Manager.Account;
```

Aspect Part\_Of can also be specified on a generic package instantiation inside a private part, to specify that all the state (visible global variables and abstract states) of the package instantiation is a constituent of an abstract state of the enclosing package:

```
package Account_Manager with
  Abstract_State => (Totals, Details)
is
    ...
private
    package Account is new Generic_Account (Max_Total) with Part_Of => Details;
    ...
end Account_Manager;
```

# 5.3.2 Package Initialization

### [SPARK]

The package initialization specifies which global data (global variables, constant with variable inputs, and abstract state) defined in the package is initialized at package startup. The corresponding global variables may either be initialized at declaration, or by the package body statements. Thus, package initialization can be seen as the output data dependencies of the package elaboration procedure generated by the compiler.

For example, we can specify that the state of package Account is initialized at package startup as follows:

```
package Account with
  Abstract_State => State,
  Initializes => State
is
   ...
end Account;
```

Then, unless Account's implementation is not in SPARK, it should initialize the corresponding global variable Total either at declaration:

```
package body Account with
  Refined_State => (State => Total)
is
  Total : Integer := 0;
    ...
end Account;
```

or in the package body statements:

```
package body Account with
  Refined_State => (State => Total)
is
  Total : Integer;
  ...
begin
  Total := 0;
end Account;
```

These initializations need not correspond to direct assignments, but may be performed in a call, for example here to procedure Init\_Total as seen in *State Abstraction and Dependencies*. A mix of initializations at declaration and in package body statements is also possible.

Package initializations also serve as dependency contracts for global variables' initial values. That is, if the initial value of a global variable, state abstraction, or constant with variable inputs listed in a package initialization depends on the value of a variable defined outside the package, then this dependency must be listed in the package's initialization. For example, we can initialize Total by reading the value of an external variable:

```
package Account with
  Abstract_State => State,
    Initializes => (State => External_Variable)
is
    ...
end Account;

package body Account with
    Refined_State => (State => Total)
is
    Total : Integer := External_Variable;
    ...
end Account;
```

# 5.3.3 Package Initial Condition

### [SPARK]

The package initial condition specifies the properties holding after package startup. Thus, package initial condition can be seen as the postcondition of the package elaboration procedure generated by the compiler. For example, we can specify that the value of Total defined in package Account's implementation is initially zero:

```
package Account with
  Abstract_State => State,
  Initial_Condition => Get_Total = 0
is
  function Get_Total return Integer;
   ...
end Account;
```

This is ensured either by initializing Total with value zero at declaration, or by assigning the value zero to Total in the package body statements, as seen in *Package Initialization*.

When the program is compiled with assertions (for example with switch -gnata in GNAT), the initial condition of a package is checked at run time after package startup. An exception is raised if the initial condition fails.

When a package is analyzed with GNATprove, it checks that the initial condition of a package cannot fail. GNATprove also analyzes the initial condition expression to ensure that it is free from run-time errors, like any other assertion.

# 5.3.4 Interfaces to the Physical World

[SPARK]

### **Volatile Variables**

Most embedded programs interact with the physical world or other programs through so-called *volatile* variables, which are identified as volatile to protect them from the usual compiler optimizations. In SPARK, volatile variables are also analyzed specially, so that possible changes to their value from outside the program are taken into account, and so that changes to their value from inside the program are also interpreted correctly (in particular for checking flow dependencies).

For example, consider package <code>Volatile\_Or\_Not</code> which defines a volatile variable <code>V</code> and a non-volatile variable <code>N</code>, and procedure <code>Swap\_Then\_Zero</code> which starts by swapping the values of <code>V</code> and <code>N</code> before zeroing them out:

```
package Volatile_Or_Not with
2
      SPARK_Mode,
      Initializes => V
   is
       V : Integer with Volatile;
5
       N : Integer;
6
       procedure Swap_Then_Zero with
8
         Global => (In\_Out => (N, V)),
9
         Depends \Rightarrow (V \Rightarrow N, N \Rightarrow null, null \Rightarrow V);
10
11
   end Volatile_Or_Not;
12
```

```
package body Volatile Or Not with
1
     SPARK Mode
2
   is
3
      procedure Swap_Then_Zero is
4
         Tmp : constant Integer := V;
6
         -- Swap values of V and N
         V := N;
8
         N := Tmp;
9
         -- Zero out values of V and N
10
         V := 0;
11
         N := 0;
12
      end Swap_Then_Zero;
13
14
   end Volatile_Or_Not;
```

Compare the difference in contracts between volatile variable V and non-volatile variable N:

- The *Package Initialization* of package Volatile\_Or\_Not mentions V although this variable is not initialized at declaration or in the package body statements. This is because a volatile variable is assumed to be initialized.
- The Flow Dependencies of procedure Swap\_Then\_Zero are very different for V and N. If both variables were not volatile, the correct contract would state that both input values are not used with null => (V, N) and that both output values depend on no inputs with (V, N) => null. The difference lies with the special treatment of volatile variable V: as its value may be read at any time, the intermediate value N assigned to V on line 8 of volatile\_or\_not.adb needs to be mentioned in the flow dependencies for output V.

GNATprove checks that Volatile\_Or\_Not and Swap\_Then\_Zero implement their contract, and it issues a warning on the first assignment to N:

```
volatile_or_not.adb:9:09: warning: unused assignment
volatile_or_not.ads:3:03: info: flow dependencies proved
volatile_or_not.ads:9:06: info: data dependencies proved
volatile_or_not.ads:10:06: info: flow dependencies proved
```

This warning points to a real issue, as the intermediate value of N is not used before N is zeroed out on line 12. But note that no warning is issued on the similar first assignment to V, because the intermediate value of V may be read outside the program before V is zeroed out on line 11.

Note that in real code, the memory address of the volatile variable is set through aspect Address or the corresponding representation clause, so that it can be read or written outside the program.

### **Properties of Volatile Variables**

Not all volatile variables are read and written outside the program, sometimes they are only read or only written outside the program. For example, the log introduced in *State Abstraction* could be implemented as an output port for the program logging the information, and as an input port for the program performing the logging. Two aspects are defined in SPARK to distinguish these different properties of volatile variables:

- Aspect Async\_Writers indicates that the value of the variable may be changed at any time (asynchronously) by hardware or software outside the program.
- Aspect Async\_Readers indicates that the value of the variable may be read at any time (asynchronously) by hardware or software outside the program.

Aspect Async\_Writers has an effect on GNATprove's proof: two successive reads of such a variable may return different results. Aspect Async\_Readers has an effect on GNATprove's flow analysis: an assignment to such a variable always has a potential effect, even if the value is never read in the program, since an external reader might actually read the value assigned.

These aspects are well suited to model respectively a sensor and a display, but not an input stream or an actuator, for which the act of reading or writing has an effect that should be reflected in the flow dependencies. Two more aspects are defined in SPARK to further refine the previous properties of volatile variables:

- Aspect Effective\_Reads indicates that reading the value of the variable has an effect (for example, removing a value from an input stream). It can only be specified on a variable that also has Async\_Writers set.
- Aspect Effective\_Writes indicates that writing the value of the variable has an effect (for example, sending a command to an actuator). It can only be specified on a variable that also has Async\_Readers set.

Both aspects Effective\_Reads and Effective\_Writes have an effect on GNATprove's flow analysis: reading the former or writing the latter is modelled as having an effect on the value of the variable, which needs to be reflected in flow dependencies. Because reading a variable with Effective\_Reads set has an effect on its value, such a variable cannot be only a subprogram input, it must be also an output.

For example, the program writing in a log each value passed as argument to procedure Add\_To\_Total may model the output port Log\_Out as a volatile variable with Async\_Readers and Effective\_Writes set:

```
package Logging_Out with
SPARK_Mode

is

Total : Integer;
Log_Out : Integer with Volatile, Async_Readers, Effective_Writes;

procedure Add_To_Total (Incr : in Integer) with
Global => (In_Out => Total, Output => Log_Out),
Depends => (Total =>+ Incr, Log_Out => Incr);

end Logging_Out;
```

```
package body Logging_Out with
SPARK_Mode
is
```

```
procedure Add_To_Total (Incr : in Integer) is

begin

Total := Total + Incr;

Log_Out := Incr;
end Add_To_Total;

end Logging_Out;
```

while the logging program may model the input port Log\_In as a volatile variable with Async\_Writers and Effective\_Reads set:

```
package Logging_In with
     SPARK_Mode
2
   is
      Log_In : Integer with Volatile, Async_Writers, Effective_Reads;
      type Integer_Array is array (Positive range 1 .. 100) of Integer;
6
              : Integer_Array;
      Log_Size : Natural;
      procedure Get with
10
        Global => (In_Out => (Log, Log_Size, Log_In)),
11
        Depends => ((Log_Size, Log_In) =>+ null, Log =>+ (Log_Size, Log_In));
12
13
   end Logging_In;
14
```

```
package body Logging_In with
SPARK_Mode
is

procedure Get is
begin
Log_Size := Log_Size + 1;
Log (Log_Size) := Log_In;
end Get;

end Logging_In;
```

GNAT prove checks the specified data and flow dependencies on both programs.

A volatile variable on which none of the four aspects <code>Async\_Writers</code>, <code>Async\_Readers</code>, <code>Effective\_Reads</code> or <code>Effective\_Writes</code> is set is assumed to have all four aspects set to <code>True</code>. A volatile variable on which some of the four aspects are set to <code>True</code> is assumed to have the remaining ones set to <code>False</code>. See SPARK RM 7.1.3 for details.

### **External State Abstraction**

Volatile variables may be part of *State Abstraction*, in which case the volatility of the abstract name must be specified by using aspect External on the abstract name, as follows:

```
package Account with
  Abstract_State => (State with External)
is
    ...
end Account;
```

An external state may represent both volatile variables and non-volatile ones, for example:

```
package body Account with
  Refined_State => (State => (Total, Log, Log_Size))
is
  Total : Integer;
  Log : Integer_Array with Volatile;
  Log_Size : Natural with Volatile;
  ...
end Account;
```

The different *Properties of Volatile Variables* may also be specified in the state abstraction, which is then used by GNATprove to refine the analysis. For example, the program writing in a log seen in the previous section can be rewritten to abstract global variables as follows:

```
package Logging_Out_Abstract with
SPARK_Mode,
Abstract_State => (State with External => (Async_Readers, Effective_Writes)),
Initializes => State
is
procedure Add_To_Total (Incr : in Integer) with
Global => (In_Out => State),
Depends => (State =>+ Incr);
end Logging_Out_Abstract;
```

```
package body Logging_Out_Abstract with
2
     SPARK_Mode,
     Refined_State => (State => (Log_Out, Total))
      Total : Integer := 0;
      Log_Out : Integer := 0 with Volatile, Async_Readers, Effective_Writes;
6
      procedure Add_To_Total (Incr : in Integer) with
        Refined_Global => (In_Out => Total, Output => Log_Out),
        Refined_Depends => (Total =>+ Incr, Log_Out => Incr)
10
11
      begin
12
         Total := Total + Incr;
13
         Log_Out := Incr;
14
15
      end Add_To_Total;
   end Logging_Out_Abstract;
```

while the logging program seen in the previous section may be rewritten to abstract global variables as follows:

```
package Logging_In_Abstract with

SPARK_Mode,
Abstract_State => (State with External => (Async_Writers, Effective_Reads))

is

procedure Get with
Global => (In_Out => State),
Depends => (State =>+ null);

end Logging_In_Abstract;
```

```
package body Logging_In_Abstract with
SPARK_Mode,
Refined_State => (State => (Log_In, Log, Log_Size))
```

```
4
      Log_In : Integer with Volatile, Async_Writers, Effective_Reads;
5
6
      type Integer_Array is array (Positive range 1 .. 100) of Integer;
           : Integer_Array := (others => 0);
      Log_Size : Natural := 0;
10
      procedure Get with
11
        Refined_Global => (In_Out => (Log, Log_Size, Log_In)),
12
        Refined_Depends => ((Log_Size, Log_In) =>+ null, Log =>+ (Log_Size, Log_In))
13
14
      is
      begin
15
         Log_Size := Log_Size + 1;
16
         Log (Log_Size) := Log_In;
17
      end Get;
18
19
   end Logging_In_Abstract;
```

GNAT prove checks the specified data and flow dependencies on both programs.

An external abstract state on which none of the four aspects <code>Async\_Writers</code>, <code>Async\_Readers</code>, <code>Effective\_Reads</code> or <code>Effective\_Writes</code> is set is assumed to have all four aspects set to <code>True</code>. An external abstract state on which some of the four aspects are set to <code>True</code> is assumed to have the remaining ones set to <code>False</code>. See SPARK RM 7.1.2 for details.

# **5.4 Type Contracts**

SPARK contains various features to constrain the values of a given type:

- A scalar range may be specified on a scalar type or subtype to bound its values.
- A record discriminant may be specified on a record type to distinguish between variants of the same record.
- A *predicate* introduced by aspect Static\_Predicate, Dynamic\_Predicate or Predicate may be specified on a type or subtype to express a property verified by objects of the (sub)type.
- A *type invariant* introduced by aspect Type\_Invariant or Invariant may be specified on the completion of a private type to express a property that is only guaranteed outside of the type scope.
- A *default initial condition* introduced by aspect Default\_Initial\_Condition on a private type specifies the initialization status and possibly properties of the default initialization for a type.

Note that SPARK does not yet support aspect Type\_Invariant from Ada 2012.

## 5.4.1 Scalar Ranges

[Ada 83]

Scalar types (signed integer types, modulo types, fixed-point types, floating-point types) can be given a low bound and a high bound to specify that values of the type must remain within these bounds. For example, the global counter Total can never be negative, which can be expressed in its type:

```
Total : Integer range 0 .. Integer'Last;
```

Any attempt to assign a negative value to variable Total results in raising an exception at run time. During analysis, GNATprove checks that all values assigned to Total are positive or null. The anonymous subtype above can also be given an explicit name:

```
subtype Nat is Integer range 0 .. Integer'Last;
Total : Nat;
```

or we can use the equivalent standard subtype Natural:

```
Total : Natural;
```

or Nat can be defined as a derived type instead of a subtype:

```
type Nat is new Integer range 0 .. Integer'Last;
Total : Nat;
```

or as a new signed integer type:

```
type Nat is range 0 .. Integer'Last;
Total : Nat;
```

All the variants above result in the same range checks both at run-time and in GNATprove. GNATprove also uses the range information for proving properties about the program (for example, the absence of overflows in computations).

### **5.4.2 Record Discriminants**

[Ada 83]

Record types can use discriminants to:

- · define multiple variants and associate each component with a specific variant
- bound the size of array components

For example, the log introduced in *State Abstraction* could be implemented as a discriminated record with a discriminant Kind selecting between two variants of the record for logging either only the minimum and maximum entries or the last entries, and a discriminant Capacity specifying the maximum number of entries logged:

```
package Logging_Discr with
     SPARK_Mode
2
   is
3
      type Log_Kind is (Min_Max_Values, Last_Values);
4
      type Integer_Array is array (Positive range <>) of Integer;
      type Log_Type (Kind : Log_Kind; Capacity : Natural) is record
         case Kind is
            when Min_Max_Values =>
               Min_Entry : Integer;
10
               Max_Entry : Integer;
11
            when Last_Values =>
12
               Log_Data : Integer_Array (1 .. Capacity);
               Log_Size : Natural;
         end case;
15
      end record;
16
17
      subtype Min_Max_Log is Log_Type (Min_Max_Values, 0);
18
      subtype Ten_Values_Log is Log_Type (Last_Values, 10);
19
20
      function Log_Size (Log : Log_Type) return Natural;
21
22
      function Last_Entry (Log : Log_Type) return Integer with
23
        Pre => Log.Kind = Last_Values and then Log.Log_Size in 1 .. Log.Capacity;
```

```
25
26 end Logging_Discr;
```

Subtypes of Log\_Type can specify fixed values for Kind and Capacity, like in Min\_Max\_Log and Ten\_Values\_Log. The discriminants Kind and Capacity are accessed like regular components, for example:

```
package body Logging_Discr with
     SPARK_Mode
2
3
      function Log_Size (Log : Log_Type) return Natural is
4
      begin
5
         case Log.Kind is
6
            when Min_Max_Values =>
                return 2;
             when Last_Values =>
               return Log.Log_Size;
10
         end case;
11
      end Log_Size;
12
13
14
      function Last_Entry (Log : Log_Type) return Integer is
         return Log.Log_Data (Log.Log_Size);
16
      end Last_Entry;
17
18
   end Logging_Discr;
```

Any attempt to access a component not present in a variable (because it is of a different variant), or to access an array component outside its bounds, results in raising an exception at run time. During analysis, GNATprove checks that components accessed are present, and that array components are accessed within bounds:

```
logging_discr.adb:10:23: info: discriminant check proved logging_discr.adb:16:17: info: discriminant check proved logging_discr.adb:16:31: info: discriminant check proved logging_discr.adb:16:31: info: index check proved logging_discr.ads:13:13: info: range check proved logging_discr.ads:13:13: info: range check proved logging_discr.ads:18:37: info: range check proved logging_discr.ads:18:53: info: range check proved logging_discr.ads:19:40: info: range check proved logging_discr.ads:19:53: info: range check proved logging_discr.ads:24:48: info: discriminant check proved
```

## 5.4.3 Predicates

[Ada 2012]

Predicates can be used on any subtype to express a property verified by objects of the subtype at all times. Aspects Static\_Predicate and Dynamic\_Predicate are defined in Ada 2012 to associate a predicate with a subtype. Aspect Dynamic\_Predicate allows to express more general predicates than aspect Static\_Predicate, at the cost of restricting the use of variables of the subtype. The following table summarizes the main similarities and differences between both aspects:

Feature	Static_Predicate	Dynamic_Predicate
Applicable to scalar subtype	Yes	Yes
Applicable to array/record subtype	No	Yes
Allows simple comparisons with static values	Yes	Yes
Allows conjunctions/disjunctions	Yes	Yes
Allows function calls	No	Yes
Allows general Boolean properties	No	Yes
Can be used in membership test	Yes	Yes
Can be used as range in for-loop	Yes	No
Can be used as choice in case-statement	Yes	No
Can be used as prefix with attributes First, Last or Range	No	No
Can be used as index subtype in array	No	No

Aspect Predicate is specific to GNAT and can be used instead of Static\_Predicate or Dynamic\_Predicate. GNAT treats it as a Static\_Predicate whenever possible and as a Dynamic\_Predicate in the remaining cases, thus not restricting uses of variables of the subtype more than necessary.

Predicates are inherited by subtypes and derived types. If a subtype or a derived type inherits a predicate and defines its own predicate, both predicates are checked on values of the new (sub)type. Predicates are restricted in SPARK so that they cannot depend on variable input. In particular, a predicate cannot mention a global variable in SPARK, although it can mention a global constant.

GNATprove checks that all values assigned to a subtype with a predicate are allowed by its predicate (for all three forms of predicate: Predicate, Static\_Predicate and Dynamic\_Predicate). GNATprove generates a predicate check even in cases where there is no corresponding run-time check, for example when assigning to a component of a record with a predicate. GNATprove also uses the predicate information for proving properties about the program.

### **Static Predicates**

A static predicate allows specifying which values are allowed or forbidden in a scalar subtype, when this specification cannot be expressed with *Scalar Ranges* (because it has *holes*). For example, we can express that the global counter Total cannot be equal to 10 or 100 with the following static predicate:

```
subtype Count is Integer with
  Static_Predicate => Count /= 10 and Count /= 100;
Total : Count;
```

### or equivalently:

```
subtype Count is Integer with
   Static_Predicate => Count in Integer'First .. 9 | 11 .. 99 | 101 .. Integer'Last;
Total : Count;
```

Uses of the name of the subtype Count in the predicate refer to variables of this subtype. Scalar ranges and static predicates can also be combined, and static predicates can be specified on subtypes, derived types and new signed integer types. For example, we may define Count as follows:

```
type Count is new Natural with
  Static_Predicate => Count /= 10 and Count /= 100;
```

Any attempt to assign a forbidden value to variable Total results in raising an exception at run time. During analysis, GNATprove checks that all values assigned to Total are allowed.

Similarly, we can express that values of subtype Normal\_Float are the *normal* 32-bits floating-point values (thus excluding *subnormal* values), assuming here that Float is the 32-bits floating-point type on the target:

```
subtype Normal_Float is Float with
   Static_Predicate => Normal_Float <= -2.0**(-126) or Normal_Float = 0.0 or Normal_
   →Float >= 2.0**(-126);
```

Any attempt to assign a subnormal value to a variable of subtype Normal\_Float results in raising an exception at run time. During analysis, GNATprove checks that only normal values are assigned to such variables.

## **Dynamic Predicates**

A dynamic predicate allows specifying properties of scalar subtypes that cannot be expressed as static predicates. For example, we can express that values of subtype Odd and Even are distributed according to their name as follows:

```
subtype Odd is Natural with
  Dynamic_Predicate => Odd mod 2 = 1;
subtype Even is Natural with
  Dynamic_Predicate => Even mod 2 = 0;
```

or that values of type Prime are prime numbers as follows:

```
type Prime is new Positive with
  Dynamic_Predicate => (for all Divisor in 2 .. Prime / 2 => Prime mod Divisor /= 0);
```

A dynamic predicate also allows specifying relations between components of a record. For example, we can express that the values paired together in a record are always distinct as follows:

```
type Distinct_Pair is record
  Val1, Val2 : Integer;
end record
  with Dynamic_Predicate => Distinct_Pair.Val1 /= Distinct_Pair.Val2;
```

or that a record stores pairs of values with their greatest common divisor as follows:

or that the number of elements Count in a resizable table is always less than or equal to its maximal number of elements Max as follows:

```
type Resizable_Table (Max : Natural) is record
   Count : Natural;
   Data : Data_Array(1 .. Max);
end record
   with Dynamic_Predicate => Resizable_Table.Count <= Resizable_Table.Max;</pre>
```

A dynamic predicate also allows specifying global properties over the content of an array. For example, we can express that elements of an array are stored in increasing order as follows:

or that a special end marker is always present in the array as follows:

```
type Ended_Array is array (Index) of Integer
with Dynamic_Predicate =>
   (for some I in Index => Ended_Array(I) = End_Marker);
```

Dynamic predicates are checked only at specific places at run time, as mandated by the Ada Reference Manual:

- when converting a value to the subtype with the predicate
- when returning from a call, for each in-out and out parameter passed by reference
- when declaring an object, except when there is no initialization expression and no subcomponent has a default expression

Thus, not all violations of the dynamic predicate are caught at run time. On the contrary, during analysis, GNATprove checks that initialized variables whose subtype has a predicate always contain a value allowed by the predicate.

# **5.4.4 Type Invariants**

[Ada 2012]

In SPARK, type invariants can only be specified on completions of private types (and not directly on private type declarations). They express a property that is only guaranteed outside of the immediate scope of the type bearing the invariant. Aspect Type\_Invariant is defined in Ada 2012 to associate an invariant with a type. Aspect Invariant is specific to GNAT and can be used instead of Type\_Invariant.

GNATprove checks that, outside of the immediate scope of a type with an invariant, all values of this type are allowed by its invariant. In order to provide such a strong guarantee, GNATprove generates an invariant check even in cases where there is no corresponding run-time check, for example on global variables that are modified by a subprogram. GNATprove also uses the invariant information for proving properties about the program.

As an example, let us consider a stack, which can be queried for the maximum of the elements stored in it:

```
package P is
    type Stack is private;
    function Max (S : Stack) return Element;
private
```

In the implementation, an additional component is allocated for the maximum, which is kept up to date by the implementation of the stack. This information is a type invariant, which can be specified using a Type\_Invariant aspect:

```
type Stack is record
    Content : Element_Array := (others => 0);
    Size : My_Length := 0;
    Max : Element := 0;
end record with
```

Like for subtype predicates, the name of the type can be used inside the invariant expression to refer to the current instance of the type. Here the subtype predicate of Stack expresses that the Max field of a valid stack is the maximum of the elements stored in the stack.

To make sure that the invariant holds for every value of type Stack outside of the package P, GNATprove introduces invariant checks in several places. First, at the type declaration, it will make sure that the invariant holds every time an object of type Stack is default initialized. Here, as the stack is empty by default and the default value of Max is 0, the check will succeed. It is also possible to forbid default initialization of objects of type Stack altogether by using a *Default Initial Condition* of False:

```
type Stack is private with Default_Initial_Condition => False;

type Stack is record
   Content : Element_Array;
   Size : My_Length;
   Max : Element;
end record with Type_Invariant => Is_Valid (Stack);
```

A check is also introduced to make sure the invariant holds for every global object declared in the scope of Stack after it has been initialized:

Here the global variable The\_Stack is allowed to break its invariant during the elaboration of P. The invariant check will only be done at the end of the elaboration of P, and will succeed.

In the same way, variables and parameters of a subprogram are allowed to break their invariants in the subprogram body. Verification conditions are generated to ensure that no invariant breaking value can leak outside of P. More precisely, invariant checks on subprogram parameters are performed:

- when calling a subprogram visible outside of P from inside of P. Such a subprogram can be either declared in the visible part of P or in another unit,
- when returning from a subprogram declared in the visible part of P.

For example, let us consider the implementation of a procedure Push that pushes an element of top of a stack. It is declared in the visible part of the specification of P:

```
function Size (S : Stack) return My_Length;

procedure Push (S : in out Stack; E : Element) with
   Pre => Size (S) < My_Length'Last;

procedure Push_Zero (S : in out Stack) with
   Pre => Size (S) < My_Length'Last;</pre>
```

It is then implemented using an internal procedure Push\_Internal declared in the body of P:

```
procedure Push_Internal (S : in out Stack; E : Element) with
  Pre => S.Size < My_Length'Last,
  Post => S.Size = S.Size'Old + 1 and S.Content (S.Size) = E
  and S.Content (1 .. S.Size) 'Old = S.Content (1 .. S.Size - 1)
  and S.Max = S.Max'Old
is
begin
  S.Size := S.Size + 1;
   S.Content (S.Size) := E;
end Push_Internal;
procedure Push (S : in out Stack; E : Element) is
begin
  Push_Internal (S, E);
  if S.Max < E then</pre>
      S.Max := E;
   end if;
end Push;
procedure Push_Zero (S : in out Stack) is
   Push (S, 0);
end Push_Zero;
```

On exit of Push\_Internal, the invariant of Stack is broken. It is OK since Push\_Internal is not visible from outside of P. Invariant checks are performed when exiting Push and when calling it from inside Push\_Zero. They both succeed. Note that, because of invariant checks on parameters, it is not allowed in SPARK to call a function that is visible from outside P in the invariant of Stack otherwise this would lead to a recursive proof. In particular, it is not allowed to make Is\_Valid visible in the public declarations of P. In the same way, the function Size cannot be used in the invariant of Stack. We also avoid using Size in the contract of Push\_Internal as it would have enforced additional invariant checks on its parameter.

Checks are also performed for global variables accessed by subprograms inside P. Even if it is allowed to break the invariant of a global variable when inside the body of a subprogram declared in P, invariant checks are performed when calling and returning from every subprogram inside P. For example, if Push and Push\_Internal are accessing directly the global stack The\_Stack instead of taking it as a parameter, there will be a failed invariant check on exit of Push\_Internal:

```
procedure Push_Internal (E : Element) with
   Pre => The_Stack.Size < My_Length'Last
is
begin
   The_Stack.Size := The_Stack.Size + 1;
   The_Stack.Content (The_Stack.Size) := E;
end Push_Internal;

procedure Push (E : Element) is</pre>
```

```
begin
   Push_Internal (E);
   if The_Stack.Max < E then
        The_Stack.Max := E;
   end if;
end Push;</pre>
```

In this way, users will never have to use contracts to ensure that the invariant holds on global variable The\_Stack through local subprogram calls.

### 5.4.5 Default Initial Condition

### [SPARK]

Private types in a package define an encapsulation mechanism that prevents client units from accessing the implementation of the type. That boundary may also be used to specify properties that hold for default initialized values of that type in client units. For example, the log introduced in *State Abstraction* could be implemented as a private type with a default initial condition specifying that the size of the log is initially zero, where uses of the name of the private type Log\_Type in the argument refer to variables of this type:

```
package Logging_Priv with
     SPARK_Mode
2
   is
3
      Max_Count : constant := 100;
4
5
      type Log_Type is private with
6
        Default_Initial_Condition => Log_Size (Log_Type) = 0;
7
      function Log_Size (Log : Log_Type) return Natural;
10
      procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
11
        Pre => Log_Size (Log) < Max_Count;</pre>
12
13
   private
14
15
      type Integer_Array is array (1 .. Max_Count) of Integer;
16
17
      type Log_Type is record
18
        Log_Data : Integer_Array;
19
        Log_Size : Natural := 0;
20
      end record;
21
22
      function Log_Size (Log : Log_Type) return Natural is (Log.Log_Size);
23
24
   end Logging_Priv;
```

This may be useful to analyze with GNATprove client code that defines a variable of type Log\_Type with default initialization, and then proceeds to append values to this log, as procedure Append\_To\_Log's precondition requires that the log size is not maximal:

```
The_Log : Log_Type;
...
Append_To_Log (The_Log, X);
```

GNATprove's flow analysis also uses the presence of a default initial condition as an indication that default initialized variables of that type are considered as fully initialized. So the code snippet above would pass flow analysis without

messages being issued on the read of The\_Log. If the full definition of the private type is in SPARK, GNATprove also checks that the type is indeed fully default initialized, and if not issues a message like here:

```
logging_priv.ads:18:04: medium: type "Log_Type" is not fully initialized
```

If partial default initialization of the type is intended, in general for efficiency like here, then the corresponding message can be justified with pragma Annotate, see section *Justifying Check Messages*.

Aspect Default\_Initial\_Condition can also be specified without argument to only indicate that default initialized variables of that type are considered as fully initialized. This is equivalent to Default\_Initial\_Condition => True:

```
type Log_Type is private with
  Default_Initial_Condition;
```

The argument can also be null to specify that default initialized variables of that type are *not* considered as fully initialized:

```
type Log_Type is private with
  Default_Initial_Condition => null;
```

This is different from an argument of False which can be used to indicate that variables of that type should always be explicitly initialized (otherwise GNAT prove will not be able to prove the condition False on the default initialization and will issue a message during proof).

# 5.5 Specification Features

SPARK contains many features for specifying the intended behavior of programs. Some of these features come from Ada 2012 (*Attribute Old* and *Expression Functions* for example). Other features are specific to SPARK (*Attribute Loop\_Entry* and *Ghost Code* for example). In this section, we describe these features and their impact on execution and formal verification.

## 5.5.1 Aspect Constant\_After\_Elaboration

Aspect Constant\_After\_Elaboration can be specified on a library level variable that has an initialization expression. When specified, the corresponding variable can only be changed during the elaboration of its enclosing package. SPARK ensures that users of the package do not change the variable. This feature can be particularly useful in tasking code since variables that are Constant\_After\_Elaboration are guaranteed to prevent unsynchronized modifications (see *Tasks and Data Races*).

```
package CAE is
   Var : Integer := 0 with
        Constant_After_Elaboration;

-- The following is illegal because users of CAE could call Illegal
-- and that would cause an update of Var after CAE has been
-- elaborated.
   procedure Illegal with
        Global => (Output => Var);
end CAE;

package body CAE is
   procedure Illegal is
   begin
```

```
Var := 10;
end Illegal;

-- The following subprogram is legal because it is declared inside
-- the body of CAE and therefore it cannot be directly called
-- from a user of CAE.
procedure Legal is
begin
    Var := Var + 2;
end Legal;

begin
-- The following statements are legal since they take place during
-- the elaboration of CAE.
Var := Var + 1;
Legal;
end CAE;
```

### 5.5.2 Attribute Old

[Ada 2012]

### In a Postcondition

Inside *Postconditions*, attribute Old refers to the values that expressions had at subprogram entry. For example, the postcondition of procedure Increment might specify that the value of parameter X upon returning from the procedure has been incremented:

```
procedure Increment (X : in out Integer) with
Post => X = X'Old + 1;
```

At run time, a copy of the variable X is made when entering the subprogram. This copy is then read when evaluating the expression X 'Old in the postcondition. Because it requires copying the value of X, the type of X cannot be limited.

Strictly speaking, attribute Old must apply to a *name* in Ada syntax, for example a variable, a component selection, a call, but not an addition like X + Y. For expressions that are not *names*, attribute Old can be applied to their qualified version, for example:

```
procedure Increment_One_Of (X, Y : in out Integer) with
Post => X + Y = Integer'(X + Y)'Old + 1;
```

Because the compiler unconditionally creates a copy of the expression to which attribute old is applied at subprogram entry, there is a risk that this feature might confuse users in more complex postconditions. Take the example of a procedure Extract, which copies the value of array A at index J into parameter V, and zeroes out this value in the array, but only if J is in the bounds of A:

```
procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
Post => (if J in A'Range then V = A(J)'old); -- INCORRECT
```

Clearly, the value of A(J) at subprogram entry is only meaningful if J is in the bounds of A. If the code above was allowed, then a copy of A(J) would be made on entry to subprogram Extract, even when J is out of bounds, which would raise a run-time error. To avoid this common pitfall, use of attribute old in expressions that are potentially unevaluated (like the then-part in an if-expression, or the right argument of a shortcut boolean expression - See Ada

RM 6.1.1) is restricted to plain variables: A is allowed, but not A (J). The GNAT compiler issues the following error on the code above:

```
prefix of attribute "Old" that is potentially unevaluated must denote an entity
```

The correct way to specify the postcondition in the case above is to apply attribute Old to the entity prefix A:

```
procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
Post => (if J in A'Range then V = A'Old(J));
```

#### In Contract Cases

The rule for attribute Old inside *Contract Cases* is more permissive. Take for example the same contract as above for procedure Extract, expressed with contract cases:

Only the expressions used as prefixes of attribute Old in the *currently enabled case* are copied on entry to the subprogram. So if Extract is called with J out of the range of A, then the second case is enabled, so A(J) is not copied when entering procedure Extract. Hence, the above code is allowed.

It may still be the case that some contracts refer to the value of objects at subprogram entry inside potentially unevaluated expressions. For example, an incorrect variation of the above contract would be:

For the same reason that such uses are forbidden by Ada RM inside postconditions, the SPARK RM forbids these uses inside contract cases (see SPARK RM 6.1.3(2)). The GNAT compiler issues the following error on the code above:

```
prefix of attribute "Old" that is potentially unevaluated must denote an entity
```

The correct way to specify the consequence expression in the case above is to apply attribute Old to the entity prefix A:

## In a Potentially Unevaluated Expression

In some cases, the compiler issues the error discussed above (on attribute old applied to a non-entity in a potentially unevaluated context) on an expression that can safely be evaluated on subprogram entry, for example:

```
procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
Post => (if J in A'Range then V = Get_If_In_Range(A, J)'Old); -- ERROR
```

where function Get\_If\_In\_Range returns the value A(J) when J is in the bounds of A, and a default value otherwise.

In that case, the solution is either to rewrite the postcondition using non-shortcut boolean operators, so that the expression is not *potentially evaluated* anymore, for example:

```
procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
Post => J not in A'Range or V = Get_If_In_Range(A, J)'Old;
```

or to rewrite the postcondition using an intermediate expression function, so that the expression is not *potentially* evaluated anymore, for example:

```
function Extract_Post (A : My_Array; J : Integer; V, Get_V : Value) return Boolean is
   (if J in A'Range then V = Get_V);

procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
   Post => Extract_Post (A, J, V, Get_If_In_Range(A, J)'Old);
```

or to use the GNAT pragma <code>Unevaluated\_Use\_Of\_Old</code> to allow such uses of attribute <code>Old</code> in potentially unevaluated expressions:

```
pragma Unevaluated_Use_Of_Old (Allow);

procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
   Post => (if J in A'Range then V = Get_If_In_Range(A,J)'Old);
```

GNAT does not issue an error on the code above, and always evaluates the call to Get\_If\_In\_Range on entry to procedure Extract, even if this value may not be used when executing the postcondition. Note that the formal verification tool GNATprove correctly generates all required checks to prove that this evaluation on subprogram entry does not fail a run-time check or a contract (like the precondition of Get\_If\_In\_Range if any).

Pragma Unevaluated\_Use\_Of\_Old applies to uses of attribute Old both inside postconditions and inside contract cases. See GNAT RM for a detailed description of this pragma.

## 5.5.3 Attribute Result

[Ada 2012]

Inside *Postconditions* of functions, attribute Result refers to the value returned by the function. For example, the postcondition of function Increment might specify that it returns the value of parameter X plus one:

```
function Increment (X : Integer) return Integer with
Post => Increment'Result = X + 1;
```

Contrary to Attribute Old, attribute Result does not require copying the value, hence it can be applied to functions that return a limited type. Attribute Result can also be used inside consequence expressions in *Contract Cases*.

## 5.5.4 Attribute Loop\_Entry

[SPARK]

It is sometimes convenient to refer to the value of variables at loop entry. In many cases, the variable has not been modified between the subprogram entry and the start of the loop, so this value is the same as the value at subprogram entry. But *Attribute Old* cannot be used in that case. Instead, we can use attribute Loop\_Entry. For example, we can express that after J iterations of the loop, the value of parameter array X at index J is equal to its value at loop entry plus one:

```
procedure Increment_Array (X : in out Integer_Array) is
begin
   for J in X'Range loop
```

```
X(J) := X(J) + 1;
pragma Assert (X(J) = X'Loop_Entry(J) + 1);
end loop
end Increment_Array;
```

At run time, a copy of the variable X is made when entering the loop. This copy is then read when evaluating the expression X'Loop\_Entry. No copy is made if the loop is never entered. Because it requires copying the value of X, the type of X cannot be limited.

Attribute Loop\_Entry can only be used in top-level *Assertion Pragmas* inside a loop. It is mostly useful for expressing complex *Loop Invariants* which relate the value of a variable at a given iteration of the loop and its value at loop entry. For example, we can express that after J iterations of the loop, the value of parameter array X at all indexes already seen is equal to its value at loop entry plus one, and that its value at all indexes not yet seen is unchanged, using *Quantified Expressions*:

```
procedure Increment_Array (X : in out Integer_Array) is
begin
    for J in X'Range loop
        X(J) := X(J) + 1;
        pragma Loop_Invariant (for all K in X'First .. J => X(K) = X'Loop_Entry(K) + 1);
        pragma Loop_Invariant (for all K in J + 1 .. X'Last => X(K) = X'Loop_Entry(K));
    end loop;
end Increment_Array;
```

Attribute Loop\_Entry may be indexed by the name of the loop to which it applies, which is useful to refer to the value of a variable on entry to an outter loop. When used without loop name, the attribute applies to the closest enclosing loop. For examples, X'Loop\_Entry is the same as X'Loop\_Entry (Inner) in the loop below, which is not the same as X'Loop\_Entry (Outter) (although all three assertions are true):

```
procedure Increment_Matrix (X : in out Integer_Matrix) is
begin
   Outter: for J in X'Range(1) loop
        Inner: for K in X'Range(2) loop
        X(J,K) := X(J,K) + 1;
        pragma Assert (X(J,K) = X'Loop_Entry(J,K) + 1);
        pragma Assert (X(J,K) = X'Loop_Entry(Inner)(J,K) + 1);
        pragma Assert (X(J,K) = X'Loop_Entry(Outter)(J,K) + 1);
        end loop Inner;
   end loop Outter;
end Increment_Matrix;
```

By default, similar restrictions exist for the use of attribute Loop\_Entry and the use of attribute Old *In a Potentially Unevaluated Expression*. The same solutions apply here, in particular the use of GNAT pragma Unevaluated\_Use\_Of\_Old.

## 5.5.5 Attribute Update

### [SPARK]

It is quite common in *Postconditions* to relate the input and output values of parameters. While this can be as easy as X = X'Old + 1 in the case of scalar parameters, it is more complex to express for array and record parameters. Attribute Update is useful in that case, to denote the updated value of a composite variable. For example, we can express more clearly that procedure Zero\_Range zeroes out the elements of its array parameter X between From and To by using attribute Update:

```
procedure Zero_Range (X : in out Integer_Array; From, To : Positive) with
Post => X = X'Old'Update(From .. To => 0);
```

than with an equivalent postcondition using Quantified Expressions and Conditional Expressions:

Attribute Update takes in argument a list of associations between indexes (for arrays) or components (for records) and values. Components can only be mentioned once, with the semantics that all values are evaluated before any update. Array indexes may be mentioned more than once, with the semantics that updates are applied in left-to-right order. For example, the postcondition of procedure Swap expresses that the values at indexes J and K in array X have been swapped:

```
procedure Swap (X : in out Integer_Array; J, K : Positive) with
Post => X = X'Old'Update(J => X'Old(K), K => X'Old(J));
```

and the postcondition of procedure  $Rotate\_Clockwize\_Z$  expresses that the point P given in parameter has been rotated 90 degrees clockwise around the Z axis (thus component Z is preserved while components X and Y are modified):

```
procedure Rotate_Clockwize_Z (P : in out Point_3D) with
Post => P = P'Old'Update(X => P.Y'Old, Y => - P.X'Old);
```

Similarly to its use in combination with attribute Old in postconditions, attribute Update is useful in combination with *Attribute Loop\_Entry* inside *Loop Invariants*. For example, we can express the property that, after iteration J in the main loop in procedure Zero\_Range, the value of parameter array X at all indexes already seen is equal to zero:

```
procedure Zero_Range (X : in out Integer_Array; From, To : Positive) is
begin
   for J in From .. To loop
       X(J) := 0;
       pragma Loop_Invariant (X = X'Loop_Entry'Update(From .. J => 0));
   end loop;
end Zero_Range;
```

Attribute Update can also be used outside of assertions. It is particularly useful in expression functions. For example, the functionality in procedure Rotate\_Clockwize\_Z could be expressed equivalently as an expression function:

```
function Rotate_Clockwize_Z (P : Point_3D) return Point_3D is
   (P'Update(X => P.Y, Y => - P.X));
```

Because it requires copying the value of P, the type of P cannot be limited.

## 5.5.6 Conditional Expressions

[Ada 2012]

A conditional expression is a way to express alternative possibilities in an expression. It is like the ternary conditional expression cond? expr1: expr2 in C or Java, except more powerful. There are two kinds of conditional expressions in Ada:

- if-expressions are the counterpart of if-statements in expressions
- case-expressions are the counterpart of case-statements in expressions

For example, consider the variant of procedure Add\_To\_Total seen in *Contract Cases*, which saturates at a given threshold. Its postcondition can be expressed with an if-expression as follows:

Each branch of an if-expression (there may be one, two or more branches when elsif is used) can be seen as a logical implication, which explains why the above postcondition can also be written:

or equivalently (as the absence of else branch above is implicitly the same as else True):

If-expressions are not necessarily of boolean type, in which case they must have an else branch that gives the value of the expression for cases not covered in previous conditions (as there is no implicit else True in such a case). For example, here is a postcondition equivalent to the above, that uses an if-expression of Integer type:

Although case-expressions can be used to cover cases of any scalar type, they are mostly used with enumerations, and the compiler checks that all cases are disjoint and that together they cover all possible cases. For example, consider a variant of procedure Add\_To\_Total which takes an additional Mode global input of enumeration value Single, Double, Negate or Ignore, with the intuitive corresponding leverage effect on the addition. The postcondition of this variant can be expressed using a case-expression as follows:

Like if-expressions, case-expressions are not necessarily of boolean type. For example, here is a postcondition equivalent to the above, that uses a case-expression of Integer type:

A last case of others can be used to denote all cases not covered by previous conditions. If-expressions and case-expressions should always be parenthesized.

# 5.5.7 Quantified Expressions

[Ada 2012]

A quantified expression is a way to express a property over a collection, either an array or a container (see *Formal Containers Library*):

- a universally quantified expression using for all expresses a property that holds for all elements of a collection
- an existentially quantified expression using for some expresses a property that holds for at least one element of a collection

For example, consider the procedure Increment\_Array that increments each element of its array parameter X by one. Its postcondition can be expressed using a universally quantified expression as follows:

```
procedure Increment_Array (X : in out Integer_Array) with
Post => (for all J in X'Range => X(J) = X'Old(J) + 1);
```

The negation of a universal property being an existential property (the opposite is true too), the postcondition above can be expressed also using an existentially quantified expression as follows:

```
procedure Increment_Array (X : in out Integer_Array) with
Post => not (for some J in X'Range => X(J) /= X'Old(J) + 1);
```

At run time, a quantified expression is executed like a loop, which exits as soon as the value of the expression is known: if the property does not hold (resp. holds) for a given element of a universally (resp. existentially) quantified expression, execution of the loop does not proceed with remaining elements and returns the value False (resp. True) for the expression.

When a quantified expression is analyzed with GNATprove, it uses the logical counterpart of the quantified expression. GNATprove also checks that the expression is free from run-time errors. For this checking, GNATprove checks that the enclosed expression is free from run-time errors over the *entire range* of the quantification, not only at points that would actually be reached at run time. As an example, consider the following expression:

```
(for all I in 1 .. 10 => 1 / (I - 3) > 0)
```

This quantified expression cannot raise a run-time error, because the enclosed expression 1 / (I - 3) > 0 is false for the first value of the range I = 1, so the execution of the loop exits immediately with the value False for the quantified expression. GNATprove is stricter and requires the enclosed expression 1 / (I - 3) > 0 to be free from run-time errors over the entire range I in 1 ... 10 (including I = 3) so it issues a check message for a possible division by zero in this case.

Quantified expressions should always be parenthesized.

## 5.5.8 Expression Functions

[Ada 2012]

An expression function is a function whose implementation is given by a single expression. For example, the function Increment can be defined as an expression function as follows:

```
function Increment (X : Integer) return Integer is (X + 1);
```

For compilation and execution, this definition is equivalent to:

```
function Increment (X : Integer) return Integer is
begin
   return X + 1;
end Increment;
```

For GNATprove, this definition as expression function is equivalent to the same function body as above, plus a post-condition:

```
function Increment (X : Integer) return Integer with
  Post => Increment'Result = X + 1
is
begin
  return X + 1;
end Increment;
```

Thus, a user does not need in general to add a postcondition to an expression function, as the implicit postcondition generated by GNATprove is the most precise one. If a user adds a postcondition to an expression function, GNATprove uses this postcondition to analyze the function's callers as well as the most precise implicit postcondition.

On the contrary, it may be useful in general to add a precondition to an expression function, to constrain the contexts in which it can be called. For example, parameter X passed to function Increment should be less than the maximal integer value, otherwise an overflow would occur. We can specify this property in Increment's precondition as follows:

```
function Increment (X : Integer) return Integer is (X + 1) with
Pre => X < Integer'Last;</pre>
```

Note that the contract of an expression function follows its expression.

Expression functions can be defined in package declarations, hence they are well suited for factoring out common properties that are referred to in contracts. For example, consider the procedure Increment\_Array that increments each element of its array parameter X by one. Its precondition can be expressed using expression functions as follows:

```
package Increment_Utils is
  function Not_Max (X : Integer) return Boolean is (X < Integer'Last);
  function None_Max (X : Integer_Array) return Boolean is
     (for all J in X'Range => Not_Max (X(J)));

  procedure Increment_Array (X : in out Integer_Array) with
     Pre => None_Max (X);
end Increment_Utils;
```

Expression functions can be defined over private types, and still be used in the contracts of publicly visible subprograms of the package, by declaring the function publicly and defining it in the private part. For example:

```
package Increment_Utils is
    type Integer_Array is private;
    function None_Max (X : Integer_Array) return Boolean;
    procedure Increment_Array (X : in out Integer_Array) with
        Pre => None_Max (X);

private
```

```
type Integer_Array is array (Positive range <>) of Integer;
function Not_Max (X : Integer) return Boolean is (X < Integer'Last);
function None_Max (X : Integer_Array) return Boolean is
    (for all J in X'Range => Not_Max (X(J)));
end Increment_Utils;
```

If an expression function is defined in a unit spec, GNATprove can use its implicit postcondition at every call. If an expression function is defined in a unit body, GNATprove can use its implicit postcondition at every call in the same unit, but not at calls inside other units. This is true even if the expression function is declared in the unit spec and defined in the unit body.

### 5.5.9 Ghost Code

#### [SPARK]

Sometimes, the variables and functions that are present in a program are not sufficient to specify intended properties and to verify these properties with GNATprove. In such a case, it is possible in SPARK to insert in the program additional code useful for specification and verification, specially identified with the aspect Ghost so that it can be discarded during compilation. So-called *ghost code* in SPARK are these parts of the code that are only meant for specification and verification, and have no effect on the functional behavior of the program.

Various kinds of ghost code are useful in different situations:

- Ghost functions are typically used to express properties used in contracts.
- Global ghost variables are typically used to keep track of the current state of a program, or to maintain a log of past events of some type. This information can then be referred to in contracts.
- Local ghost variables are typically used to hold intermediate values during computation, which can then be referred to in assertion pragmas like loop invariants.
- *Ghost types* are those types only useful for defining ghost variables.
- *Ghost procedures* can be used to factor out common treatments on ghost variables. Ghost procedures should not have non-ghost outputs, either output parameters or global outputs.
- Ghost packages provide a means to encapsulate all types and operations for a specific kind of ghost code.
- *Imported ghost subprograms* are used to provide placeholders for properties that are defined in a logical language, when using manual proof.

When the program is compiled with assertions (for example with switch -gnata in GNAT), ghost code is executed like normal code. Ghost code can also be selectively enabled by setting pragma Assertion\_Policy as follows:

```
pragma Assertion_Policy (Ghost => Check);
```

GNATprove checks that ghost code cannot have an effect on the behavior of the program. GNAT compiler also performs some of these checks, although not all of them. Apart from these checks, GNATprove treats ghost code like normal code during its analyses.

### **Ghost Functions**

Ghost functions are useful to express properties only used in contracts, and to factor out common expressions used in contracts. For example, function Get\_Total introduced in *State Abstraction and Functional Contracts* to retrieve

the value of variable Total in the contract of Add\_To\_Total could be marked as a ghost function as follows:

```
function Get_Total return Integer with Ghost;
```

and still be used exactly as seen in State Abstraction and Functional Contracts:

```
procedure Add_To_Total (Incr : in Integer) with
  Pre => Incr >= 0 and then Get_Total in 0 .. Integer'Last - Incr,
  Post => Get_Total = Get_Total'Old + Incr;
```

The definition of Get\_Total would be also the same:

```
Total : Integer;
function Get_Total return Integer is (Total);
```

Although it is more common to define ghost functions as *Expression Functions*, a regular function might be used too:

```
function Get_Total return Integer is
begin
    return Total;
end Get_Total;
```

In that case, GNATprove uses only the contract of Get\_Total (either user-specified or the default one) when analyzing its callers, like for a non-ghost regular function. (The same exception applies as for regular functions, when GNATprove can analyze a subprogram in the context of its callers, as described in *Contextual Analysis of Subprograms Without Contracts*.)

All functions which are only used in specification can be marked as ghost, but most don't need to. However, there are cases where marking a specification-only function as ghost really brings something. First, as ghost entities are not allowed to interfere with normal code, marking a function as ghost avoids having to break state abstraction for the purpose of specification. For example, marking Get\_Total as ghost will prevent users of the package Account from accessing the value of Total from non-ghost code.

Then, in the usual context where ghost code is not kept in the final executable, the user is given more freedom to use in ghost code constructs that are less efficient than in normal code, which may be useful to express rich properties. For example, the ghost functions defined in the *Formal Containers Library* in GNAT typically copy the entire content of the argument container, which would not be acceptable for non-ghost functions.

#### **Ghost Variables**

Ghost variables are useful to keep track of local or global information during the computation, which can then be referred to in contracts or assertion pragmas.

### Case 1: Keeping Intermediate Values

Local ghost variables are commonly used to keep intermediate values. For example, we can define a local ghost variable Init\_Total to hold the initial value of variable Total in procedure Add\_To\_Total, which allows checking the relation between the initial and final values of Total in an assertion:

```
procedure Add_To_Total (Incr : in Integer) is
    Init_Total : Integer := Total with Ghost;
begin
    Total := Total + Incr;
    pragma Assert (Total = Init_Total + Incr);
end Add_To_Total;
```

### Case 2: Keeping Memory of Previous State

Global ghost variables are commonly used to memorize the value of a previous state. For example, we can define a global ghost variable Last\_Incr to hold the previous value passed in argument when calling procedure Add\_To\_Total, which allows checking in its precondition that the sequence of values passed in argument is non-decreasing:

```
Last_Incr : Integer := Integer'First with Ghost;

procedure Add_To_Total (Incr : in Integer) with
    Pre => Incr >= Last_Incr;

procedure Add_To_Total (Incr : in Integer) is
begin
    Total := Total + Incr;
    Last_Incr := Incr;
end Add_To_Total;
```

### **Case 3: Logging Previous Events**

Going beyond the previous case, global ghost variables can be used to store a complete log of events. For example, we can define global ghost variables Log and Log\_Size to hold the sequence of values passed in argument to procedure Add\_To\_Total, as in *State Abstraction*:

```
Log : Integer_Array with Ghost;
Log_Size : Natural with Ghost;

procedure Add_To_Total (Incr : in Integer) with

Post => Log_Size = Log_Size'Old + 1 and Log = Log'Old'Update (Log_Size => Incr);

procedure Add_To_Total (Incr : in Integer) is
begin

Total := Total + Incr;
Log_Size := Log_Size + 1;
Log (Log_Size) := Incr;
end Add_To_Total;
```

The postcondition of Add\_To\_Total above expresses that Log\_Size is incremented by one at each call, and that the current value of parameter Incr is appended to Log at each call (using *Attribute Old* and *Attribute Update*).

### **Case 4: Expressing Existentially Quantified Properties**

In SPARK, universal quantification is only allowed in restricted cases (over integer ranges and over the content of a container). To express the existence of a particular object, it is sometimes easier to simply provide it. This can be done using a global ghost variable. This can be used in particular to split the specification of a complex procedure into smaller parts:

```
X_Interm : T with Ghost;

procedure Do_Two_Thing (X : in out T) with
  Post => First_Thing_Done (X'Old, X_Interm) and then
```

```
Second_Thing_Done (X_Interm, X)
is
    X_Init : constant T := X with Ghost;
begin
    Do_Something (X);
    pragma Assert (First_Thing_Done (X_Init, X));
    X_Interm := X;

    Do_Something_Else (X);
    pragma Assert (Second_Thing_Done (X_Interm, X));
end Do_Two_Things;
```

More complicated uses can also be envisioned, up to constructing ghost data structures reflecting complex properties. For example, we can express that two arrays are a permutation of each other by constructing a permutation from one to the other:

```
Perm : Permutation with Ghost;

procedure Permutation_Sort (A : Nat_Array) with
   Post => A = Apply_Perm (Perm, A'Old)
is
begin
   -- Initalize Perm with the identity
   Perm := Identity_Perm;

for Current in A'First .. A'Last - 1 loop
    Smallest := Index_Of_Minimum_Value (A, Current, A'Last);
   if Smallest /= Current then
        Swap (A, Current, Smallest);

        -- Update Perm each time we permute two elements in A
        Permute (Perm, Current, Smallest);
   end if;
   end loop;
end Permutation_Sort;
```

## **Ghost Types**

Ghost types can only be used to define ghost variables. For example, we can define ghost types Log\_Type and Log\_Size\_Type that specialize the types Integer\_Array and Natural for ghost variables:

```
subtype Log_Type is Integer_Array with Ghost;
subtype Log_Size_Type is Natural with Ghost;
Log : Log_Type with Ghost;
Log_Size : Log_Size_Type with Ghost;
```

### **Ghost Procedures**

Ghost procedures are useful to factor out common treatments on ghost variables. For example, we can define a ghost procedure Append\_To\_Log to append a value to the log as seen previously.

```
Log : Integer_Array with Ghost;
Log_Size : Natural with Ghost;
```

```
procedure Append_To_Log (Incr : in Integer) with
   Ghost,
   Post => Log_Size = Log_Size'Old + 1 and Log = Log'Old'Update (Log_Size => Incr);

procedure Append_To_Log (Incr : in Integer) is
begin
   Log_Size := Log_Size + 1;
   Log (Log_Size) := Incr;
end Append_To_Log;
```

Then, this procedure can be called in Add\_To\_Total as follows:

```
procedure Add_To_Total (Incr : in Integer) is
begin
   Total := Total + Incr;
   Append_To_Log (Incr);
end Add_To_Total;
```

### **Ghost Packages**

Ghost packages are useful to encapsulate all types and operations for a specific kind of ghost code. For example, we can define a ghost package Logging to deal with all logging operations on package Account:

```
package Logging with
   Ghost
is
   Log : Integer_Array;
   Log_Size : Natural;

procedure Append_To_Log (Incr : in Integer) with
   Post => Log_Size = Log_Size'Old + 1 and Log = Log'Old'Update (Log_Size => Incr);
   ...
end Logging;
```

The implementation of package Logging is the same as if it was not a ghost package. In particular, a Ghost aspect is implicitly added to all declarations in Logging, so it is not necessary to specify it explicitly. Logging can be defined either as a local ghost package or as a separate unit. In the latter case, unit Account needs to reference unit Logging in a with-clause like for a non-ghost unit:

```
with Logging;
package Account is
...
end Account;
```

### **Imported Ghost Subprograms**

When using manual proof (see *GNAT prove and Manual Proof*), it may be more convenient to define some properties in the logical language of the prover rather than in SPARK. In that case, ghost functions might be marked as imported, so that no implementation is needed. For example, the ghost procedure Append\_To\_Log seen previously may be defined equivalently as a ghost imported function as follows:

```
function Append_To_Log (Log : Log_type; Incr : in Integer) return Log_Type with
   Ghost,
   Import;
```

where  $Log_Type$  is an Ada type used also as placeholder for a type in the logical language of the prover. To avoid any inconsistency between the interpretations of  $Log_Type$  in GNATprove and in the manual prover, it is preferable in such a case to mark the definition of  $Log_Type$  as not in SPARK, so that GNATprove does not make any assumptions on its content. This can be achieved by defining  $Log_Type$  as a private type and marking the private part of the enclosing package as not in SPARK:

```
package Logging with
    SPARK_Mode,
    Ghost
is
    type Log_Type is private;

function Append_To_Log (Log : Log_type; Incr : in Integer) return Log_Type with
    Import;

...

private
    pragma SPARK_Mode (Off);

    type Log_Type is new Integer; -- Any definition is fine here
end Logging;
```

A ghost imported subprogram cannot be executed, so calls to Append\_To\_Log above should not be enabled during compilation, otherwise a compilation error is issued. Note also that GNATprove will not attempt proving the contract of a ghost imported subprogram, as it does not have its body.

#### **Ghost Models**

When specifying a program, it is common to use a model, that is, an alternative, simpler view of a part of the program. As they are only used in annotations, models can be computed using ghost code.

### **Models of Control Flow**

Global variables can be used to enforce properties over call cahains in the program. For example, we may want to express that Total cannot be incremented twice in a row without registering the transaction in between. This can be done by introducing a ghost global variable Last\_Transaction\_Registered, used to encode whether Register\_Transaction was called since the last call to Add\_To\_Total:

```
Last_Transaction_Registered : Boolean := True with Ghost;

procedure Add_To_Total (Incr : Integer) with
   Pre => Last_Transaction_Registered,
   Post => not Last_Transaction_Registered;

procedure Register_Transaction with
   Post => Last_Transaction_Registered;
```

The value of Last\_Transaction\_Registered should also be updated in the body of Add\_To\_Total and Register\_Transaction to reflect their contracts:

```
procedure Add_To_Total (Incr : in Integer) is
begin
   Total := Total + Incr;
   Last_Transaction_Registered := False;
end Add_To_Total;
```

More generally, the expected control flow of a program can be modeled using an automaton. We can take as an example a mailbox containing only one message. The expected way Receive and Send should be interleaved can be expressed as a two state automaton. The mailbox can either be full, in which case Receive can be called but not Send, or it can be empty, in which case it is Send that can be called and not Receive. To express this property, we can define a ghost global variable of a ghost enumeration type to hold the state of the automaton:

```
type Mailbox_Status_Kind is (Empty, Full) with Ghost;
Mailbox_Status : Mailbox_Status_Kind := Empty with Ghost;

procedure Receive (X : out Message) with
   Pre => Mailbox_Status = Full,
   Post => Mailbox_Status = Empty;

procedure Send (X : Message) with
   Pre => Mailbox_Status = Empty,
   Post => Mailbox_Status = Full;
```

Like before, Receive and Send should update Mailbox\_Status in their bodies. Note that all the transitions of the automaton need not be specified, only the part which are relevant to the properties we want to express.

If the program also has some regular state, an invariant can be used to link the value of this state to the value of the ghost state of the automaton. For example, in our mailbox, we may have a regular variable Message\_Content holding the content of the current message, which is only known to be valid after a call to Send. We can introduce a ghost function linking the value of Message\_Content to the value of Mailbox\_Status, so that we can ensure that Message\_Content is always valid when accessed from Receive:

### **Models of Data Structures**

For specifying programs that use complex data structures (doubly-linked lists, maps...), it can be useful to supply a model for the data structure. A model is an alternative, simpler view of the data-structure which allows to write properties more easily. For example, a ring buffer, or a doubly-linked list, can be modeled using an array containing the elements from the buffer or the list in the right order. Typically, though simpler to reason with, the model is less efficient than the regular data structure. For example, inserting an element at the beginning of a doubly-linked list or at the beginning of a ring buffer can be done in constant time whereas inserting an element at the beginning of an array requires to slide all the elements to the right. As a result, models of data structures are usually supplied using ghost code. As an example, the package Ring\_Buffer offers an implementation of a single instance ring buffer. A ghost variable Buffer\_Model is used to write the specification of the Enqueue procedure:

```
package Ring_Buffer is
  function Get_Model return Nat_Array with Ghost;

procedure Enqueue (E : Natural) with
   Post => Get_Model = E & Get_Model'Old (1 .. Max - 1);

private
  Buffer_Content : Nat_Array;
  Buffer_Top : Natural;
  Buffer_Model : Nat_Array with Ghost;

function Get_Model return Nat_Array is (Buffer_Model);
end Ring_Buffer;
```

Then, just like for models of control flow, an invariant should be supplied to link the regular data structure to its model:

```
package Ring_Buffer is
 function Get_Model return Nat_Array with Ghost;
 function Invariant return Boolean with Ghost;
 procedure Enqueue (E : Natural) with
   Pre => Invariant,
   Post => Invariant and then Get_Model = E & Get_Model'Old (1 .. Max - 1);
private
 Buffer_Content : Nat_Array;
 Buffer_Top
                : Natural;
 Buffer_Model : Nat_Array with Ghost;
 function Get_Model return Nat_Array is (Buffer_Model);
 function Invariant return Boolean is
    (Buffer_Model = Buffer_Content (Buffer_Top .. Max)
                 & Buffer_Content (1 .. Buffer_Top - 1));
end Ring_Buffer;
```

If a data structure type is defined, a ghost function can be provided to compute a model for objects of the data structure type, and the invariant can be stated as a postcondition of this function:

```
package Ring_Buffer is
  type Buffer_Type is private;
  subtype Model_Type is Nat_Array with Ghost;
  function Invariant (X : Buffer_Type; M : Model_Type) return Boolean with
   Ghost:
  function Get_Model (X : Buffer_Type) return Model_Type with
   Ghost,
   Post => Invariant (X, Get_Model'Result);
  procedure Enqueue (X : in out Buffer_Type; E : Natural) with
   Post \Rightarrow Get_Model (X) = E & Get_Model (X) 'Old (1 .. Max - 1);
private
  type Buffer_Type is record
   Content : Nat_Array;
   Top
           : Natural;
  end record;
end Ring_Buffer;
```

More complex examples of models of data structure can be found in the Formal Containers Library.

#### **Removal of Ghost Code**

By default, GNAT completely discards ghost code during compilation, so that no ghost code is present in the object code or the executable. This ensures that, even if parts of the ghost could have side-effects when executed (writing to variables, performing system calls, raising exceptions, etc.), by default the compiler ensures that it cannot have any effect on the behavior of the program.

This is also essential in domains submitted to certification where all instructions in the object code should be traceable to source code and requirements, and where testing should ensure coverage of the object code. As ghost code is not present in the object code, there is no additional cost for maintaining its traceability and ensuring its coverage by tests.

GNAT provides an easy means to check that no ignored ghost code is present in a given object code or executable, which relies on the property that, by definition, each ghost declaration or ghost statement mentions at least one ghost entity. GNAT prefixes all names of such ignored ghost entities in the object code with the string \_\_\_\_ghost\_ (except for names of ghost compilation units). The initial triple underscore ensures that this substring cannot appear anywhere in the name of non-ghost entities or ghost entities that are not ignored. Thus, one only needs to check that the substring \_\_\_\_ghost\_ does not appear in the list of names from the object code or executable.

On Unix-like platforms, this can done by checking that the following command does not output anything:

```
nm <object files or executable> | grep ___ghost_
```

The same can be done to check that a ghost compilation unit called my\_unit (whatever the capitalization) is not included at all (entities in that unit would have been detected by the previous check) in the object code or executable. For example on Unix-like platforms:

nm <object files or executable> | grep my\_unit

# 5.6 Assertion Pragmas

SPARK contains features for directing formal verification with GNAT prove. These features may also be used by other tools, in particular the GNAT compiler. Assertion pragmas are refinements of pragma Assert defined in Ada. For all assertion pragmas, an exception Assertion\_Error is raised at run time when the property asserted does not hold, if the program was compiled with assertions. The real difference between assertion pragmas is how they are used by GNAT prove during proof.

### 5.6.1 Pragma Assert

[Ada 2005]

Pragma Assert is the simplest assertion pragma. GNATprove checks that the property asserted holds, and uses the information that it holds for analyzing code that follows. For example, consider two assertions of the same property X > 0 in procedure Assert\_Twice:

```
procedure Assert_Twice (X : Integer) with

SPARK_Mode

is

begin

pragma Assert (X > 0);

pragma Assert (X > 0);

end Assert_Twice;
```

As expected, the first assertion on line 5 is not provable in absence of a suitable precondition for Assert\_Twice, but GNATprove proves that it holds the second time the property is asserted on line 6:

```
assert_twice.adb:5:19: medium: assertion might fail, cannot prove X > 0 [possible_ →explanation: subprogram at line 1 should mention X in a precondition] assert_twice.adb:6:19: info: assertion proved
```

GNATprove considers that an execution of Assert\_Twice with X <= 0 stops at the first assertion that fails. Thus X > 0 when execution reaches the second assertion. This is true if assertions are executed at run time, but not if assertions are discarded during compilation. In the latter case, unproved assertions should be inspected carefully to ensure that the property asserted will indeed hold at run time. This is true of all assertion pragmas, which GNATprove analyzes like pragma Assert in that respect.

### 5.6.2 Pragma Assertion\_Policy

[Ada 2005/Ada 2012]

Assertions can be enabled either globally or locally. Here, *assertions* denote either *Assertion Pragmas* of all kinds (among which *Pragma Assert*) or functional contracts of all kinds (among which *Preconditions* and *Postconditions*).

By default, assertions are ignored in compilation, and can be enabled globally by using the compilation switch —gnata. They can be enabled locally by using pragma Assertion\_Policy in the program, or globally if the pragma is put in a configuration file. They can be enabled for all kinds of assertions or specific ones only by using the version of pragma Assertion Policy that takes named associations which was introduced in Ada 2012.

When used with the standard policies Check (for enabling assertions) or Ignore (for ignoring assertions), pragma Assertion\_Policy has no effect on GNATprove. GNATprove takes all assertions into account, whatever the assertion policy in effect at the point of the assertion. For example, consider a code with some assertions enabled and some ignored:

```
pragma Assertion_Policy (Pre => Check, Post => Ignore);
2
   procedure Assert_Enabled (X : in out Integer) with
3
4
     SPARK_Mode,
     Pre \Rightarrow X > 0,
                     -- executed at run time
5
     Post => X > 2
                     -- ignored at run time
6
   is
7
      pragma Assertion_Policy (Assert => Check);
      pragma Assert (X >= 0); -- executed at run time
      pragma Assertion_Policy (Assert => Ignore);
11
      pragma Assert (X >= 0); -- ignored at run time
12
   begin
13
      X := X - 1;
14
   end Assert_Enabled;
```

Although the postcondition and the second assertion are not executed at run time, GNATprove analyzes them and issues corresponding messages:

```
assert_enabled.adb:6:11: medium: postcondition might fail, cannot prove X > 2 (e.g. → when X = 0)
assert_enabled.adb:9:19: info: assertion proved
assert_enabled.adb:12:19: info: assertion proved
assert_enabled.adb:14:11: info: overflow check proved
```

On the contrary, when used with the GNAT-specific policy Disable, pragma Assertion\_Policy causes the corresponding assertions to be skipped both during execution and analysis with GNAT prove. For example, consider the same code as above where policy Ignore is replaced with policy Disable:

```
pragma Assertion_Policy (Pre => Check, Post => Disable);
1
2
   procedure Assert_Disabled (X : in out Integer) with
3
     SPARK_Mode,
     Pre \Rightarrow X > 0, -- executed at run time
     Post => X > 2
                     -- ignored at compile time and in analysis
      pragma Assertion_Policy (Assert => Check);
8
      pragma Assert (X >= 0); -- executed at run time
9
10
      pragma Assertion_Policy (Assert => Disable);
11
      pragma Assert (X \ge 0); -- ignored at compile time and in analysis
12
   begin
13
      X := X - 1;
14
   end Assert_Disabled;
```

On this program, GNATprove does not analyze the postcondition and the second assertion, and it does not issue corresponding messages:

```
assert_disabled.adb:9:19: info: assertion proved assert_disabled.adb:14:11: info: overflow check proved
```

The policy of Disable should thus be reserved for assertions that are not compilable, typically because a given build environment does not define the necessary entities.

## 5.6.3 Loop Invariants

#### [SPARK]

Pragma Loop\_Invariant is a special kind of assertion used in loops. GNATprove performs two checks that ensure that the property asserted holds at each iteration of the loop:

- 1. *loop invariant initialization*: GNATprove checks that the property asserted holds during the first iteration of the loop.
- 2. *loop invariant preservation*: GNATprove checks that the property asserted holds during an arbitrary iteration of the loop, assuming that it held in the previous iteration.

Each of these properties can be independently true or false. For example, in the following loop, the loop invariant is false during the first iteration and true in all remaining iterations:

```
Prop := False;
for J in 1 .. 10 loop

pragma Loop_Invariant (Prop);
Prop := True;
end loop;
```

Thus, GNATprove checks that property 2 holds but not property 1:

```
simple_loops.adb:8:30: info: loop invariant preservation proved simple_loops.adb:8:30: medium: loop invariant might fail in first iteration, cannot_ prove Prop (e.g. when Prop = False)
```

Conversely, in the following loop, the loop invariant is true during the first iteration and false in all remaining iterations:

```
Prop := True;
for J in 1 .. 10 loop
```

```
pragma Loop_Invariant (Prop);

Prop := False;
end loop;
```

Thus, GNATprove checks that property 1 holds but not property 2:

The following loop shows a case where the loop invariant holds both during the first iteration and all remaining iterations:

```
Prop := True;
for J in 1 .. 10 loop
pragma Loop_Invariant (Prop);
Prop := Prop;
end loop;
```

GNAT prove checks here that both properties 1 and 2 hold:

```
simple_loops.adb:20:30: info: loop invariant initialization proved simple_loops.adb:20:30: info: loop invariant preservation proved
```

In general, it is not sufficient that a loop invariant is true for GNATprove to prove it. The loop invariant should also be *inductive*: it should be precise enough that GNATprove can check loop invariant preservation by assuming *only* that the loop invariant held during the last iteration. For example, the following loop is the same as the previous one, except the loop invariant is true but not inductive:

```
Prop := True;
for J in 1 .. 10 loop
pragma Loop_Invariant (if J > 1 then Prop);
Prop := Prop;
end loop;
```

GNAT prove cannot check property 2 on that loop:

Note that using CodePeer static analysis allows here to fully prove the loop invariant, which is possible because CodePeer generates its own sound approximation of loop invariants (see *Using CodePeer Static Analysis* for details):

```
simple_loops_cdp.adb:26:30: info: loop invariant proved
```

Note also that not using an assertion (*Pragma Assert*) instead of a loop invariant also allows here to fully prove the corresponding property, by relying on *Automatic Unrolling of Simple For-Loops*:

```
simple_loops_unroll.adb:26:22: info: assertion proved
```

Returning to the case where neither automatic loop unrolling nor CodePeer are used, the reasoning of GNATprove for checking property 2 in that case can be summarized as follows:

- Let's take iteration K of the loop, where K > 1 (not the first iteration).
- Let's assume that the loop invariant held during iteration K-1, so we know that if K-1 > 1 then Prop holds.

- The previous assumption can be rewritten: if K > 2 then Prop.
- But all we know is that K > 1, so we cannot deduce Prop.

See How to Write Loop Invariants for further guidelines.

Pragma Loop\_Invariant may appear anywhere at the top level of a loop: it is usually added at the start of the loop, but it may be more convenient in some cases to add it at the end of the loop, or in the middle of the loop, in cases where this simplifies the asserted property. In all cases, GNATprove checks loop invariant preservation by reasoning on the virtual loop that starts and ends at the loop invariant.

It is possible to use multiple loop invariants, which should be grouped together without intervening statements or declarations. The resulting complete loop invariant is the conjunction of individual ones. The benefits of writing multiple loop invariants instead of a conjunction can be improved readability and better provability (because GNATprove checks each pragma Loop\_Invariant separately).

Finally, Attribute Loop\_Entry and Attribute Update can be very useful to express complex loop invariants.

**Note:** Users that are already familiar with the notion of loop invariant in other proof systems should be aware that loop invariants in SPARK are slightly different from the usual ones. In SPARK, a loop invariant must hold when execution reaches the corresponding pragma inside the loop. Hence, it needs not hold when the loop is never entered, or when exiting the loop.

## 5.6.4 Loop Variants

#### [SPARK]

Pragma Loop\_Variant is a special kind of assertion used in loops. GNATprove checks that the given scalar value decreases (or increases) at each iteration of the loop. Because a scalar value is always bounded by its type in Ada, it cannot decrease (or increase) at each iteration an infinite number of times, thus one of two outcomes is possible:

- 1. the loop exits, or
- 2. a run-time error occurs.

Therefore, it is possible to prove the termination of loops in SPARK programs by proving both a loop variant for each plain-loop or while-loop (for-loops always terminate in Ada) and the absence of run-time errors.

For example, the while-loops in procedure Terminating\_Loops compute the value of  $X - X \mod 3$  (or equivalently X / 3 \* 3) in variable Y:

```
procedure Terminating_Loops (X : Natural) with
     SPARK_Mode
2
   is
      Y : Natural;
   begin
      Y := 0;
6
      while X - Y >= 3 loop
         Y := Y + 3;
8
         pragma Loop_Variant (Increases => Y);
      end loop;
10
11
      Y := 0;
12
      while X - Y >= 3 loop
13
         Y := Y + 3;
14
         pragma Loop_Variant (Decreases => X - Y);
      end loop;
   end Terminating_Loops;
```

GNATprove is able to prove both loop variants, as well as absence of run-time errors in the subprogram, hence that loops terminate:

```
terminating_loops.adb:4:04: info: initialization of "Y" proved terminating_loops.adb:7:12: info: overflow check proved terminating_loops.adb:8:14: info: overflow check proved terminating_loops.adb:9:07: info: loop variant proved terminating_loops.adb:13:12: info: overflow check proved terminating_loops.adb:14:14: info: overflow check proved terminating_loops.adb:15:07: info: loop variant proved terminating_loops.adb:15:43: info: overflow check proved
```

Pragma Loop\_Variant may appear anywhere a loop invariant appears. It is also possible to use multiple loop variants, which should be grouped together with loop invariants. A loop variant may be more complex than a single decreasing (or increasing) value, and be given instead by a list of either decreasing or increasing values (possibly a mix of both). In that case, the order of the list defines the lexicographic order of progress. See SPARK RM 5.5.3 for details.

# 5.6.5 Pragma Assume

### [SPARK]

Pragma Assume is a variant of *Pragma Assert* that does not require GNATprove to check that the property holds. This is used to convey trustable information to GNATprove, in particular properties about external objects that GNATprove has no control upon. GNATprove uses the information that the assumed property holds for analyzing code that follows. For example, consider an assumption of the property X > 0 in procedure Assume\_Then\_Assert, followed by an assertion of the same property:

```
procedure Assume_Then_Assert (X : Integer) with

SPARK_Mode

is
begin

pragma Assume (X > 0);
pragma Assert (X > 0);
end Assume_Then_Assert;
```

As expected, GNATprove does not check the property on line 5, but used it to prove that the assertion holds on line 6:

```
assume_then_assert.adb:6:19: info: assertion proved
```

GNATprove considers that an execution of Assume\_Then\_Assert with X <= 0 stops at the assumption on line 5, and it does not issue a message in that case because the user explicitly indicated that this case is not possible. Thus X > 0 when execution reaches the assertion on line 6. This is true if assertions (of which assumptions are a special kind) are executed at run time, but not if assertions are discarded during compilation. In the latter case, assumptions should be inspected carefully to ensure that the property assumed will indeed hold at run time. This inspection may be facilitated by passing a justification string as the second argument to pragma Assume.

### 5.6.6 Pragma Assert\_And\_Cut

#### [SPARK]

Pragma Assert\_And\_Cut is a variant of *Pragma Assert* that allows hiding some information to GNATprove. GNATprove checks that the property asserted holds, and uses *only* the information that it holds for analyzing code that follows. For example, consider two assertions of the same property X = 1 in procedure Forgetful\_Assert, separated by a pragma Assert\_And\_Cut:

```
procedure Forgetful_Assert (X : out Integer) with
1
     SPARK_Mode
2
3
   is
   begin
      X := 1;
      pragma Assert (X = 1);
      pragma Assert_And_Cut (X > 0);
9
10
      pragma Assert (X > 0);
11
      pragma Assert (X = 1);
12
   end Forgetful_Assert;
13
```

GNAT prove proves that the assertion on line 7 holds, but it cannot prove that the same assertion on line 12 holds:

GNATprove *forgets* the exact value of X after line 9. All it knows is the information given in pragma Assert\_And\_Cut, here that X > 0. And indeed GNATprove proves that such an assertion holds on line 11. But it cannot prove the assertion on line 12, and the counterexample displayed mentions a possible value of 2 for X, showing indeed that GNATprove forgot its value of 1.

Pragma Assert\_And\_Cut may be useful in two cases:

- 1. When the automatic provers are overwhelmed with information from the context, pragma Assert\_And\_Cut may be used to simplify this context, thus leading to more automatic proofs.
- 2. When GNATprove is proving checks for each path through the subprogram (see switch --proof in *Running GNATprove from the Command Line*), and the number of paths is very large, pragma Assert\_And\_Cut may be used to reduce the number of paths, thus leading to faster automatic proofs.

For example, consider procedure P below, where all that is needed to prove that the code using X is free from run-time errors is that X is positive. Let's assume that we are running GNATprove with switch  $--proof=per\_path$  so that a formula is generated for each execution path. Without the pragma, GNATprove considers all execution paths through P, which may be many. With the pragma, GNATprove only considers the paths from the start of the procedure to the pragma, and the paths from the pragma to the end of the procedure, hence many fewer paths.

```
procedure P is
X : Integer;
begin
-- complex computation that sets X
pragma Assert_And_Cut (X > 0);
-- complex computation that uses X
end P;
```

### 5.7 Overflow Modes

Annotations such as preconditions, postconditions, assertions, loop invariants, are analyzed by GNATprove with the exact same meaning that they have during execution. In particular, evaluating the expressions in an annotation may

raise a run-time error, in which case GNAT prove will attempt to prove that this error cannot occur, and report a warning otherwise.

Integer overflows are a kind of run-time error that occurs when the result of an arithmetic computation does not fit in the bounds of the machine type used to hold the result. In some cases, it is convenient to express properties in annotations as they would be expressed in mathematics, where quantities are unbounded, for example:

```
function Add (X, Y : Integer) return Integer with

Pre => X + Y in Integer,
Post => Add'Result = X + Y;
```

The precondition of Add states that the result of adding its two parameters should fit in type Integer. In the default mode, evaluating this expression will fail an overflow check, because the result of X + Y is stored in a temporary of type Integer. If the compilation switch -gnato13 is used, then annotations are compiled specially, so that arithmetic operations use unbounded intermediate results. In this mode, GNATprove does not generate a check for the addition of X and Y in the precondition of Add, as there is no possible overflow here.

There are three overflow modes:

- Use base type for intermediate operations (STRICT): in this mode, all intermediate results for predefined arithmetic operators are computed using the base type, and the result must be in range of the base type.
- Most intermediate overflows avoided (MINIMIZED): in this mode, the compiler attempts to avoid intermediate overflows by using a larger integer type, typically Long\_Long\_Integer, as the type in which arithmetic is performed for predefined arithmetic operators.
- All intermediate overflows avoided (ELIMINATED): in this mode, the compiler avoids all intermediate overflows by using arbitrary precision arithmetic as required.

The desired mode for handling intermediate overflow can be specified using either the Overflow\_Mode pragma or an equivalent compiler switch. The pragma has the form:

```
pragma Overflow_Mode ([General =>] MODE [, [Assertions =>] MODE]);
```

where MODE is one of

- STRICT: intermediate overflows checked (using base type)
- MINIMIZED: minimize intermediate overflows
- ELIMINATED: eliminate intermediate overflows

For example:

```
pragma Overflow_Mode (General => Strict, Assertions => Eliminated);
```

specifies that general expressions outside assertions be evaluated in the usual strict mode, and expressions within assertions be evaluated in "eliminate intermediate overflows" mode. Currently, GNATprove only supports pragma Overflow\_Mode being specified in a configuration pragma file.

Additionally, a compiler switch -gnato?? can be used to control the checking mode default. Here ? is one of the digits I through 3:

- 1. use base type for intermediate operations (STRICT)
- 2. minimize intermediate overflows (MINIMIZED)
- 3. eliminate intermediate overflows (ELIMINATED)

The switch <code>-gnato13</code>, like the <code>Overflow\_Mode</code> pragma above, specifies that general expressions outside assertions be evaluated in the usual strict mode, and expressions within assertions be evaluated in "eliminate intermediate overflows" mode.

Note that these modes apply only to the evaluation of predefined arithmetic, membership, and comparison operators for signed integer arithmetic.

For further details of the meaning of these modes, and for further information about the treatment of overflows for fixed-point and floating-point arithmetic please refer to the "Overflow Check Handling in GNAT" appendix in the GNAT User's Guide.

# 5.8 Object Oriented Programming and Liskov Substitution Principle

SPARK supports safe Object Oriented Programming by checking behavioral subtyping between parent types and derived types, a.k.a. Liskov Substitution Principle: every overriding operation of the derived type should behave so that it can be substituted for the corresponding overridden operation of the parent type anywhere.

### 5.8.1 Class-Wide Subprogram Contracts

[Ada 2012]

Specific *Subprogram Contracts* are required on operations of tagged types, so that GNATprove can check Liskov Substitution Principle on every overriding operation:

- The class-wide precondition introduced by aspect Pre'Class is similar to the normal precondition.
- The class-wide postcondition introduced by aspect Post 'Class is similar to the normal postcondition.

Although these contracts are defined in Ada 2012, they have a stricter meaning in SPARK for checking Liskov Substitution Principle:

- The class-wide precondition of an overriding operation should be weaker (more permissive) than the class-wide precondition of the corresponding overridden operation.
- The class-wide postcondition of an overriding operation should be stronger (more restrictive) than the class-wide postcondition of the corresponding overridden operation.

For example, suppose that the Logging unit introduced in *Ghost Packages* defines a tagged type Log\_Type for logs, with corresponding operations:

```
package Logging with
     SPARK Mode
2
   is
3
      Max_Count : constant := 10_000;
4
5
      type Log_Count is range 0 .. Max_Count;
6
      type Log_Type is tagged private;
      function Log_Size (Log : Log_Type) return Log_Count;
10
11
      procedure Init_Log (Log : out Log_Type) with
12
        Post'Class => Log.Log_Size = 0;
13
14
      procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
15
        Pre'Class => Log.Log_Size < Max_Count,</pre>
16
        Post'Class => Log.Log_Size = Log.Log_Size'Old + 1;
17
   private
19
20
      subtype Log_Index is Log_Count range 1 .. Max_Count;
21
```

```
type Integer_Array is array (Log_Index) of Integer;
22
23
      type Log_Type is tagged record
24
         Log_Data : Integer_Array;
25
          Log_Size : Log_Count;
      end record;
27
28
      function Log_Size (Log : Log_Type) return Log_Count is (Log.Log_Size);
29
30
   end Logging;
31
```

and that this type is derived in Range\_Logging.Log\_Type which additionally keeps track of the minimum and maximum values in the log, so that they can be accessed in constant time:

```
with Logging; use type Logging.Log_Count;
2
   package Range_Logging with
     SPARK_Mode
   is
5
      type Log_Type is new Logging.Log_Type with private;
6
      not overriding
      function Log_Min (Log : Log_Type) return Integer;
10
      not overriding
11
      function Log_Max (Log : Log_Type) return Integer;
12
13
      overriding
14
      procedure Init_Log (Log : out Log_Type) with
15
        Post'Class => Log.Log_Size = 0 and
                       Log.Log_Min = Integer'Last and
17
                       Log.Log_Max = Integer'First;
18
19
      overriding
20
      procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
21
        Pre'Class => Log.Log_Size < Logging.Max_Count,</pre>
22
        Post'Class => Log.Log_Size = Log.Log_Size'Old + 1 and
23
                       Log.Log_Min = Integer'Min (Log.Log_Min'Old, Incr) and
24
                       Log.Log_Max = Integer'Max (Log.Log_Max'Old, Incr);
25
26
   private
27
28
      type Log_Type is new Logging.Log_Type with record
29
        Min_Entry : Integer;
30
        Max_Entry : Integer;
31
      end record;
32
33
      function Log_Min (Log : Log_Type) return Integer is (Log.Min_Entry);
34
      function Log_Max (Log : Log_Type) return Integer is (Log.Max_Entry);
   end Range_Logging;
```

GNATprove proves that the contracts on Logging. Append\_To\_Log and its overriding Range\_Logging. Append\_To\_Log respect the Liskov Substitution Principle:

```
range_logging.ads:16:20: info: class-wide postcondition is stronger than overridden_

→one

range_logging.ads:22:20: info: class-wide precondition is weaker than overridden one
```

```
range_logging.ads:23:20: info: class-wide postcondition is stronger than overridden_

→one
```

Units Logging and Range\_Logging need not be implemented, or available, or in SPARK. It is sufficient that the specification of Logging and Range\_Logging are in SPARK for this checking. Here, the postcondition of Range\_Logging.Append\_To\_Log is strictly stronger than the postcondition of Logging.Append\_To\_Log, as it also specifies the new expected value of the minimum and maximum values. The preconditions of both procedures are exactly the same, which is the most common case, but in other cases it might be useful to be more permissive in the overriding operation's precondition. For example, Range\_Logging.Append\_To\_Log could allocate dynamically additional memory for storing an unbounded number of events, instead of being limited to Max\_Count events like Logging.Append\_To\_Log, in which case its precondition would be simply True (the default precondition).

A derived type may inherit both from a parent type and from one or more interfaces, which only provide abstract operations and no components. GNATprove checks Liskov Substitution Principle on every overriding operation, both when the overridden operation is inherited from the parent type and when it is inherited from an interface.

GNATprove separately checks that a subprogram implements its class-wide contract, like for a specific contract.

## 5.8.2 Mixing Class-Wide and Specific Subprogram Contracts

[Ada 2012]

It is possible to specify both a specific contract and a class-wide contract on a subprogram, in order to use a more precise contract (the specific one) for non-dispatching calls and a contract compatible with the Liskov Substitution Principle (the class-wide contract) for dispatching calls. In that case, GNAT prove checks that:

- The specific precondition is weaker (more permissive) than the class-wide precondition.
- The specific postcondition is stronger (more restrictive) than the class-wide postcondition.

For example, Logging.Append\_To\_Log could set a boolean flag Special\_Value\_Logged when some Special\_Value is appended to the log, and express this property in its specific postcondition so that it is available for analyzing non-dispatching calls to the procedure:

This additional postcondition would play no role in dispatching calls, thus it is not involved in checking the Liskov Substitution Principle. Note that the absence of specific precondition on procedure Append\_To\_Log does not mean that the default precondition of True is used: as a class-wide precondition is specified on procedure Append\_To\_Log, it is also used as specific precondition. Similarly, if a procedure has a class-wide contract and a specific precondition, but no specific postcondition, then the class-wide postcondition is also used as specific postcondition.

When both a specific contract and a class-wide contract are specified on a subprogram, GNATprove only checks that the subprogram implements its specific (more precise) contract.

# **5.8.3 Dispatching Calls and Controlling Operands**

[Ada 2012]

In a dispatching call, the *controlling operand* is the parameter of class-wide type whose dynamic type determinates the actual subprogram called. The dynamic type of this controlling operand may be any type derived from the specific type corresponding to the class-wide type of the parameter (the specific type is T when the class-wide type is T'Class).

Thus, in general it is not possible to know in advance which subprograms may be called in a dispatching call, when separately analyzing a unit.

In SPARK, there is no need to know all possible subprograms called in order to analyze a dispatching call, which makes it possible for GNATprove to perform this analysis without knowledge of the whole program. As SPARK enforces Liskov Substitution Principle, the class-wide contract of an overriding operation is always less restrictive than the class-wide contract of the corresponding overridden operation. Thus, GNATprove uses the class-wide contract of the operation for the specific type of controlling operand to analyze a dispatching call.

For example, suppose a global variable The\_Log of class-wide type defines the log that should be used in the program:

```
The_Log : Logging.Log_Type'Class := ...
```

The call to Append\_To\_Log in procedure Add\_To\_Total may dynamically call either Logging. Append\_To\_Log or Range\_Logging.Append\_To\_Log:

```
procedure Add_To_Total (Incr : in Integer) is
begin
   Total := Total + Incr;
   The_Log.Append_To_Log (Incr);
end Add_To_Total;
```

Because GNATprove separately checks Liskov Substitution Principle for procedure Append\_To\_Log, it can use the class-wide contract of Logging.Append\_To\_Log for analyzing procedure Add\_To\_Total.

# 5.8.4 Dynamic Types and Invisible Components

#### [SPARK]

The *Data Initialization Policy* in SPARK applies specially to objects of tagged type. In general, the dynamic type of an object of tagged type may be different from its static type, hence the object may have invisible components, that are only revealed when the object is converted to a class-wide type.

For objects of tagged type, modes on parameters and data dependency contracts have a different meaning depending on the object's static type:

- For objects of a specific (not class-wide) tagged type, the constraints described in *Data Initialization Policy* apply to the visible components of the object only.
- For objects of a class-wide type, the constraints described in *Data Initialization Policy* apply to all components of the object, including invisible ones.

GNATprove checks during flow analysis that no uninitialized data is read in the program, and that the specified data dependencies and flow dependencies are respected in the implementation, based on the semantics above for objects of tagged type. For example, it detects no issues during flow analysis on procedure Use\_Logging which initializes parameter Log and then updates it:

```
with Logging; use Logging;

procedure Use_Logging (Log : out Log_Type) with

SPARK_Mode

is
begin
Log.Init_Log;
Log.Append_To_Log (1);
end Use_Logging;
```

If parameter Log is of dynamic type Logging. Log\_Type, then the call to Init\_Log initializes all components of Log as expected, and the call to Append\_To\_Log can safely read those. If parameter Log is of dynamic type

Range\_Logging.Log\_Type, then the call to Init\_Log only initializes those components of Log that come from the parent type Logging.Log\_Type, but since the call to Append\_To\_Log only read those, then there is no read of uninitialized data. This is in contrast with what occurs in procedure Use\_Logging\_Classwide:

```
with Logging; use Logging;

procedure Use_Logging_Classwide (Log : out Log_Type'Class) with

SPARK_Mode
is
begin
Log_Type (Log).Init_Log;
Log.Append_To_Log (2);
end Use_Logging_Classwide;
```

on which GNAT prove issues an error during flow analysis:

```
use_logging_classwide.adb:8:04: high: extension of "Log" is not initialized
```

Indeed, the call to Init\_Log (a non-dispatching call to Logging.Init\_Log due to the conversion on its parameter) only initializes those components of Log that come from the parent type Logging.Log\_Type, but the call to Append\_To\_Log may read other components from Range\_Logging.Log\_Type which may not be initialized.

A consequence of these rules for data initialization policy is that a parameter of a specific tagged type cannot be converted to a class-wide type, for example for a dispatching call. A special aspect <code>Extensions\_Visible</code> is defined in SPARK to allow this case. When <code>Extensions\_Visible</code> is specified on a subprogram, the data initialization policy for the subprogram parameters of a specific tagged type requires that the constraints described in <code>Data Initialization Policy</code> apply to all components of the object, as if the parameter was of a class-wide type. This allows converting this object to a class-wide type.

# 5.9 Concurrency and Ravenscar Profile

Concurrency in SPARK requires enabling the Ravenscar profile (see *Guide for the use of the Ada Ravenscar Profile in high integrity systems* by Alan Burns, Brian Dobbing, and Tullio Vardanega). This profile defines a subset of the Ada concurrency features suitable for hard real-time/embedded systems requiring stringent analysis, such as certification and safety analyses. In particular, it is concerned with determinism, analyzability, and memory-boundedness.

In addition to the subset defined by the Ravenscar profile, concurrency in SPARK also requires that tasks do not start executing before the program has been completely elaborated, which is expressed by setting pragma Partition\_Elaboration\_Policy to the value Sequential. Together with the requirement to apply the Ravenscar profile, this means that a concurrent SPARK program should define the following configuration pragmas, either in a configuration pragma file (see Setting the Default SPARK\_Mode for an example of defining a configuration pragma file in your project file) or at the start of files:

```
pragma Profile (Ravenscar);
pragma Partition_Elaboration_Policy (Sequential);
```

GNAT prove also supports the GNAT Extended Ravenscar profile (see Section 4.5 "The Extended Ravenscar Profiles" in GNAT User's Guide Supplement for GNAT Pro Safety-Critical and GNAT Pro High-Security). To use the GNAT Extended Ravenscar profile simply replace Ravenscar with GNAT\_Extended\_Ravenscar in the pragma Profile in the above code. The extended profile is intended for hard real-time/embedded systems that may require schedulability analysis but not the most stringent analyses required for other domains.

In particular, to increase expressive power the GNAT Extended Ravenscar profile relaxes certain restrictions defined by the standard Ravenscar profile. Notably, these relaxed constraints allow multiple protected entries per protected object, multiple queued callers per entry, and more expressive protected entry barrier expressions. The profile also allows the use of relative delay statements in addition to the absolute delay statements allowed by Ravenscar. The two forms of delay statement are processed by GNATprove based on the type of their expression, as follows (absolute and relative delays, respectively):

- If the expression is of the type Ada.Real\_Time.Time then for the purposes of determining global inputs and outputs the absolute delay statement is considered just like the relative delay statement, i.e., to reference the state abstraction Ada.Real\_Time.Clock\_Time as an input (see SPARK RM 9(17) for details).
- If the expression is of the type Ada.Calendar.Time then it is considered to reference the state abstraction Ada.Calendar.Clock\_Time, which is defined similarly to Ada.Real\_Time.Clock\_Time but represents a different time base.

#### 5.9.1 Tasks and Data Races

#### [Ravenscar]

Concurrent Ada programs are made of several *tasks*, that is, separate threads of control which share the same address space. In Ravenscar, only library-level, nonterminating tasks are allowed.

### **Task Types and Task Objects**

Like ordinary objects, tasks have a type in Ada and can be stored in composite objects such as arrays and records. The definition of a task type looks like the definition of a subprogram. It is made of two parts: a declaration, usually empty as Ravenscar does not allow tasks to have entries (for task rendezvous), and a body containing the list of statements to be executed by objects of the task type. The body of nonterminating tasks (the only ones allowed in Ravenscar) usually takes the form of an infinite loop. For task objects of a given type to be parameterized, task types can have discriminants. As an example, a task type Account\_Management can be declared as follows:

Then, tasks of type Account\_Management can be created at library level, either as complete objects or as components of other objects:

```
package Bank is
    Special_Accounts : Account_Management;

    type Account_Type is (Regular, Premium, Selective);
    type Account_Array is array (Account_Type) of Account_Management;
    All_Accounts : Account_Array;
end Bank;
```

If only one object of a given task type is needed, then the task object can be declared directly giving a declaration and a body. An anonymous task type is then defined implicitly for the declared type object. For example, if we only need one task Account\_Management then we can write:

```
package Account is
   Num_Accounts : Natural := 0;

   task Account_Management;
end Account;

package body Account is

  task body Account_Management is
  begin
   loop
      Get_Next_Account_Created;
      Num_Accounts := Num_Accounts + 1;
  end loop;
  end Account_Management;
end Account;
```

### **Preventing Data Races**

In Ravenscar, communication between tasks can only be done through shared objects (tasks cannot communicate through rendezvous as task entries are not allowed in Ravenscar). In SPARK, the language is further restricted to avoid the possibility of erroneous concurrent access to shared data (a.k.a. data races). More precisely, tasks can only share *synchronized* objects, that is, objects that are protected against concurrent accesses. These include atomic objects, protected objects (see *Protected Objects and Deadlocks*), and suspension objects (see *Suspension Objects*). As an example, our previous definition of the Account\_Management task type was not in SPARK. Indeed, data races could occur when accessing the global variable Num\_Accounts, as detected by GNATprove:

```
bank1.ads:5:04: high: possible data race when accessing variable "account1.num_ 

accounts"

bank1.ads:5:04: high: with task "bank1.all_accounts"

bank1.ads:5:04: high: with task "bank1.special_accounts"
```

To avoid this problem, shared variable Num\_Account can be declared atomic:

```
package Account is
   Num_Accounts : Natural := 0 with Atomic;

task type Account_Management;
end Account;
```

With this modification, GNATprove now alerts us that the increment of Num\_Account is not legal, as a volatile variable (which is the case of atomic variables) cannot be read as a subexpression of a larger expression in SPARK:

```
account2.adb:15:26: volatile object cannot appear in this context (SPARK RM 7.1.3(12))
```

This can be fixed by copying the current value of Num\_Account in a temporary before the increment:

```
declare
   Tmp : constant Natural := Num_Accounts;
begin
```

```
Num_Accounts := Tmp + 1;
end;
```

But note that even with that fix, there is no guarantee that Num\_Accounts is incremented by one each time an account is created. Indeed, two tasks may read the same value of Num\_Accounts and store this value in Tmp before both updating it to Tmp + 1. In such a case, two accounts have been created but Num\_Accounts has been increased by 1 only. There is no *data race* in this program, which is confirmed by running GNATprove with no error, but there is by design a *race condition* on shared data that causes the program to malfunction. The correct way to fix this in SPARK is to use *Protected Types and Protected Objects*.

As they cannot cause data races, constants and variables that are constant after elaboration (see *Aspect Constant\_After\_Elaboration*) are considered as synchronized and can be accessed by multiple tasks. For example, we can declare a global constant Max\_Accounts and use it inside Account\_Management without risking data races:

```
package Account is
   Num_Accounts : Natural := 0 with Atomic;
  Max_Accounts : constant Natural := 100;
   task type Account_Management;
end Account;
package body Account is
   task body Account_Management is
  begin
      loop
         Get_Next_Account_Created;
         declare
            Tmp : constant Natural := Num_Accounts;
            if Tmp < Max_Accounts then</pre>
               Num_Accounts := Tmp + 1;
            end if;
         end:
      end loop;
   end Account_Management;
end Account;
```

It is possible for a task to access an unsynchronized global variable only if this variable is declared in the same package as the task and if there is a single task accessing this variable. To allow this property to be statically verified, only tasks of an anonymous task type are allowed to access unsynchronized variables and the variables accessed should be declared to belong to the task using aspect Part\_Of. Global variables declared to belong to a task are handled just like local variables of the task, that is, they can only be referenced from inside the task body. As an example, we can state that Num\_Accounts is only accessed by the task object Account\_Management in the following way:

```
package Account is
   task Account_Management;

Num_Accounts : Natural := 0 with Part_Of => Account_Management;
end Account;
```

#### 5.9.2 Task Contracts

[SPARK]

Dependency contracts can be specified on tasks. As tasks should not terminate in SPARK, such contracts specify the dependencies between outputs and inputs of the task *updated while the task runs*:

- The data dependencies introduced by aspect Global specify the global data read and written by the task.
- The flow dependencies introduced by aspect Depends specify how task outputs depend on task inputs.

This is a difference between tasks and subprograms, for which such contracts describe the dependencies between outputs and inputs when the subprogram returns.

### **Data Dependencies**

Data dependencies on tasks follow the same syntax as the ones on subprograms (see *Data Dependencies*). For example, data dependencies can be specified for task (type or object) Account\_Management as follows:

```
package Account is
   Num_Accounts : Natural := 0 with Atomic;

task type Account_Management with
   Global => (In_Out => Num_Accounts);
end Account;
```

### **Flow Dependencies**

Flow dependencies on tasks follow the same syntax as the ones on subprograms (see *Flow Dependencies*). For example, flow dependencies can be specified for task (type or object) Account\_Management as follows:

Notice that the task unit itself is both an input and an output of the task:

- It is an input because task discriminants (if any) and task attributes may be read in the task body.
- It is an output so that the task unit may be passed as in out parameter in a subprogram call. But note that the task object cannot be modified once created.

The dependency of the task on itself can be left implicit as well, as follows:

```
package Account is
   Num_Accounts : Natural := 0 with Atomic;

task type Account_Management with
   Depends => (Num_Accounts => Num_Accounts);
end Account;
```

### 5.9.3 Protected Objects and Deadlocks

#### [Ravenscar]

In Ada, protected objects are used to encapsulate shared data and protect it against data races (low-level unprotected concurrent access to data) and race conditions (lack of proper synchronization between reads and writes of shared

data). They coordinate access to the protected data guaranteeing that read-write accesses are always exclusive while allowing concurrent read-only accesses. In Ravenscar, only library-level protected objects are allowed.

### **Protected Types and Protected Objects**

Definitions of protected types resemble package definitions. They are made of two parts, a declaration (divided into a public part and a private part) and a body. The public part of a protected type's declaration contains the declarations of the subprograms that can be used to access the data declared in its private part. The body of these subprograms are located in the protected type's body. In Ravenscar, protected objects should be declared at library level, either as complete objects or as components of other objects. As an example, here is how a protected type can be used to coordinate concurrent accesses to the global variable Num\_Accounts:

```
package Account is
   protected type Protected_Natural is
      procedure Incr;
      function Get return Natural;
   private
      The_Data : Natural := 0;
   end Protected_Natural;
  Num_Accounts : Protected_Natural;
   Max_Accounts : constant Natural := 100;
   task type Account_Management;
end Account;
package body Account is
   protected body Protected_Natural is
     procedure Incr is
        The_Data := The_Data + 1;
      end Incr:
      function Get return Natural is (The_Data);
   end Protected_Natural;
   task body Account_Management is
   begin
      loop
         Get_Next_Account_Created;
         if Num_Accounts.Get < Max_Accounts then</pre>
            Num_Accounts.Incr;
         end if;
      end loop;
   end Account_Management;
end Account;
```

Contrary to the previous version using an atomic global variable (see *Preventing Data Races*), this version prevents also any race condition when incrementing the value of Num\_Accounts. But note that there is still a possible race condition between the time the value of Num\_Accounts is read and checked to be less than Max\_Accounts and the time it is incremented. So this version does not guarantee that Num\_Accounts stays below Max\_Accounts. The correct way to fix this in SPARK is to use protected entries (see *Protected Subprograms*).

Note that, in SPARK, to avoid initialization issues on protected objects, both private variables and variables belonging

to a protected object must be initialized at declaration (either explicitly or through default initialization).

Just like for tasks, it is possible to directly declare a protected object if it is the only one of its type. In this case, an anonymous protected type is implicitly declared for it. For example, if Num\_Account is the only Protected\_Natural we need, we can directly declare:

```
package Account is
   protected Num_Accounts is
      procedure Incr;
      function Get return Natural;
   private
      The_Data : Natural := 0;
   end Num_Accounts;
end Account;
package body Account is
  protected body Num_Accounts is
      procedure Incr is
     begin
         The_Data := The_Data + 1;
      end Incr;
      function Get return Natural is (The_Data);
   end Num_Accounts;
end Account;
```

### **Protected Subprograms**

The access mode granted by protected subprograms depends on their kind:

- Protected procedures provide exclusive read-write access to the private data of a protected object.
- Protected functions offer concurrent read-only access to the private data of a protected object.
- Protected *entries* are conceptually procedures with a *barrier*. When an entry is called, the caller waits until the condition of the barrier is true to be able to access the protected object.

So that scheduling is deterministic, Ravenscar requires that at most one entry is specified in a protected unit and at most one task is waiting on a given entry at every time. To ensure this, GNATprove checks that no two tasks can call the same protected object's entry. As an example, we could replace the procedure Incr of Protected\_Natural to wait until The\_Data is smaller than Max\_Accounts before incrementing it. As only simple Boolean variables are allowed as entry barriers in Ravenscar, we add such a Boolean flag Not\_Full as a component of the protected object:

```
package Account is

protected type Protected_Natural is
entry Incr;
function Get return Natural;
private
   The_Data: Natural := 0;
   Not_Full: Boolean:= True;
end Protected_Natural;
```

```
Num_Accounts : Protected_Natural;
  Max Accounts : constant Natural := 100;
   task type Account_Management;
end Account;
package body Account is
  protected body Protected_Natural is
      entry Incr when Not_Full is
     begin
         The_Data := The_Data + 1;
         if The_Data = Max_Accounts then
            Not_Full := False;
         end if;
      end Incr;
      function Get return Natural is (The_Data);
   end Protected_Natural;
   task body Account_Management is
  begin
      loop
         Get_Next_Account_Created;
        Num_Accounts.Incr;
      end loop;
   end Account_Management;
end Account;
```

This version fixes the remaining race condition on this example, thus ensuring that every new account created bumps the value of Num\_Accounts by 1, and that Num\_Accounts stays below Max\_Accounts.

To avoid data races, protected subprograms should not access unsynchronized objects (see *Tasks and Data Races*). Like for tasks, it is still possible for subprograms of a protected object of an anonymous protected type to access an unsynchronized object declared in the same package as long as it is not accessed by any task or subprogram from other protected objects. In this case, the unsynchronized object should have a Part\_Of aspect referring to the protected object. It is then handled as if it was a private variable of the protected object. This is typically done so that the address in memory of the variable can be specified, using either aspect Address or a corresponding representation clause. Here is how this could be done with Num\_Account:

```
package Account is
    protected Protected_Num_Accounts is
    procedure Incr;
    function Get return Natural;
end Protected_Num_Accounts;

Num_Accounts: Natural := 0 with
    Part_Of => Protected_Num_Accounts,
    Address => ...
end Account;
```

As it can prevent access to a protected object for an unbounded amount of time, a task should not be blocked or delayed while inside a protected subprogram. Actions that can block a task are said to be *potentially blocking*. For example, calling a protected entry, explicitly waiting using a delay\_until statement (note that delay statements are forbidden in Ravenscar), or suspending on a suspension object (see *Suspension Objects*) are potentially blocking actions. In Ada, it is an error to do a potentially blocking action while inside a protected subprogram. Note that a call

to a function or a procedure on another protected object is not considered to be potentially blocking. Indeed, such a call cannot block a task in the absence of deadlocks (which is enforced in Ravenscar using the priority ceiling protocol, see *Avoiding Deadlocks and Priority Ceiling Protocol*).

GNATprove verifies that no potentially blocking action is performed from inside a protected subprogram in a modular way on a per subprogram basis. Thus, if a subprogram can perform a potentially blocking operation, every call to this subprogram from inside a protected subprogram will be flagged as a potential error. As an example, the procedure Incr\_Num\_Accounts is potentially blocking and thus should not be called, directly or indirectly, from a protected subprogram:

```
package Account is

   protected type Protected_Natural is
        entry Incr;
   private
        The_Data : Natural := 0;
   end Protected_Natural;

   Num_Accounts : Protected_Natural;

   procedure Incr_Num_Accounts;

end Account;

package body Account is

   procedure Incr_Num_Accounts is
   begin
        Num_Accounts.Incr;
   end Incr_Num_Accounts;

end Account;
```

### **Avoiding Deadlocks and Priority Ceiling Protocol**

To ensure exclusivity of read-write accesses, when a procedure or an entry of a protected object is called, the protected object is locked so that no other task can access it, be it in a read-write or a read-only mode. In the same way, when a protected function is called, no other task can access the protected object in read-write mode. A *deadlock* happens when two or more tasks are unable to run because each of them is trying to access a protected object that is currently locked by another task.

To ensure absence of deadlocks on a single core, Ravenscar requires the use of the Priority Ceiling Protocol. This protocol ensures that no task can be blocked trying to access a protected object locked by another task. It relies on task's *priorities*. The priority of a task is a number encoding its urgency. On a single core, scheduling ensures that the current running task can only be preempted by another task if it has a higher priority. Using this property, the Priority Ceiling Protocol works by increasing the priorities of tasks accessing a protected object to a priority that is at least as high as the priorities of other tasks accessing this object. This ensures that, while holding a lock, the currently running task cannot be preempted by a task which could later be blocked by this lock.

To enforce this protocol, every task is associated with a *base priority*, either given at declaration using the Priority aspect or defaulted. This base priority is static and cannot be modified after the task's declaration. A task also has an *active priority* which is initially the task's base priority but will be increased when the task enters a protected action. For example, we can set the base priority of Account\_Management to 5 at declaration:

```
package Account is
   task type Account_Management with Priority => 5;
end Account;
```

Likewise, each protected object is associated at declaration with a *ceiling priority* which should be equal or higher than the active priority of any task accessing it. The ceiling priority of a protected object does not need to be static, it can be set using a discriminant for example. Still, like for tasks, Ravenscar requires that it is set once and for all at the object's declaration and cannot be changed afterwards. As an example, let us attach a ceiling priority to the protected object Num\_Accounts. As Num\_Accounts will be used by Account\_Management, its ceiling priority should be no lower than 5:

```
package Account is

protected Num_Accounts with Priority => 7 is
    procedure Incr;
    function Get return Natural;
private
    The_Data : Natural := 0;
end Num_Accounts;

task type Account_Management with Priority => 5;
end Account;
```

# 5.9.4 Suspension Objects

#### [Ravenscar]

The language-defined package Ada. Synchronous\_Task\_Control provides a type for semaphores called suspension objects. They allow lighter synchronization mechanisms than protected objects (see Protected Objects and Deadlocks). More precisely, a suspension object has a Boolean state which can be set atomically to True using the Set\_True procedure. When a task suspends on a suspension object calling the Suspend\_Until\_True procedure, it is blocked until the state of the suspension object is True. At that point, the state of the suspension object is set back to False and the task is unblocked. Note that Suspend\_Until\_True is potentially blocking and therefore should not be called directly or indirectly from within Protected Subprograms. In the following example, the suspension object Semaphore is used to make sure T1 has initialized the shared data by the time T2 begins processing it:

```
Semaphore : Suspension_Object;
task T1;
task T2;
task body T1 is
begin
  Initialize_Shared_Data;
  Set_True (Semaphore);
  loop
  end loop;
end T1;
task body T2 is
begin
  Suspend_Until_True (Semaphore);
  loop
  end loop;
end T2;
```

In Ada, an exception is raised if a task tries to suspend on a suspension object on which another task is already waiting on that same suspension object. Like for verifying that no two tasks can be queued on a protected entry, this verification is done by GNATprove by checking that no two tasks ever suspend on the same suspension object. In the following example, the suspension objects Semaphorel and Semaphore2 are used to ensure that T1 and T2 never call Enter\_Protected\_Region at the same time. GNATprove will successfully verify that only one task can suspend on each suspension object:

```
Semaphore1, Semaphore2: Suspension_Object;
task T1;
task T2;
task body T1 is
begin
  loop
    Suspend_Until_True (Semaphore1);
   Enter_Protected_Region;
    Set_True (Semaphore2);
  end loop;
end T1;
task body T2 is
begin
  loop
    Suspend_Until_True (Semaphore2);
   Enter_Protected_Region;
    Set_True (Semaphore1);
  end loop;
end T2;
```

# 5.9.5 State Abstraction and Concurrency

#### [SPARK]

Protected objects, as well as suspension objects, are *effectively volatile* which means that their value as seen from a given task may change at any time due to some other task accessing the protected object or suspension object. If they are part of a state abstraction, the volatility of the abstract state must be specified by using the <code>External</code> aspect (see *External State Abstraction*). Note that task objects, though they can be part of a package's hidden state, are not effectively volatile and can therefore be components of normal state abstractions. For example, the package <code>Synchronous\_Abstractions</code> defines two abstract states, one for external objects, containing the atomic variable V, the suspension object S, and the protected object P, and one for normal objects, containing the task T:

```
package Synchronous_Abstractions with
   Abstract_State => (Normal_State, (Synchronous_State with External))
is
end Synchronous_Abstractions;

package body Synchronous_Abstractions with
   Refined_State => (Synchronous_State => (P,V,S), Normal_State => T)
is
   task T;
S : Suspension_Object;
V : Natural := 0 with Atomic, Async_Readers, Async_Writers;
protected P is
```

```
function Read return Natural;
private
   V : Natural := 0;
end P;

protected body P is
   function Read return Natural is (V);
end P;

task body T is ...
end Synchronous_Abstractions;
```

To avoid data races, task bodies, as well as protected subprograms, should only access synchronized objects (see *Preventing Data Races*). State abstractions containing only synchronized objects can be specified to be synchronized using the Synchronous aspect. Only synchronized state abstractions can be accessed from task bodies and protected subprograms. For example, if we want the procedure Do\_Something to be callable from the task Use\_Synchronized\_State, then the state abstraction Synchronous\_State must be annotated using the Synchronous aspect:

# 5.9.6 Project-wide Tasking Analysis

Tasking-related analysis, as currently implemented in GNATprove, is subject to two limitations:

First, the analysis is always done when processing a source file with task objects or with a subprogram that can be used as a main subprogram of a partition (i.e. is at library level, has no parameters, and is either a procedure or a function returning an integer type).

In effect, you might get spurious checks when:

- a subprogram satisfies conditions for being used as a main subprogram of a partition but is not really used that way, i.e. it is not specified in the Main attribute of the GNAT project file you use to build executables, and
- it "withs" or is "withed" (directly or indirectly) from a library-level package that declares some task object, and
- both the fake "main" subprogram and the task object access the same resource in a way that violates tasking-related rules (e.g. suspends on the same suspension object).

As a workaround, either wrap the fake "main" subprogram in a library-level package or give it a dummy parameter.

Second, the analysis is only done in the context of all the units "withed" (directly and indirectly) by the currently analyzed source file.

In effect, you might miss checks when:

- building a library that declares tasks objects in unrelated source files, i.e. files that are never "withed" (directly or indirectly) from the same file, and those tasks objects access the same resource in a way that violates tasking-related rules, or
- using a library that internally declares some tasks objects, they access some tasking-sensitive resource, and your main subprogram also accesses this resource.

As a workaround, when building library projects add a dummy main subprogram that "withs" all the library-level packages of your project.

# 5.9.7 Interrupt Handlers

SPARK puts no restrictions on the Ada interrupt handling and GNATprove merely checks that interrupt handlers will be safely executed. In Ada interrupts handlers are defined by annotating protected procedures, for example:

```
with Ada.Interrupts.Names; use Ada.Interrupts.Names;
protected P is
    procedure Signal with Attach_Handler => SIGINT;
end P;
```

Currently GNATprove emits a check for each handler declaration saying that the corresponding interrupt might be already reserved. In particular, it might be reserved by either the system or the Ada runtime; see GNAT pragmas Interrupt\_State and Unreserve\_All\_Interrupts for details. Once examined, those checks can be suppressed with pragma Annotate.

If pragma Priority or Interrupt\_Priority is explicitly specified for a protected type, then GNATprove will check that its value is in the range of the System.Any\_Priority or System.Interrupt\_Priority, respectively; see Ada RM D.3(6.1/3).

For interrupt handlers whose bodies are annotated with SPARK\_Mode => On, GNATprove will additionally check that:

- the interrupt handler does not call (directly or indirectly) the Ada.Task\_Identification.Current\_Task routine, which might cause a Program\_Error runtime exception; see Ada RM C.7.1(17/3);
- all global objects read (either as an Input or a Proof\_In) by the interrupt handler are initialized at elaboration;
- there are no unsynchronized objects accessed both by the interrupt handler and by some task (or by some other interrupt handler);
- there are no protected objects locked both by the interrupt handler and by some task (or by some other interrupt handler).

# 5.10 SPARK Libraries

### 5.10.1 Functional Containers Library

To model complex data structures, one often needs simpler, mathematical like containers. The mathematical containers provided in the SPARK library are unbounded and may contain indefinite elements. Furthermore, to be usable in every context, they are neither controlled nor limited. So that these containers can be used safely, we have made them functional, that is, no primitives are provided which would allow modifying an existing container. Instead, their API features functions creating new containers from existing ones. As an example, functional containers provide no Insert procedure but rather a function Add which creates a new container with one more element than its parameter:

```
function Add (C : Container; E : Element_Type) return Container;
```

As a consequence, these containers are highly inefficient. They are also memory consuming as the allocated memory is not reclaimed when the container is no longer referenced. Thus, they should in general be used in ghost code and annotations so that they can be removed from the final executable.

There are 3 functional containers, which are part of the GNAT standard library:

- Ada.Containers.Functional\_Maps
- Ada.Containers.Functional\_Sets
- Ada. Containers. Functional Vectors

Sequences defined in Functional\_Vectors are no more than ordered collections of elements. In an Ada like manner, the user can choose the range used to index the elements:

```
function Length (S : Sequence) return Count_Type;
function Get (S : Sequence; N : Index_Type) return Element_Type;
```

Functional sets offer standard mathematical set functionalities such as inclusion, union, and intersection. They are neither ordered nor hashed:

```
function Contains (S : Set; E : Element_Type) return Boolean;
function "<=" (Left : Set; Right : Set) return Boolean;</pre>
```

Functional maps offer a dictionary between any two types of elements:

```
function Has_Key (M : Map; K : Key_Type) return Boolean;
function Get (M : Map; K : Key_Type) return Element_Type;
```

Each functional container type supports iteration as appropriate, so that its elements can easily be quantified over.

These containers can easily be used to model user defined data structures. They were used to this end to annotate and verify a package of allocators (see *allocators* example in the *Examples in the Toolset Distribution*). In this example, an allocator featuring a free list implemented in an array is modeled by a record containing a set of allocated resources and a sequence of available resources:

```
type Status is (Available, Allocated);
type Cell is record
   Stat : Status;
   Next : Resource;
end record;
type Allocator is array (Valid_Resource) of Cell;
type Model is record
   Available : Sequence;
   Allocated : Set;
end record;
```

**Note:** Functional sets and maps represent elements modulo equivalence. For proof, the range of quantification over their content includes all elements that are equivalent to elements included in the container. On the other hand, for execution, the iteration is only done on elements which have actually been included in the container. This difference may make interaction between test and proof tricky when the equivalence relation is not the equality.

# **5.10.2 Formal Containers Library**

Containers are generic data structures offering a high-level view of collections of objects, while guaranteeing fast access to their content to retrieve or modify it. The most common containers are lists, vectors, sets and maps, which

are defined as generic units in the Ada Standard Library. In critical software where verification objectives severely restrict the use of pointers, containers offer an attractive alternative to pointer-intensive data structures.

The Ada Standard Library defines two kinds of containers:

- The controlled containers using dynamic allocation, for example Ada.Containers.Vectors. They define containers as controlled tagged types, so that memory for the container is automatic reallocated during assignment and automatically freed when the container object's scope ends.
- The bounded containers not using dynamic allocation, for example Ada.Containers. Bounded\_Vectors. They define containers as discriminated tagged types, so that the memory for the container can be reserved at initialization.

Although bounded containers are better suited to critical software development, neither controlled containers nor bounded containers can be used in SPARK, because their API does not lend itself to adding suitable contracts (in particular preconditions) ensuring correct usage in client code.

The formal containers are a variation of the bounded containers with API changes that allow adding suitable contracts, so that GNATprove can prove that client code manipulates containers correctly. There are 7 formal containers, which are part of the GNAT standard library:

- Ada.Containers.Formal\_Vectors
- Ada.Containers.Formal\_Indefinite\_Vectors
- Ada.Containers.Formal\_Doubly\_Linked\_Lists
- Ada.Containers.Formal\_Hashed\_Sets
- Ada.Containers.Formal Ordered Sets
- Ada.Containers.Formal\_Hashed\_Maps
- Ada.Containers.Formal\_Ordered\_Maps

Lists, sets and maps can only be used with definite objects (objects for which the compiler can compute the size in memory, hence not String nor T'Class). Vectors come in two flavors for definite objects (Formal\_Vectors) and indefinite objects (Formal\_Indefinite\_Vectors).

Lists, sets, maps, and definite vectors are always bounded. Indefinite vectors can be bounded or unbounded depending on the value of the formal parameter Bounded when instantiating the generic unit. Bounded containers do not use dynamic allocation. Unbounded vectors use dynamic allocation to expand their internal block of memory.

### **Modified API of Formal Containers**

The visible specification of formal containers is in SPARK, with suitable contracts on subprograms to ensure correct usage, while their private part and implementation is not in SPARK. Hence, GNAT prove can be used to prove correct usage of formal containers in client code, but not to prove that formal containers implement their specification.

Procedures Update\_Element or Query\_Element that iterate over a container are not defined on formal containers. Specification and analysis of such procedures that take an access-to-procedure in parameter is beyond the capabilities of SPARK and GNATprove. See *Excluded Ada Features*.

Procedures and functions that query the content of a container take the container in parameter. For example, function Has\_Element that queries if a container has an element at a given position is declared as follows:

```
function Has_Element (Container : T; Position : Cursor) return Boolean;
```

This is different from the API of controlled containers and bounded containers, where it is sufficient to pass a cursor to these subprograms, as the cursor holds a reference to the underlying container:

```
function Has_Element (Position : Cursor) return Boolean;
```

Cursors of formal containers do not hold a reference to a specific container, as this would otherwise introduce aliasing between container and cursor variables, which is not supported in SPARK. See *Absence of Interferences*. As a result, the same cursor can be applied to multiple container objects.

For each container type, the library provides model functions that are used to annotate subprograms from the API. The different models supply different levels of abstraction of the container's functionalities. These model functions are grouped in *Ghost Packages* named Formal\_Model.

The higher level view of a container is usually the mathematical structure of element it represents. We use a sequence for ordered containers such as lists and vectors and a mathematical map for imperative maps. This allows us to specify the effects of a subprogram in a very high level way, not having to consider cursors nor order of elements in a map:

```
procedure Increment_All (L : in out List) with
  Post =>
    (for all N in 1 .. Length (L) =>
        Element (Model (L), N) = Element (Model (L)'Old, N) + 1);

procedure Increment_All (S : in out Map) with
  Post =>
    (for all K of Model (S)'Old => Has_Key (Model (S), K))
        and
    (for all K of Model (S) =>
        Has_Key (Model (S)'Old, K)
        and Get (Model (S), K) = Get (Model (S)'Old, K) + 1);
```

For sets and maps, there is a lower level model representing the underlying order used for iteration in the container, as well as the actual values of elements/keys. It is a sequence of elements/keys. We can use it if we want to specify in Increment\_All on maps that the order and actual values of keys are preserved:

```
procedure Increment_All (S : in out Map) with
Post =>
   Keys (S) = Keys (S)'Old
   and
   (for all K of Model (S) =>
      Get (Model (S), K) = Get (Model (S)'Old, K) + 1);
```

Finally, cursors are modeled using a functional map linking them to their position in the container. For example, we can state that the positions of cursors in a list are not modified by a call to Increment\_All:

```
procedure Increment_All (L : in out List) with
Post =>
  Positions (L) = Positions (L)'Old
  and
  (for all N in 1 .. Length (L) =>
      Element (Model (L), N) = Element (Model (L)'Old, N) + 1);
```

Switching between the different levels of model functions allows to express precise considerations when needed without polluting upper level specifications. For example, consider a variant of the List.Find function defined in the API of formal containers, which returns a cursor holding the value searched if there is one, and the special cursor No\_Element otherwise:

```
with Element_Lists; use Element_Lists; use Element_Lists.Lists;
with Ada.Containers; use Ada.Containers; use Element_Lists.Lists.Formal_Model;

function My_Find (L : List; E : Element_Type) return Cursor with
```

```
SPARK_Mode,
Contract_Cases =>
(Contains (L, E) => Has_Element (L, My_Find'Result) and then
Element (L, My_Find'Result) = E,
not Contains (L, E) => My_Find'Result = No_Element);
```

The ghost functions mentioned above are specially useful in *Loop Invariants* to refer to cursors, and positions of elements in the containers. For example, here, ghost function Positions is used in the loop invariant to query the position of the current cursor in the list, and Model is used to specify that the value searched is not contained in the part of the container already traversed (otherwise the loop would have exited):

```
function My_Find (L : List; E : Element_Type) return Cursor with
     SPARK_Mode
2
   is
3
      Cu : Cursor := First (L);
4
5
   begin
6
      while Has_Element (L, Cu) loop
7
         pragma Loop_Invariant (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
8
                                      Element (Model (L), I) /= E);
9
10
          if Element (L, Cu) = E then
11
             return Cu;
12
13
          end if;
14
         Next (L, Cu);
15
      end loop;
16
17
      return No_Element;
18
   end My_Find;
```

GNAT prove proves that function My\_Find implements its specification:

```
my_find.adb:8:30: info: loop invariant initialization proved
my_find.adb:8:30: info: loop invariant preservation proved
my_find.adb:8:49: info: precondition proved
my_find.adb:9:33: info: precondition proved
my_find.adb:11:10: info: precondition proved
my_find.adb:15:07: info: precondition proved
my_find.ads:6:03: info: complete contract cases proved
my_find.ads:6:03: info: disjoint contract cases proved
my_find.ads:7:26: info: contract case proved
my_find.ads:8:29: info: precondition proved
my_find.ads:9:26: info: contract case proved
```

#### **Quantification over Formal Containers**

Quantified Expressions can be used over the content of a formal container to express that a property holds for all elements of a container (using for all) or that a property holds for at least one element of a container (using for some).

For example, we can express that all elements of a formal list of integers are prime as follows:

```
(for all Cu in My_List => Is_Prime (Element (My_List, Cu)))
```

On this expression, the GNAT compiler generates code that iterates over My\_List using the functions First,

Has\_Element and Next given in the Iterable aspect applying to the type of formal lists, so the quantified expression above is equivalent to:

```
declare
   Cu : Cursor_Type := First (My_List);
   Result : Boolean := True;
begin
   while Result and then Has_Element (My_List, Cu) loop
      Result := Is_Prime (Element (My_List, Cu));
      Cu := Next (My_List, Cu);
   end loop;
end;
```

where Result is the value of the quantified expression. See GNAT Reference Manual for details on aspect Iterable.

### 5.10.3 SPARK Lemma Library

As part of the SPARK product, a library of lemmas is available through the project file spark\_install>/lib/gnat/spark\_lemmas.gpr. To use this library in a program, you need to add a corresponding dependency in your project file, for example:

```
with "spark_lemmas";
project My_Project is
    ...
end My_Project;
```

You may need to update the environment variable GPR\_PROJECT\_PATH for the lemma library project to be found by GNAT compiler, as described in *Installation of GNAT prove*.

You also need to set the environment variable SPARK\_LEMMAS\_OBJECT\_DIR to the absolute path of the object directory where you want compilation and verification artefacts for the lemma library to be created. This should be an absolute path (not a relative one) otherwise these artefacts will be created inside you SPARK install.

Finally, if you instantiate in your code a generic from the lemma library, you also need to pass -gnateDSPARK\_BODY\_MODE=Off as a compilation switch for these generic units.

This library consists in a set of ghost null procedures with contracts (called *lemmas*). Here is an example of such a lemma:

```
procedure Lemma_Div_Is_Monotonic
  (Val1 : Int;
   Val2 : Int;
   Denom : Pos)
with
   Global => null,
   Pre => Val1 <= Val2,
   Post => Val1 / Denom <= Val2 / Denom;</pre>
```

whose body is simply a null procedure:

```
procedure Lemma_Div_Is_Monotonic
  (Val1 : Int;
   Val2 : Int;
   Denom : Pos)
is null;
```

This procedure is ghost (as part of a ghost package), which means that the procedure body and all calls to the procedure are compiled away when producing the final executable without assertions (when switch -gnata is not set). On the contrary, when compiling with assertions for testing (when switch -gnata is set) the precondition of the procedure is executed, possibly detecting invalid uses of the lemma. However, the main purpose of such a lemma is to facilitate automatic proof, by providing the prover specific properties expressed in the postcondition. In the case of Lemma\_Div\_Is\_Monotonic, the postcondition expresses an inequality between two expressions. You may use this lemma in your program by calling it on specific expressions, for example:

```
R1 := X1 / Y;
R2 := X2 / Y;
Lemma_Div_Is_Monotonic (X1, X2, Y);
-- at this program point, the prover knows that R1 <= R2
-- the following assertion is proved automatically:

pragma Assert (R1 <= R2);
```

Note that the lemma may have a precondition, stating in which contexts the lemma holds, which you will need to prove when calling it. For example, a precondition check is generated in the code above to show that X1 <= X2. Similarly, the types of parameters in the lemma may restrict the contexts in which the lemma holds. For example, the type Pos for parameter Denom of Lemma\_Div\_Is\_Monotonic is the type of positive integers. Hence, a range check may be generated in the code above to show that Y is positive.

All the lemmas provided in the SPARK lemma library have been proved either automatically or using Coq interactive prover. The Why3 session file recording all proofs, as well as the individual Coq proof scripts, are available as part of the SPARK product under directory <spark-install>/lib/gnat/proof. For example, the proof of lemma Lemma\_Div\_Is\_Monotonic is a Coq proof of the mathematical property (in Coq syntax):

```
1 subgoals
h1 : in_range val1
h2 : in_range val2
h3 : in_range1 denom
h4 : (val1 <= val2)%Z

______(1/1)
(val1 ÷ denom <= val2 ÷ denom)%Z</pre>
```

Currenly, the SPARK lemma library provides the following lemmas:

- Lemmas on signed integer arithmetic in file spark-arithmetic\_lemmas.ads, that are instantiated for 32 bits signed integers (Integer) in file spark-integer\_arithmetic\_lemmas.ads and for 64 bits signed integers (Long\_Integer) in file spark-long\_integer\_arithmetic\_lemmas.ads.
- Lemmas on modular integer arithmetic in file spark-mod\_arithmetic\_lemmas.ads, that are instantiated for 32 bits modular integers (Interfaces.Unsigned\_32) in file spark-mod32\_arithmetic\_lemmas.ads and for 64 bits modular integers (Interfaces. Unsigned\_64) in file spark-mod64\_arithmetic\_lemmas.ads.
- GNAT-specific lemmas on fixed-point arithmetic in file spark-fixed\_point\_arithmetic\_lemmas. ads, that need to be instantiated by the user for her specific fixed-point type.
- Lemmas on floating point arithmetic in file spark-floating\_point\_arithmetic\_lemmas.ads, that are instantiated for single-precision floats (Float) in file spark-float\_arithmetic\_lemmas.ads and for double-precision floats (Long\_Float) in file spark-long\_float\_arithmetic\_lemmas.ads.
- Lemmas on unconstrained arrays in file spark-unconstrained\_array\_lemmas.ads, that need to be instantiated by the user for her specific type of index and element, and specific ordering function between elements.

To apply lemmas to signed or modular integers of different types than the ones used in the instances provided in the library, just convert the expressions passed in arguments, as follows:

```
R1 := X1 / Y;
R2 := X2 / Y;
Lemma_Div_Is_Monotonic (Integer(X1), Integer(X2), Integer(Y));
-- at this program point, the prover knows that R1 <= R2
-- the following assertion is proved automatically:

pragma Assert (R1 <= R2);
```

#### 5.10.4 Higher Order Function Library

The SPARK product also includes a library of higher order functions for unconstrained arrays. It is available using the same project file as the SPARK Lemma Library.

This library consists in a set of generic entities defining usual operations on arrays. As an example, here is a generic function for the map higher-level function on arrays. It applies a given function F to each element of an array, returning an array of results in the same order.

```
generic
  type Index_Type is range <>;
  type Element_In is private;
  type Array_In is array (Index_Type range <>) of Element_In;
  type Element_Out is private;
  type Array_Out is array (Index_Type range <>) of Element_Out;
  with function Init_Prop (A : Element_In) return Boolean;
   -- Potential additional constraint on values of the array to allow Map
  with function F (X : Element_In) return Element_Out;
   -- Function that should be applied to elements of Array_In
function Map (A : Array_In) return Array_Out with
 Pre => (for all I in A'Range => Init_Prop (A (I))),
 Post => Map'Result'First = A'First
 and then Map'Result'Last = A'Last
 and then (for all I in A'Range =>
             Map'Result (I) = F (A (I));
```

This function can be instantiated by providing two unconstrained array types ranging over the same index type and a function F mapping a component of the first array type to a component of the second array type. Additionally, a constraint Init\_Prop can be supplied for the components of the first array to be allowed to apply F. If no such constraint is needed, Init\_Prop can be instantiated with an always True function.

```
type Nat_Array is array (Positive range <>) of Natural;

function Small_Enough (X : Natural) return Boolean is
   (X < Integer'Last);

function Increment_One (X : Integer) return Integer is (X + 1) with
   Pre => X < Integer'Last;

function Increment_All is new SPARK.Higher_Order.Map
   (Index_Type => Positive,
   Element_In => Natural,
   Array_In => Nat_Array,
   Element_Out => Natural,
   Array_Out => Nat_Array,
```

```
Init_Prop => Small_Enough,
F => Increment_One);
```

The Increment\_All function above will take as an argument an array of natural numbers small enough to be incremented and will return an array containing the result of incrementing each number by one:

Currently, the higher-order function library provides the following functions:

- Map functions over unconstrained one-dimensional arrays in file spark-higher\_order.ads. These include both in place and functional map subprograms, with and without an additional position parameter.
- Fold functions over unconstrained one-dimensional and two-dimensional arrays in file spark-higher\_order-fold.ads. Both left to right and right to left fold functions are available for one-dimensional arrays. For two-dimensional arrays, fold functions go on a line by line, left to right, top-to-bottom way. For ease of use, these functions have been instantiated for the most common cases. Sum and Sum\_2 respectively compute the sum of all the elements of a one-dimensional or two-dimensional array, and Count and Count\_2 the number of elements with a given Choose property.

**Note:** Unlike the *SPARK Lemma Library*, these generic functions are not verified once and for all as their correction depends on the functions provided at each instance. As a result, each instance should be verified by running the SPARK tools.

**CHAPTER** 

SIX

#### SPARK TUTORIAL

This chapter describes a simple use of the SPARK toolset on a program written completely in SPARK, within the GPS integrated development environment. All the tools may also be run from the command-line, see *Command Line Invocation*.

**Note:** If you're using SPARK Discovery instead of SPARK Pro, some of the proofs in this tutorial may not be obtained automatically. See the section on *Alternative Provers* to install additional provers that are not present in SPARK Discovery.

# **6.1 Writing SPARK Programs**

As a running example, we consider a naive searching algorithm for an unordered collection of elements. The algorithm returns whether the collection contains the desired value, and if so, at which index. The collection is implemented here as an array. We deliberately start with an incorrect program for package Search, in order to explain how the SPARK toolset can help correct these errors. The final version of the linear\_search example is part of the Examples in the Toolset Distribution.

We start with creating a GNAT project file in search.gpr:

```
project Search is

for Source_Dirs use (".");

package Compiler is
    for Default_Switches ("Ada") use ("-gnatwa");
end Compiler;
end Search;
```

It specifies that the source code to inspect is in the current directory, and that the code should be compiled at maximum warning level (switch -gnatwa). GNAT projects are used by most tools in the GNAT toolsuite; for in-depth documentation of this technology, consult the GNAT User's Guide. Documentation and examples for the SPARK language and tools are also available via the  $Help \rightarrow SPARK$  menu in GPS.

The obvious specification of Linear\_Search is given in file linear\_search.ads, where we specify that the spec is in SPARK by using aspect SPARK\_Mode.

```
package Linear_Search
with SPARK_Mode
is

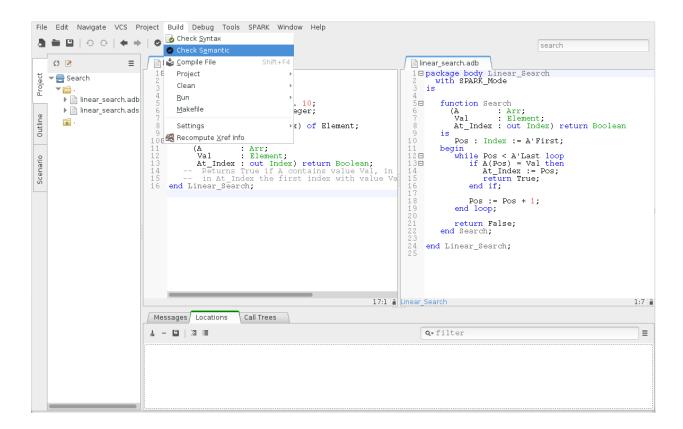
type Index is range 1 .. 10;
type Element is new Integer;
```

```
7
      type Arr is array (Index) of Element;
8
      function Search
10
              : Arr;
11
        (A
               : Element;
        Val
        At_Index : out Index) return Boolean;
13
      -- Returns True if A contains value Val, in which case it also returns
14
      -- in At Index the first index with value Val. Returns False otherwise.
15
   end Linear_Search;
```

The implementation of Linear\_Search is given in file linear\_search.adb, where we specify that the body is in SPARK by using aspect SPARK\_Mode. It is as obvious as its specification, using a loop to go through the array parameter A and looking for the first index at which Val is found, if there is such an index.

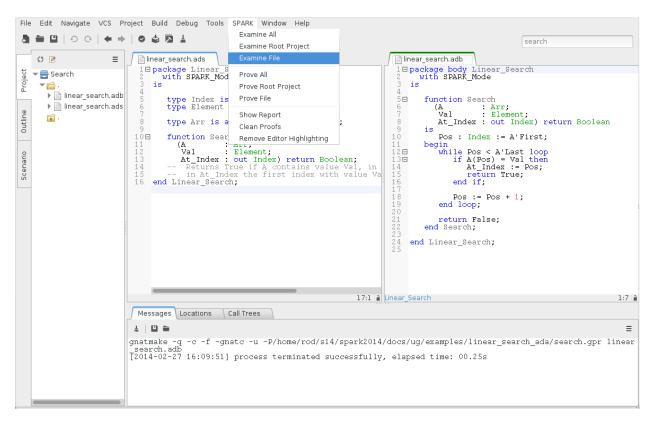
```
package body Linear_Search
     with SPARK_Mode
2
   is
3
       function Search
5
                : Arr;
6
7
          Val
                   : Element;
          At_Index : out Index) return Boolean
          Pos : Index := A'First;
      begin
11
          while Pos < A'Last loop</pre>
12
             if A(Pos) = Val then
13
                At_Index := Pos;
14
                return True;
15
             end if;
16
17
             Pos := Pos + 1;
18
          end loop;
19
20
          return False;
21
22
      end Search;
   end Linear_Search;
```

We can check that the above code is valid Ada by using the Build > Check Semantic menu, which completes without any errors or warnings:

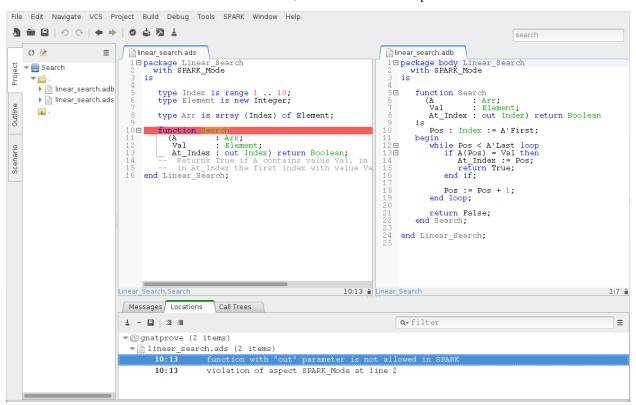


### 6.1.1 Checking SPARK Legality Rules

Now, let us run GNATprove on this unit, using the  $SPARK \rightarrow Examine\ File$  menu, so that it issues errors on SPARK code that violates SPARK rules:



It detects here that function Search is not in SPARK, because it has an out parameter:



The permission in Ada 2012 to have out parameters to functions is not allowed in SPARK, because it causes calls to have side-effects (assigning to their out parameters), which means that various calls in the same expression may be

conflicting, yielding different results depending on the order of evaluation of the expression.

We correct this problem by defining a record type Search\_Result in linear\_search.ads holding both the Boolean result and the index for cases when the value is found, and making Search return this type:

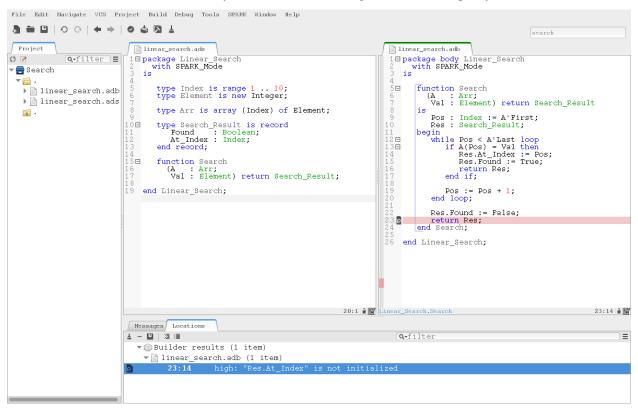
```
package Linear_Search
     with SPARK_Mode
2
   is
3
4
      type Index is range 1 .. 10;
5
      type Element is new Integer;
6
7
      type Arr is array (Index) of Element;
8
      type Search_Result is record
10
         Found : Boolean;
11
         At_Index : Index;
12
      end record;
14
      function Search
15
        (A : Arr;
16
         Val : Element) return Search_Result;
17
18
   end Linear_Search;
```

The implementation of Search in linear\_search.adb is modified to use this type:

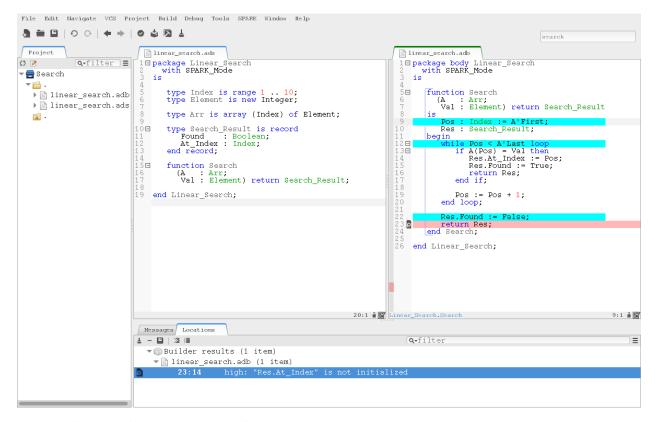
```
package body Linear_Search
2
     with SPARK_Mode
3
      function Search
5
         (A : Arr;
6
         Val : Element) return Search_Result
7
8
          Pos : Index := A'First;
9
         Res : Search_Result;
10
      begin
11
          while Pos < A'Last loop
12
             if A(Pos) = Val then
13
                Res.At_Index := Pos;
                Res.Found := True;
                return Res;
16
             end if;
17
18
             Pos := Pos + 1;
19
          end loop;
20
21
22
          Res.Found := False;
          return Res;
23
      end Search;
24
25
   end Linear_Search;
```

### 6.1.2 Checking SPARK Initialization Policy

Re-running GNATprove on this unit, still using the  $SPARK \rightarrow Examine \ File$  menu, now reports a different kind of error. This time it is the static analysis pass of GNATprove called *flow analysis* that detects an attempt of the program to return variable Res while it is not fully initialized, thus violating the initialization policy of SPARK:



Inside the GPS editor, we can click on the icon, either on the left of the message, or on line 23 in file linear\_search.adb, to show the path on which Res.At\_Index is not initialized:



Another click on the icon makes the path disappear.

This shows that, when the value is not found, the component At\_Index of the value returned is indeed not initialized. Although that is allowed in Ada, SPARK requires that all inputs and outputs of subprograms are completely initialized (and the value returned by a function is such an output). As a solution, we could give a dummy value to component At\_Index when the search fails, but we choose here to turn the type Search\_Result in linear\_search.ads into a discriminant record, so that the component At\_Index is only usable when the search succeeds:

```
type Search_Result (Found : Boolean := False) is record
case Found is
when True =>
At_Index : Index;
when False =>
null;
end case;
end record;
```

Then, in the implementation of Search in linear\_search.adb, we change the value of the discriminant depending on the success of the search:

```
function Search
        (A
            : Arr;
2
         Val : Element) return Search_Result
3
      is
4
         Pos : Index := A'First;
         Res : Search_Result;
6
      begin
         while Pos < A'Last loop
            if A(Pos) = Val then
                Res := (Found
                                  => True,
10
                        At_Index => Pos);
11
```

```
return Res;
end if;

Pos := Pos + 1;
end loop;

Res := (Found => False);
return Res;
end Search;
```

Now re-running GNAT prove on this unit, using the  $SPARK \rightarrow Examine\ File$  menu, shows that there are no reads of uninitialized data.

### **6.1.3 Writing Functional Contracts**

We now have a valid SPARK program. It is not yet very interesting SPARK code though, as it does not contain any contracts, which are necessary to be able to apply formal verification modularly on each subprogram, independently of the implementation of other subprograms. The precondition constrains the value of input parameters, while the postcondition states desired properties of the result of the function. See *Preconditions* and *Postconditions* for more details. Here, we can require in the precondition of Search in linear\_search.ads that callers of Search always pass a non-negative value for parameter Val, and we can state that, when the search succeeds, the index returned points to the desired value in the array:

```
function Search

(A : Arr;

Val : Element) return Search_Result

with

Pre => Val >= 0,

Post => (if Search'Result.Found then

A (Search'Result.At_Index) = Val),
```

Notice the use of an if-expression in the postcondition to express an implication: if the search succeeds it implies that the value at the returned index is the value that was being searched for. Note also the use of Search'Result to denote the value returned by the function.

This contract is still not very strong. Many faulty implementations of the search would pass this contract, for example one that always fails (thus returning with Search'Result.Found = False). We could reinforce the postcondition, but we choose here to do it through a contract by cases, which adds further constraints to the usual contract by precondition and postcondition. We want to consider here three cases:

- the desired value is found at the first index (1)
- the desired value is found at other indexes (2 to 10)
- the desired value is not found in the range 1 to 10

In the first case, we want to state that the index returned is 1. In the second case, we want to state that the search succeeds. In the third case, we want to state that the search fails. We use a helper function Value\_Found\_In\_Range in linear\_search.ads to express that a value Val is found in an array A within given bounds Low and Up:

```
function Value_Found_In_Range

(A : Arr;
Val : Element;
Low, Up : Index) return Boolean
is (for some J in Low .. Up => A(J) = Val);

function Search
```

```
8
          Val : Element) return Search_Result
9
10
      with
        Pre \Rightarrow Val \Rightarrow 0,
11
        Post => (if Search'Result.Found then
                    A (Search'Result.At_Index) = Val),
        Contract_Cases =>
           (A(1) = Val =>
15
              Search'Result.At_Index = 1,
16
            Value_Found_In_Range (A, Val, 2, 10) =>
17
              Search'Result.Found,
18
            (for all J in Arr'Range => A(J) /= Val) =>
19
              not Search'Result.Found);
```

Note that we express Value\_Found\_In\_Range as an expression function, a function whose body consists of a single expression, which can be given in a specification file.

Note also the use of quantified expressions to express properties over collections: for some in Value\_Found\_In\_Range expresses an existential property (there exists an index in this range such that ...), for all in the third contract case expresses a universal property (all indexes in this range are such that ...).

Each contract case consists of a guard (on the left of the arrow symbol) evaluated on subprogram entry, and a consequence (on the right of the arrow symbol) evaluated on subprogram exit. The special expression Search'Result may be used in consequence expressions. The three guards here should cover all possible cases, and be disjoint. When a contract case is activated (meaning its guard holds on entry), its consequence should hold on exit.

The program obtained so far is a valid SPARK program, which GNAT analyzes semantically without errors or warnings.

# **6.2 Testing SPARK Programs**

We can compile the above program, and test it on a set of selected inputs. The following test program in file test\_search.adb exercises the case where the searched value is present in the array and the case where it is not:

```
with Linear_Search; use Linear_Search;
2
   with Ada.Text_IO;
                       use Ada.Text_IO;
   procedure Test_Search is
4
         : constant Arr := (1, 5, 3, 8, 8, 2, 0, 1, 0, 4);
5
      Res : Search_Result;
6
   begin
      Res := Search (A, 1);
      if Res.Found then
10
         if Res.At_Index = 1 then
11
            Put_Line ("OK: Found existing value at first index");
12
         else
13
            Put_Line ("not OK: Found existing value at other index");
14
         end if;
16
         Put_Line ("not OK: Did not find existing value");
17
      end if;
18
19
      Res := Search (A, 6);
      if not Res.Found then
```

```
Put_Line ("OK: Did not find non-existing value");
else
Put_Line ("not OK: Found non-existing value");
end if;
end Test_Search;
```

We can check that the implementation of Linear\_Search passes this test by compiling and running the test program:

```
$ gnatmake test_search.adb
$ test_search
> OK: Found existing value at first index
> OK: Did not find non-existing value
```

**Note:** We use above the command-line interface to compile and run the test program test\_search.adb. You can do the same inside GPS by selecting the menu  $Project \rightarrow Properties$  and inside the panel Main of folder Sources, add test\_search.adb as a main file. Then, click OK. To generate the test\_search executable, you can now select the menu  $Build \rightarrow Project \rightarrow test\_search.adb$  and to run the test\_search executable, you can select the menu  $Build \rightarrow Run \rightarrow test\_search$ .

But only part of the program was really tested, as the contract was not checked during execution. To check the contract at run time, we recompile with the switch -gnata (a for assertions, plus switch -f to force recompilation of sources that have not changed):

- a check is inserted that the precondition holds on subprogram entry
- a check is inserted that the postcondition holds on subprogram exit
- a check is inserted that the guards of contract cases are disjoint on subprogram entry (no two cases are activated at the same time)
- a check is inserted that the guards of contract cases are complete on subprogram entry (one case must be activated)
- a check is inserted that the consequence of the activated contract case holds on subprogram exit

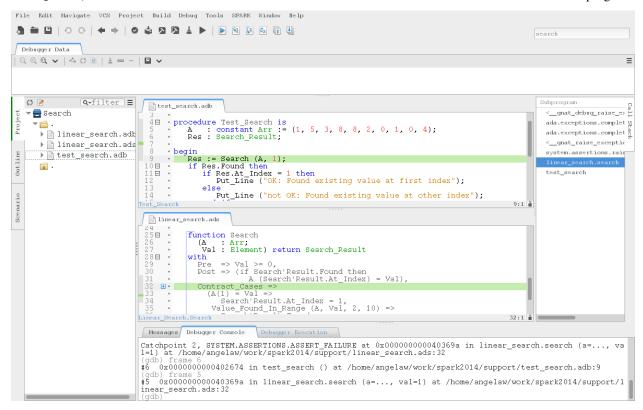
Note that the evaluation of the above assertions may also trigger other run-time check failures, like an index out of bounds. With these additional run-time checks, an error is reported when running the test program:

**Note:** We use above the command-line interface to add compilation switch -gnata and force recompilation with switch -f. You can do the same inside GPS by selecting the menu  $Project \rightarrow Properties$  and inside the panel Ada of the subfolder Switches of folder Build, select the checkbox Enable assertions. Then, click OK. To force recompilation with the new switch, you can now select the menu  $Build \rightarrow Clean \rightarrow Clean \ All$  followed by recompilation with  $Build \rightarrow Project \rightarrow test\_search.adb$ . Then run the test\\_search executable with  $Build \rightarrow Run \rightarrow test\_search$ .

It appears that two contract cases for Search are activated at the same time! More information can be generated at run time if the code is compiler with the switch -gnateE:

```
$ gnatmake -gnate -f test_search.adb
$ test_search
```

It shows here that the guards of the first and second contract cases hold at the same time. This failure in annotations can be debugged with gdb like a failure in the code (provided the program was compiled with appropriate switches, like -g -00). The stack trace inside GPS shows that the error occurs on the first call to Search in the test program:



Indeed, the value 1 is present twice in the array, at indexes 1 and 8, which makes the two guards A(1) = Val and Value\_Found\_In\_Range (A, Val, 2, 10) evaluate to True. We correct the contract of Search in linear\_search.ads by strengthening the guard of the second contract case, so that it only applies when the value is not found at index 1:

```
Contract_Cases =>

(A(1) = Val =>

Search'Result.At_Index = 1,

A(1) /= Val and then Value_Found_In_Range (A, Val, 2, 10) =>

Search'Result.Found,

(for all J in Arr'Range => A(J) /= Val) =>

not Search'Result.Found);
```

With this updated contract, the test passes again, but this time with assertions checked at run time:

```
$ gnatmake -gnata test_search.adb
$ test_search
> OK: Found existing value at first index
> OK: Did not find non-existing value
```

The program obtained so far passes successfully a test campaign (of one test!) that achieves 100% coverage for all the

common coverage criteria, once impossible paths have been ruled out: statement coverage, condition coverage, the MC/DC coverage used in avionics, and even the full static path coverage.

## **6.3 Proving SPARK Programs**

Formal verification of SPARK programs is a two-step process:

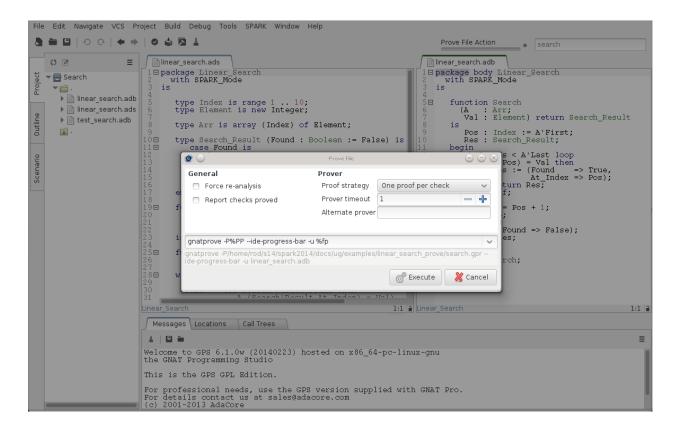
- 1. the first step checks that flows through the program correctly implement the specified flows (if any), and that all values read are initialized.
- 2. the second step checks that the program correctly implement its specified contracts (if any), and that no run-time error can be raised.

Step 1 is implemented as a static analysis pass in the tool GNATprove, in flow mode. We have seen this flow analysis at work earlier (see *Checking SPARK Initialization Policy*). Step 2 is implemented as a deductive verification (a.k.a. *proof*) pass in the tool GNATprove, in the default all mode.

The difference between these two steps should be emphasized. Flow analysis in step 1 is a terminating algorithm, which typically takes 2 to 10 times as long as compilation to complete. Proof in step 2 is based on the generation of logical formulas for each check to prove, which are then passed on to automatic provers to decide whether the logical formula holds or not. The generation of logical formulas is a translation phase, which typically takes 10 times as long as compilation to complete. The automatic proof of logical formulas may take a very long time, or never terminate, hence the use of a timeout (1s at proof level 0) for each call to the automatic provers. It is this last step which takes the most time when calling GNATprove on a program, but it is also a step which can be completely parallelized (using switch -j to specify the number of parallel processes): each logical formula can be proved independently, so the more cores are available the faster it completes.

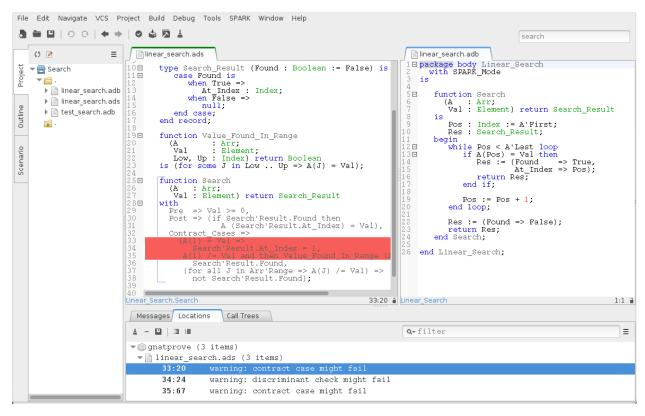
**Note:** The proof results presented in this tutorial may slightly vary from the results you obtain on your machine, as automatic provers may take more or less time to complete a proof depending on the platform and machine used.

Let us continue with our running example. This time we will see how step 2 works to prove contracts and absence of run-time errors, using the main mode all of GNATprove reached through the  $SPARK \rightarrow Prove\ File$  menu.



**Note:** The proof panels presented in this tutorial correspond to an advanced user profile. A simpler proof panel is displayed when the basic user profile is selected (the default). You can switch to the advanced user profile in menu  $Edit \rightarrow Preferences \rightarrow SPARK$ , by changing the value of *User profile* from Basic to Advanced. See *Running GNAT prove from GPS* for details.

We use the default settings and click on *Execute*. It completes in a few seconds, with a message stating that some checks could not be proved:

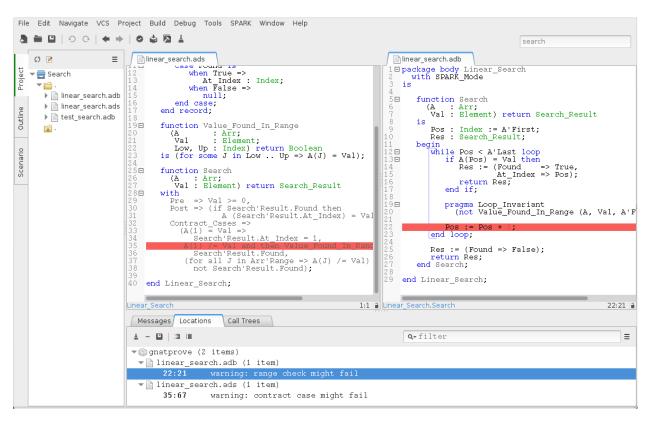


Note that there is no such message on the postcondition of Search, which means that it was proved. Likewise, there are no such messages on the body of Search, which means that no run-time errors can be raised when executing the function.

These messages correspond to checks done when exiting from Search. It is expected that not much can be proved at this point, given that the body of Search has a loop but no loop invariant, so the formulas generated for these checks assume the worst about locations modified in the loop. A loop invariant is a special pragma Loop\_Invariant stating an assertion in a loop, which can be both executed at run-time like a regular pragma Assert, and used by GNATprove to summarize the effect of successive iterations of the loop. We need to add a loop invariant in linear\_search.adb stating enough properties about the cumulative effect of loop iterations, so that the contract cases of Search become provable. Here, it should state that the value searched was not previously found:

```
pragma Loop_Invariant
   (not Value_Found_In_Range (A, Val, A'First, Pos));
```

As stated above, this invariant holds exactly between the two statements in the loop in linear\_search.adb (after the if-statement, before the increment of the index). Thus, it should be inserted at this place. With this loop invariant, two checks previously not proved are now proved, and a check previously proved becomes unproved:



The new unproved checks may seem odd, since all we did was add information in the form of a loop invariant. The reason is that we also removed information at the same time. By adding a loop invariant, we require GNAT prove to prove iterations around the (virtual) loop formed by the following steps:

- 1. Take any context satisfying the loop invariant, which summarizes all previous iterations of the loop.
- 2. Execute the end of a source loop iteration (just the increment here).
- 3. Test whether the loop exits, and continue with values which do not exit.
- 4. Execute the start of a source loop iteration (just the if-statement here).
- 5. Check that the loop invariant still holds.

Around this virtual loop, nothing guarantees that the index Pos is below the maximal index at step 2 (the increment), so the range check cannot be proved. It was previously proved because, in the absence of a loop invariant, GNAT prove proves iterations around the source loop, and then we get the information that, since the loop did not exit, its test Pos < A'Last is false, so the range check can be proved.

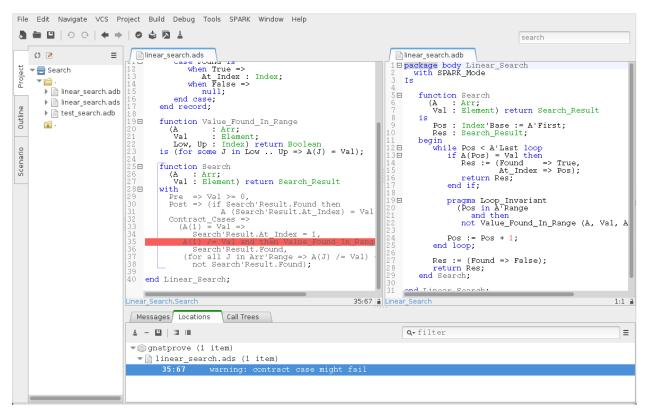
We solve this issue by setting the type of Pos in linear\_search.adb to the base type of Index, which ranges past the last value of Index. (This may not be the simplest solution, but we use it here for the dynamics of this tutorial.)

```
Pos : Index'Base := A'First;
```

And we add the range information for Pos to the loop invariant in linear\_search.adb:

```
pragma Loop_Invariant
  (Pos in A'Range
         and then
         not Value_Found_In_Range (A, Val, A'First, Pos));
```

This allows GNAT prove to prove the range check, but not the contract:



This is actually progress! Indeed, the loop invariant should be strong enough to:

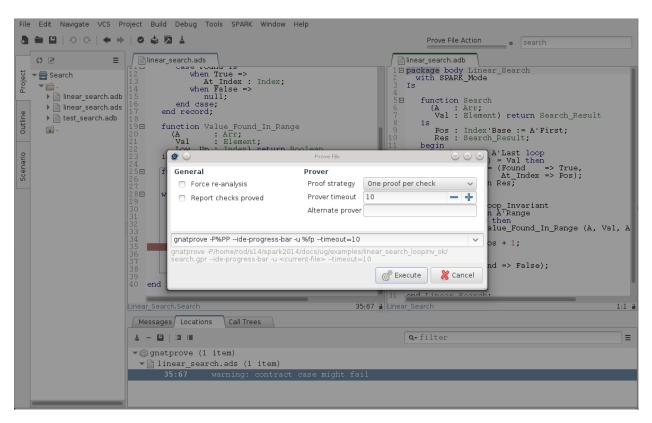
- 1. prove the absence of run-time errors in the loop and after the loop
- 2. prove that it is preserved from iteration to iteration
- 3. prove the postcondition and contract cases of the subprogram

So we have just achieved goal 1 above!

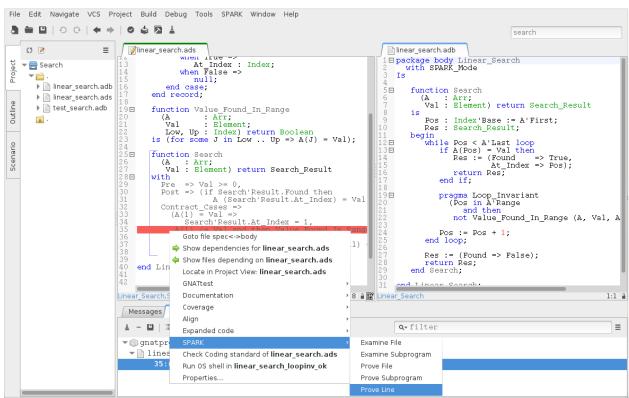
As we have modified the code and annotations, it is a good time to compile and run our test program, before doing any more formal verification work. This helps catch bugs early, and it's easy to do! In particular, the loop invariant will be dynamically checked at each iteration through the loop. Here, testing does not show any problems:

```
$ gnatmake -gnata test_search.adb
$ test_search
> OK: Found existing value at first index
> OK: Did not find non-existing value
```

The next easy thing to do is to increase the timeout of automatic provers. Its default of 1s is deliberately low, to facilitate interaction with GNATprove during the development of annotations, but it is not sufficient to prove the more complex checks. Let's increase it to 10s (or equivalently set the Proof level to 2 in the proof panel corresponding to a basic user profile), and rerun GNATprove:

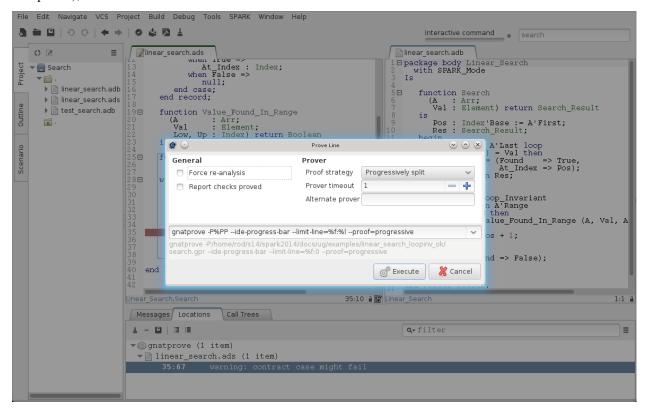


The unproved check remains in the contract cases of Linear\_Search. The next step is to use the  $SPARK \rightarrow Prove$  Line contextual menu available on line 35:

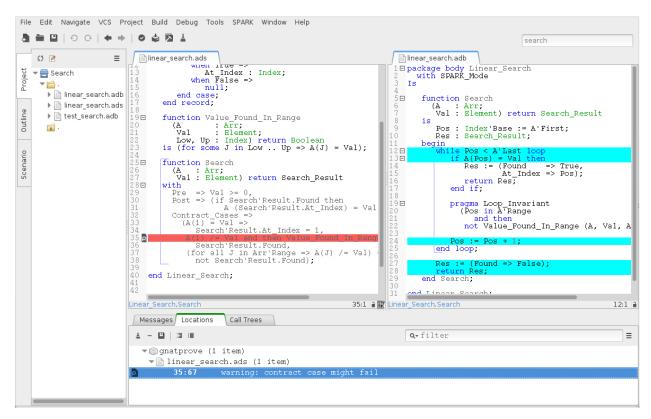


We select the Progressively split value for choice Proof strategy in the window raised in order to

maximize proof precision (or equivalently set the Proof level to 3 in the proof panel corresponding to a basic user profile), and click on *Execute*:



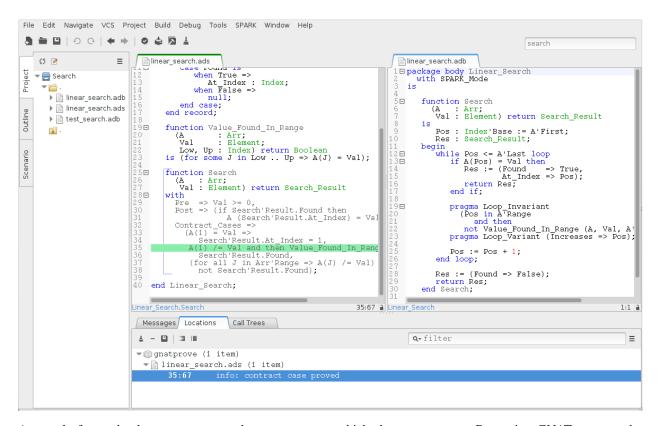
This runs GNATprove only on the checks that originate from line 35, in a special mode which considers separately individual execution paths if needed. The check is still not proved, but GPS now displays an icon, either on the left of the message, or on line 35 in file linear\_search.ads, to show the path on which the contract case is not proved:



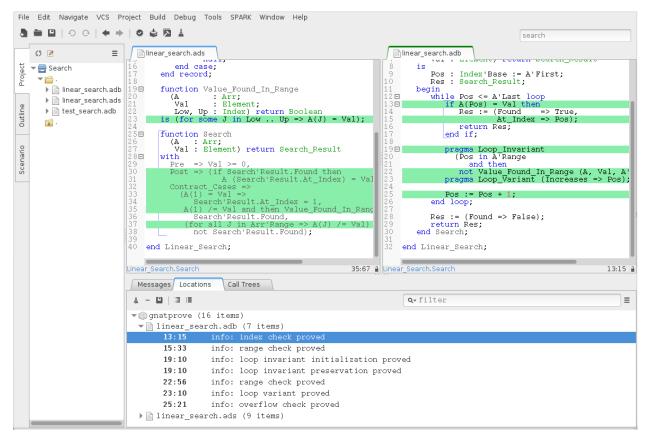
This corresponds to a case where the implementation of Search does not find the searched value, but the guard of the second contract case holds, meaning that the value is present in the range 2 to 10. Looking more closely at the path highlighted, we can see that the loop exits when Pos = A'Last, so the value 10 is never considered! We correct this bug by changing the loop test in linear\_search.adb from a strict to a non-strict comparison operation:

```
while Pos <= A'Last loop</pre>
```

On this modified code, we rerun GNAT prove on line 35, checking the box Report checks proved to get information even when a check is proved. The reassuring green color (and the accompanying info message) show that the check was proved this time:



As usual after code changes, we rerun the test program, which shows no errors. Rerunning GNATprove on the complete file shows no more unproved checks. The Linear\_Search unit has been fully proved. To see all the checks that were proved, we can rerun the tool with box Report checks proved checked, which displays the results previously computed:



Note that one thing that was not proved is that Search terminates. As it contains a while-loop, it could loop forever. To prove that it is not the case, we add a loop variant, which specifies a quantity varying monotonically with each iteration. Since this quantity is bounded by its type, and we have proved absence of run-time errors in Search, proving this monotonicity property also shows that there cannot be an infinite number of iterations of the loop. The natural loop variant for Search is the index Pos, which increases at each loop iteration:

```
pragma Loop_Variant (Increases => Pos);
```

With this line inserted after the loop invariant in linear\_search.adb, the test program still runs without errors (it checks dynamically that the loop variant is respected), and the program is still fully proved. Here is the final version of Linear\_Search, with the complete annotations:

```
package Linear_Search
     with SPARK_Mode
2
   is
3
4
      type Index is range 1 .. 10;
      type Element is new Integer;
      type Arr is array (Index) of Element;
8
      type Search_Result (Found : Boolean := False) is record
10
         case Found is
11
            when True =>
12
                At_Index : Index;
             when False =>
                null;
15
         end case;
16
      end record;
```

```
18
       function Value_Found_In_Range
19
                 : Arr;
20
         (A
                   : Element;
          Val
21
          Low, Up : Index) return Boolean
22
23
       is (for some J in Low .. Up \Rightarrow A(J) = Val);
24
       function Search
25
         (A : Arr;
26
          Val : Element) return Search_Result
27
       with
28
         Pre \Rightarrow Val \Rightarrow 0,
29
         Post => (if Search'Result.Found then
30
                     A (Search'Result.At_Index) = Val),
31
         Contract_Cases =>
32
           (A(1) = Val =>
33
               Search'Result.At_Index = 1,
34
            A(1) /= Val and then Value_Found_In_Range (A, Val, 2, 10) =>
35
               Search'Result.Found,
             (for all J in Arr'Range => A(J) /= Val) =>
37
               not Search'Result.Found);
38
39
   end Linear_Search;
40
```

```
package body Linear_Search
     with SPARK_Mode
2
   is
3
       function Search
5
         (A : Arr;
6
          Val : Element) return Search_Result
7
          Pos : Index'Base := A'First;
          Res : Search_Result;
10
       begin
11
          while Pos <= A'Last loop</pre>
12
             if A(Pos) = Val then
13
                Res := (Found
                                 => True,
14
                         At_Index => Pos);
15
                 return Res;
16
17
             end if;
18
             pragma Loop_Invariant
19
                (Pos in A'Range
20
                   and then
21
                 not Value_Found_In_Range (A, Val, A'First, Pos));
22
             pragma Loop_Variant (Increases => Pos);
23
24
             Pos := Pos + 1;
25
          end loop;
26
27
          Res := (Found => False);
28
          return Res;
29
30
       end Search;
31
   end Linear_Search;
```

The final version of the linear\_search example is part of the Examples in the Toolset Distribution. This concludes

our tutorial on the SPARK toolset.

**CHAPTER** 

SEVEN

#### FORMAL VERIFICATION WITH GNATPROVE

The GNAT prove tool is packaged as an executable called gnatprove. Like other tools in GNAT toolsuite, GNAT prove is based on the structure of GNAT projects, defined in .gpr files.

A crucial feature of GNATprove is that it interprets annotations exactly like they are interpreted at run time during tests. In particular, their executable semantics includes the verification of run-time checks, which can be verified statically with GNATprove. GNATprove also performs additional verifications on the specification of the expected behavior itself, and its correspondence to the code.

# 7.1 How to Run GNATprove

#### 7.1.1 Setting Up a Project File

#### **Basic Project Set Up**

If not already done, create a GNAT project file (.gpr), as documented in the GNAT User's Guide, section GNAT Project Manager. See also Project Attributes for optional project attributes to specify the proof directory and other GNAT prove switches in the project file directly.

Note that you can use the project wizard from GPS to create a project file interactively, via the menu  $File \rightarrow New$  Project... In the dialog, see in particular the default option (Single Project).

If you want to get started quickly, and assuming a standard naming scheme using .ads/.adb lower case files and a single source directory, then your project file will look like:

```
project My_Project is
   for Source_Dirs use (".");
end My_Project;
```

saved in a file called my\_project.gpr.

#### **Having Different Switches for Compilation and Verification**

In some cases, you may want to pass different compilation-level switches to GNAT and GNATprove, for example use warning switches only for compilation, in the same project file. In that case, you can use a scenario variable to specify different switches for compilation and verification. We recommend to use the predefined GPR\_TOOL variable for this purpose:

```
project My_Project is

Mode := External ("GPR_TOOL");
```

```
package Compiler is
    case Mode is
    when "gnatprove" =>
        for Switches ("Ada") use ...
    when others =>
        for Switches ("Ada") use ...
    end case;
end Compiler;
end My_Project;
```

With the above project, compilation will be automatically done in the "normal" mode (the "others" branch above):

```
gprbuild -P my_project.gpr
```

while GNATprove automatically sets the GPR\_TOOL variable to the gnatprove value:

```
gnatprove -P my_project.gpr
```

Other tools set the value of this variable to other values. See the documentation of other AdaCore tools to know more about this.

Note that before SPARK Pro 20, the GPR\_TOOL was not set automatically by the tool. You can set it manually in this case:

```
gnatprove -P my_project.gpr -XGPR_TOOL=gnatprove
```

### 7.1.2 Running GNATprove from the Command Line

GNAT prove can be run from the command line as follows:

```
gnatprove -P project-file.gpr>
```

In the appendix, section *Command Line Invocation*, you can find an exhaustive list of switches; here we only give an overview over the most common uses. Note that GNATprove cannot be run without a project file.

There are essentially three common ways you can select the files which will be analyzed by GNATprove:

• Analyze everything:

```
gnatprove -P project-file.gpr> -U
```

With switch -U, all units of all projects in the project tree are analyzed. This includes units that are not used yet.

This is usually what you want to use for an overnight analysis of a complex project.

• Analyze this project:

```
gnatprove -P project-file.gpr>
```

All main units in the project and all units they (recursively) depend on are analyzed. If there are no main units specified, analyze all files in the project.

This is what you want to use for the analysis of a particular executable only, or if you want to analyze different executables within a complex project with different options.

• Analyze files:

```
gnatprove -P <project-file.gpr> [-u] FILES...
```

If -u is specified, we only analyze the given files. If -u is not specified, we also analyze all units these files (recursively) depend on.

This is intended for the day-to-day command-line or IDE use of GNATprove when implementing a project.

GNATprove consists of two distinct analyses: flow analysis and proof. Flow analysis checks the correctness of aspects related to data flow (Global, Depends, Abstract\_State, Initializes, and refinement versions of these), and verifies the initialization of variables. Proof verifies the absence of run-time errors and the correctness of assertions such as Pre and Post aspects. Using the switch --mode=<mode>, whose possible values are check, check\_all, flow, prove all, stone, bronze, silver and gold, you can choose which analysis is performed:

- In mode check, GNATprove partially checks that the program does not violate SPARK restrictions. The benefit of using this mode prior to mode check\_all is that it is much faster, as it does not require the results of flow analysis.
- In mode check\_all (stone is a synonym for this mode), GNATprove fully checks that the program does not violate SPARK restrictions, including checks not performed in mode check like the absence of side-effects in functions. Mode check\_all includes mode check.
- In mode flow (bronze is a synonym for this mode), GNATprove checks that no uninitialized data are read in the program, and that the specified data dependencies and flow dependencies are respected in the implementation. Mode flow includes mode check\_all. This phase is called *flow analysis*.
- In mode prove, GNATprove checks that the program is free from run-time errors, and that the specified functional contracts are respected in the implementation. Mode prove includes mode check\_all, as well as the part of mode flow that checks that no uninitialized data are read, to guarantee soundness of the proof results. This phase is called *proof*.
- In the default mode all, GNATprove does both flow analysis and proof. The silver and gold modes are synonyms for this mode.

Using the option <code>--limit-line=</code> one can limit proofs to a particular file and line of an Ada file. For example, if you want to prove only line 12 of file <code>example.adb</code>, you can add the option <code>--limit-line=example.adb:12</code> to the call to GNATprove. Using the option <code>--limit-subp=</code> one can limit proofs to a subprogram declared in a particular file at a particular line. Using <code>--limit-region=</code> one can limit proofs to a range of lines in a particular file. For example, <code>--limit-region=example.adb:12:14</code> will limit analysis to lines 12 to 14 in <code>example.adb</code>.

A number of options exist to influence the behavior for proof. Internally, the prover(s) specified with option <code>--prover</code> is/are called repeatedly for each check or assertion. Using the options <code>--timeout</code> and <code>--memlimit</code>, one can change the maximal time and memory that is allocated to each prover to prove each check or assertion. Using the option <code>--steps</code> (default: 100), one can set the maximum number of reasoning steps that the prover is allowed to perform before giving up. The <code>steps</code> option should be used when predictable results are required, because the results with a timeout and memory limit may differ depending on the computing power, current load or platform of the machine. The option <code>-j</code> activates parallel compilation and parallel proofs. With <code>-jnnn</code>, at most nnn cores can be used in parallel. With the special value <code>-j0</code>, at most N cores can be used in parallel, when N is the number of cores on the machine.

**Note:** When the project has a main file, or a file is passed as starting point to gnatprove, and the dependencies in the project are very linear (unit A depends only on unit B, which depends only on unit C, etc), then even when the -j switch is used, gnatprove may only consider one file at a time. This problem can be avoided by additionally using the -U switch.

**Note:** The –memlimit switch is currently ineffective on the Mac OS X operating system, due to limitations of the underlying system call on that system.

The way checks are passed to the prover can also be influenced using the option <code>--proof</code>. By default, the prover is invoked a single time for each check or assertion (mode <code>per\_check</code>). This can be changed using mode <code>per\_path</code> to invoke the prover for each <code>path</code> that leads to the check. This option usually takes much longer, because the prover is invoked much more often, but may give better proof results. Finally, in mode <code>progressive</code>, invoking the prover a single time on the entire check is tried, and only if the check is not proved, then other techniques that progressively consider each path in isolation are tried.

The proof mode set with <code>--proof</code> can be extended with a qualifier <code>all</code> or <code>lazy</code>, so that the entire switch may for example look like this: <code>--proof=progressive:all</code>. With this qualifier, one can select if proof should stop at the first unproved formula (to save time) for a check or should continue attempting to prove the other formulas related to the same check (typically to identify more precisely which formulas are left unproved, which can be then be handled with manual proof). The former is most suited for fully automatic proof, it is the default value, and can be explicitly selected with <code>lazy</code>. The latter is most suited for combination of automatic and manual proof and can be selected with <code>all</code>.

Instead of setting individually switches that influence the speed and power of proof, one may use the switch --level, which corresponds to predefined proof levels, from the faster level 0 to the more powerful level 4. More precisely, each value of --level is equivalent to directly setting a collection of other switches discussed above:

- --level=0 is equivalent to --prover=cvc4 --timeout=1 --memlimit=1000 --steps=0
- --level=1 is equivalent to --prover=cvc4,z3,altergo --timeout=1 --memlimit=1000 --steps=0
- --level=2 is equivalent to --prover=cvc4,z3,altergo --timeout=5 --memlimit=1000 --steps=0
- --level=3 is equivalent to --prover=cvc4,z3,altergo --timeout=20 --memlimit=2000 --steps=0
- --level=4 is equivalent to --prover=cvc4,z3,altergo --timeout=60 --memlimit=2000 --steps=0

If both ——level is set and an underlying switch is set (——prover, ——timeout, or ——proof), the value of the latter takes precedence over the value set through ——level.

Note that using <code>--level</code> does not provide results that are reproducible accross different machines. For nightly builds or shared repositories, consider using the <code>--steps</code> or <code>--replay</code> switches instead. The number of steps required to proved an example can be accessed by running GNATprove with the option <code>--report=statistics</code>.

GNAT prove also supports using the static analysis tool CodePeer as an additional source for the proof of checks, by specifying the command line option --codepeer=on (see *Using CodePeer Static Analysis*).

By default, GNAT prove avoids reanalyzing unchanged files, on a per-unit basis. This mechanism can be disabled with the option -f.

When GNATprove proves a check, it stores this result in a session file, along with the required time and steps for this check to be proved. This information can be used to replay the proofs, to check that they are indeed correct. When GNATprove is invoked using the <code>--replay</code> option, it will attempt such a replay, using the same prover that was able to prove the check last time, with some slightly higher time and step limit. In this mode, the user-provided steps and time limits are ignored. If the <code>--prover</code> option is not provided, GNATprove will attempt to replay all checks, otherwise it will replay only the proofs proved by one of the specified provers. If all replays succeeded, GNATprove output will be exactly the same as a normal run of GNATprove. If a replay failed, the corresponding check will be reported as not proved. If a replay has not been attempted because the corresponding prover is not available (a third-party prover that is not configured, or the user has selected other provers using the <code>--prover</code> option), a warning will

be issued that the proof could not be replayed, but the check will still be marked as proved.

By default, GNATprove stops at the first unit where it detect errors (violations of Ada or SPARK legality rules). The option –k can be used to get GNATprove to issue errors of the same kind for multiple units. If there are any violations of Ada legality rules, GNATprove does not attempt any analysis. If there are violations of SPARK legality rules, GNATprove stops after the checking phase and does not attempt flow analysis or proof.

GNATprove returns with a non-zero exit status when an error is detected. This includes cases where GNATprove issues unproved check messages when switch --checks-as-errors is used, as well as cases where GNATprove issues warnings when switch --warnings=error is used. In such cases, GNATprove also issues a message about termination in error. Otherwise, GNATprove returns with an exit status of zero, even when unproved check messages and warnings are issued.

### 7.1.3 Using the GNAT Target Runtime Directory

If you are using GNAT as your target compiler and explicitly specify a runtime and target to use in your project, for instance:

```
for Target use "arm-eabi";
for Runtime ("Ada") use "ravenscar-sfp-stm32f4";
```

GNAT prove will take such setting into account and will use the GNAT runtime directory, as long as your target compiler is found in your PATH environment variable. Note that you will need to use a matching version of GNAT and SPARK (e.g. GNAT 18.2 and SPARK 18.2).

The handling of runtimes of GNATprove is in fact unified with that of the GNAT compiler. For details, see "GNAT User's Guide Supplement for Cross Platforms", Section 3. If you specify a target, note that GNATprove requires additional configuration, see the section *Specifying the Target Architecture and Implementation-Defined Behavior*.

If you're using GNAT Common Code Generator to generate C code from SPARK, you can specify the target and runtime as follows:

```
for Target use "c";
for Runtime ("Ada") use "ccg";
```

### 7.1.4 Specifying the Target Architecture and Implementation-Defined Behavior

A SPARK program is guaranteed to be unambiguous, so that formal verification of properties is possible. However, some behaviors (for example some representation attribute values like the Size attribute) may depend on the compiler used. By default, GNATprove adopts the same choices as the GNAT compiler. GNATprove also supports other compilers by providing special switches:

- -qnateT for specifying the target configuration
- --pedantic for warnings about possible implementation-defined behavior

Note that, even with switch --pedantic, GNATprove only detects some implementation-defined behaviors. For more details, see the dedicated section on how to *Ensure Portability of Programs*.

Note that GNATprove will always choose the smallest multiple of 8 bits for the base type, which is a safe and conservative choice for any Ada compiler.

#### **Target Parameterization**

By default, GNATprove assumes that the compilation target is the same as the host on which it is run, for setting target dependent values, such as endianness or sizes and alignments of standard types. If your target is not the same as the

host on which you run GNATprove, you have to tell GNATprove the specificities of your target.

Note that specifying the Target attribute of project files is not enough for GNATprove. In addition, you need to add the following to your project file, under a scenario variable as seen in *Having Different Switches for Compilation and Verification*:

where target.atp is a file stored here in the same directory as the project file my\_project.gpr, which contains the target parametrization. The format of this file is described in the GNAT User's Guide as part of the -gnateT switch description.

Target parameterization can be used:

- to specify a target different than the host on which GNAT prove is run, when cross-compilation is used. If GNAT is the cross compiler, the configuration file can be generated by calling the compiler for your target with the switch -qnatet=target.atp. Otherwise, the target file should be generated manually.
- to specify the parameters for a different compiler than GNAT, even when the host and target are the same. In that case, the target file should be generated manually.

Here is an example of a configuration file for a bare board PowerPC 750 processor configured as big-endian:

```
Bits BE
                           1
Bits_Per_Unit
                           8
Bits_Per_Word
                           32
Bytes_BE
                           1
Char_Size
                           8
Double_Float_Alignment
                           0
Double_Scalar_Alignment
                           0
Double_Size
                          64
Float Size
                          32
Float_Words_BE
                           1
                          32
Int_Size
Long_Double_Size
                          64
Long_Long_Size
                          64
Long_Size
                          32
Maximum_Alignment
                          16
Max_Unaligned_Field
Pointer_Size
                          32
Short_Enums
                           Ω
Short_Size
                          16
__
Strict_Alignment
                          1
System_Allocator_Alignment
                          8
Wchar_T_Size
                          32
Words_BE
                           1
float
             6 I 32 32
```

```
double 15 I 64 64
long double 15 I 64 64
```

### 7.1.5 Using CodePeer Static Analysis

**Note:** CodePeer is only available in SPARK Pro. It is not available in the following SPARK releases:

- the Community release
- · SPARK Discovery
- on the MacOS X operating system

CodePeer is a static analysis tool developed and commercialized by AdaCore (see http://www.adacore.com/codepeer). GNATprove supports using CodePeer as an additional source for the proof of checks, by specifying the command line option <code>--codepeer=on</code>. CodePeer will be run before automatic provers. If it proves a check, GNATprove will not attempt to run another prover on this check.

When run by GNATprove, CodePeer does not attempt to generate preconditions, and relies instead on user-provided preconditions for its analysis. CodePeer analysis inside GNATprove is sound, in that it does not allow to prove a check that could fail. CodePeer analysis may allow to prove more properties than the strict contract-based reasoning performed in SPARK allow in general:

- 1. CodePeer generates a sound approximation of data dependencies for subprograms based on the implementation of subprograms and the call-graph relating subprograms. Hence CodePeer may be able to prove properties which cannot be deduced otherwise based on too coarse user-provided data dependencies.
- 2. CodePeer generates a sound approximation of loop invariants for loops. Hence CodePeer may be able to prove properties which cannot be deduced otherwise based on imprecise loop invariants, or in absence of a loop invariant.
- 3. CodePeer ignores the SPARK\_Mode pragma and aspects; in particular it uses information that is hidden from SPARK using pragma SPARK\_Mode (Off) or the equivalent aspect.

In addition, CodePeer is using the same choice as GNAT compiler for the rounding of fixed-point multiplication and division. This makes it more precise for the analysis of code compiled with GNAT. If some code using fixed-point arithmetic is compiled with another compiler than GNAT, and the code uses fixed-point multiplication or division, the choice of rounding made in CodePeer may not be suitable, in which case —codepeer=on should not be used.

CodePeer analysis is particularly interesting when analyzing code using floating-point computations, as CodePeer is both fast and precise for proving bounds of floating-point operations.

## 7.1.6 Running GNATprove from GPS

GNATprove can be run from GPS. When GNATprove is installed and found on your PATH, a *SPARK* menu is available with the following entries:

Submenu	Action
Examine All	This runs GNAT prove in flow analysis mode on all mains and the units they depend on in
	the project.
Examine All	This runs GNAT prove in flow analysis mode on all files in the project.
Sources	
Examine File	This runs GNAT prove in flow analysis mode on the current unit, its body and any subunits.
Prove All	This runs GNAT prove on all mains and the units they depend on in the project.
Prove All Sources	This runs GNATprove on all files in the project.
Prove File	This runs GNATprove on the current unit, its body and any subunits.
Show Report	This displays the report file generated by GNATprove.
Clean Proofs	This removes all files generated by GNATprove.

The three "Prove..." entries run GNATprove in the mode given by the project file, or in the default mode "all" if no mode is specified.

The menus  $SPARK \to Examine/Prove\ All\ run\ GNAT$  prove on all main files in the project, and all files they depend on (recursively). Both main files in the root project and in projects that are included in the root project are considered. The menus  $SPARK \to Examine/Prove\ All\ Sources\ run\ GNAT$  prove on all files in all projects. On a project that has neither main files nor includes other projects, menus  $SPARK \to Examine/Prove\ All\ and\ SPARK \to Examine/Prove\ All\ Sources\ are\ equivalent.$ 

Keyboard shortcuts for these menu items can be set using the  $Edit \rightarrow Preferences$  dialog in GPS, and opening the  $General \rightarrow Key Shortcuts$  section.

**Note:** The changes made by users in the panels raised by these submenus are persistent from one session to the other. Be sure to check that the selected checkboxes and additional switches that were previously added are still appropriate.

When editing an Ada file, GNATprove can also be run from a *SPARK* contextual menu, which can be obtained by a right click:

Submenu	Action
Examine	This runs GNATprove in flow analysis mode on the current unit, its body and any subunits.
File	
Examine	This runs GNATprove in flow analysis mode on the current subprogram.
Subprogram	
Prove File	This runs GNATprove on the current unit, its body and any subunits.
Prove	This runs GNATprove on the current subprogram.
Subprogram	
Prove Line	This runs GNATprove on the current line.
Prove	This runs GNATprove on the currently selected region.
Selected	
Region	
Prove	This runs GNATprove on the current failing condition. GNATprove must have been run at least
Check	once for this option to be available in order to know which conditions are failing.

Except from *Examine File* and *Prove File*, all other submenus are also applicable to code inside generic units, in which case the corresponding action is applied to all instances of the generic unit in the project. For example, if a generic unit is instantiated twice, selecting *Prove Subprogram* on a subprogram inside the generic unit will apply proof to the two corresponding subprograms in instances of the generic unit.

The menus  $SPARK \rightarrow Examine$  ... open a panel which allows setting various switches for GNATprove's analysis. The main choice offered in this panel is to select the mode of analysis, among modes <code>check\_all</code> and <code>flow</code> (the default).

The menus  $SPARK \rightarrow Prove$  ... open a panel which allows setting various switches for GNATprove's analysis. By default, this panel offers a few simple choices, like the proof level (see description of switch --level in Running

GNATprove from the Command Line). If the user changes its User profile for SPARK (in the SPARK section of the Preferences dialog - menu  $Edit \rightarrow Preferences$ ) from Basic to Advanced, then a more complex panel is displayed for proof, with more detailed switches.

GNAT prove project switches can be edited from the panel GNAT prove (menu  $Edit \rightarrow Project \ Properties$ , in the  $Build \rightarrow Switches$  section of the dialog).

When proving a check fails on a specific path through a subprogram (for both checks verified in flow analysis and in proof), GNATprove may generate path information for the user to see. The user can display this path in GPS by clicking on the icon to the left of the failed proof message, or to the left of the corresponding line in the editor. The path is hidden again when re-clicking on the same icon.

For checks verified in proof, GNATprove may also generate counterexample information for the user to see (see *Understanding Counterexamples*). The user can display this counterexample in GPS by clicking on the icon to the left of the failed proof message, or to the left of the corresponding line in the editor. The counterexample is hidden again when re-clicking on the same icon.

A monospace font with ligature like Fira Code (https://github.com/tonsky/FiraCode) or Hasklig (https://github.com/i-tu/Hasklig) can be separately installed and selected to make contracts more readable inside GPS or GNATbench. See the following screenshot which shows how symbols like => (arrow) or >= (greater than or equal) are displayed in such a font:

```
10 y function LCP (A : Text; X, Y : Integer) return Natural with
11
      SPARK_Mode,
12
      Pre ⇒ X in A'Range and then Y in A'Range,
13
      Post \Rightarrow
        (for all K in 0 .. LCP'Result - 1 \Rightarrow A (X + K) = A (Y + K))
14
15
          and then (X + LCP'Result = A'Last + 1
16
                       or else Y + LCP'Result = A'Last + 1
                       or else A (X + LCP'Result) /= A (Y + LCP'Result)),
17
18
      Contract Cases ⇒
         (A (X) \neq A (Y) \Rightarrow LCP'Result = 0,
19
                           ⇒ LCP'Result = A'Last - X + 1,
20
          X = Y
                           ⇒ LCP'Result ≥ 0);
21
          others
```

### 7.1.7 Running GNATprove from GNATbench

GNATprove can be run from GNATbench. When GNATprove is installed and found on your PATH, a *SPARK* menu is available with the following entries:

Submenu	Action
Examine All	This runs GNAT prove in flow analysis mode on all mains and the units they depend on in
	the project.
Examine All	This runs GNAT prove in flow analysis mode on all files in the project.
Sources	
Examine File	This runs GNAT prove in flow analysis mode on the current unit, its body and any subunits.
Prove All	This runs GNAT prove on all mains and the units they depend on in the project.
Prove All Sources	This runs GNATprove on all files in the project.
Prove File	This runs GNATprove on the current unit, its body and any subunits.
Show Report	This displays the report file generated by GNATprove.
Clean Proofs	This removes all files generated by GNATprove.

The three "Prove..." entries run GNATprove in the mode given by the project file, or in the default mode "all" if no mode is specified.

The menus  $SPARK \to Examine/Prove\ All\ run\ GNAT$  prove on all main files in the project, and all files they depend on (recursively). Both main files in the root project and in projects that are included in the root project are considered. The menus  $SPARK \to Examine/Prove\ All\ Sources\ run\ GNAT$  prove on all files in all projects. On a project that has neither main files nor includes other projects, menus  $SPARK \to Examine/Prove\ All\ and\ SPARK \to Examine/Prove\ All\ Sources\ are equivalent.$ 

**Note:** The changes made by users in the panels raised by these submenus are persistent from one session to the other. Be sure to check that the selected checkboxes and additional switches that were previously added are still appropriate.

When editing an Ada file, GNATprove can also be run from a SPARK contextual menu, which can be obtained by a right click:

Submenu	Action
Examine File	This runs GNATprove in flow analysis mode on the current unit, its body and any
	subunits.
Examine	This runs GNATprove in flow analysis mode on the current subprogram.
Subprogram	
Prove File	This runs GNATprove on the current unit, its body and any subunits.
Prove Subprogram	This runs GNATprove on the current subprogram.
Prove Line	This runs GNATprove on the current line.

### 7.1.8 GNATprove and Manual Proof

When automated provers fail to prove some condition that is valid, the validity may be proved using manual proof inside GPS or an external interactive prover.

In the appendix, section *Alternative Provers*, is explained how to use different provers than the one GNATprove uses as default.

#### Calling an Interactive Prover From the Command Line

When the prover used by GNATprove is configured as interactive, for each analysed condition, either:

- It is the first time the prover is used on the condition then a file (containing the condition as input to the specified prover) is created in the project's proof directory (see *Project Attributes*). GNATprove outputs a message concerning this condition indicating the file that was created. The created file should be edited by the user in order to prove the condition.
- The prover has already been used on this condition and the editable file exists. The prover is run on the file and the success or failure of the proof is reported in the same way it is done with the default prover.

**Note:** Once a manual proof file is created and has been edited by the user, in order to run the prover on the file, the same prover must be once again specified to GNATprove. Once the condition is proved, the result will be saved in the why3 session so GNATprove won't need to be specified the prover again to know that the condition is valid.

Analysis with GNAT prove can be limited to a single condition with the --limit-line option:

```
gnatprove -P project-file.gpr> --prover=check-kind>
```

Please use the output of gnatprove ——list—categories to determine the check—kind to be provided in this command.

#### Calling an Interactive Prover From GPS

After running GNATprove with proof mode, the menu  $SPARK \rightarrow Prove\ Check$  is available by right-clicking on a check message in the location tab or by right-clicking on a line that fails because of a single condition (i.e. there is only one check in the output of GNATprove concerning this line).

In the dialog box, the field "Alternate prover" can be filled to use another prover than Alt-Ergo. If the alternative prover is configured as "interactive", after the execution of  $SPARK \rightarrow Prove\ Check$ , GPS opens the manual proof file with the editor corresponding to the prover under the condition that an editor is specified in the configuration of the alternative prover.

Once the editor is closed, GPS re-executes  $SPARK \rightarrow Prove\ Check$ . The user should verify the same alternative prover as before is still specified. After execution, GPS will offer to re-edit the file if the proof fails.

#### **Manual Proof Within GPS**

After running GNATprove with proof mode, the menu  $SPARK \rightarrow Start\ Manual\ Proof$  is available by right-clicking on a check message in the location tab.

The manual proof interface immediately starts. It will change the GPS window by adding a Manual Proof console, a Proof Tree and the current Verification Condition being dealt with. This is an experimental system that allows the user to directly visualize the condition given to the prover. We provide safe transformations that can be used to help the prover. For example, you can directly provide a value to an existential in the goal, perform an induction on an integer or instantiate hypothesis with values that should be used by the prover.

At first, you can type help in the Manual Proof console. This will return the available commands. The most useful commands to the beginner are list-provers and list-transforms. list-provers returns the list of provers available on your machine. You can use any of them on your goal by typing its name in the console. For example, one can type z3 to launch z3 on the current Verification Condition. list-transforms returns a list of transformations that can be used on the Verification Condition. You can then try transformations like assert (0 = 0). It will add two subgoals in the Proof Tree, one asking you to prove 0 = 0 and one assuming 0 = 0 to prove the current condition. The first one is easy, CVC4 should be able to solve it. The corresponding part of the Proof Tree switched to green because CVC4 proved the subgoal.

Once the goal is completely proved, you will get a popup window asking you if you want to save the session and exit. Answer yes and run GNATprove again on your file. The condition that was failing before should now be reported as checked. If you want to exit manual proof, you can select  $SPARK \rightarrow Exit Manual Proof$  in the menu. It is recommended to close it using the menu because it makes sure to close everything related to manual proof.

More details on how to use it are available in Manual Proof Using GPS.

### 7.1.9 How to Speed Up a Run of GNATprove

GNATprove can take some time on large programs with difficult checks to prove. This section describes how one can improve the running time of the GNATprove tool. Note that some of the suggested settings will decrease the number of proved checks or decrease usability of the tool, because spending more time often results in more successful proofs. You may still want to try some of the suggestions here to see if the time spent by GNATprove is really useful in your context.

These settings will speed up GNATprove:

• Use the -j switch to use more than one core on your machine. GNATprove can make efficient usage of multi-processing. If your machine has more than one processor or core, we strongly suggest to enable multi-processing, using the -j switch. This switch should not have an impact on proof results, only on running time.

- Use --no-loop-unrolling to deactivate loop unrolling. Loop unrolling can often avoid the use of a loop invariant, but it almost always will be more costly to analyze than a loop with a loop invariant. See also *Automatic Unrolling of Simple For-Loops*.
- Use --no-inlining to deactivate contextual analysis of local subprograms without contracts. This feature can often avoid the use of subprogram contracts, but it will be more costly to analyze such subprograms in their calling context than analyzing them separately. See also *Contextual Analysis of Subprograms Without Contracts*.
- Use --no-counterexample to deactive counterexamples. Counter-examples are very useful to understand the reason for a failed proof attempt. You can disable this feature if you are not working on a failed proof attempt.
- Use the --level switch to use a lower level and faster presets. Generally, a lower level is faster than higher levels. See also *Running GNAT prove from the Command Line*.
- More fine-grained than the --level switch, you can directly set the --prover, --timeout and --steps options. Using only one prover with a small timeout or a small steps limit will result in much faster execution.

### 7.1.10 GNATprove and Network File Systems or Shared Folders

On Linux and Mac-OS, GNATprove needs to create a Unix domain socket file. This might be a problem if GNATprove attempts to create such a file in a directory that is a shared folder or on a network file system like NFS, which does not support such folders. To minimize changes for this to occur, GNATprove determines the folder to create that special file as follows:

- if the environment variable TMPDIR is set, and the corresponding directory exists and is writeable, use that;
   otherwise.
- if /tmp exists and is writable, use that; otherwise,
- use the gnatprove subfolder of the object directory of the root project.

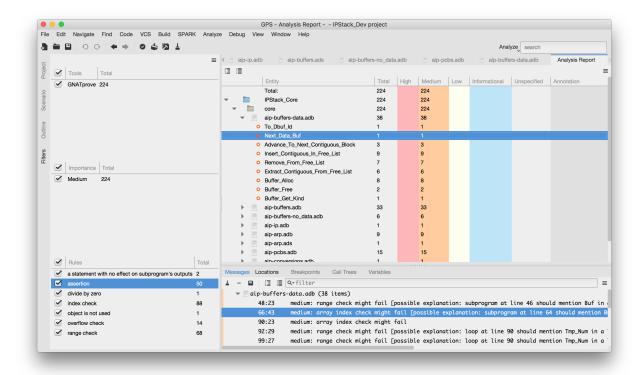
# 7.2 How to View GNATprove Output

GNAT prove produces two kinds of outputs: the one which is echoed to standard output or displayed in your IDE (GPS or GNAT bench), and a textual summary of the analysis results.

### 7.2.1 The Analysis Report Panel

GPS can display an interactive view reporting the results of the analysis, with a count of issues per file, subprogram and severity, as well as filters to selectively view a subset of the issues only. This interactive view is displayed using the menu  $SPARK \rightarrow Show\ Report$ . This menu becomes available after the checkbox Display analysis report is checked in the SPARK section of the Preferences dialog - menu  $Edit \rightarrow Preferences$ , and only if GNAT prove was run so that there are results to display.

Here is an example of this view:



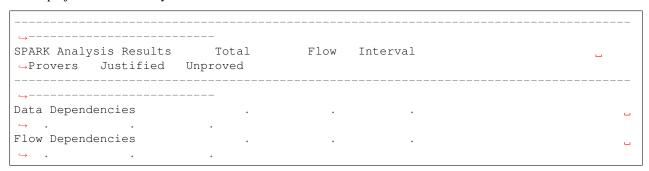
### 7.2.2 The Analysis Results Summary File

GNATprove generates global project statistics in file gnatprove.out, which can be displayed in GPS using the menu  $SPARK \rightarrow Show\ Log$ . The file gnatprove.out is generated in the gnatprove subdirectory of the object directory of the project.

When switch --output-header is used, this file starts with a header containing extra information about the run including:

- The date and time of GNATprove run
- The GNATprove version that has generated this report
- The host for which GNATprove is configured (e.g. Windows 32 bits)
- The full command-line of the GNAT prove invocation, including project file
- The GNAT prove switches specified in the project file

A summary table at the start of file gnatprove.out provides an overview of the verification results for all checks in the project. The table may look like this:



Initialization		2100	2079	•					
↔ .		21							
Non-Aliasing									
<b>⇔</b> •									
Run-time Checks		596			480	(altergo	31%,	CVC4	
<b>→</b> 69% <b>)</b>		116							
Assertions		3			3	(altergo	33%,	CVC4	]
→ 67%)									
Functional Contra	acts	323			168	(altergo	24%,	CVC4	ш
<b>→</b> 76%)		155							
LSP Verification									
<b>↔</b> .									
<b>⇔</b>									
Total		3022	2079 (69%)					651	7
<b>⇔ (</b> 22% <b>)</b>	•	292 (9%)							

The following table explains the lines of the summary table:

Line Description	Explanation		
Data Dependencies	Verification of Data Dependencies and parameter modes		
Flow Dependencies	Verification of Flow Dependencies		
Initialization	Verification of Data Initialization Policy		
Non-Aliasing	Verification of Absence of Interferences		
Run-time Checks	Verification of absence of run-time errors (AoRTE) (except those raising		
	Storage_Error)		
Assertions	Verification of Assertion Pragmas		
Functional Contracts	Verification of functional contracts (includes Subprogram Contracts, Package Contracts		
	and Type Contracts)		
LSP Verification	Verification related to Object Oriented Programming and Liskov Substitution Principle		

We now explain the columns of the table.

- The Total column describes the total number of checks in this category.
- The Flow column describes the number of checks proved by flow analysis.
- The Interval column describes the number of checks (overflow and range checks) proved by a simple static analysis of bounds for floating-point expressions based on type bounds of sub-expressions.
- The Provers column describes the number of checks proved by automatic or manual provers. The column also gives information on the provers used, and the percentage of checks proved by each prover. Note that sometimes a check is proved by a combination of provers, hence the use of percentage instead of an absolute count. Also note that generally the prover which is run first (as determined by the --prover command line switch) proves the most checks, because each prover is called only on those checks that were not previously proved. The prover percentages are provided in alphabetical order.
- The Justified column contains the number of checks for which the user has provided a *Direct Justification* with *Pragma Annotate*.
- Finally, the column Unproved counts the checks which have neither been proved nor justified.

After the summary table, a line states the maximal steps that were consumed by automated provers. The line may look like this:

```
max steps used for successful proof: 1234
```

The use of this line is to help with reproducability of a run of GNAT prove that proved all checks and properties. If the user provides the given number via the --steps option to GNAT prove, and disables the time and memory limits,

(if enabled directly or indirectly such as via the --level switch), then GNATprove will again prove all checks and properties. For example, if a user has proved all checks in a project using an invocation of GNATprove as follows:

then the following command will also prove all checks:

```
gnatprove -P ctfile> --level=2 --timeout=0 --memlimit=0 --steps=1234
```

The next contents in the file are statistics describing:

- which units were analyzed (with flow analysis, proof, or both)
- which subprograms in these units were analyzed (with flow analysis, proof, or both)
- the results of this analysis

### 7.2.3 Categories of Messages

GNAT prove issues four different kinds of messages: errors, warnings, check messages and information messages.

- Errors are issued for SPARK violations or other language legality problems, or any other problem which does not allow to proceed to analysis. Errors cannot be suppressed and must be fixed to proceed with analysis.
- Warnings are issued for any suspicious situation like unused values of variables, useless assignments, etc. Warnings are prefixed with the text "warning: " and can be suppressed with pragma Warnings, see section Suppressing Warnings.
- Check messages are issued for any potential problem in the code which could affect the correctness of the program, such as missing initialization, possible failing run-time checks or unproved assertions. Checks come with a severity, and depending on the severity the message text is prefixed with "low: ", "medium: " or "high: ". Check messages cannot be suppressed like warnings, but they can be individually justified with pragma Annotate, see section *Justifying Check Messages*.
- Information messages are issued to notify the user of limitations of GNAT prove on some constructs, or to prevent possible confusion in understanding the output of GNAT prove. They are also issued to report proved checks in some modes of GNAT prove.

### 7.2.4 Effect of Mode on Output

GNATprove can be run in four different modes, as selected with the switch --mode=<mode>, whose possible values are check, check\_all, flow, prove and all (see *Running GNATprove from the Command Line*). The output depends on the selected mode.

In modes check and check\_all, GNATprove prints on the standard output a list of error messages for violations of SPARK restrictions on all the code for which SPARK\_Mode is On.

In modes flow and prove, this checking is done as a first phase.

In mode flow, GNATprove prints on the standard output messages for possible reads of uninitialized data, mismatches betwen the specified data dependencies and flow dependencies and the implementation, and suspicious situations such as unused assignments and missing return statements. These messages are all based on flow analysis.

In mode prove, GNATprove prints on the standard output messages for possible reads of uninitialized data (using flow analysis), possible run-time errors and mismatches between the specified functional contracts and the implementation (using proof).

In mode all, GNATprove prints on the standard output both messages for mode flow and for mode prove.

If switch --report=all, --report=provers or --report=statistics is specified, GNATprove additionally prints on the standard output information messages for proved checks.

### 7.2.5 Description of Messages

This section lists the different messages which GNATprove may output. Each message points to a very specific place in the source code. For example, if a source file file.adb contains a division as follows:

```
if X / Y > Z then ...
```

GNAT prove may output a message such as:

```
file.adb:12:37: medium: divide by zero might fail
```

where the division sign / is precisely on line 12, column 37. Looking at the explanation in the first table below, which states that a division check verifies that the divisor is different from zero, it is clear that the message is about Y, and that GNATprove was unable to prove that Y cannot be zero. The explanations in the table below should be read with the context that is given by the source location.

When switch ——cwe is used, a corresponding CWE id is included in the message when relevant. For example, on the example above, GNATprove will output a message such as:

```
file.adb:12:37: medium: divide by zero might fail [CWE 369]
```

Note that CWE ids are only included in check messages and warnings, never in information messages about proved checks. For more information on CWE, see the MITRE Corporation's Common Weakness Enumeration (CWE) Compatibility and Effectiveness Program (http://cwe.mitre.org/). The current version of GNATprove is based on CWE version 3.2 released on January 3, 2019.

### Messages reported by Proof

Message Kind	CWE	Explanation
run-time checks		
divide by zero	CWE 369	Check that the second operand of the division, mod or
		rem operation is different from zero.
index check	CWE 120	Check that the given index is within the bounds of the
		array.
overflow check	CWE 190	Check that the result of the given integer arithmetic
		operation is within the bounds of the base type.
fp_overflow check	CWE 739	Check that the result of the given floating point opera-
		tion is within the bounds of the base type.
range check	CWE 682	Check that the given value is within the bounds of the
		expected scalar subtype.
predicate check	CWE 682	Check that the given value respects the applicable type
		predicate.
predicate check on default value	CWE 682	Check that the default value for the type respects the
		applicable type predicate.
null pointer dereference	CWE 476	Check that the given pointer is not null so that it can
		be dereferenced.
null exclusion		Check that the subtype_indication of the allocator
		does not specify a null_exclusion
		Continued on next page

Table 7.1 – continued from previous page

Message Kind	<ul><li>continued from pr</li><li>CWE</li></ul>	Explanation
length check		Check that the given array is of the length of the ex-
6		pected array subtype.
discriminant check	CWE 136	Check that the discriminant of the given discriminated
distriminant check	0112130	record has the expected value. For variant records, this
		can happen for a simple access to a record field. But
		there are other cases where a fixed value of the dis-
		criminant is required.
tag check	CWE 136	Check that the tag of the given tagged object has the
ing theth	0112130	expected value.
ceiling priority in Interrupt_Priority		Check that the ceiling priority specified for a pro-
		tected object containing a procedure with an aspect At-
		tach_Handler is in Interrupt_Priority.
use of an uninitialized variable	CWE 457	Check that a variable is initialized
interrupt is reserved		Check that the interrupt specified by Attach_Handler
		is not reserved.
invariant check		Check that the given value respects the applicable type
		invariant.
invariant check on default value		Check that the default value for the type respects the
		applicable type invariant.
ceiling priority protocol		Check that the ceiling priority protocol is respected,
		i.e., when a task calls a protected operation, the active
		priority of the task is not higher than the priority of the
		protected object (Ada RM Annex D.3).
task termination		Check that the task does not terminate, as required by
		Ravenscar.
assertions		
initial condition		Check that the initial condition of a package is true
mittai condition		after elaboration.
default initial condition		Check that the default initial condition of a type is true
default fillitial colldition		after default initialization of an object of the type.
precondition		Check that the precondition aspect of the given call
precondition		evaluates to True.
precondition of main		Check that the precondition aspect of the given main
precondition of main		procedure evaluates to True after elaboration.
postcondition		Check that the postcondition aspect of the subprogram
posicondition		evaluates to True.
refined postcondition		Check that the refined postcondition aspect of the sub-
remed postcondition		program evaluates to True.
		Check that all cases of the contract case evaluate to
contract case		
contract case		
		true at the end of the subprogram.
contract case disjoint contract cases		true at the end of the subprogram.  Check that the cases of the contract cases aspect are all
disjoint contract cases		true at the end of the subprogram.  Check that the cases of the contract cases aspect are all mutually disjoint.
		true at the end of the subprogram.  Check that the cases of the contract cases aspect are all mutually disjoint.  Check that the cases of the contract cases aspect cover
disjoint contract cases		true at the end of the subprogram.  Check that the cases of the contract cases aspect are all mutually disjoint.  Check that the cases of the contract cases aspect cover the state space that is allowed by the precondition as-
disjoint contract cases  complete contract cases		true at the end of the subprogram.  Check that the cases of the contract cases aspect are all mutually disjoint.  Check that the cases of the contract cases aspect cover the state space that is allowed by the precondition aspect.
disjoint contract cases		true at the end of the subprogram.  Check that the cases of the contract cases aspect are all mutually disjoint.  Check that the cases of the contract cases aspect cover the state space that is allowed by the precondition aspect.  Check that the loop invariant evaluates to True on all
disjoint contract cases  complete contract cases  loop invariant		true at the end of the subprogram.  Check that the cases of the contract cases aspect are all mutually disjoint.  Check that the cases of the contract cases aspect cover the state space that is allowed by the precondition aspect.  Check that the loop invariant evaluates to True on all iterations of the loop.
disjoint contract cases  complete contract cases		true at the end of the subprogram.  Check that the cases of the contract cases aspect are all mutually disjoint.  Check that the cases of the contract cases aspect cover the state space that is allowed by the precondition aspect.  Check that the loop invariant evaluates to True on all

Table 7.1 – continued from previous page

Message Kind	CWE	Explanation
loop invariant after first iteration		Check that the loop invariant evaluates to True at each
		further iteration of the loop.
loop variant	CWE 835	Check that the given loop variant decreases/increases
		as specified during each iteration of the loop. This im-
		plies termination of the loop.
assertion		Check that the given assertion evaluates to True.
raised exception		Check that the raise statement can never be reached.
Inline_For_Proof annotation		Check that an Annotate pragma with the In-
		line_For_Proof identifier is correct.
Liskov Substitution Principle		
precondition weaker than class-wide precondition		Check that the precondition aspect of the subprogram
		is weaker than its class-wide precondition.
precondition not True while class-wide precondition is True		Check that the precondition aspect of the subprogram
		is True if its class-wide precondition is True.
postcondition stronger than class-wide postcondition		Check that the postcondition aspect of the subprogram
		is stronger than its class-wide postcondition.
class-wide precondition weaker than overridden one		Check that the class-wide precondition aspect of the
		subprogram is weaker than its overridden class-wide
		precondition.
class-wide postcondition stronger than overridden one		Check that the class-wide postcondition aspect of the
		subprogram is stronger than its overridden class-wide
		postcondition.

## **Messages reported by Flow Analysis**

The following table shows all flow analysis messages, (E)rrors, (W)arnings and (C)hecks.

Message Kind	Class	CWE	Explanation
aliasing between subprogram parameters	С		Aliasing between formal parameters or global objects
dead code	W	CWE 561	A statement is never executed.
wrong Default_Initial_Condition aspect	С	CWE 457	A type is wrongly declared as initialized by default.
input item missing from the null dependency clause	С		An input item is missing from the null dependenc
			clause.
input item missing from the dependency clause	С		An input is missing from the dependency clause.
output item missing from the dependency clause	С		An output item is missing from the dependency clause
extra input item in the dependency clause	С		Extra input item in the dependency clause.
incomplete Global or Initializes contract	Е		A Global or Initializes contract fails to mention som
			objects.
an extra item in the Global or Initializes contract	С		A Global or Initializes contract wrongly mention
			some objects.
subprogram output depends on a Proof_In global	С		Subprogram output depends on a Proof_In global.
constants with variable inputs that is not a state con-	С		Constants with variable inputs that are not state cor
stituent			stituents.
illegal write of a global input	С		Illegal write of a global input.
a state abstraction that is impossible to initialize	С		A state abstraction that is impossible to initialize.
a statement with no effect on subprogram's outputs	W	CWE 1164	A statement with no effect on subprogram's outputs.
an extra item in the Initializes contract	С		An object that shall not appear in the Initializes cor
			tract
an IN OUT parameter or an In_Out global that is not	С		An IN OUT parameter or an In_Out global that is no
written			written.
all execution paths raise exceptions or do not return	С		All execution paths raise exceptions or do not return.
illegal write of an object declared as constant after	С		Illegal write of an object declared as constant after
elaboration			elaboration.
use of an abstract state of a package that was not yet	С		Use of an abstract state of a package that was not ye
elaborated			elaborated.
a missing pragma Elaborate_Body	С		A missing pragma Elaborate_Body.
constant with no variable inputs as an abstract state's	С		Constant with no variable inputs as an abstract state
constituent			constituent.
function with side effects	Е		A function with side effects.
loop with stable statement	W		A loop with stable statement.
use of an uninitialized variable	С	CWE 457	Flow analysis has detected the use of an uninitialize
			variable.
object is not used	W	CWE 563	A global or locally declared object is never used.
initial value of an object is not used	W	CWE 563	The initial value of an object is not used.
volatile function wrongly declared as non-volatile	С		A volatile function wrongly declared as non-volatile.
non-volatile function wrongly declared as volatile	С		A non-volatile function wrongly declared as volatile.
illegal reference to a global object in precondition of a	С		An illegal reference to global in precondition of a pro
protected operation			tected operation

**Note:** Certain messages emitted by flow analysis are classified as errors and consequently cannot be suppressed or justified.

Messages of a specific category or related to a specific CWE can be filtered inside GPS by typing the desired substring in the search bar of the Locations panel. For example, search for "CWE" to get all messages with a corresponding CWE, or "CWE 369" to get all messages related to division by zero vulnerability.

### 7.2.6 Understanding Counterexamples

When a check cannot be proved, GNATprove may generate a counterexample. A counterexample consists in two parts:

- a path (or set of paths) through the subprogram
- an assignment of values to variables that appear on that path

The best way to look at a counterexample is to display it in GPS by clicking on the icon to the left of the failed proof message, or to the left of the corresponding line in the editor (see *Running GNATprove from GPS*). GNATprove then displays the path in one color, and the values of variables on the path by inserting lines in the editor only (not in the file) which display these values. For example, consider procedure Counterex:

```
procedure Counterex (Cond : Boolean; In1, In2 : Integer; R : out Integer) with
       SPARK_Mode,
2
       \texttt{Pre} \implies \texttt{In1} \iff \texttt{25} \;\; \textbf{and} \;\; \texttt{In2} \iff \texttt{25}
    begin
5
        R := 0;
6
        if Cond then
            R := R + In1;
             if In1 < In2 then</pre>
                 R := R + In2;
                pragma Assert (R < 42);</pre>
11
            end if;
12
        end if:
13
    end Counterex;
```

The assertion on line 11 may fail when input parameter Cond is True and input parameters I1 and I2 are too big. The counterexample generated by GNATprove is displayed as follows in GPS, where each line highlighted in the path is followed by a line showing the value of variables from the previous line:

```
counterex.adb
 1 v procedure Counterex (Cond: Boolean; In1, In2: Integer; R: out Integ
         Cond = True and In1 = 17 and In2 = 25 and R = 0
 2
      SPARK Mode,
 3
      Pre \Rightarrow In1 \leq 25 and In2 \leq 25
 4
    is
 5
    begin
 6
       R := 0;
            R = 0
 7 ~
       if Cond then
 8
           R := R + In1;
               R = 17
 9
           if In1 < In2 then
10
              R := R + In2;
                  R = 42
11 🚇
              pragma Assert (R < 42);</pre>
                   R = 42
12
           end if;
13
       end if;
14
    end Counterex;
```

GNATprove also completes the message for the failed proof with an explanation giving the values of variables from the checked expression for the counterexample. Here, the message issued by GNATprove on line 11 gives the value of output parameter R:

```
counterex.adb:11:25: medium: assertion might fail, cannot prove R < 42 (e.g. when R = _{-} _{-}42)
```

The counterexample generated by GNATprove does not always correspond to a feasible execution of the program:

1. When some contracts or loop invariants are missing, thus causing the property to become unprovable (see details in section on *Investigating Unprovable Properties*), the counterexample may help point to the missing contract or loop invariant. For example, the postcondition of procedure <code>Double\_In\_Call</code> is not provable because the postcondition of the function <code>Double</code> that it calls is too weak, and the postcondition of procedure <code>Double\_In\_Loop</code> is not provable because its loop does not have a loop invariant:

```
package Counterex_Unprovable with
     SPARK_Mode
2
   is
       type Int is new Integer range -100 .. 100;
5
6
       function Double (X : Int) return Int with
         Pre => abs X <= 10,
9
         Post => abs Double'Result <= 20;
10
       procedure Double_In_Call (X : in out Int) with
11
         Pre \Rightarrow abs X \iff 10,
12
         Post \Rightarrow X = 2 * X'Old;
13
14
       procedure Double_In_Loop (X : in out Int) with
15
         Pre \Rightarrow abs X \iff 10,
16
         Post \Rightarrow X = 2 * X'Old;
17
18
   end Counterex_Unprovable;
19
```

```
package body Counterex_Unprovable with
2
     SPARK_Mode
   is
3
      function Double (X : Int) return Int is
5
      begin
          return 2 * X;
      end Double;
      procedure Double_In_Call (X : in out Int) is
10
      begin
11
          X := Double(X);
12
      end Double_In_Call;
13
14
      procedure Double_In_Loop (X : in out Int) is
15
          Result : Int := 0;
16
17
      begin
          for J in 1 \dots 2 loop
18
             Result := Result + X;
19
          end loop;
20
          X := Result;
21
      end Double_In_Loop;
22
```

```
end Counterex_Unprovable;
```

The counterexample generated by GNATprove in both cases shows that the prover could deduce wrongly that X on ouput is -3 when its value is 1 on input, due to a missing contract in the function called or a missing loop invariant the loop executed:

```
counterex_unprovable.adb:7:16: info: overflow check proved counterex_unprovable.adb:7:16: info: range check proved counterex_unprovable.adb:12:12: info: precondition proved counterex_unprovable.adb:19:27: info: range check proved counterex_unprovable.ads:8:14: info: overflow check proved counterex_unprovable.ads:9:14: info: overflow check proved counterex_unprovable.ads:9:14: info: postcondition proved counterex_unprovable.ads:12:14: info: overflow check proved counterex_unprovable.ads:13:14: medium: postcondition might fail, cannot prove X_ == 2 * X'old (e.g. when X = -1 and X'Old = 0) counterex_unprovable.ads:13:20: info: overflow check proved counterex_unprovable.ads:16:14: info: overflow check proved counterex_unprovable.ads:17:14: info: postcondition proved counterex_unprovable.ads:17:20: info: overflow check proved
```

- 2. When some property cannot be proved due to prover shortcomings (see details in section on *Investigating Prover Shortcomings*), the counterexample may explain why the prover cannot prove the property. However, note that since the counterexample is always generated only using CVC4 prover, it can just explain why this prover cannot prove the property. Also note that if CVC4 is not selected and generating of a counterexample is not disabled by --no-counterexample switch, a counterexample is still attempted to be generated using CVC4, but the proof result of CVC4 is not taken into account in this case.
- 3. When using a short value of timeout or steps, the prover may hit the resource bound before it has produced a full counterexample. In such a case, the counterexample produced may not correspond to a feasible execution.
- 4. When the value of --proof switch is per\_check (the default value), then the counterexample gives values to variables on all paths through the subprogram, not only the path which corresponds to the feasible execution. One can rerun GNATprove with value progressive or per\_path to separate possible execution paths in the counterexample.

# 7.3 How to Use GNATprove in a Team

The most common use of GNATprove is as part of a regular quality control or quality assurance activity inside a team. Usually, GNATprove is run every night on the current codebase, and during the day by developers either on their computer or on servers. For both nightly and daily runs, GNATprove results need to be shared between team members, either for viewing results or to compare new results with the shared results. These various processes are supported by specific ways to run GNATprove and share its results.

In all cases, the source code should not be shared directly (say, on a shared drive) between developers, as this is bound to cause problems with file access rights and concurrent accesses. Rather, the typical usage is for each user to do a check out of the sources/environment, and use therefore her own version/copy of sources and project files, instead of physically sharing sources across all users.

The project file should also always specify a local, non shared, user writable directory as object directory (whether explicitly or implicitly, as the absence of an explicit object directory means the project file directory is used as object directory).

#### 7.3.1 Possible Workflows

Multiple workflows allow to use GNATprove in a team:

- 1. GNATprove is run on a server or locally, and no warnings or check messages should be issued. Typically this is achieved by suppressing spurious warnings and justifying unproved check messages.
- 2. GNATprove is run on a server or locally, and textual results are shared in Configuration Management.
- 3. GNATprove is run on a server, and textual results are sent to a third-party qualimetry tool (like GNATdashboard, SonarQube, SQUORE, etc.)
- 4. GNATprove is run on a server or locally, and the GNATprove session files are shared in Configuration Management

In all workflows (but critically for the first workflow), messages can be suppressed or justified. Indeed, like every sound and complete verification tool, GNATprove may issue false alarms. A first step is to identify the type of message:

- warnings can be suppressed, see Suppressing Warnings
- check messages can be justified, see Justifying Check Messages

Check messages from proof may also correspond to provable checks, which require interacting with GNATprove to find the correct contracts and/or analysis switches, see *How to Investigate Unproved Checks*.

The textual output in workflow 3 corresponds to the compiler-like output generated by GNATprove and controlled with switches --report and --warnings (see *Running GNATprove from the Command Line*). By default messages are issued only for unproved checks and warnings.

The textual output in workflow 2 comprises this compiler-like output, and possibly additional output generated by GNATprove in file gnatprove.out (see *Effect of Mode on Output* and *Managing Assumptions*).

Workflow 4 requires sharing session files used by GNATprove to record the state of formal verification on each source package. This is achieved by specifying in the *Project Attributes* the Proof\_Dir proof directory, and sharing this directory under Configuration Management. To avoid conflicts, it is recommended that developers do not push their local changes to this directory in Configuration Management, but instead periodically retrieve an updated version of the directory. For example, a nightly run on a server, or a dedicated team member, can be responsible for updating the proof directory with the latest version generated by GNATprove.

A benefit of workflow 4 compared to other workflows is that it avoids reproving locally properties that were previously proved, as the shared session files keep track of which checks were proved.

### 7.3.2 Suppressing Warnings

GNAT prove issues two kinds of warnings, which are controlled separately:

- Compiler warnings are controlled with the usual GNAT compilation switches:
  - -gnatws suppresses all warnings
  - gnatwa enables all optional warnings
  - -gnatw? enables a specific warning denoted by the last character

See the GNAT User's Guide for more details. These should passed through the compilation switches specified in the project file.

- GNATprove specific warnings are controlled with switch --warnings:
  - --warnings=off suppresses all warnings
  - --warnings=error treats warnings as errors

- --warnings=continue issues warnings but does not stop analysis (default)

The default is that GNAT prove issues warnings but does not stop.

Both types of warnings can be suppressed selectively by the use of pragma Warnings in the source code. For example, GNATprove issues three warnings on procedure Warn, which are suppressed by the three pragma Warnings in the source code:

```
pragma Warnings (Off, "unused initial value of ""X""",
                    Reason => "Parameter mode is mandated by API");
2
   procedure Warn (X : in out Integer) with
     SPARK_Mode
5
6
      pragma Warnings (Off, "initialization has no effect",
7
                       Reason => "Coding standard requires initialization");
8
      Y : Integer := 0;
9
      pragma Warnings (On, "initialization has no effect");
10
11
   begin
12
      pragma Warnings (Off, "unused assignment",
13
                       Reason => "Test program requires double assignment");
14
      X := Y:
15
      pragma Warnings (On, "unused assignment");
      X := Y;
   end Warn;
```

Warnings with the specified message are suppressed in the region starting at pragma Warnings Off and ending at the matching pragma Warnings On or at the end of the file (pragma Warnings is purely textual, so its effect does not stop at the end of the enclosing scope). The Reason argument string is optional. A regular expression can be given instead of a specific message in order to suppress all warnings of a given form. Pragma Warnings Off can be added in a configuration file to suppress the corresponding warnings across all units in the project. Pragma Warnings Off can be specified for an entity to suppress all warnings related to this entity.

Pragma Warnings can also take a first argument of GNAT or GNAT prove to specify that it applies only to GNAT compiler or GNAT prove. For example, the previous example can be modified to use these refined pragma Warnings:

```
pragma Warnings (GNATprove, Off, "unused initial value of ""X""",
                    Reason => "Parameter mode is mandated by API");
2
3
   procedure Warn2 (X : in out Integer) with
4
     SPARK Mode
5
   is
6
      pragma Warnings (GNATprove, Off, "initialization has no effect",
                       Reason => "Coding standard requires initialization");
      Y : Integer := 0;
      pragma Warnings (GNATprove, On, "initialization has no effect");
10
11
   begin
12
      pragma Warnings (GNATprove, Off, "unused assignment",
13
                       Reason => "Test program requires double assignment");
14
15
      pragma Warnings (GNATprove, On, "unused assignment");
16
      X := Y;
17
   end Warn2;
```

Besides the documentation benefit of using this refined version of pragma Warnings, it makes it possible to detect useless pragma Warnings, that do not suppress any warning, with switch -gnatw.w. Indeed, this switch can then be used both during compilation with GNAT and formal verification with GNAT prove, as pragma Warnings that

apply to only one tool can be identified as such.

See the GNAT Reference Manual for more details.

Additionally, GNATprove can issue warnings as part of proof, on preconditions or postconditions or pragma Assume that are always false, dead code after loops and unreachable branches in assertions and contracts. These warnings are not enabled by default, as they require calling a prover for each potential warning, which incurs a small cost (1 sec for each property thus checked). They can be enabled with switch <code>--proof-warnings</code>, and their effect is controlled by switch <code>--warnings</code> and pragma <code>Warnings</code> as described previously.

Note that GNATprove, just like GNAT, suppresses warnings about unused variables if their name contains any of the substrings DISCARD, DUMMY, IGNORE, JUNK, UNUSED, in any casing.

### 7.3.3 Suppressing Information Messages

Information messages can be suppressed by the use of pragma Warnings in the source code, like for warnings.

### 7.3.4 Justifying Check Messages

GNATprove's analysis relies on the fact that, at any given point in the program, previous checks on any execution reaching that program point have been successful. Thus, given two successive assertions of the same property:

```
pragma Assert (Prop); -- possibly not proved
pragma Assert (Prop); -- proved
```

The second assertion will be reported as proved by GNATprove, even if the first assertion is reported as not proved. This is because any execution that fails the first assertion is not analyzed further by GNATprove.

Similarly, consider two successive calls to the same procedure with a precondition:

```
Proc (Args); -- precondition possibly not proved
Proc (Args); -- precondition proved
```

The precondition of the second call will be reported as proved by GNATprove, even if the precondition of the first call is reported as not proved. This is because any execution that fails the first precondition is not analyzed further by GNATprove.

This applies to all proof checks, and to a lesser extent to flow analysis checks. For example, outputs of a subprogram are considered fully initialtized in a caller, as explained in *Data Initialization Policy*. In particular, such outputs are considered to have values that respect the constraints of their type, which is used during proof.

Thus, the user should be careful when justifying check messages, as the incorrect justification of a check message that could fail could also hide other possible failures later for the same execution of the analyzed program.

#### **Direct Justification with Pragma Annotate**

Check messages generated by GNATprove's flow analysis or proof can be selectively justified by adding a pragma Annotate in the source code. For example, the check message about a possible division by zero in the return expression below can be justified as follows:

The pragma has the following form:

```
pragma Annotate (GNATprove, Category, Pattern, Reason);
```

where the following table explains the different entries:

Item	Explanation
GNATprove	is a fixed identifier
Category	is one of False_Positive or Intentional
Pattern	is a string literal describing the pattern of the check messages which shall be
	justified
Reason	is a string literal providing a justification for reviews

All arguments should be provided.

The Category currently has no impact on the behavior of the tool but serves a documentation purpose:

- False\_Positive indicates that the check cannot fail, although GNATprove was unable to prove it.
- Intentional indicates that the check can fail but that it is not considered to be a bug.

Pattern should be a substring of the check message to justify.

*Reason* is a string provided by the user as a justification for reviews. This reason may be present in a GNAT prove report.

Placement rules are as follows: in a statement list or declaration list, pragma Annotate applies to the preceding item in the list, ignoring other pragma Annotate. If there is no preceding item, the pragma applies to the enclosing construct. For example, if the pragma is the first element of the then-branch of an if-statement, it will apply to condition in the if-statement.

If the preceding or enclosing construct is a subprogram body, the pragma applies to both the subprogram body and the spec including its contract. This allows to place a justification for a check message issued by GNATprove either on the spec when it is relevant for callers. Note that this placement of a justification is ineffective on subprograms analyzed only in the context of their calls (see details in *Contextual Analysis of Subprograms Without Contracts*).

An aspect on a package or subprogram declaration/body can be used instead of a pragma at the beginning of the corresponding declaration list inside the declaration/body:

As a point of caution, the following placements of pragma Annotate will apply the pragma to a possibly large range of source lines:

- when the pragma appears in a statement list after a block, it will apply to the entire block (e.g. an if statement including all branches, or a loop including the loop body).
- when the pragma appears directly after a subprogram body, it will apply to the entire body and the spec of the subprogram.

Users should take care to not justify checks which were not intended to be justified, when placing pragma Annotate in such places.

or on the body when it is an implementation choice that need not be visible to users of the unit:

```
procedure Do_Something_2 (X, Y : in out Integer) with
Depends => ((X, Y) => (X, Y));
```

Pragmas Annotate of the form above that do not justify any check message are useless and result in a warning by GNATprove. Like other warnings emitted by GNATprove, this warning is treated like an error if the switch --warnings=error is set.

#### **Indirect Justification with Pragma Assume**

Check messages generated by GNATprove's proof can alternatively be justified indirectly by adding a *Pragma Assume* in the source code, which allows the check to be proved. For example, the check message about a possible integer overflow in the assignment statement below can be justified as follows:

Using pragma Assume is more powerful than using pragma Annotate, as the property assumed may be used to prove more than one check. Thus, one should in general use pragma Annotate rather than pragma Assume to justify simple runtime checks. There are some cases though where using a pragma Assume may be preferred. In particular:

• To keep assumptions local:

If the precondition of External\_Call changes, it may not be valid anymore to assume it here, though the assumption will stay True for the same reasons it used to be. Incompatible changes in the precondition of External\_Call will lead to a failure in the proof of External\_Call's precondition.

• To sum up what is expected from the outside world so that it can be reviewed easily:

Maintenance and review is easier with a single pragma Assume than if it is spread out into various pragmas Annotate. If the information is required at several places, the pragma Assume can be factorized into a procedure:

In general, assumptions should be kept as small as possible (only assume what is needed for the code to work). Indirect justifications with pragma Assume should be carefully inspected as they can easily introduce errors in the verification process.

### 7.3.5 Sharing Proof Results Via a Memcached Server

GNATprove can cache and share results between distinct runs of the tool, even across several computers, via a Memcached server. To use this feature, you need to setup a memcached server (see <a href="https://memcached.org/">https://memcached.org/</a>) on your network or on your local machine. Then, if you add the option <code>--memcached-server=hostname:portnumber</code> to your invocation of gnatprove (or use the <code>Switches</code> Attribute of the <code>Prove</code> Package of your project file), then caching will be used, and speedups should be observed in many cases.

#### 7.3.6 Managing Assumptions

Because GNATprove analyzes separately subprograms and packages, its results depend on assumptions about other subprograms and packages. For example, the verification that a subprogram is free from run-time errors depends on the property that all the subprograms it calls implement their specified contract. If a program is completely analyzed with GNATprove, GNATprove will report messages on those other subprograms, if they might not implement their contract correctly. But in general, a program is partly in SPARK and partly in other languages, mostly Ada, C and assembly languages. Thus, assumptions on parts of the program that cannot be analyzed with GNATprove need to be recorded for verification by other means, like testing, manual analysis or reviews.

When switch—assumptions is used, GNATprove generates information about remaining assumptions in its result file gnatprove.out. These remaining assumptions need to be justified to ensure that the desired verification objectives are met. An assumption on a subprogram may be generated in various cases:

- the subprogram was not analyzed (for example because it is marked SPARK\_Mode => Off)
- the subprogram was not completely verified by GNATprove (that is, some unproved checks remain)

Note that currently, only assumptions on called subprograms are output, and not assumptions on calling subprograms.

The following table explains the meaning of assumptions and claims which gnatprove may output:

Assumption	Explanation
effects on parameters and global variables	The subprogram does not read or write any other parameters or global variables
	than what is described in its spec (signature + data dependencies).
absence of run-time errors	The subprogram is free from run-time errors.
the postcondition	The postconditon of the subprogram holds after each call of the subprogram.

## 7.4 How to Write Subprogram Contracts

GNAT prove relies on contracts to perform its analysis. User-specified subprogram contracts are assumed to analyze a subprogram's callers, and verified when the body of the subprogram is analyzed.

By default, no contracts are compulsory in GNATprove. In the absence of user-provided contracts, GNATprove internally generates default contracts, which may or not be suitable depending on the verification objective:

• data dependencies (Global)

See *Generation of Dependency Contracts*. The generated contract may be exact when completed from user-specified flow dependencies (Depends), or precise when generated from a body in SPARK, or coarse when generated from a body in full Ada.

• flow dependencies (Depends)

See *Generation of Dependency Contracts*. The contract is generated from the user-specified or generated data dependencies, by considering that all outputs depend on all inputs.

• precondition (Pre)

A default precondition of True is used in absence of a user-specified precondition.

• postcondition (Post)

A default postcondition of True is used in absence of a user-specified postcondition, except for expression functions. For the latter, the body of the expression function is used to generate a matching postcondition. See *Expression Functions*.

Knowing which contracts to write depends on the specific verification objectives to achieve.

## 7.4.1 Generation of Dependency Contracts

By default, GNATprove does not require the user to write data dependencies (introduced with aspect Global) and flow dependencies (introduced with aspect Depends), as it can automatically generate them from the program.

This behavior can be disabled using the --no-global-generation switch, which means a missing data dependency is the same as Global => null. Note that this option also forces --no-inlining (see *Contextual Analysis of Subprograms Without Contracts*).

**Note:** GNATprove does not generate warning or check messages when the body of a subprogram does not respect a generated contract. Indeed, the generated contract is a safe over-approximation of the real contract, hence it is unlikely that the subprogram body respects it. The generated contract is used instead to verify proper initialization and respect of dependency contracts in the callers of the subprogram.

**Note:** Intrinsic subprograms such as arithmetic operations, and shift/rotate functions without user-provided functional contracts (precondition, postcondition or contract cases) are handled specially by GNATprove.

**Note:** The --no-global-generation switch makes GNATprove behave more like the previous SPARK 2005 tools, which makes this switch attractive for project trying to migrate to the new GNATprove tools, or for projects that maintain dual annotations.

#### **Auto Completion for Incomplete Contracts**

When only the data dependencies (resp. only the flow dependencies) are given on a subprogram, GNATprove completes automatically the subprogram contract with the matching flow dependencies (resp. data dependencies).

#### **Writing Only the Data Dependencies**

When only the data dependencies are given on a subprogram, GNATprove completes them with flow dependencies that have all outputs depending on all inputs. This is a safe over-approximation of the real contract of the subprogram, which allows to detect all possible errors of initialization and contract violation in the subprogram and its callers, but which may also lead to false alarms because it is imprecise.

Take for example procedures Add and Swap for which data dependencies are given, but no flow dependencies:

```
package Only_Data_Dependencies with
2
      SPARK_Mode
   is
3
       V : Integer;
4
       procedure Add (X : Integer) with
6
         Global => (In_Out => V);
7
8
       procedure Swap (X : in out Integer) with
9
         Global => (In_Out => V);
10
11
       procedure Call_Add (X, Y : Integer) with
12
         Global => (In\_Out => V),
13
         Depends \Rightarrow (V \Rightarrow + (X, Y));
14
15
       procedure Call_Swap (X, Y : in out Integer) with
16
         Global => (In_Out => V),
17
         Depends \Rightarrow (X \Rightarrow Y, Y \Rightarrow X, V \Rightarrow V);
18
19
   end Only_Data_Dependencies;
```

GNAT prove completes the contract of Add and Swap with flow dependencies that are equivalent to:

```
procedure Add (X : Integer) with
  Global => (In_Out => V),
  Depends => (V =>+ X);

procedure Swap (X : in out Integer) with
  Global => (In_Out => V),
  Depends => ((X, V) => (X, V));
```

Other flow dependencies with fewer dependencies between inputs and outputs would be compatible with the given data dependencies of Add and Swap. GNATprove chooses the contracts with the most dependencies. Here, this corresponds to the actual contract for Add, but to an imprecise contract for Swap:

```
package body Only_Data_Dependencies with
1
     SPARK Mode
2
3
   is
      procedure Add (X : Integer) is
4
      begin
         V := V + X;
      end Add;
8
      procedure Swap (X : in out Integer) is
9
          Tmp : constant Integer := V;
10
      begin
11
         V := X;
12
         X := Tmp;
13
      end Swap;
14
15
      procedure Call_Add (X, Y : Integer) is
16
      begin
17
         Add (X);
          Add (Y);
      end Call_Add;
20
21
      procedure Call_Swap (X, Y : in out Integer) is
22
      begin
23
          Swap (X);
24
          Swap (Y);
25
          Swap (X);
26
      end Call_Swap;
27
28
   end Only_Data_Dependencies;
```

This results in false alarms when GNAT prove verifies the dependency contract of procedure Call\_Swap which calls Swap, while it succeeds in verifying the dependency contract of Call\_Add which calls Add:

```
only_data_dependencies.ads:7:06: info: data dependencies proved only_data_dependencies.ads:10:06: info: data dependencies proved only_data_dependencies.ads:13:06: info: data dependencies proved only_data_dependencies.ads:14:06: info: flow dependencies proved only_data_dependencies.ads:17:06: info: data dependencies proved only_data_dependencies.ads:18:18: medium: missing dependency "X => V" only_data_dependencies.ads:18:18: medium: missing self-dependency "X => X" only_data_dependencies.ads:18:26: medium: missing dependency "Y => V" only_data_dependencies.ads:18:26: medium: missing self-dependency "Y => Y" only_data_dependencies.ads:18:34: medium: missing dependency "V => X" only_data_dependencies.ads:18:34: medium: missing dependency "V => Y"
```

The most precise dependency contract for Swap would be:

```
procedure Swap (X : in out Integer) with
Global => (In_Out => V),
Depends => (V => X, X => V);
```

If you add this precise contract in the program, then GNATprove can also verify the dependency contract of Call\_Swap.

Note that the generated dependency contracts are used in the analysis of callers, but GNATprove generates no warnings or check messages if the body of Add or Swap have fewer flow dependencies, as seen above. That's a difference between these contracts being present in the code or auto completed.

#### **Writing Only the Flow Dependencies**

When only the flow dependencies are given on a subprogram, GNAT prove completes it with the only compatible data dependencies.

Take for example procedures Add and Swap as previously, expect now flow dependencies are given, but no data dependencies:

```
package Only_Flow_Dependencies with
      SPARK_Mode
2
   is
3
       V : Integer;
       procedure Add (X : Integer) with
6
         Depends => (V => + X);
8
       procedure Swap (X : in out Integer) with
9
         Depends \Rightarrow (V \Rightarrow X, X \Rightarrow V);
10
11
       procedure Call_Add (X, Y : Integer) with
12
         Global => (In_Out => V),
13
         Depends \Rightarrow (V \Rightarrow (X, Y));
14
15
       procedure Call_Swap (X, Y : in out Integer) with
16
         Global => (In_Out => V),
17
         Depends \Rightarrow (X \Rightarrow Y, Y \Rightarrow X, V \Rightarrow V);
   end Only_Flow_Dependencies;
20
```

The body of the unit is the same as before:

```
package body Only_Flow_Dependencies with
2
     SPARK_Mode
   is
3
      procedure Add (X : Integer) is
4
      begin
         V := V + X;
      end Add;
      procedure Swap (X : in out Integer) is
9
         Tmp : constant Integer := V;
10
      begin
11
         V := X;
12
13
         X := Tmp;
14
       end Swap;
15
      procedure Call_Add (X, Y : Integer) is
16
      begin
17
         Add (X);
18
19
         Add (Y);
      end Call_Add;
21
      procedure Call_Swap (X, Y : in out Integer) is
22
      begin
23
          Swap (X);
24
25
          Swap (Y);
          Swap (X);
       end Call_Swap;
```

```
28
29 end Only_Flow_Dependencies;
```

GNAT prove verifies the data and flow dependencies of all subprograms, including Call\_Add and Call\_Swap, based on the completed contracts for Add and Swap.

#### **Precise Generation for SPARK Subprograms**

When no data or flow dependencies are given on a SPARK subprogram, GNATprove generates precise data and flow dependencies by using path-sensitive flow analysis to track data flows in the subprogram body:

- if a variable is written completely on all paths in a subprogram body, it is considered an output of the subprogram;
   and
- other variables that are written in a subprogram body are considered both inputs and outputs of the subprogram (even if they are not read explicitly, their output value may depend on their input value); and
- if a variable is only read in a subprogram body, it is considered an input of the subprogram; and
- all outputs are considered to potentially depend on all inputs.

#### **Case 1: No State Abstraction**

Take for example a procedure Set\_Global without contract which initializes a global variable V and is called in a number of contexts:

```
package Gen_Global with
SPARK_Mode
is
procedure Set_Global;

procedure Do_Nothing;

procedure Set_Global_Twice;
end Gen_Global;
```

```
package body Gen_Global with
     SPARK_Mode
2
   is
      V : Boolean;
      procedure Set_Global is
6
      begin
         V := True;
      end Set_Global;
10
      procedure Do_Nothing is
11
      begin
12
          null;
13
      end Do_Nothing;
14
15
      procedure Set_Global_Twice is
17
          Set_Global;
18
          Set_Global;
```

```
end Set_Global_Twice;
20
21
       procedure Set_Global_Conditionally (X : Boolean) with
22
         Global => (Output => V),
23
         Depends => (V => X)
24
25
       begin
26
          if X then
27
              Set_Global;
28
          else
29
             V := False;
30
          end if;
31
       end Set_Global_Conditionally;
32
33
   end Gen_Global;
```

GNAT prove generates data and flow dependencies for procedure Set\_Global that are equivalent to:

```
procedure Set_Global with
  Global => (Output => V),
  Depends => (V => null);
```

Note that the above contract would be illegal as given, because it refers to global variable V which is not visible at the point where Set\_Global is declared in gen\_global.ads. Instead, a user who would like to write this contract on Set\_Global would have to use abstract state.

That generated contract for Set\_Global allows GNATprove to both detect possible errors when calling Set\_Global and to verify contracts given by the user on callers of Set\_Global. For example, procedure Set\_Global\_Twice calls Set\_Global twice in a row, which makes the first call useless as the value written in V is immediately overwritten by the second call. This is detected by GNATprove, which issues two warnings on line 18:

```
gen_global.adb:18:07: warning: statement has no effect gen_global.adb:18:07: warning: unused assignment to "V" gen_global.adb:23:06: info: data dependencies proved gen_global.adb:23:28: info: initialization of "V" proved gen_global.adb:24:06: info: flow dependencies proved gen_global.ads:6:14: warning: subprogram "Do_Nothing" has no effect
```

Note that GNATprove also issues a warning on subprogram Do\_Nothing which has no effect, while it correctly analyzes that Set\_Global has an effect, even if it has the same signature with no contract as Do\_Nothing.

GNATprove also uses the generated contract for Set\_Global to analyze procedure Set\_Global\_Conditionally, which allows it to verify the contract given by the user for Set\_Global\_Conditionally:

```
procedure Set_Global_Conditionally (X : Boolean) with
Global => (Output => V),
Depends => (V => X)
```

#### Case 2: State Abstraction Without Dependencies

If an abstract state (see *State Abstraction*) is declared by the user but no dependencies are specified on subprogram declarations, then GNATprove generates data and flow dependencies which take abstract state into account.

For example, take unit Gen\_Global previously seen, where an abstract state State is defined for package Gen\_Abstract\_Global, and refined into global variable V in the body of the package:

```
package Gen_Abstract_Global with
     SPARK_Mode,
2
     Abstract_State => State
3
   is
4
      procedure Set_Global;
      procedure Set_Global_Twice;
      procedure Set_Global_Conditionally (X : Boolean) with
        Global => (Output => State),
10
        Depends => (State => X);
11
12
   end Gen_Abstract_Global;
```

```
package body Gen_Abstract_Global with
     SPARK_Mode,
2
     Refined_State => (State => V)
3
4
      V : Boolean;
5
6
      procedure Set_Global is
      begin
          V := True;
       end Set_Global;
11
      procedure Set_Global_Twice is
12
13
      begin
          Set_Global;
14
          Set_Global;
15
       end Set_Global_Twice;
16
17
       procedure Set_Global_Conditionally (X : Boolean) with
18
         Refined_Global => (Output => V),
19
         {\tt Refined\_Depends} \ => \ ({\tt V} \ => \ {\tt X})
20
21
      is
22
      begin
          if X then
             Set_Global;
24
          else
25
             V := False;
26
27
          end if:
28
       end Set_Global_Conditionally;
   end Gen_Abstract_Global;
```

We have chosen here to declare procedure Set\_Global\_Conditionally in gen\_abstract\_global.ads, and so to express its user contract abstractly. We could also have kept it local to the unit.

GNATprove gives the same results on this unit as before: it issues warnings for the possible error in Set\_Global\_Twice and it verifies the contract given by the user for Set\_Global\_Conditionally:

```
gen_abstract_global.adb:14:07: warning: statement has no effect
gen_abstract_global.adb:14:07: warning: unused assignment to "V" constituent of "State

""
gen_abstract_global.adb:19:36: info: initialization of "V" constituent of "State"

"proved
```

```
gen_abstract_global.ads:10:06: info: data dependencies proved
gen_abstract_global.ads:11:06: info: flow dependencies proved
```

#### **Case 3: State Abstraction Without Refined Dependencies**

If abstract state is declared by the user and abstract dependencies are specified on subprogram declarations, but no refined dependencies are specified on subprogram implementations (as described *State Abstraction and Dependencies*), then GNATprove generates refined data and flow dependencies for subprogram implementations.

For example, take unit Gen\_Abstract\_Global previously seen, where only abstract data and flow dependencies are specified:

```
package Gen_Refined_Global with
     SPARK_Mode,
2
3
     Abstract_State => State
   is
      procedure Set_Global with
5
        Global => (Output => State);
6
7
      procedure Set_Global_Twice with
        Global => (Output => State);
10
      procedure Set_Global_Conditionally (X : Boolean) with
11
        Global => (Output => State),
12
        Depends => (State => X);
13
14
   end Gen_Refined_Global;
```

```
package body Gen_Refined_Global with
     SPARK_Mode,
2
3
     Refined_State => (State => V)
4
5
      V : Boolean;
6
      procedure Set_Global is
      begin
          V := True;
      end Set_Global;
10
11
      procedure Set_Global_Twice is
12
      begin
13
14
          Set_Global;
          Set_Global;
      end Set_Global_Twice;
16
17
      procedure Set_Global_Conditionally (X : Boolean) is
18
19
      begin
         if X then
20
             Set_Global;
21
          else
22
             Set_Global;
23
          end if;
24
      end Set_Global_Conditionally;
25
26
   end Gen_Refined_Global;
```

GNATprove gives the same results on this unit as before: it issues warnings for the possible error in Set\_Global\_Twice and it verifies the contract given by the user for Set\_Global\_Conditionally:

```
gen_refined_global.adb:14:07: warning: statement has no effect gen_refined_global.adb:14:07: warning: unused assignment to "V" constituent of "State" gen_refined_global.ads:6:06: info: data dependencies proved gen_refined_global.ads:9:06: info: data dependencies proved gen_refined_global.ads:12:06: info: data dependencies proved gen_refined_global.ads:13:06: info: flow dependencies proved
```

Note that although abstract and refined dependencies are the same here, this is not always the case, and GNATprove will use the more precise generated dependencies to analyze calls to subprograms inside the unit.

#### Coarse Generation for non-SPARK Subprograms

When no data or flow dependencies are given on a non-SPARK subprogram, GNATprove generates coarser data and flow dependencies based on the reads and writes to variables in the subprogram body:

- if a variable is written in a subprogram body, it is considered both an input and an output of the subprogram; and
- if a variable is only read in a subprogram body, it is considered an input of the subprogram; and
- all outputs are considered to potentially depend on all inputs.

For example, take unit Gen\_Global previously seen, where the body of Set\_Global is marked with SPARK\_Mode => Off:

```
package Gen_Ada_Global with
SPARK_Mode
is
procedure Set_Global;
procedure Set_Global_Twice;
end Gen_Ada_Global;
```

```
package body Gen_Ada_Global with
     SPARK_Mode
2
3
      V : Boolean;
4
5
      procedure Set_Global with
6
         SPARK_Mode => Off
7
8
      begin
9
          V := True;
10
       end Set_Global;
11
12
      procedure Set_Global_Twice is
13
      begin
14
          Set_Global;
15
          Set_Global;
16
       end Set_Global_Twice;
17
       procedure Set_Global_Conditionally (X : Boolean) with
19
         Global => (Output => V),
20
         Depends => (V => X)
21
22
```

```
begin

if X then

Set_Global;

else

V := False;

end if;

end Set_Global_Conditionally;

end Gen_Ada_Global;
```

GNAT prove generates a data and flow dependencies for procedure Set\_Global that are equivalent to:

```
procedure Set_Global with
  Global => (In_Out => V),
  Depends => (V => V);
```

This is a safe over-approximation of the real contract for <code>Set\_Global</code>, which allows to detect all possible errors of initialization and contract violation in <code>Set\_Global</code> callers, but which may also lead to false alarms because it is imprecise. Here, <code>GNATprove</code> generates a wrong high message that the call to <code>Set\_Global</code> on line 25 reads an uninitialized value for <code>V</code>:

This is because the generated contract for Set\_Global is not precise enough, and considers V as an input of the procedure. Even if the body of Set\_Global is not in SPARK, the user can easily provide the precise information to GNATprove by adding a suitable contract to Set\_Global, which requires to define an abstract state State like in the previous section:

```
procedure Set_Global with
  Global => (Output => State),
  Depends => (State => null);
```

With such a user contract on Set\_Global, GNATprove can verify the contract of Set\_Global\_Conditionally without false alarms.

#### **Writing Dependency Contracts**

Since GNATprove generates data and flow dependencies, you don't need in general to add such contracts if you don't want to.

The main reason to add such contracts is when you want GNATprove to verify that the implementation respects specified data dependencies and flow dependencies. For those projects submitted to certification, verification of data coupling and input/output relations may be a required verification objective, which can be achieved automatically with GNATprove provided the specifications are written as contracts.

Even if you write dependency contracts for the publicly visible subprograms, which describe the services offered by the unit, there is no need to write similar contracts on internal subprograms defined in the unit body. GNATprove can generate data and flow dependencies on these.

Also, as seen in the previous section, the data and flow dependencies generated by GNATprove may be imprecise, in which case it is necessary to add manual contracts to avoid false alarms.

### 7.4.2 Writing Contracts for Program Integrity

The most common use of contracts is to ensure program integrity, that is, the program keeps running within safe boundaries. For example, this includes the fact that the control flow of the program cannot be circumvented (e.g. through a buffer overflow vulnerability) and that data is not corrupted (e.g. data invariants are preserved).

Preconditions can be written to ensure program integrity, and in particular they ensure:

- absence of run-time errors (AoRTE): no violations of language rules which would lead to raising an exception at run time (preconditions added to all subprograms which may raise a run-time error); and
- defensive programming: no execution of a subprogram from an unexpected state (preconditions added to subprograms in the public API, to guard against possible misuse by client units); and
- support of maintenance: prevent decrease in integrity (regressions, code rot) introduced during program evolution (preconditions added to internal subprograms, to guard against violations of the conditions to call these subprograms inside the unit itself); and
- invariant checking: ensure key data invariants are maintained throughout execution (preconditions added to all subprograms which may break the invariant).

For example, unit Integrity contains examples of all four kinds of preconditions:

- Precondition X >= 0 on procedure Seen\_One ensures AoRTE, as otherwise a negative value for X would cause the call to Update to fail a range check, as Update expects a non-negative value for its parameter.
- Precondition X < Y on procedure Seen\_Two ensures defensive programming, as the logic of the procedure is
  only correctly updating global variables Max1 and Max2 to the two maximal values seen if parameters X and Y
  are given in strictly increasing order.</li>
- Precondition X > Max2 on procedure Update ensures support of maintenance, as this internal procedure relies on this condition on its parameter to operate properly.
- Precondition Invariant on procedure Update ensures invariant checking, as the property that Max2 is less than Max1 expressed in Invariant should be always respected.

```
pragma Assertion_Policy (Pre => Check);
2
   package Integrity with
3
     SPARK Mode
4
   is
5
      procedure Seen_One (X : Integer) with
6
        Pre \Rightarrow X \Rightarrow 0; -- AORTE
7
8
      procedure Seen_Two (X, Y : Natural) with
9
         Pre => X < Y; -- defensive programming
10
11
   end Integrity;
12
```

```
package body Integrity with
     SPARK Mode
2
   is
     Max1 : Natural := 0; -- max value seen
     Max2 : Natural := 0; -- second max value seen
      function Invariant return Boolean is
        (Max2 \le Max1);
9
     procedure Update (X : Natural) with
10
11
       Pre => X > Max2 and then -- support of maintenance
                                     invariant checking
              Invariant
12
```

```
13
       begin
14
          if X > Max1 then
15
             Max2 := Max1;
             Max1 := X;
          elsif X < Max1 then</pre>
             Max2 := X;
19
          end if;
20
       end Update;
21
22
       procedure Seen_One (X : Integer) is
23
       begin
24
          if X > Max2 then
25
              Update (X);
26
          end if;
27
       end Seen_One;
28
29
       procedure Seen_Two (X, Y : Natural) is
       begin
31
          if X > Max1 then
32
             Max1 := Y;
33
             Max2 := X;
34
          elsif X > Max2 then
35
              Update (Y);
36
              Seen_One (X);
          else
38
              Seen_One (Y);
39
          end if;
40
       end Seen_Two;
41
42
   end Integrity;
```

Note that pragma Assertion\_Policy (Pre => Check) in integrity.ads ensures that the preconditions on the public procedures Seen\_One and Seen\_Two are always enabled at run time, while the precondition on internal subprogram Update is only enabled at run time if compiled with switch -gnata (typically set only for debugging or testing). GNATprove always takes contracts into account, whatever value of Assertion\_Policy.

GNATprove cannot verify that all preconditions on Integrity are respected. Namely, it cannot verify that the call to Update inside Seen\_One respects its precondition, as it is not known from the calling context that Invariant holds:

```
integrity.adb:26:10: medium: precondition might fail, cannot prove (Invariant) (e.g., when Max1 = 0 and Max2 = 1) [possible explanation: precondition of subprogram at integrity.ads:6 should mention Max1 and Max2] integrity.adb:26:18: info: range check proved integrity.adb:36:10: info: precondition proved integrity.adb:37:10: info: precondition proved integrity.adb:39:10: info: precondition proved
```

Note that, although Invariant is not required to hold either on entry to Seen\_Two, the tests performed in if-statements in the body of Seen\_Two ensure that Invariant holds when calling Update inside Seen\_Two.

To prove completely the integrity of unit Integrity, it is sufficient to add Invariant as a precondition and postcondition on every subprogram which modifies the value of global variables Max1 and Max2:

```
pragma Assertion_Policy (Pre => Check);

package Integrity_Proved with
```

```
SPARK_Mode
4
   is
5
      procedure Seen_One (X : Integer) with
6
       Pre \Rightarrow X \Rightarrow 0 and then -- AORTE
7
                Invariant, -- invariant checking
        Post => Invariant;
                                  -- invariant checking
10
      procedure Seen_Two (X, Y : Natural) with
11
        Pre => X < Y and then -- defensive programming
12
                                  -- invariant checking
               Invariant,
13
                                  -- invariant checking
        Post => Invariant;
14
15
16
      function Invariant return Boolean;
17
   end Integrity_Proved;
18
```

```
package body Integrity_Proved with
1
     SPARK_Mode
2
   is
3
      Max1 : Natural := 0; -- max value seen
4
      Max2 : Natural := 0; -- second max value seen
5
      function Invariant return Boolean is (Max2 <= Max1);</pre>
8
      procedure Update (X : Natural) with
9
        Pre => X > Max2 and then -- support of maintenance
10
                                     -- invariant checking
                Invariant,
11
                                    -- invariant checking
        Post => Invariant
12
      is
13
      begin
14
         if X > Max1 then
15
            Max2 := Max1;
16
             Max1 := X;
17
          elsif X < Max1 then</pre>
18
            Max2 := X;
19
          end if;
20
      end Update;
21
22
      procedure Seen_One (X : Integer) is
23
      begin
24
         if X > Max2 then
25
            Update (X);
26
         end if;
27
      end Seen_One;
28
29
      procedure Seen_Two (X, Y : Natural) is
30
      begin
31
         if X > Max1 then
32
            Max1 := Y;
            Max2 := X;
34
35
          elsif X > Max2 then
            Update (Y);
36
             Seen_One (X);
37
          else
38
             Seen_One (Y);
39
          end if;
40
41
      end Seen_Two;
42
```

```
end Integrity_Proved;
```

Here is the result of running GNATprove:

```
integrity_proved.adb:12:14: info: postcondition proved integrity_proved.adb:26:10: info: precondition proved integrity_proved.adb:26:18: info: range check proved integrity_proved.adb:36:10: info: precondition proved integrity_proved.adb:37:10: info: precondition proved integrity_proved.adb:39:10: info: precondition proved integrity_proved.adb:9:14: info: postcondition proved integrity_proved.ads:9:14: info: postcondition proved
```

### 7.4.3 Writing Contracts for Functional Correctness

Going beyond program integrity, it is possible to express functional properties of the program as subprogram contracts. Such a contract can express either partially or completely the behavior of the subprogram. Typical simple functional properties express the range/constraints for parameters on entry and exit of subprograms (encoding their *type-state*), and the state of the module/program on entry and exit of subprograms (encoding a safety or security automaton). For those projects submitted to certification, expressing a subprogram requirement or specification as a complete functional contract allows GNATprove to verify automatically the implementation against the requirement/specification.

For example, unit Functional is the same as Integrity\_Proved seen previously, with additional functional contracts:

- The postcondition on procedure Update (expressed as a Post aspect) is a complete functional description of the behavior of the subprogram. Note the use of an if-expression.
- The postcondition on procedure Seen\_Two (expressed as a Post aspect) is a partial functional description of the behavior of the subprogram.
- The postcondition on procedure Seen\_One (expressed as a Contract\_Cases aspect) is a complete functional description of the behavior of the subprogram. There are three cases which correspond to different possible behaviors depending on the values of parameter X and global variables Max1 and Max2. The benefit of expressing the postcondition as contract cases is both the gain in readability (no need to use 'Old for the guards, as in the postcondition of Update) and the automatic verification that the cases are disjoint and complete.

Note that global variables Max1 and Max2 are referred to through public accessor functions Max\_Value\_Seen and Second\_Max\_Value\_Seen. These accessor functions can be declared after the contracts in which they appear, as contracts are semantically analyzed only at the end of package declaration.

```
pragma Assertion_Policy (Pre => Check);
2
   package Functional with
3
     SPARK_Mode
4
      procedure Seen_One (X : Integer) with
6
        Pre \Rightarrow X \Rightarrow 0 and then -- AORTE
7
                Invariant,
                                        invariant checking
8
        Post => Invariant,
                                   -- invariant checking
9
                                   -- full functional
        Contract_Cases =>
10
          (X > Max_Value_Seen =>
11
             -- max value updated
             Max_Value_Seen = X and
13
             Second_Max_Value_Seen = Max_Value_Seen'Old,
14
           X > Second_Max_Value_Seen and
15
           X < Max_Value_Seen =>
```

```
-- second max value updated
17
             Max_Value_Seen = Max_Value_Seen'Old and
18
              Second_Max_Value_Seen = X,
19
           X = Max_Value_Seen or
20
           X <= Second_Max_Value_Seen =>
21
              -- no value updated
22
              Max_Value_Seen = Max_Value_Seen'Old and
23
              Second_Max_Value_Seen = Second_Max_Value_Seen'Old);
24
25
      procedure Seen_Two (X, Y : Natural) with
26
        Pre => X < Y and then
                                                -- defensive programming
27
                                                -- invariant checking
                 Invariant,
28
                                                -- invariant checking
        Post => Invariant and then
29
                 Max_Value_Seen > 0 and then -- partial functional
30
                 Max_Value_Seen /= Second_Max_Value_Seen;
31
32
      function Invariant return Boolean;
33
34
      function Max_Value_Seen return Integer;
35
36
      function Second_Max_Value_Seen return Integer;
37
38
   end Functional;
39
```

```
package body Functional with
1
     SPARK_Mode
2
3
   is
      Max1 : Natural := 0; -- max value seen
4
      Max2 : Natural := 0; -- second max value seen
5
6
      function Invariant return Boolean is (Max2 <= Max1);</pre>
7
      function Max_Value_Seen return Integer is (Max1);
Q
10
      function Second_Max_Value_Seen return Integer is (Max2);
11
12
      procedure Update (X : Natural) with
13
        Pre => X > Max2 and then
                                        -- support of maintenance
14
                                          -- invariant checking
                 Invariant.
15
        Post => Invariant and then
                                         -- invariant checking
16
                 (if X > Max1'Old then -- complete functional
17
                    Max2 = Max1'Old and Max1 = X
18
                  elsif X < Max1'Old then</pre>
19
                    Max2 = X and Max1 = Max1'Old
20
                  else
21
                    Max2 = Max2'Old and Max1 = Max1'Old)
22
23
      is
      begin
24
          if X > Max1 then
            Max2 := Max1;
26
            Max1 := X;
27
          elsif X < Max1 then</pre>
28
             Max2 := X;
29
          end if;
30
      end Update;
31
32
      procedure Seen_One (X : Integer) is
33
      begin
```

```
if X > Max2 then
35
             Update (X);
36
          end if:
37
       end Seen_One;
38
       procedure Seen_Two (X, Y : Natural) is
41
      begin
          if X > Max1 then
42
             Max1 := Y;
43
             Max2 := X;
44
          elsif X > Max2 then
45
              Update (Y);
              Seen_One (X);
47
48
              Seen_One (Y);
49
          end if;
50
       end Seen_Two;
51
   end Functional;
```

GNAT prove manages to prove automatically almost all of these functional contracts, except for the postcondition of Seen\_Two (note in particular the proof that the contract cases for Seen\_One on line 10 are disjoint and complete):

```
functional.adb:16:14: info: postcondition proved
functional.adb:36:10: info: precondition proved
functional.adb:36:18: info: range check proved
functional.adb:46:10: info: precondition proved
functional.adb:47:10: info: precondition proved
functional.adb:49:10: info: precondition proved
functional.adb:49:10: info: precondition proved
functional.ads:9:14: info: postcondition proved
functional.ads:10:06: info: complete contract cases proved
functional.ads:10:06: info: disjoint contract cases proved
functional.ads:11:28: info: contract case proved
functional.ads:16:28: info: contract case proved
functional.ads:21:36: info: contract case proved
functional.ads:31:14: medium: postcondition might fail, cannot prove Max_Value_Seen /

-= (Second_Max_Value_Seen) (e.g. when Max1 = Natural'Last and Max2 = Natural'Last)
```

The counterexample displayed for the postcondition not proved corresponds to a case where Max1 = Max2 = 2 on entry to procedure Seen\_Two. By highlighting the path for the counterexample in GPS (see *Running GNAT prove from GPS*), the values of parameters for this counterexample are also displayed, here X = 0 and Y = 1. With these values, Max1 and Max2 would still be equal to 2 on exit, thus violating the part of the postcondition stating that  $Max_Value_Seen$  /= Second\_Max\_Value\_Seen.

Another way to see it is to run GNATprove in mode per\_path (see *Running GNATprove from the Command Line* or *Running GNATprove from GPS*), and highlight the path on which the postcondition is not proved, which shows that when the last branch of the if-statement is taken, the following property is not proved:

The missing piece of information here is that Max1 and Max2 are never equal, except when they are both zero (the initial value). This can be added to function Invariant as follows:

```
function Invariant return Boolean is
  (if Max1 = 0 then Max2 = 0 else Max2 < Max1);</pre>
```

With this more precise definition for Invariant, all contracts are now proved by GNATprove:

```
functional_proved.adb:17:14: info: postcondition proved functional_proved.adb:37:10: info: precondition proved functional_proved.adb:37:18: info: range check proved functional_proved.adb:47:10: info: precondition proved functional_proved.adb:48:10: info: precondition proved functional_proved.adb:50:10: info: precondition proved functional_proved.ads:9:14: info: postcondition proved functional_proved.ads:10:06: info: complete contract cases proved functional_proved.ads:10:06: info: disjoint contract cases proved functional_proved.ads:11:28: info: contract case proved functional_proved.ads:16:28: info: contract case proved functional_proved.ads:21:36: info: contract case proved functional_proved.ads:21:36: info: contract case proved functional_proved.ads:29:14: info: postcondition proved
```

In general, it may be needed to further refine the preconditions of subprograms to be able to prove their functional postconditions, to express either specific constraints on their calling context, or invariants maintained throughout the execution.

### 7.4.4 Writing Contracts on Main Programs

Parameterless procedures and parameterless functions with Integer return type, that are in their own compilation unit, are identified by GNATprove as potential main subprograms. These subprograms are special because they can serve as an entry point to the program. If a main subprogram has a precondition, SPARK will generate a check that this precondition holds at the beginning of the execution of the main program, assuming the Initial\_Condition aspects of all with'ed packages.

Note that apart from this additional check, main subprograms behave like any other subprogram. They can be called from anywhere, and their preconditions need to be checked when they are called.

### 7.4.5 Writing Contracts on Imported Subprograms

Contracts are particularly useful to specify the behavior of imported subprograms, which cannot be analyzed by GNATprove. It is compulsory to specify in data dependencies the global variables these imported subprograms may read and/or write, otherwise GNATprove assumes null data dependencies (no global variable read or written).

**Note:** A subprogram whose implementation is not available to GNATprove, either because the corresponding unit body has not been developed yet, or because the unit body is not part of the files analyzed by GNATprove (see *Specifying Files To Analyze* and *Excluding Files From Analysis*), is treated by GNATprove like an imported subprogram.

**Note:** Intrinsic subprograms such as arithmetic operations and shift/rotate functions are handled specially by GNAT-prove. Except for shift/rotate operations with a user-provided functional contract (precondition, postcondition or contract cases) which are treated like regular functions.

For example, unit Gen\_Imported\_Global is a modified version of the Gen\_Abstract\_Global unit seen previously in *Generation of Dependency Contracts*, where procedure Set\_Global is imported from C:

```
package Gen_Imported_Global with

SPARK_Mode,
Abstract_State => State
is
procedure Set_Global with
```

```
Import,
6
        Convention => C,
7
        Global => (Output => State);
      procedure Set_Global_Twice;
10
11
      procedure Set_Global_Conditionally (X : Boolean) with
12
        Global => (Output => State),
13
        Depends => (State => X);
14
15
   end Gen_Imported_Global;
```

Note that we added data dependencies to procedure Set\_Global, which can be used to analyze its callers. We did not add flow dependencies, as they are the same as the auto completed ones (see *Auto Completion for Incomplete Contracts*).

```
with System.Storage_Elements;
2
   package body Gen_Imported_Global with
3
     SPARK_Mode,
4
     Refined_State => (State => V)
5
   is
6
      V : Boolean with
7
         Address => System.Storage_Elements.To_Address (16#8000_0000#);
      procedure Set_Global_Twice is
10
      begin
11
          Set_Global;
12
          Set_Global;
13
      end Set_Global_Twice;
14
15
      procedure Set_Global_Conditionally (X : Boolean) with
16
         Refined_Global => (Output => V),
17
         Refined_Depends \Rightarrow (V \Rightarrow X)
18
19
20
      begin
21
          if X then
             Set_Global;
22
          else
             V := False;
24
          end if;
25
      end Set_Global_Conditionally;
26
27
   end Gen_Imported_Global;
```

Note that we added an Address aspect to global variable V, so that it can be read/written from a C file.

GNATprove gives the same results on this unit as before: it issues warnings for the possible error in Set\_Global\_Twice and it verifies the contract given by the user for Set\_Global\_Conditionally:

```
gen_imported_global.adb:12:07: warning: statement has no effect
gen_imported_global.adb:12:07: warning: unused assignment to "V" constituent of "State

""
gen_imported_global.adb:17:36: info: initialization of "V" constituent of "State"

"proved
gen_imported_global.ads:13:06: info: data dependencies proved
gen_imported_global.ads:14:06: info: flow dependencies proved
```

It is also possible to add functional contracts on imported subprograms, which GNATprove uses to prove properties of their callers. It is compulsory to specify in a precondition the conditions for calling these imported subprograms without errors, otherwise GNATprove assumes a default precondition of True (no constraints on the calling context). One benefit of these contracts is that they are verified at run time when the corresponding assertion is enabled in Ada (either with pragma Assertion\_Policy or compilation switch -gnata).

**Note:** A subprogram whose implementation is not in SPARK is treated by GNATprove almost like an imported subprogram, except that coarse data and flow dependencies are generated (see *Coarse Generation for non-SPARK Subprograms*). In particular, unless the user adds a precondition to such a subprogram, GNATprove assumes a default precondition of True.

For example, unit Functional\_Imported is a modified version of the Functional\_Proved unit seen previously in *Writing Contracts for Functional Correctness*, where procedures Update and Seen\_One are imported from C:

```
pragma Assertion_Policy (Pre => Check);
2
   package Functional_Imported with
3
     SPARK_Mode,
4
5
     Abstract_State => Max_And_Snd,
     Initializes => Max_And_Snd
6
   is
7
      procedure Seen_One (X : Integer) with
8
9
        Import,
        Convention \Rightarrow C,
10
11
        Global => (In_Out => Max_And_Snd),
        Pre \Rightarrow X \Rightarrow 0 and then -- AORTE
12
                Invariant,
                                  -- invariant checking
13
        Post => Invariant,
                                    -- invariant checking
14
        Contract Cases =>
                                    -- full functional
15
           (X > Max_Value_Seen =>
16
              -- max value updated
17
             Max_Value_Seen = X and
18
              Second_Max_Value_Seen = Max_Value_Seen'Old,
19
           X > Second_Max_Value_Seen and
20
           X < Max Value Seen =>
21
              -- second max value updated
22
             Max_Value_Seen = Max_Value_Seen'Old and
23
              Second_Max_Value_Seen = X,
24
           X = Max_Value_Seen or
25
            X <= Second_Max_Value_Seen =>
26
              -- no value updated
27
              Max_Value_Seen = Max_Value_Seen'Old and
28
              Second_Max_Value_Seen = Second_Max_Value_Seen'Old);
29
30
      procedure Seen_Two (X, Y : Natural) with
31
        Pre => X < Y and then
                                                -- defensive programming
32
                 Invariant,
                                                   invariant checking
33
        Post => Invariant and then
                                                    invariant checking
34
                 Max_Value_Seen > 0 and then -- partial functional
35
                 Max_Value_Seen /= Second_Max_Value_Seen;
36
37
      function Invariant return Boolean;
      function Max_Value_Seen return Integer;
40
41
```

```
function Second_Max_Value_Seen return Integer;

end Functional_Imported;
```

```
with System.Storage_Elements;
2
   package body Functional_Imported with
     SPARK_Mode,
     Refined_State => (Max_And_Snd => (Max, Snd))
6
      Max : Natural := 0; -- max value seen
      for Max'Address use System.Storage_Elements.To_Address (16#8000_0000#);
      Snd : Natural := 0; -- second max value seen
10
      for Snd'Address use System.Storage_Elements.To_Address (16#8000_0004#);
11
12
      function Invariant return Boolean is
13
         (if Max = 0 then Snd = 0 else Snd < Max);
14
15
      function Max_Value_Seen return Integer is (Max);
17
      function Second_Max_Value_Seen return Integer is (Snd);
18
19
      procedure Update (X : Natural) with
20
        Import,
21
        Convention => C,
22
        Global => (In_Out => (Max, Snd)),
23
        Pre => X > Snd and then -- support of maintenance
24
                 Invariant,
                                            invariant checking
25
        Post => Invariant and then
                                        -- invariant checking
26
                 (if X > Max'Old then -- complete functional
27
                    Snd = Max'Old and Max = X
28
                  elsif X < Max'Old then</pre>
29
                    Snd = X and Max = Max'Old
                  else
31
                    Snd = Snd'Old and Max = Max'Old);
32
33
      procedure Seen_Two (X, Y : Natural) is
34
      begin
35
         if X > Max then
36
37
            Max := Y;
             Snd := X;
38
         elsif X > Snd then
39
            Update (Y);
40
             Seen_One (X);
41
         else
42
             Seen_One (Y);
         end if;
      end Seen_Two;
45
46
   end Functional_Imported;
```

Note that we added data dependencies to the imported procedures, as GNAT prove would assume otherwise incorrectly null data dependencies.

As before, all contracts are proved by GNATprove:

```
functional_imported.adb:40:10: info: precondition proved functional_imported.adb:41:10: info: precondition proved functional_imported.adb:43:10: info: precondition proved functional_imported.ads:6:03: info: flow dependencies proved functional_imported.ads:15:06: info: complete contract cases proved functional_imported.ads:15:06: info: disjoint contract cases proved functional_imported.ads:34:14: info: postcondition proved
```

#### 7.4.6 Contextual Analysis of Subprograms Without Contracts

It may be convenient to create local subprograms without necessarily specifying a contract for these. GNATprove attempts to perform a contextual analysis of these local subprograms without contract, at each call site, as if the code of the subprograms was inlined. Thus, the analysis proceeds in that case as if it had the most precise contract for the local subprogram, in the context of its calls.

Let's consider as previously a subprogram which adds two to its integer input:

```
package Arith_With_Local_Subp
with SPARK_Mode
is
procedure Add_Two (X : in out Integer) with
Pre => X <= Integer'Last - 2,
Post => X = X'Old + 2;
end Arith_With_Local_Subp;
```

And let's implement it by calling two local subprograms without contracts (which may or not have a separate declaration), which each increment the input by one:

```
package body Arith_With_Local_Subp
     with SPARK_Mode
2
   is
3
          Local procedure without external visibility
4
      procedure Increment_In_Body (X : in out Integer) is
         X := X + 1;
      end Increment_In_Body;
      procedure Add_Two (X : in out Integer) is
10
11
         -- Local procedure defined inside Add_Two
12
13
         procedure Increment_Nested (X : in out Integer) is
         begin
14
            X := X + 1;
15
         end Increment Nested;
16
17
      begin
18
         Increment_In_Body (X);
         Increment_Nested (X);
      end Add_Two;
21
22
   end Arith_With_Local_Subp;
```

GNATprove would not be able to prove that the addition in Increment\_In\_Body or Increment\_Nested cannot overflow in any context. If it was using only the default contract for these subprograms, it also would not prove

that the contract of Add\_Two is respected. But since it analyzes these subprograms in the context of their calls only, it proves here that no overflow is possible, and that the two increments correctly implement the contract of Add\_Two:

```
arith_with_local_subp.adb:7:14: info: overflow check proved, in call inlined at arith_
with_local_subp.adb:19
arith_with_local_subp.adb:15:17: info: overflow check proved, in call inlined at_
warith_with_local_subp.adb:20
arith_with_local_subp.ads:6:14: info: postcondition proved
arith_with_local_subp.ads:6:24: info: overflow check proved
```

This contextual analysis is available only for regular functions (not expression functions) or procedures that are not externally visible (not declared in the public part of the unit), without contracts (any of Global, Depends, Pre, Post, Contract\_Cases), and respect the following conditions:

- does not contain nested subprogram or package declarations or instantiations
- · not recursive
- · not a generic instance
- not defined in a generic instance
- has a single point of return at the end of the subprogram
- · not called in an assertion or a contract
- · not called in a potentially unevaluated context
- not called before its body is seen

If any of the above conditions is violated, GNATprove issues a warning to explain why the subprogram could not be analyzed in the context of its calls, and then proceeds to analyze it normally, using the default contract. Otherwise, both flow analysis and proof are done for the subprogram in the context of its calls.

Note that it is very simple to prevent contextual analysis of a local subprogram, by adding a contract to it, for example a simple Pre => True or Global => null. To prevent contextual analysis of all subprograms, pass the switch --no-inlining to GNATprove. This may be convenient during development if the ultimate goal is to add contracts to subprograms to analyze them separately, as contextual analysis may cause the analysis to take much more time and memory.

### 7.4.7 Subprogram Termination

GNATprove is only concerned with partial correctness of subprograms, that is, it only checks that the contract of a subprogram holds when it terminates normally. What is more, GNATprove will enforce that no exception will be raised at runtime. Together, these two points ensure that every SPARK subprogram formally verified using GNATprove will always return normally in a state that respects its postcondition, as long as it terminates.

In general, GNATprove does not attempt to verify termination of subprograms. It can be instructed to do so using a GNATprove specific Annotate pragma. On the following example, we instruct GNATprove that the five F functions should terminate:

```
package Terminating_Annotations with SPARK_Mode is

function F_Rec (X : Natural) return Natural;
pragma Annotate (GNATprove, Terminating, F_Rec);

function F_While (X : Natural) return Natural;
pragma Annotate (GNATprove, Terminating, F_While);

function F_Not_SPARK (X : Natural) return Natural;
```

```
pragma Annotate (GNATprove, Terminating, F_Not_SPARK);

procedure Not_SPARK (X : Natural);
function F_Call (X : Natural) return Natural;
pragma Annotate (GNATprove, Terminating, F_Call);

function F_Term (X : Natural) return Natural;
pragma Annotate (GNATprove, Terminating, F_Term);
end Terminating_Annotations;
```

If every subprogram in a package is terminating, the package itself can be annotated with the terminating annotation. If the annotation is located on a generic package, then it should be valid for every instance of the package.

An aspect can be used instead of a pragma for both packages and subprograms:

```
package Pack with
   Annotate => (GNATprove, Terminating)
is
   procedure Proc with
      Annotate => (GNATprove, Terminating);
...
```

If a subprogram in SPARK is explicitly annotated as terminating, flow analysis will attempt to make sure that all the paths through the subprogram effectively return. In effect, it will look for while loops with no loop variants, recursive calls and calls to subprograms which are not known to be terminating. If GNATprove cannot make sure that the annotated subprogram is always terminating, it will then emit a failed check. As an example, let us consider the following implementation of the five F functions:

```
package body Terminating_Annotations with SPARK_Mode is
2
      function F Rec (X : Natural) return Natural is
3
      begin
         if X = 0 then
             return 0;
          else
             return F_Rec (X - 1);
8
          end if;
      end F_Rec;
10
11
      function F_While (X : Natural) return Natural is
12
          Y : Natural := X;
13
      begin
14
         while Y > 0 loop
15
             Y := Y - 1;
16
          end loop;
17
          return Y;
18
      end F_While;
20
      function F_Not_SPARK (X : Natural) return Natural with SPARK_Mode => Off is
21
          Y : Natural := X;
22
      begin
23
          while Y > 0 loop
24
             Y := Y - 1;
25
          end loop;
          return Y;
27
      end F_Not_SPARK;
28
29
      procedure Not_SPARK (X : Natural) with SPARK_Mode => Off is
```

```
31
       begin
          null;
32
       end Not_SPARK;
33
34
       function F_Call (X : Natural) return Natural is
      begin
          Not_SPARK (X);
37
          return 0;
38
       end F_Call;
39
40
       function F_Term (X : Natural) return Natural is
41
          Y : Natural := X;
42
      begin
43
          Y := F_Rec (Y);
44
          Y := F_While (Y);
45
          Y := F_Not_SPARK (Y);
46
          Y := F_Call(Y);
47
          while Y > 0 loop
             pragma Loop_Variant (Decreases => Y);
50
             Y := Y - 1;
51
          end loop;
52
          return Y;
53
       end F_Term;
54
   end Terminating_Annotations;
```

As can be easily verified by review, all these functions terminate, and all return 0. As can be seen below, GNATprove will fail to verify that F\_Rec, F\_While, and F\_Call terminate.

Let us look at each function to understand what happens. The function F\_Rec is recursive, and the function F\_While contains a while loop. Both cases can theoretically lead to an infinite path in the subprogram, which is why GNATprove cannot verify that they terminate. GNATprove does not complain about not being able to verify the termination of F\_Not\_SPARK. Clearly, it is not because it could verify it, as it contains exactly the same loop as F\_While. It is because, as the body of F\_Not\_SPARK has been excluded from analysis using SPARK\_Mode => Off, GNATprove does not attempt to prove that it terminates. When looking at the body of F\_Call, we can see that it calls a procedure Not\_SPARK. Clearly, this procedure is terminating, as it does not do anything. But, as the body of No\_SPARK has been hidden from analysis using SPARK\_Mode => Off, GNATprove cannot deduce that it terminates. As a result, it stays in the safe side, and assumes that Not\_SPARK could loop, which causes the verification of F\_Call to fail. Finally, GNATprove is able to verify that F\_Term terminates, though it contains a while loop. Indeed, the number of possible iterations of the loop has been bounded using a Loop\_Variant. Also note that, though it was not able to prove termination of F\_Rec, F\_While, and F\_Call, GNATprove will still trust the annotation and consider them as terminating when verifying F\_Term.

**Note:** Possible nontermination of a subprogram may influence GNATprove proof capabilities. Indeed, to avoid soundness issues due to nontermination in logical formulas, GNATprove will not be able to see the contract of nonterminating functions if they are called from definitions of constants, from contracts, or from assertions. In such a case, an information message will be emitted, stating that (implicit) contracts of the function are not available for proof.

# 7.5 How to Write Object Oriented Contracts

Object Oriented Programming (OOP) may require the use of special *Class-Wide Subprogram Contracts* for dispatching subprograms, so that GNATprove can check Liskov Substitution Principle on every overriding subprogram.

### 7.5.1 Object Oriented Code Without Dispatching

In the special case where OOP is used without dispatching, it is possible to use the regular *Subprogram Contracts* instead of the special *Class-Wide Subprogram Contracts*.

For example, consider a variant of the Logging and Range\_Logging units presented in *Class-Wide Subprogram Contracts*, where no dispatching is allowed. Then, it is possible to use regular preconditions and postconditions as contracts, provided Log\_Type is publicly declared as an untagged private type in both units:

```
package Logging_No_Dispatch with
     SPARK_Mode
2
   is
      Max_Count : constant := 10_000;
      type Log_Count is range 0 .. Max_Count;
      type Log_Type is private;
      function Log_Size (Log : Log_Type) return Log_Count;
10
11
      procedure Init_Log (Log : out Log_Type) with
12
        Post => Log_Size (Log) = 0;
13
14
      procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
15
        Pre => Log_Size (Log) < Max_Count,
16
        Post => Log_Size (Log) = Log_Size (Log) 'Old + 1;
17
19
   private
20
      subtype Log_Index is Log_Count range 1 .. Max_Count;
21
      type Integer_Array is array (Log_Index) of Integer;
22
23
24
      type Log_Type is tagged record
25
         Log_Data : Integer_Array;
         Log_Size : Log_Count;
26
      end record;
27
28
      function Log_Size (Log : Log_Type) return Log_Count is (Log.Log_Size);
29
30
   end Logging_No_Dispatch;
```

```
with Logging_No_Dispatch; use Logging_No_Dispatch;

package Range_Logging_No_Dispatch with

SPARK_Mode

is

type Log_Type is private;
```

```
function Log_Size (Log : Log_Type) return Log_Count;
8
      function Log_Min (Log : Log_Type) return Integer;
10
11
      function Log_Max (Log : Log_Type) return Integer;
12
13
      procedure Init_Log (Log : out Log_Type) with
14
        Post => Log_Size (Log) = 0 and
15
                 Log_Min (Log) = Integer'Last and
16
                 Log_Max (Log) = Integer'First;
17
18
      procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
19
        Pre => Log_Size (Log) < Logging_No_Dispatch.Max_Count,
20
        Post => Log_Size (Log) = Log_Size (Log) 'Old + 1 and
21
                 Log_Min (Log) = Integer'Min (Log_Min (Log)'Old, Incr) and
22
                 Log_Max (Log) = Integer'Max (Log_Max (Log)'Old, Incr);
23
24
   private
25
26
      type Log_Type is tagged record
27
        Log : Logging_No_Dispatch.Log_Type;
28
        Min_Entry : Integer;
29
        Max_Entry : Integer;
30
      end record;
32
      function Log_Size (Log : Log_Type) return Log_Count is (Log_Size (Log.Log));
33
34
      function Log_Min (Log : Log_Type) return Integer is (Log.Min_Entry);
35
      function Log_Max (Log : Log_Type) return Integer is (Log.Max_Entry);
36
   end Range_Logging_No_Dispatch;
```

## 7.5.2 Writing Contracts on Dispatching Subprograms

Whenever dispatching is used, the contract that applies in proof to a dispatching call is the class-wide contract, defined as the first one present in the following list:

- 1. the class-wide precondition (resp. postcondition) attached to the subprogram
- 2. or otherwise the class-wide precondition (resp. postcondition) being inherited by the subprogram from the subprogram it overrides
- 3. or otherwise the default class-wide precondition (resp. postcondition) of True.

For abstract subprograms (on interfaces or regular tagged types), only a class-wide contract can be specified. For other dispatching subprograms, it is possible to specify both a regular contract and a class-wide contract. In such a case, GNATprove uses the regular contract to analyze static calls to the subprogram and the class-wide contract to analyze dispatching calls to the subprogram, and it checks that the specific contract is a refinement of the class-wide contract, as explained in *Mixing Class-Wide and Specific Subprogram Contracts*.

Let's consider the various cases that may occur when overridding a subprogram:

```
package Geometry with
SPARK_Mode
is
type Shape is tagged record
Pos_X, Pos_Y : Float;
```

```
end record;
6
7
      function Valid (S : Shape) return Boolean is
         (S.Pos_X in -100.0 .. 100.0 and S.Pos_Y in -100.0 .. 100.0);
10
      procedure Operate (S : in out Shape) with
11
        Pre'Class => Valid (S);
12
13
      procedure Set_Default (S : in out Shape) with
14
        Post'Class => Valid (S);
15
16
      procedure Set_Default_Repeat (S : in out Shape) with
17
        Post'Class => Valid (S);
18
19
      procedure Set_Default_No_Post (S : in out Shape);
20
21
      type Rectangle is new Shape with record
22
         Len_X, Len_Y : Float;
23
      end record;
24
25
      function Valid (S : Rectangle) return Boolean is
26
         (Valid (Shape (S)) and S.Len_X in 0.0 .. 10.0 and S.Len_Y in 0.0 .. 10.0);
27
28
      procedure Operate (S : in out Rectangle);
29
      procedure Set_Default (S : in out Rectangle);
31
32
      procedure Set_Default_Repeat (S : in out Rectangle) with
33
        Post'Class => Valid (S);
34
35
      procedure Set_Default_No_Post (S : in out Rectangle) with
        Post'Class => Valid (S);
38
   end Geometry;
```

In package Geometry, a type Shape is derived in a type Rectangle. A function Shape. Valid defines what it is to be a valid shape. It is overridden by Rectangle. Valid which defines what it is to be a valid rectangle. Here, a valid rectangle is also a valid shape, but that need not be the case. Procedure Set\_Default and its variants demonstrate the various configurations that can be found in practice:

- 1. The overridden subprogram Shape.Set\_Default defines a class-wide contract (here only a postcondition), which is inherited in the overriding subprogram Rectangle.Set\_Default. By the semantics of Ada, the postcondition of Shape.Set\_Default calls Shape.Valid, while the inherited postcondition of Rectangle.Set\_Default calls Rectangle.Valid.
- 2. Both the overridden subprogram Shape.Set\_Default\_Repeat and the overriding subprogram Rectangle.Set\_Default\_Repeat define a class-wide contract (here only a postcondition). Here, since the contract is simply repeated, this is equivalent to case 1 above of inheriting the contract: the postcondition of Shape.Set\_Default\_Repeat calls Shape.Valid, while the postcondition of Rectangle. Set\_Default\_Repeat calls Rectangle.Valid.
- 3. Only the overriding subprogram Rectangle.Set\_Default\_No\_Post defines a class-wide contract (here only a postcondition). The default class-wide postcondition of True is used for the overridden Shape. Set\_Default\_No\_Post.

In case 1, the overriding subprogram satisfies Liskov Substitution Principle by construction, so GNATprove emits no check in that case. Note that this is not the same as saying that Shape.Set\_Default and Rectangle. Set\_Default have the same contract: here the two postconditions differ, as one calls Shape.Valid, while the

other calls Rectangle. Valid.

In case 2, GNATprove checks that Liskov Substitution Principle is verified between the contracts of the overridden and the overriding subprograms. Here, it checks that the postcondition of Rectangle.Set\_Default\_Repeat is stronger than the postcondition of Shape.Set\_Default\_Repeat.

In case 3, GNATprove also checks that Liskov Substitution Principle is verified between the default contract of the overridden subprogram and the specified contract of the overriding subprograms. Here, only a postcondition is specified for Rectangle.Set\_Default\_No\_Post, so it is indeed stronger than the default postcondition of Shape. Set\_Default\_No\_Post.

Hence the results of GNATprove's analysis on this program:

```
geometry.ads:34:20: info: class-wide postcondition is stronger than overridden one geometry.ads:37:20: info: class-wide postcondition is stronger than overridden one
```

Let's consider now calls to these subprograms in procedure Use\_Geometry:

```
with Geometry; use Geometry;
2
   procedure Use_Geometry (S : in out Shape'Class) with
3
     SPARK Mode
4
   is
5
   begin
6
      S.Set_Default;
      S.Operate;
      S.Set_Default_Repeat;
10
      S.Operate;
11
12
      S.Set_Default_No_Post;
13
      S.Operate;
   end Use_Geometry;
```

Here are the results of GNATprove's analysis on this program:

```
use_geometry.adb:8:05: info: precondition proved use_geometry.adb:11:05: info: precondition proved use_geometry.adb:14:05: medium: precondition might fail, cannot prove Valid (S) → [possible explanation: call at line 13 should mention S (for argument S) in a → postcondition]
```

Parameter S is of class-wide type Shape'Class, so it can be dynamically of both types Shape or Rectangle. All calls on S are dispatching. In this program, GNATprove needs to check that the precondition of the calls to Operate is satisfied. As procedures Shape.Set\_Default and Shape.Set\_Default\_Repeat state precisely this condition in postcondition, the precondition to the calls to Operate that follow can be proved. As procedure Shape. Set\_Default\_No\_Post has no postcondition, the precondition to the last call to Operate cannot be proved. Note that these proofs take into account both possible types of S, for example:

- If S is dynamically a shape, then the call to Shape. Set\_Default on line 7 ensures that Shape. Valid holds, which ensures that the precondition to the call to Shape. Operate is satisfied on line 8.
- If S is dynamically a rectangle, then the call to Rectangle.Set\_Default on line 7 ensures that Rectangle.Valid holds, which ensures that the precondition to the call to Rectangle.Operate is satisfied on line 8.

## 7.5.3 Writing Contracts on Subprograms with Class-wide Parameters

Subprograms with class-wide parameters are not in general dispatching subprograms, hence they are specified through regular *Subprogram Contracts*, not *Class-Wide Subprogram Contracts*. Inside the regular contract, calls on primitive subprograms of the class-wide parameters are dispatching though, like in the code. For example, consider procedure More\_Use\_Geometry which takes four class-wide parameters of type Shape 'Class, which can all be dynamically of both types Shape or Rectangle:

```
with Geometry; use Geometry;
2
   procedure More_Use_Geometry (S1, S2, S3, S4 : in out Shape'Class) with
     SPARK Mode,
4
     Pre => S1.Valid
   is
6
   begin
7
      S1.Operate;
8
9
      if S2.Valid then
10
          S2.Operate;
11
      end if;
12
13
      S3.Set_Default;
14
      S3.Operate;
15
16
      S4.Operate;
17
   end More_Use_Geometry;
```

The precondition of More\_Use\_Geometry specifies that S1.Valid holds, which takes into account both possible types of S1:

- If S1 is dynamically a shape, then the precondition specifies that Shape. Valid holds, which ensures that the precondition to the call to Shape. Operate is satisfied on line 8.
- If S1 is dynamically a rectangle, then the precondition specifies that Rectangle. Valid holds, which ensures that the precondition to the call to Rectangle. Operate is satisfied on line 8.

Similarly, the test on S2.Valid on line 10 ensures that the precondition to the call to S2.Operate on line 11 is satisfied, and the call to S3.Set\_Default on line 14 ensures through its postcondition that the precondition to the call to S3.Operate on line 15 is satisfied. But no precondition or test or call ensures that the precondition to the call to S4.Operate on line 17 is satisfied. Hence the results of GNATprove's analysis on this program:

# 7.6 How to Write Package Contracts

Like for subprogram contracts, GNATprove can generate default package contracts when not specified by a user. By default, GNATprove does not require the user to write any package contracts.

The default state abstraction generated by GNATprove maps every internal global variable to a different internal abstract state (which is not really *abstract* as a result).

The default package initialization generated by GNATprove lists all variables initialized either at declaration or in the package body statements. The generated Initializes aspect is an over-approximation of the actual Initializes aspect. All

outputs are considered to be initialized from all inputs. For example, consider package Init\_Data which initializes all its global variables during elaboration, from either constants or variables:

```
package External_Data with
SPARK_Mode
is
Val : Integer with Import;
end External_Data;
```

```
with External_Data;
   pragma Elaborate_All(External_Data);
2
   package Init_Data with
4
     SPARK_Mode
5
   is
6
      pragma Elaborate_Body;
7
      Start_From_Zero : Integer := 0;
Start_From_Val : Integer := External_Data.Val;
8
9
       Start_From_Zero_Bis : Integer;
10
      Start_From_Val_Bis : Integer;
11
   end Init_Data;
12
```

```
package body Init_Data with

SPARK_Mode

is
begin

Start_From_Zero_Bis := 0;
Start_From_Val_Bis := External_Data.Val;
end Init_Data;
```

GNAT prove generates a package initialization contract on package Init Data which is equivalent to:

As a result, GNATprove can check that global variables are properly initialized when calling the main procedure Main\_Proc, and it does not issue any message when analyzing this code:

```
with Init_Data;
procedure Main_Proc with

SPARK_Mode

is

Tmp : Integer;

begin

Tmp := Init_Data.Start_From_Zero;

Tmp := Init_Data.Start_From_Val;

Tmp := Init_Data.Start_From_Zero_Bis;

Tmp := Init_Data.Start_From_Zero_Bis;

Tmp := Init_Data.Start_From_Val_Bis;

end Main_Proc;
```

The user may specify explicitly package contracts to:

- name explicitly the parts of state abstraction that can be used in subprogram dependency contracts, in order to *Address Data and Control Coupling*; or
- improve scalability and running time of GNAT prove's analysis, as a single explicit abstract state may be mapped

to hundreds of concrete global variables, which would otherwise be considered separately in the analysis; or

check that initialization of global data at elaboration is as specified in the specified package initialization contracts.

# 7.7 How to Write Loop Invariants

As described in *Loop Invariants*, proving properties of subprograms that contain loops may require the addition of explicit loop invariant contracts. This section describes a systematic approach for writing loop invariants.

### 7.7.1 Automatic Unrolling of Simple For-Loops

GNAT prove automatically unrolls simple for-loops, defined as:

- for-loops over a range,
- with a number of iterations smaller than 20,
- without Loop Invariants or Loop Variants,
- that declare no local variables, or only variables of scalar type.

In addition, GNAT prove always unrolls loops of the form for J in 1 . . 1 loop that don't have a *Loop Invariants* or *Loop Variants*, even when they declare local variables of non-scalar type. This special form of loop is used to simulate forward gotos by using exit statements instead.

As a result of unrolling, GNATprove conveys the exact meaning of the loop to provers, without requiring a loop invariant. While this is quite powerful, it is best applied to loops where the body of the loop is small, otherwise the unrolling may lead to complex formulas that provers cannot prove.

For example, consider the subprograms Init and Sum below:

```
package Loop_Unrolling with
     SPARK_Mode
2
   is
3
       subtype Index is Integer range 1 .. 10;
4
      type Arr is array (Index) of Integer;
6
      procedure Init (A : out Arr) with
         Post \Rightarrow (for all J in Index \Rightarrow A(J) = J);
8
9
       function Sum (A : Arr) return Integer with
10
         Pre \Rightarrow (for all J in Index \Rightarrow A(J) = J),
11
         Post => Sum'Result = (A'First + A'Last) * A'Length / 2;
12
13
   end Loop_Unrolling;
```

```
package body Loop_Unrolling with
SPARK_Mode

is

procedure Init (A : out Arr) is
begin
for J in Index loop
A (J) := J;
end loop;
end Init;
```

```
function Sum (A : Arr) return Integer is
11
         Result : Integer := 0;
12
13
      begin
          for J in Index loop
14
            Result := Result + A (J);
          end loop;
          return Result;
17
      end Sum;
18
19
   end Loop_Unrolling;
```

As the loops in both subprograms are simple for-loops, GNATprove unrolls them and manages to prove the postconditions of Init and Sum without requiring a loop invariant:

```
loop_unrolling.adb:15:27: info: overflow check proved
loop_unrolling.ads:7:20: info: initialization of "A" proved
loop_unrolling.ads:8:14: info: postcondition proved
loop_unrolling.ads:12:14: info: postcondition proved
```

Automatic loop unrolling can be disabled locally by explicitly adding a default loop invariant at the start of the loop:

```
for X in A .. B loop
    pragma Loop_Invariant (True);
    ...
end loop;
```

It can also be disabled globally by using the switch --no-loop-unrolling.

## 7.7.2 Automatically Generated Loop Invariants

In general, GNATprove relies on the user to manually supply the necessary information about variables modified by loop statements in the loop invariant. Though variables which are not modified in the loop need not be mentioned in the invariant, it is usually necessary to state explicitly the preservation of unmodified object parts, such as record or array components. In particular, when a loop modifies a collection, which can be either an array or a container (see *Formal Containers Library*), it may be necessary to state in the loop invariant those parts of the collection that have not been modified up to the current iteration. This property called *frame condition* in the scientific literature is essential for GNATprove, which otherwise must assume that all elements in the collection may have been modified. Special care should be taken to write adequate frame conditions, as they usually look obvious to programmers, and so it is very common to forget to write them and not being able to realize what's the problem afterwards.

To alleviate this problem, the GNAT prove tool generates automatically frame conditions in some cases. As examples of use of such generated frame conditions, consider the code of procedures <code>Update\_Arr</code> and <code>Update\_Rec</code> below:

```
package Frame_Condition with
     SPARK_Mode
2
   is
3
      type Index is range 1 .. 100;
4
      type Arr is array (Index) of Integer;
6
      procedure Update_Arr (A : in out Arr; Idx : Index) with
        Post \Rightarrow A(Idx + 1 .. A'Last) \Rightarrow A(Idx + 1 .. A'Last)'Old;
      type Rec is record
10
          A : Arr;
          X : Integer;
12
      end record;
```

```
procedure Update_Rec (R : in out Rec) with
Post => R.X = R.X'Old;
end Frame_Condition;
```

```
package body Frame_Condition with
     SPARK_Mode
2
   is
3
      procedure Update_Arr (A : in out Arr; Idx : Index) is
4
      begin
5
         for J in A'First .. Idx loop
6
            A(J) := Integer(J);
          end loop;
8
      end Update_Arr;
10
      procedure Update_Rec (R : in out Rec) is
11
12
      begin
         for J in R.A'Range loop
13
            R.A(J) := Integer(J);
          end loop;
15
      end Update_Rec;
16
17
   end Frame_Condition;
18
```

Without this feature, GNATprove would not be able to prove the postconditions of either procedure because:

- To prove the postcondition of Update\_Arr, one needs to know that only the indexes up to Idx have been updated in the loop.
- To prove the postcondition of Update\_Rec, one needs to know that only the component A of record R has been updated in the loop.

Thanks to this feature, GNATprove automatically proves the postconditions of both procedures, without the need for loop invariants:

```
frame_condition.ads:8:14: info: postcondition proved
frame_condition.ads:8:14: info: range check proved
frame_condition.ads:8:37: info: range check proved
frame_condition.ads:16:14: info: postcondition proved
```

In particular, it is able to infer the preservation of unmodified components of record variables. It also handles unmodified components of array variables as long as they are preserved at every index in the array. As an example, consider the following loop which only updates some record component of a nested data structure:

```
procedure Preserved_Fields with SPARK_Mode is

type R is record

F1 : Integer := 0;
F2 : Integer := 0;
end record;

type R_Array is array (1 .. 100) of R;

type R_Array_Record is record
F3 : R_Array;
F4 : R_Array;
end record;

end record;
```

```
D : R_Array_Record;
14
15
16
   begin
      for I in 1 .. 100 loop
17
         D.F3 (I).F1 := 0;
         pragma Assert (for all J in 1 .. 100 =>
                            D.F3 (J).F2 = D.F3'Loop_Entry (J).F2);
20
         pragma Assert (D.F4 = D.F4'Loop_Entry);
21
      end loop;
22
23
   end Preserved_Fields;
24
```

Despite the absence of a loop invariant in the above code, GNATprove is able to prove that the assertions on lines 19-21 about variable D which is modified in the loop are proved, thanks to the generated loop invariants:

```
preserved_fields.adb:14:04: info: initialization of "D" proved
preserved_fields.adb:19:22: info: assertion proved
preserved_fields.adb:21:22: info: assertion proved
```

Note that GNATprove will not generate a frame condition for a record component if the record variable is modified as a whole either through an assignment or through a procedure call, et cetera, even if the component happens to be preserved by the modification.

GNATprove can also infer preservation of unmodified array components for arrays that are only updated at constant indexes or at indexes equal to the loop index. As an example, consider the following loops, only updating some cells of a matrix of arrays:

```
procedure Preserved_Components with SPARK_Mode is
2
      type A is array (1 .. 100) of Natural with Default_Component_Value => 1;
3
4
      type A_Matrix is array (1 .. 100, 1 .. 100) of A;
5
6
      M : A_Matrix;
   begin
9
      L1: for I in 1 .. 100 loop
10
          M (I, 1) (1 ... 50) := (others => 0);
11
          pragma Assert
12
            (for all K1 in 1 \dots 100 =>
13
                (for all K2 in 1 \dots 100 \Rightarrow
                     (for all K3 in 1 .. 100 =>
15
                           (if K1 > I or else K2 /= 1 or else K3 > 50 then
16
                                    M (K1, K2) (K3) = M'Loop\_Entry (K1, K2)
                                                                                 (K3)))));
17
      end loop L1;
18
19
      L2: for I in 1 .. 99 loop
20
          M (I + 1, I) (I ... 100) := (others => 0);
21
          pragma Assert
22
            (for all K1 in 1 \dots 100 =>
23
                (for all K2 in 1 \dots 100 =>
24
                     (for all K3 in 1 \dots 100 =>
25
                           (if K1 > I + 1 then
26
                                   M (K1, K2) (K3) = M'Loop\_Entry (K1, K2) (K3))));
27
          pragma Assert
28
            (for all K1 in 1 \dots 100 =>
29
                (for all K2 in 1 \dots 100 =>
30
                     (for all K3 in 1 \dots 100 =>
31
```

Despite the absence of a loop invariant in the above code, GNATprove can successfully verify the assertion on line 13 thanks to the generated loop invariant. Note that loop invariant generation for preserved array components is based on heuristics, and that it is therefore far from complete. In particular, it does not handle updates to variable indexes different from the loop index, as can be seen by the failed attempt to verify the assertion on line 22. GNATprove does not either handle dependences between indexes in an update, resulting in the failed attempt to verify the assertion on line 33:

```
preserved_components.adb:7:04: info: initialization of "M" proved
preserved_components.adb:13:10: info: assertion proved
preserved_components.adb:21:07: info: range check proved
preserved_components.adb:21:31: info: length check proved
preserved_components.adb:21:34: info: length check proved
preserved_components.adb:21:34: info: length check proved
preserved_components.adb:27:30: medium: assertion might fail, cannot prove M (K1, K2)

(K3) = M'Loop_Entry (K1, K2) (K3) (e.g. when K1 = 4 and K2 = 1 and K3 = 1)

(Possible explanation: loop at line 20 should mention M in a loop invariant]
preserved_components.adb:33:30: medium: assertion might fail, cannot prove M (K1, K2)

(K3) = M'Loop_Entry (K1, K2) (K3) (e.g. when K1 = 1 and K2 = 2 and K3 = 1)

(Possible explanation: loop at line 20 should mention M in a loop invariant]
```

### 7.7.3 The Four Properties of a Good Loop Invariant

A loop invariant can describe more or less precisely the behavior of a loop. What matters is that the loop invariant allows proving absence of run-time errors in the subprogram, that the subprogram respects its contract, and that the loop invariant itself holds at each iteration of the loop. There are four properties that a good loop invariant should fulfill:

- 1. [INIT] It should be provable in the first iteration of the loop.
- 2. [INSIDE] It should allow proving absence of run-time errors and local assertions inside the loop.
- 3. [AFTER] It should allow proving absence of run-time errors, local assertions and the subprogram postcondition after the loop.
- 4. [PRESERVE] It should be provable after the first iteration of the loop.

As a first example, here is a variant of the search algorithm described in *SPARK Tutorial*, which returns whether a collection contains a desired value, and if so, at which index. The collection is implemented as an array.

The specification of Linear\_Search is given in file linear\_search.ads. The postcondition of Search expresses that, either the search returns a result within the array bounds, in which case it is the desired index, otherwise the array does not contain the value searched.

```
package Linear_Search
with SPARK_Mode

is

type Opt_Index is new Natural;

subtype Index is Opt_Index range 1 .. Opt_Index'Last - 1;

No_Index : constant Opt_Index := 0;
```

```
type Ar is array (Index range <>) of Integer;

function Search (A : Ar; I : Integer) return Opt_Index with

Post => (if Search'Result in A'Range then A (Search'Result) = I

else (for all K in A'Range => A (K) /= I));

end Linear_Search;
```

The implementation of Linear\_Search is given in file linear\_search.adb. The loop invariant of Search expresses that, at the end of each iteration, if the loop has not been exited before, then the value searched is not in the range of indexes between the start of the array A'First and the current index Pos.

```
package body Linear_Search
     with SPARK_Mode
2
   is
3
4
      function Search (A : Ar; I : Integer) return Opt_Index is
      begin
6
         for Pos in A'Range loop
             if A (Pos) = I then
8
                return Pos;
Q
             end if;
10
11
             pragma Loop_Invariant (for all K in A'First .. Pos => A (K) /= I);
12
          end loop;
13
         return No_Index;
15
      end Search;
16
17
   end Linear_Search;
```

With this loop invariant, GNATprove is able to prove all checks in Linear\_Search, both those related to absence of run-time errors and those related to verification of contracts:

```
linear_search.adb:9:20: info: range check proved
linear_search.adb:12:33: info: loop invariant initialization proved
linear_search.adb:12:33: info: loop invariant preservation proved
linear_search.adb:12:67: info: index check proved
linear_search.ads:13:14: info: postcondition proved
linear_search.ads:13:57: info: index check proved
linear_search.ads:14:48: info: index check proved
```

In particular, the loop invariant fulfills all four properties that we listed above:

- 1. [INIT] It is proved in the first iteration (message on line 2).
- 2. [INSIDE] It allows proving absence of run-time errors inside the loop (messages on lines 1 and 4).
- 3. [AFTER] It allows proving absence of run-time errors after the loop (messages on lines 6 and 7) and the sub-program postcondition (message on line 5).
- 4. [PRESERVE] It is proved after the first iteration (message on line 3).

Note that the loop invariant closely resembles the second line in the postcondition of the subprogram, except with a different range of values in the quantification: instead of stating a property for all indexes in the array A, the loop invariant states the same property for all indexes up to the current loop index Pos. In fact, if we equate Pos to A'Last for the last iteration of the loop, the two properties are equal. This explains here how the loop invariant allows proving the subprogram postcondition when the value searched is not found.

Note also that we chose to put the loop invariant at the end of the loop. We could as easily put it at the start of the loop. In that case, the range of values in the quantification should be modified to state that, at the start of each iteration, if the loop has not been exited before, then the value searched is not in the range of indexes between the start of the array A'First and the current index Pos excluded:

```
pragma Loop_Invariant (for all K in A'First .. Pos - 1 => A (K) /= I);
```

Indeed, the test for the value at index Pos is done after the loop invariant in that case.

We will now demonstrate techniques to complete a loop invariant so that it fulfills all four properties [INIT], [INSIDE], [AFTER] and [PRESERVE], on a more complex algorithm searching in an ordered collection of elements. Like the naive search algorithm just described, this algorithm returns whether the collection contains the desired value, and if so, at which index. The collection is also implemented as an array.

The specification of this Binary\_Search is given in file binary\_search.ads:

```
package Binary_Search
2
     with SPARK_Mode
   is
3
      type Opt_Index is new Natural;
4
5
      subtype Index is Opt_Index range 1 .. Opt_Index'Last - 1;
6
      No_Index : constant Opt_Index := 0;
8
      type Ar is array (Index range <>) of Integer;
10
11
      function Empty (A : Ar) return Boolean is (A'First > A'Last);
12
13
      function Sorted (A : Ar) return Boolean is
          (for all I1 in A'Range =>
15
             (for all I2 in I1 .. A'Last => A (I1) <= A (I2)));
16
17
      function Search (A : Ar; I : Integer) return Opt_Index with
18
        Pre => Sorted (A),
19
        Post => (if Search'Result in A'Range then A (Search'Result) = I
20
                  else (for all Index in A'Range => A (Index) /= I));
21
22
   end Binary_Search;
23
```

The implementation of Binary\_Search is given in file binary\_search.adb:

```
package body Binary_Search
     with SPARK_Mode
2
   is
3
4
      function Search (A : Ar; I : Integer) return Opt_Index is
5
          Left : Index;
6
         Right : Index;
         Med
                : Index;
8
      begin
9
          if Empty (A) then
10
             return No_Index;
11
          end if;
12
13
          Left := A'First;
14
          Right := A'Last;
15
16
          if Left = Right and A (Left) = I then
```

```
return Left:
18
          elsif A (Left) > I or A (Right) < I then
19
             return No Index;
20
          end if;
21
          while Left <= Right loop
             Med := Left + (Right - Left) / 2;
24
25
             if A (Med) < I then
26
                Left := Med + 1;
27
             elsif A (Med) > I then
28
                Right := Med - 1;
29
30
                 return Med;
31
             end if;
32
          end loop;
33
34
          return No_Index;
      end Search;
   end Binary_Search;
```

Note that, although function Search has a loop, we have not given an explicit loop invariant yet, so the default loop invariant of True will be used by GNATprove. We are running GNATprove with a prover timeout of 60 seconds (switch --timeout=60) to get the results presented in the rest of this section.

## 7.7.4 Proving a Loop Invariant in the First Iteration

Property [INIT] is the easiest one to prove. This is equivalent to proving a pragma Assert in the sequence of statements obtained by unrolling the loop once. In particular, if the loop invariant is at the start of the loop, this is equivalent to proving a pragma Assert just before the loop. Therefore, the usual techniques for investigating unproved checks apply, see *How to Investigate Unproved Checks*.

## 7.7.5 Completing a Loop Invariant to Prove Checks Inside the Loop

Let's start by running GNATprove on program Binary\_Search without loop invariant. It generates two medium messages, one corresponding to a possible run-time check failure, and one corresponding to a possible failure of the postcondition:

We will focus here on the message inside the loop, which corresponds to property [INSIDE]. The problem is that variable Med varies in the loop, so GNATprove only knows that its value is in the range of its type Index at the start of an iteration (line 23), and that it is then assigned the value of Left + (Right - Left) / 2 (line 24) before being used as an index into array A (lines 26 and 28) and inside expressions assigned to Left and Right (lines 27 and 29).

As Left and Right also vary in the loop, GNATprove cannot use the assignment on line 24 to compute a more precise range for variable Med, hence the message on index check.

What is needed here is a loop invariant that states that the values of Left and Right stay within the bounds of A inside the loop:

```
while Left <= Right loop
    pragma Loop_Invariant (Left in A'Range and Right in A'Range);

Med := Left + (Right - Left) / 2;</pre>
```

With this simple loop invariant, GNATprove now reports that the check on line 26 is proved. GNATprove computes that the value assigned to Med in the loop is also within the bounds of A.

### 7.7.6 Completing a Loop Invariant to Prove Checks After the Loop

With the simple loop invariant given before, GNATprove still reports that the postcondition of Search may fail, which corresponds to property [AFTER]. By instructing GNATprove to prove checks progressively, as seens in *Proving SPARK Programs*, we even get a precise message pointing to the part of the postcondition that could not be proved:

```
binary_search.ads:21:49: medium: postcondition might fail, cannot prove A (Index) /=\Box \Box (e.g. when A = (1 => 0, 3 => 0, 4 => 0, others => -1) and A'First = 2 and A'Last \Box \Box 4 and I = 0 and Index = 3)
```

Here, the message shows that the second line of the postcondition could not be proved. This line expresses that, in the case where Search returns No\_Index after the loop, the array A should not contain the value searched I.

One can very easily check that, if GNATprove can prove this property, it can also prove the postcondition. Simply insert a pragma Assert after the loop stating this property:

```
end loop;
pragma Assert (for all Index in A'Range => A (Index) /= I);
return No_Index;
```

GNATprove now succeeds in proving the postcondition, but it fails to prove the assertion:

```
binary_search.adb:36:50: medium: assertion might fail, cannot prove A (Index) /= I (e. 

g. when A = (1 => -1, others => 0) and A'First = 1 and A'Last = 2 and I = 0 and 

Index = 2) [possible explanation: precondition of subprogram at binary_search. 

ads:18 should mention I]
```

The problem is that GNATprove only knows what the user specified about A in the precondition, namely that it is sorted in ascending order. Nowhere it is said that A does not contain the value I. Note that adding this assertion is not compulsory. It simply helps identifying what is needed to achieve property [AFTER], but it can be removed afterwards.

What is needed here is a loop invariant stating that, if A contains the value I, it must be at an index in the range Left..Right, so when the loop exits because Left > Right (so the loop test becomes false), A cannot contain the value I.

One way to express this property is to state that the value of A at index Left -1 is less than I, while the value of A at index Right +1 is greater than I. Taking into account the possibility that there are no such indexes in A if either Left or Right are at the boundaries of the array, we can express it as follows:

```
while Left <= Right loop
    pragma Loop_Invariant (Left in A'Range and Right in A'Range);
    pragma Loop_Invariant (Left = A'First or else A (Left - 1) < I);
    pragma Loop_Invariant (Right = A'Last or else I < A (Right + 1));

Med := Left + (Right - Left) / 2;</pre>
```

GNATprove manages to prove these additional loop invariants, but it still cannot prove the assertion after the loop. The reason is both simple and far-reaching. Although the above loop invariant together with the property that the array is sorted imply the property we want to express, it still requires additional work for the prover to reach the same conclusion, which may prevent automatic proof in the allocated time. In that case, it is better to express the equivalent but more explicit property directly, as follows:

GNATprove now proves the assertion after the loop. In general, it is simpler to understand the relationship between the loop invariant and the checks that follow the loop when the loop invariant is directly followed by the exit statement that controls loop termination. In a "for" or "while" loop, this can mean it is easier to place the Loop\_Invariant pragmas at the *end* of the loop body, where they precede the (implicit) exit statement. In such cases, the loop invariant is more likely to resemble the postcondition.

### 7.7.7 Proving a Loop Invariant After the First Iteration

With the loop invariant given before, GNATprove also proves that the loop invariant of Search holds after the first iteration, which corresponds to property [PRESERVE]. In fact, we have now arrived at a loop invariant which allows GNATprove to prove all checks for subprogram Search.

This is not always the case. In general, when the loop invariant is not proved after the first iteration, the problem is that the loop invariant is not precise enough. The only information that GNATprove knows about the value of variables that are modified in the loop, at each loop iteration, is the information provided in the loop invariant. If the loop invariant is missing some crucial information about these variables, which is needed to prove the loop invariant after N iterations, GNATprove won't be able to prove that the loop invariant holds at each iteration.

In loops that modify variables of composite types (records and arrays), it is usually necessary at this stage to add in the loop invariant some information about those parts of the modified variables which are not modified by the loop, or which are not modified in the first N iterations of the loop. Otherwise, GNATprove assumes that these parts may also be modified, which can prevent it from proving the preservation of the loop invariant. See *Loop Invariants* for an example where this is needed.

In other cases, it may be necessary to guide the prover with intermediate assertions. A rule of thumb for deciding which properties to assert, and where to assert them, is to try to locate at which program point the prover does not success in proving the property of interest, and to restate other properties that are useful for the proof.

In yet other cases, where the difficulty is related to the size of the loop rather than the complexity of the properties, it may be useful to factor the loop into into local subprograms so that the subprograms' preconditions and postconditions provide the intermediate assertions that are needed to prove the loop invariant.

# 7.8 How to Investigate Unproved Checks

One of the most challenging aspects of formal verification is the analysis of failed proofs. If GNATprove fails to prove automatically that a run-time check or an assertion holds, there might be various reasons:

• [CODE] The check or assertion does not hold, because the code is wrong.

- [ASSERT] The assertion does not hold, because it is incorrect.
- [SPEC] The check or assertion cannot be proved, because of some missing assertions about the behavior of the program.
- [MODEL] The check or assertion is not proved because of current limitations in the model used by GNATprove.
- [TIMEOUT] The check or assertion is not proved because the prover timeouts.
- [PROVER] The check or assertion is not proved because the prover is not smart enough.

#### 7.8.1 Investigating Incorrect Code or Assertion

The first step is to check whether the code is incorrect [CODE] or the assertion is incorrect [ASSERT], or both. Since run-time checks and assertions can be executed at run time, one way to increase confidence in the correction of the code and assertions is to test the program on representative inputs. The following GNAT switches can be used:

- -gnato: enable run-time checking of intermediate overflows
- -gnat-p: reenable run-time checking even if -gnatp was used to suppress all checks
- -gnata: enable run-time checking of assertions

#### 7.8.2 Investigating Unprovable Properties

The second step is to consider whether the property is provable [SPEC]. A check or assertion might be unprovable because a necessary annotation is missing:

- the precondition of the enclosing subprogram might be too weak; or
- the postcondition of a subprogram called might be too weak; or
- a loop invariant for an enclosing loop might be too weak; or
- a loop invariant for a loop before the check or assertion might be too weak.

In particular, GNATprove does not look into subprogram bodies, so all the necessary information for calls should be explicit in the subprogram contracts. GNATprove may emit a tentative explanation for the unprovable property when it suspects a missing precondition, postcondition or loop invariant to be the cause of the unprovability. The explanation part follows the usual message of the form:

```
file:line:col: severity: check might fail
```

with a part in square brackets such as:

```
[possible explanation: subprogram at line xxx should mention Var in a precondition]
[possible explanation: loop at line xxx should mention Var in a loop invariant]
[possible explanation: call at line xxx should mention Var in a postcondition]
```

A focused manual review of the code and assertions can efficiently diagnose many cases of missing annotations. Even when an assertion is quite large, GNATprove precisely locates the part that it cannot prove, which can help figuring out the problem. It may useful to simplify the code during this investigation, for example by adding a simpler assertion and trying to prove it.

GNATprove provides path information that might help the code review. You can display inside the editor the path on which the proof failed, as described in *Running GNATprove from GPS*. In some cases, a counterexample is also generated on the path, with values of variables which exhibit the problem (see *Understanding Counterexamples*). In many cases, this is sufficient to spot a missing assertion.

A property can also be conceptually provable, but the model used by GNATprove can currently not reason about it [MODEL]. (See *GNATprove Limitations* for a list of the current limitations in GNATprove.) In particular using the following features of the language may yield checks that should be true, but cannot be proved:

- Floating point arithmetic (although using CodePeer integration may help here)
- The specific value of dispatching calls when the tag is known

To use CodePeer integration, pass the switch --codepeer=on to GNATprove. In those cases where no prover, including CodePeer, can prove the check, the missing information can usually be added using pragma Assume.

It may be difficult sometimes to distinguish between unprovable properties and prover shortcomings (the next section). The most generally useful action to narrow down the issue to its core is to insert assertions in the code that *test* whether the property (or part of it) can be proved at some specific point in the program. For example, if a postcondition states a property (P or Q), and the implementation contains many branches and paths, try adding assertions that P holds or Q holds where they are expected to hold. This can help distinguish between the two cases:

- In the case of an unprovable property, this may point to a specific path in the program, and a specific part of the property, which cause the issue.
- In the case of a prover shortcoming, this may also help provers to manage to prove both the assertion and the property. Then, it is good practice to keep in the code only those assertions that help getting automatic proof, and to remove other assertions that were inserted during interaction.

When using switch --info, GNATprove issues information messages regarding internal decisions that could influence provability:

- whether candidate loops for Automatic Unrolling of Simple For-Loops are effectively unrolled or not;
- whether candidate subprograms for *Contextual Analysis of Subprograms Without Contracts* are effectively inlined for proof or not;
- whether possible subprogram nontermination impacts the proof of calls to that subprogram (see the note in the section on *Subprogram Termination*)

## 7.8.3 Investigating Prover Shortcomings

The last step is to investigate if the prover would find a proof given enough time [TIMEOUT] or if another prover can find a proof [PROVER]. To that end, GNATprove provides switch --level, usable either from the command-line (see *Running GNATprove from the Command Line*), inside GPS (see *Running GNATprove from GPS*) or inside GNATbench (see *Running GNATprove from GNATbench*). The level of 0 is only adequate for simple proofs. In general, one should increase the level of proof (up to level 4) until no more automatic proofs can be obtained.

As described in the section about *Running GNATprove from the Command Line*, switch --level is equivalent to setting directly various lower level switches like --timeout, --prover, and --proof. Hence, one can also set more powerful (and thus leading to longer proof time) values for the individual switches rather than using the predefined combinations set through --level.

Note that for the above experiments, it is quite convenient to use the  $SPARK \rightarrow Prove\ Line$  or  $SPARK \rightarrow Prove\ Sub-program$  menus in GPS, as described in *Running GNAT prove from GPS* and *Running GNAT prove from GNAT bench*, to get faster results for the desired line or subprogram.

A current limitation of automatic provers is that they don't handle floating-point arithmetic very precisely, in particular when there are either a lot of operations, or some non-linear operations (multiplication, division, exponentiation). In that case, it may be profitable to use CodePeer integration, which is activated with the switch --codepeer=on, as CodePeer is both fast and precise for proving bounds of floating-point operations.

Another common limitation of automatic provers is that they don't handle non-linear arithmetic well. For example, they might fail to prove simple checks involving multiplication, division, modulo or exponentiation.

In that case, a user may either:

- add in the code a call to a lemma from the SPARK lemma library (see details in *Manual Proof Using SPARK Lemma Library*), or
- add in the code a call to a user lemma (see details in Manual Proof Using User Lemmas), or
- add an assumption in the code (see details in *Indirect Justification with Pragma Assume*), or
- add a justification in the code (see details in *Direct Justification with Pragma Annotate*), or
- manually review the unproved checks and record that they can be trusted (for example by storing the result of GNATprove under version control).

In the future, GNATprove may provide a *user view* of the formula passed to the prover, for advanced users to inspect. This view would express in an Ada-like syntax the actual formula whose proof failed, to make it easier for users to interpret it. This format is yet to be defined.

For advanced users, in particular those who would like to do manual proof, we will provide a description of the format of the proof files generated by GNATprove, so that users can understand the actual files passed to the prover. Each individual file is stored under the sub-directory gnatprove of the project object directory (default is the project directory). The file name follows the convention:

```
<file>_<line>_<column>_<check>_<num>.<ext>
```

#### where:

- file is the name of the Ada source file for the check
- line is the line where the check appears
- column is the column
- · check is an identifier for the check
- num is an optional number and identifies different paths through the program, between the start of the subprogram and the location of the check
- ext is the extension corresponding to the file format chosen. The format of the file depends on the prover used. For example, files for Alt-Ergo are are in Why3 format, and files for CVC4 are in SMTLIB2 format.

For example, the proof files generated for prover Alt-Ergo for a range check at line 160, column 42, of the file f.adb are stored in:

```
f.adb_160_42_range_check.why
f.adb_160_42_range_check_2.why
f.adb_160_42_range_check_3.why
...
```

Corresponding proof files generated for prover CVC4 are stored in:

```
f.adb_160_42_range_check.smt2
f.adb_160_42_range_check_2.smt2
f.adb_160_42_range_check_3.smt2
...
```

To be able to inspect these files, you should instruct GNATprove to keep them around by adding the switch -d to GNATprove's command line. You can also use the switch -v to get a detailed log of which proof files GNATprove is producing and attempting to prove.

#### 7.8.4 Looking at Machine-Parsable GNATprove Output

GNATprove generates files which contain the results of SPARK analysis in machine-parsable form. These files are located in the gnatprove subdirectory of the project object directory, and have the suffix .spark. The structure of these files exposes internal details such as the exact way some checks are proved, therefore the structure of these files may change. Still, we provide here the structure of these files for convenience.

At various places in these files, we refer to entities. These are Ada entities, either subprograms or packages. Entities are defined by their name and their source location (file and line). In JSON this translates to the following dictionary for entities:

```
{ "name" : string,
  "file" : string,
  "line" : int }
```

#### A . spark file is of this form:

```
{ "spark" : list spark_result,
  "flow" : list flow_result,
  "proof" : list proof_result }
```

Each entry is mapped to a list of entries whose format is described below.

The spark\_result entry is simply an entity, with an extra field for spark status, so that the entire dictionary looks like this:

Field "spark" takes value in "spec", "all" or "no" to denote respectively that only the spec is in SPARK, both spec/body are in SPARK (or spec is in SPARK for a package without body), or the spec is not in SPARK.

Entries for proof are of the following form:

```
proof_result =
              : string,
 { "file"
          : int,
: int,
   "line"
   "col"
   "suppressed" : string,
   "rule"
                : string,
   "severity"
                : string,
   "tracefile" : string,
   "check_tree" : list goal,
   "msq_id" : int,
   "how_proved" : string,
   "entity" : entity }
```

- ("file", "line", "col") describe the source location of the message.
- "rule" describes the kind of check.
- "severity" describes the kind status of the message, possible values used by gnatwhy3 are "info", "low", "medium", "high" and "error".
- "tracefile" contains the name of a trace file, if any.
- "entity" contains the entity dictionary for the entity that this check belongs to.

- "msg\_id" if present indicates that this entry corresponds to a message issued on the commandline, with the exact same msg\_id in brackets: "[#12]"
- "suppressed" if present, the message is in fact suppressed by a pragma Annotate, and this field contains the justification message.
- "how\_proved" if present, indicates how the check has been proved (i.e. which prover). Special values are "interval" and "codepeer", which designate the special interval analysis, done in the frontend, and the CodePeer analysis, respectively. Both have their own column in the summary table.
- "check\_tree" basically contains a copy of the session tree in JSON format. It's a tree structure whose nodes are goals, transformations and proof attempts:

Flow entries are of the same form as for proof. Differences are in the possible values for "rule", which can only be the ones for flow messages. Also "how\_proved" field is never set.

### 7.8.5 Understanding Proof Strategies

We now explain in more detail how the provers are run on the logical formula(s) generated for a given check, a.k.a. Verification Conditions or VCs.

- In per\_check mode, a single VC is generated for each check at the source level (e.g. an assertion, run-time check, or postcondition); in some cases two VCs can appear. Before attempting proof, this VC is then split into the conjuncts, that is, the parts that are combined with and or and then. All provers are tried on the VCs obtained in this way until one of them proves the VC or no more provers are left.
- In per\_path mode, a VC is generated not only for each check at the source level, but for each path to the check. For example, for an assertion that appears after an if-statement, at least two VCs will be generated one for each path through the if-statement. For each such VC, all provers are attempted. Unproved VCs are then further split into their conjuncts, and proof is again attempted.
- In progressive mode, first the actions described for per\_check are tried. For all unproved VCs, the VC is then split into the paths that lead to the check, like for per\_path. Each part is then attempted to be proved independently.

# 7.9 GNATprove by Example

GNATprove is based on advanced technology for modular static analysis and deductive verification. It is very different both from compilers, which do very little analysis of the code, and static analyzers, which execute symbolically the program. GNATprove does a very powerful local analysis of the program, but it generally does not cross subprogram boundaries. Instead, it uses the *Subprogram Contracts* provided by users to analyze calls. GNATprove also requires sometimes that users direct the analysis with *Assertion Pragmas*. Thus, it is essential to understand how GNATprove uses contracts and assertion pragmas. This section aims at providing a deeper insight into how GNATprove's flow analysis and proof work, through a step-by-step exploration of small code examples.

All the examples presented in this section, as well as some code snippets presented in the *Overview of SPARK Language*, are available in the example called gnatprove\_by\_example distributed with the SPARK toolset. It can be found in the share/examples/spark directory below the directory where the toolset is installed, and can be accessed from the IDE (either GPS or GNATBench) via the  $Help \rightarrow SPARK \rightarrow Examples$  menu item.

#### 7.9.1 Basic Examples

The examples in this section have no loops, and do not use more complex features of SPARK like *Ghost Code*, *Interfaces to the Physical World*, or *Object Oriented Programming and Liskov Substitution Principle*.

#### Increment

Consider a simple procedure that increments its integer parameter X:

```
procedure Increment (X : in out Integer) with

SPARK_Mode
is
begin
   X := X + 1;
end Increment;
```

As this procedure does not have a contract yet, GNATprove only checks that there are no possible reads of uninitialized data and no possible run-time errors in the procedure. Here, it issues a message about a possible overflow check failure on X + 1:

```
increment.adb:5:11: medium: overflow check might fail (e.g. when X = Integer'Last) 

→ [possible explanation: subprogram at line 1 should mention X in a precondition]
```

The counterexample displayed tells us that Increment could be called on value Integer'Last for parameter X, which would cause the increment to raise a run-time error. As suggested by the possible explanation in the message issued by GNATprove, one way to eliminate this vulnerability is to add a precondition to Increment specifying that X should be less than Integer'Last when calling the procedure:

```
procedure Increment_Guarded (X : in out Integer) with

SPARK_Mode,
Pre => X < Integer'Last

is
begin
   X := X + 1;
end Increment_Guarded;</pre>
```

As this procedure has a contract now, GNATprove checks like before that there are no possible reads of uninitialized data and no possible run-time errors in the procedure, including in its contrat, and that the procedure implements its contract. As expected, GNATprove now proves that there is no possible overflow check failure on X + 1:

```
increment_guarded.adb:6:11: info: overflow check proved
```

The precondition is usually the first contract added to a subprogram, but there are other *Subprogram Contracts*. Here is a version of Increment with:

- global dependencies (aspect Global) stating that the procedure reads and writes no global variables
- flow dependencies (aspect Depends) stating that the final value of parameter X only depends on its input value
- a precondition (aspect Pre) stating that parameter X should be less than Integer' Last on entry
- a postcondition (aspect Post) stating that parameter X should have been incremented by the procedure on exit

```
procedure Increment_Full (X : in out Integer) with

SPARK_Mode,

Global => null,

Depends => (X => X),

Pre => X < Integer'Last,

Post => X = X'Old + 1

is

begin

X := X + 1;

end Increment_Full;
```

GNATprove checks that Increment\_Full implements its contract, and that it cannot raise run-time errors or read uninitialized data. By default, GNATprove's output is empty in such a case, but we can request that it prints one line per check proved by using switch --report=all, which we do here:

```
increment_full.adb:3:03: info: data dependencies proved
increment_full.adb:4:03: info: flow dependencies proved
increment_full.adb:6:14: info: postcondition proved
increment_full.adb:6:24: info: overflow check proved
increment_full.adb:9:11: info: overflow check proved
```

As subprogram contracts are used to analyze callers of a subprogram, let's consider a procedure Increment\_Calls that calls the different versions of Increment presented so far:

```
with Increment;
   with Increment_Guarded;
2
   with Increment_Full;
3
   procedure Increment_Calls with
5
     SPARK_Mode
6
7
      X : Integer;
8
   begin
Q
      X := 0;
10
      Increment (X);
11
      Increment (X);
12
13
      X := 0;
14
      Increment_Guarded (X);
15
      Increment_Guarded (X);
17
      X := 0;
18
      Increment_Full (X);
19
      Increment_Full (X);
20
   end Increment_Calls;
```

GNATprove proves all preconditions expect the one on the second call to Increment\_Guarded:

```
increment_calls.adb:8:04: info: initialization of "X" proved
increment_calls.adb:15:04: info: precondition proved
increment_calls.adb:16:04: medium: precondition might fail, cannot prove X < Integer
    →'last (e.g. when X = Integer'Last) [possible explanation: call at line 15 should_
    →mention X (for argument X) in a postcondition]
increment_calls.adb:19:04: info: precondition proved
increment_calls.adb:20:04: info: precondition proved</pre>
```

Increment has no precondition, so there is nothing to check here except the initialization of X when calling Increment on lines 11 and 12. But remember that GNATprove did issue a message about a true vulnaribility

on Increment's implementation.

This vulnerability was corrected by adding a precondition to Increment\_Guarded. This has the effect of pushing the constraint on callers, here procedure Increment\_Calls. As expected, GNATprove proves that the first call to Increment\_Guarded on line 15 satisfies its precondition. But it does not prove the same for the second call to Increment\_Guarded on line 16, because the value of X on line 16 was set by the call to Increment\_Guarded on line 15, and the contract of Increment\_Guarded does not say anything about the possible values of X on exit.

As suggested by the possible explanation in the message issued by GNATprove, a postcondition like the one on Increment\_Full is needed so that GNATprove can check the second call to increment X. As expected, GNATprove proves that both calls to Increment\_Full on lines 19 and 20 satisfy their precondition.

In some cases, the user is not interested in specifying and verifying a complete contract like the one on Increment\_Full, typically for helper subprograms defined locally in a subprogram or package body. GNAT-prove allows performing *Contextual Analysis of Subprograms Without Contracts* for these local subprograms. For example, consider a local definition of Increment inside procedure Increment\_Local:

```
procedure Increment_Local with
     SPARK_Mode
2
   is
3
      procedure Increment (X : in out Integer) is
4
      begin
5
         X := X + 1;
6
      end Increment;
8
      X : Integer;
9
10
   begin
11
      X := 0;
12
      Increment (X);
13
      Increment (X);
      pragma Assert (X = 2);
15
   end Increment_Local;
```

Although Increment has no contract (like the previous non-local version), GNATprove proves that this program is free from run-time errors, and that the assertion on line 15 holds:

#### Swap

Consider a simple procedure that swaps its integer parameters X and Y, whose simple-minded implementation is wrong:

```
procedure Swap_Bad (X, Y : in out Integer) with

SPARK_Mode

is
begin

X := Y;
Y := X;
end Swap_Bad;
```

As this procedure does not have a contract yet, GNATprove only checks that there are no possible reads of uninitialized data and no possible run-time errors in the procedure. Here, it simply issues a warning:

```
swap_bad.adb:1:21: warning: unused initial value of "X"
```

But we know the procedure is wrong, so we'd like to get an error of some sort! We could not detect it with GNATprove because the error is functional, and GNATprove cannot guess the intended functionality of Swap\_Bad. Fortunately, we can give this information to GNATprove by adding a contract to Swap\_Bad.

One such contract is the flow dependencies introduced by aspect Depends. Here it specifies that the final value of X (resp. Y) should depend on the initial value of Y (resp. X):

```
procedure Swap_Bad_Depends (X, Y : in out Integer) with

SPARK_Mode,
Depends => (X => Y, Y => X)

is
begin
    X := Y;
Y := X;
end Swap_Bad_Depends;
```

GNATprove issues 3 check messages on Swap\_Bad\_Depends:

```
swap_bad_depends.adb:1:29: warning: unused initial value of "X"
swap_bad_depends.adb:3:03: medium: missing dependency "null => X"
swap_bad_depends.adb:3:23: medium: missing self-dependency "Y => Y"
swap_bad_depends.adb:3:28: medium: incorrect dependency "Y => X"
```

The last message informs us that the dependency Y => X stated in Swap\_Bad\_Depends's contract is incorrect for the given implementation. That might be either an error in the code or an error in the contract. Here this is an error in the code. The two other messages are consequences of this error.

Another possible contract is the postcondition introduced by aspect Post. Here it specifies that the final value of X (resp. Y) is equal to the initial value of Y (resp. X):

```
procedure Swap_Bad_Post (X, Y : in out Integer) with

SPARK_Mode,

Post => X = Y'Old and Y = X'Old

is

begin
    X := Y;
    Y := X;

end Swap_Bad_Post;
```

GNATprove issues one check message on the unproved postcondition of Swap\_Bad\_Post, with a counterexample giving concrete values of a wrong execution:

```
swap_bad_post.adb:3:25: medium: postcondition might fail, cannot prove Y = X'old (e.g. \rightarrow when X'Old = 0 and Y = 1)
```

Both the check messages on Swap\_Bad\_Depends and on Swap\_Bad\_Post inform us that the intended functionality as expressed in the contracts is not implemented in the procedure. And looking again at the warning issued by GNATprove on Swap\_Bad, this was already pointing at the same issue: swapping the values of X and Y should obviously lead to reading the initial value of X; the fact that this value is not used is a clear sign that there is an error in the implementation. The correct version of Swap uses a temporary value to hold the value of X:

```
procedure Swap (X, Y : in out Integer) with
SPARK_Mode,
```

```
Depends => (X => Y, Y => X),
Post => X = Y'Old and Y = X'Old

is
Tmp : constant Integer := X;
begin
X := Y;
Y := Tmp;
end Swap;
```

GNAT prove proves both contracts on Swap and it informs us that the postcondition was proved:

```
swap.adb:3:03: info: flow dependencies proved
swap.adb:4:14: info: postcondition proved
```

Let's now consider a well-known *in place* implementation of Swap that avoids introducing a temporary variable by using bitwise operations:

```
with Interfaces; use Interfaces;

procedure Swap_Modulo (X, Y : in out Unsigned_32) with

SPARK_Mode,

Post => X = Y'Old and Y = X'Old

is

begin

X := X xor Y;

Y := X xor Y;

X := X xor Y;

end Swap_Modulo;
```

GNAT prove understands the bitwise operations on values of modular types, and it proves here that the postcondition of Swap Modulo is proved:

```
swap_modulo.adb:5:11: info: postcondition proved
```

GNATprove's flow analysis issues warnings like the one on Swap\_Bad whenever it detects that some variables or statements are not used in the computation, which is likely uncovering an error. For example, consider procedure Swap\_Warn which assigns X and Tmp\_Y out of order:

```
procedure Swap_Warn (X, Y : in out Integer) with
     SPARK_Mode
2
   is
      Tmp_X : Integer;
      Tmp_Y : Integer;
5
   begin
6
      Tmp_X := X;
7
      X := Tmp_Y;
      Tmp_Y := Y;
      Y := Tmp_X;
10
   end Swap_Warn;
```

On this wrong implementation, GNATprove issues a high check message for the certain read of an uninitialized variable, and two warnings that point to unused constructs:

```
swap_warn.adb:1:25: warning: unused initial value of "Y"
swap_warn.adb:4:04: info: initialization of "Tmp_X" proved
swap_warn.adb:8:09: high: "Tmp_Y" is not initialized
swap_warn.adb:8:09: warning: "Tmp_Y" may be referenced before it has a value
```

```
swap_warn.adb:9:10: warning: unused assignment
```

In general, warnings issued by GNATprove's flow analysis should be carefully reviewed, as they may lead to the discovery of errors in the program.

#### Addition

Consider a simple function Addition that returns the sum of its integer parameters X and Y. As in *Increment*, we add a suitable precondition and postcondition for this function:

```
function Addition (X, Y : Integer) return Integer with

SPARK_Mode,
Depends => (Addition'Result => (X, Y)),
Pre => X + Y in Integer,
Post => Addition'Result = X + Y

is
begin
return X + Y;
end Addition;
```

We also added flow dependencies to Addition for illustration purposes, but they are the same as the default generated ones (the result of the function depends on all its inputs), so are not in general given explicitly.

GNATprove issues a check message about a possible overflow in the precondition of Addition:

```
addition.adb:3:03: info: flow dependencies proved addition.adb:4:16: medium: overflow check might fail (e.g. when X = -1 and Y = Integer → 'First) addition.adb:5:14: info: postcondition proved addition.adb:5:34: info: overflow check proved addition.adb:8:13: info: overflow check proved
```

Indeed, if we call for example Addition on values Integer 'Last for X and 1 for Y, the expression X + Y evaluated in the precondition does not fit in a machine integer and raises an exception at run time. In this specific case, some people may consider that it does not really matter that an exception is raised due to overflow as the failure of the precondition should also raise a run-time exception. But in general the precondition should not fail (just consider the precondition X + Y not in Integer for example), and even here, the different exceptions raised may be treated differently (Constraint\_Error in the case of an overflow, Assertion\_Error in the case of a failing precondition).

One way to avoid this vulnerability is to rewrite the precondition so that no overflow can occur:

```
function Addition_Rewrite (X, Y : Integer) return Integer with
SPARK_Mode,
Depends => (Addition_Rewrite'Result => (X, Y)),
Pre => (X >= 0 and then Y <= Integer'Last - X) or else (X < 0 and then Y >= ...
Integer'First - X),
Post => Addition_Rewrite'Result = X + Y

is
begin
return X + Y;
end Addition_Rewrite;
```

Although GNAT prove proves that Addition\_Rewrite implements its contract and is free from run-time errors, the rewritten precondition is not so readable anymore:

```
addition_rewrite.adb:3:03: info: flow dependencies proved addition_rewrite.adb:4:49: info: overflow check proved addition_rewrite.adb:4:97: info: overflow check proved addition_rewrite.adb:5:14: info: postcondition proved addition_rewrite.adb:5:42: info: overflow check proved addition_rewrite.adb:8:13: info: overflow check proved
```

A better way to achieve the same goal without losing in readability is to execute and analyze contracts in a special mode where overflows cannot occur, as explained in *Overflow Modes*. In that case, GNATprove proves that there are no run-time errors in function Addition, and that it implements its contract.

Finally, we can choose to expand the range of applicability of the function, by accepting any values of inputs X and Y, and saturating when the addition would overflow the bounds of machine integers. That's what function Addition\_Saturated does, and its saturating behavior is expressed in *Contract Cases*:

```
function Addition_Saturated (X, Y : Integer) return Integer with
2
     SPARK_Mode,
     Contract_Cases => ((X + Y in Integer)
                                                  => Addition_Saturated'Result = X + Y,
                          X + Y < Integer'First => Addition_Saturated'Result = Integer
    → 'First,
                          X + Y > Integer'Last => Addition_Saturated'Result = Integer
    \hookrightarrow 'Last)
   is
6
   begin
       if X < 0 and Y < 0 then -- both negative
8
          if X < Integer'First - Y then</pre>
9
             return Integer'First;
10
          else
11
             return X + Y;
          end if;
14
       elsif X > 0 and Y > 0 then -- both positive
15
          if X > Integer'Last - Y then
16
             return Integer'Last;
17
          else
18
             return X + Y;
19
          end if;
20
21
       else -- one positive or null, one negative or null, adding them is safe
22
          return X + Y;
23
       end if:
24
   end Addition_Saturated;
```

GNAT prove proves that Addition\_Saturated implements its contract and is free from run-time errors:

```
addition_saturated.adb:3:03: info: complete contract cases proved addition_saturated.adb:3:03: info: disjoint contract cases proved addition_saturated.adb:3:44: info: contract case proved addition_saturated.adb:4:44: info: contract case proved addition_saturated.adb:5:44: info: contract case proved addition_saturated.adb:9:28: info: overflow check proved addition_saturated.adb:12:19: info: overflow check proved addition_saturated.adb:16:27: info: overflow check proved addition_saturated.adb:19:19: info: overflow check proved addition_saturated.adb:19:19: info: overflow check proved addition_saturated.adb:23:16: info: overflow check proved
```

Note that we analyzed this function in ELIMINATED overflow mode, using the switch -gnato13, otherwise there would be possible overflows in the guard expressions of the contract cases.

# 7.9.2 Loop Examples

The examples in this section contain loops, and thus require in general that users write suitable *Loop Invariants*. We start by explaining the need for a loop invariant, and we continue with a description of the most common patterns of loops and their loop invariant. We summarize each pattern in a table of the following form:

Loop Pattern	Loop Over Data Structure
Proof Objective	Establish property P.
Loop Behavior	Loops over the data structure and establishes P.
Loop Invariant	Property P is established for the part of the data structure looped over so far.

The examples in this section use the types defined in package Loop\_Types:

```
with Ada.Containers.Formal_Doubly_Linked_Lists;
   with Ada.Containers.Formal_Vectors;
2
   package Loop_Types
     with SPARK_Mode
5
   is
6
      subtype Index_T is Positive range 1 .. 1000;
7
      subtype Opt_Index_T is Natural range 0 .. 1000;
      subtype Component_T is Natural;
10
      type Arr_T is array (Index_T) of Component_T;
11
12
      package Vectors is new Ada.Containers.Formal_Vectors (Index_T, Component_T);
13
      subtype Vec_T is Vectors.Vector;
14
15
      package Lists is new Ada.Containers.Formal_Doubly_Linked_Lists (Component_T);
      subtype List_T is Lists.List;
17
18
   end Loop_Types;
19
```

#### The Need for a Loop Invariant

Consider a simple procedure that increments its integer parameter X a number N of times:

```
procedure Increment_Loop (X : in out Integer; N : Natural) with
     SPARK Mode,
2
     Pre => X <= Integer'Last - N,
3
     Post => X = X'Old + N
4
  is
5
6
  begin
7
      for I in 1 .. N loop
         X := X + 1;
8
      end loop;
  end Increment_Loop;
```

The precondition of Increment\_Loop ensures that there is no overflow when incrementing X in the loop, and its postcondition states that X has been incremented N times. This contract is a generalization of the contract given for a single increment in *Increment*. GNATprove does not manage to prove either the absence of overflow or the postcondition of Increment\_Loop:

```
increment_loop.adb:4:21: info: overflow check proved
increment_loop.adb:8:14: medium: overflow check might fail (e.g. when X = Integer
    'Last) [possible explanation: loop at line 7 should mention X in a loop invariant]
```

As described in *How to Write Loop Invariants*, this is because variable X is modified in the loop, hence GNATprove knows nothing about it unless it is stated in a loop invariant. If we add such a loop invariant, as suggested by the possible explanation in the message issued by GNATprove, that describes precisely the value of X in each iteration of the loop:

```
procedure Increment_Loop_Inv (X : in out Integer; N : Natural) with
     SPARK_Mode,
2
    Pre => X <= Integer'Last - N,
     Post => X = X'Old + N
   is
   begin
6
      for I in 1 .. N loop
7
         X := X + 1;
         pragma Loop_Invariant (X = X'Loop_Entry + I);
      end loop;
10
   end Increment_Loop_Inv;
11
```

then GNATprove proves both the absence of overflow and the postcondition of Increment\_Loop\_Inv:

```
increment_loop_inv.adb:3:29: info: overflow check proved
increment_loop_inv.adb:4:11: info: postcondition proved
increment_loop_inv.adb:4:21: info: overflow check proved
increment_loop_inv.adb:8:14: info: overflow check proved
increment_loop_inv.adb:9:30: info: loop invariant initialization proved
increment_loop_inv.adb:9:30: info: loop invariant preservation proved
increment_loop_inv.adb:9:47: info: overflow check proved
```

Fortunately, many loops fall into some broad categories for which the loop invariant is known. In the following sections, we describe these common patterns of loops and their loop invariant, which involve in general iterating over the content of a collection (either an array or a container from the *Formal Containers Library*).

## **Initialization Loops**

This kind of loops iterates over a collection to initialize every element of the collection to a given value:

Loop Pattern	Separate Initialization of Each Element
Proof Objective	Every element of the collection has a specific value.
Loop Behavior	Loops over the collection and initializes every element of the collection.
Loop Invariant	Every element initialized so far has its specific value.

In the simplest case, every element is assigned the same value. For example, in procedure Init\_Arr\_Zero below, value zero is assigned to every element of array A:

```
A(J) := 0;

pragma Loop_Invariant (for all K in A'First .. J => A(K) = 0);

pragma Annotate (GNATprove, False_Positive, """A"" might not be initialized",

"Part of array up to index J is initialized at this point");

end loop;
end Init_Arr_Zero;
```

The loop invariant expresses that all elements up to the current loop index J have the value zero. With this loop invariant, GNATprove is able to prove the postcondition of Init\_Arr\_Zero, namely that all elements of the array have value zero:

```
init_arr_zero.adb:5:11: info: postcondition proved
init_arr_zero.adb:12:30: info: loop invariant initialization proved
init_arr_zero.adb:12:30: info: loop invariant preservation proved
init_arr_zero.adb:12:61: info: index check proved
```

**Note:** Pragma Annotate is used in Init\_Arr\_Zero to justify a message issued by flow analysis, about the possible read of uninitialized value A(K) in the loop invariant. Indeed, flow analysis is not currently able to infer that all elements up to the loop index J have been initialized, hence it issues a message that "A" might not be initialized. For more details, see section on *Justifying Check Messages*.

Consider now a variant of the same initialization loop over a vector:

```
with Loop_Types; use Loop_Types; use Loop_Types. Vectors;
2
3
   procedure Init_Vec_Zero (V : in out Vec_T) with
4
     SPARK_Mode,
     Post => (for all J in First_Index (V) .. Last_Index (V) => Element (V, J) = 0)
5
6
   is
   begin
7
      for J in First_Index (V) .. Last_Index (V) loop
         Replace_Element (V, J, 0);
         pragma Loop_Invariant (Last_Index (V) = Last_Index (V) 'Loop_Entry);
10
         pragma Loop_Invariant (for all K in First_Index (V) .. J \Rightarrow Element (V, K) = 0);
11
      end loop;
12
   end Init_Vec_Zero;
```

Like before, the loop invariant expresses that all elements up to the current loop index J have the value zero. Another loop invariant is needed here to express that the length of the vector does not change in the loop: as variable V is modified in the loop, GNATprove does not know its length stays the same (for example, calling procedure Append or Delete\_Last would change this length) unless the user says so in the loop invariant. This is different from arrays whose length cannot change. With this loop invariant, GNATprove is able to prove the postcondition of Init\_Vec\_Zero, namely that all elements of the vector have value zero:

```
init_vec_zero.adb:5:11: info: postcondition proved
init_vec_zero.adb:5:62: info: precondition proved
init_vec_zero.adb:5:74: info: range check proved
init_vec_zero.adb:9:07: info: precondition proved
init_vec_zero.adb:9:27: info: range check proved
init_vec_zero.adb:10:30: info: loop invariant initialization proved
init_vec_zero.adb:10:30: info: loop invariant preservation proved
init_vec_zero.adb:11:30: info: loop invariant initialization proved
init_vec_zero.adb:11:30: info: loop invariant preservation proved
init_vec_zero.adb:11:67: info: precondition proved
init_vec_zero.adb:11:79: info: range check proved
```

Similarly, consider a variant of the same initialization loop over a list:

```
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
   with Ada.Containers; use Ada.Containers; use Loop_Types.Lists.Formal_Model;
2
3
   procedure Init_List_Zero (L : in out List_T) with
     SPARK Mode,
5
     Post \Rightarrow (for all E of L \Rightarrow E = 0)
6
   is
      Cu : Cursor := First (L);
   begin
      while Has_Element (L, Cu) loop
10
         pragma Loop_Invariant (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
11
                                     Element (Model (L), I) = 0);
12
         Replace_Element (L, Cu, 0);
13
         Next (L, Cu);
      end loop;
15
   end Init_List_Zero;
```

Contrary to arrays and vectors, lists are not indexed. Instead, a cursor can be defined to iterate over the list. The loop invariant expresses that all elements up to the current cursor Cu have the value zero. To access the element stored at a given position in a list, we use the function Model which computes the mathematical sequence of the elements stored in the list. The position of a cursor in this sequence is retrieved using the Positions function. Contrary to the case of vectors, no loop invariant is needed to express that the length of the list does not change in the loop, because the postcondition remains provable here even if the length of the list changes. With this loop invariant, GNATprove is able to prove the postcondition of Init\_List\_Zero, namely that all elements of the list have value zero:

```
init_list_zero.adb:6:11: info: postcondition proved
init_list_zero.adb:6:12: info: precondition proved
init_list_zero.adb:11:30: info: loop invariant initialization proved
init_list_zero.adb:11:30: info: loop invariant preservation proved
init_list_zero.adb:11:49: info: precondition proved
init_list_zero.adb:12:32: info: precondition proved
init_list_zero.adb:13:07: info: precondition proved
init_list_zero.adb:14:07: info: precondition proved
```

The case of sets and maps is similar to the case of lists.

**Note:** The parameter of Init\_Vec\_Zero and Init\_List\_Zero is an in out parameter. This is because some components of the vector/list parameter are preserved by the initialization procedure (in particular the component corresponding to its length). This is different from Init\_Arr\_Zero which takes an out parameter, as all components of the array are initialized by the procedure (the bounds of an array are not modifiable, hence considered separately from the parameter mode).

Consider now a case where the value assigned to each element is not the same. For example, in procedure Init\_Arr\_Index below, each element of array A is assigned the value of its index:

The loop invariant expresses that all elements up to the current loop index J have the value of their index. With this loop invariant, GNATprove is able to prove the postcondition of Init\_Arr\_Index, namely that all elements of the array have the value of their index:

```
init_arr_index.adb:5:11: info: postcondition proved
init_arr_index.adb:12:30: info: loop invariant initialization proved
init_arr_index.adb:12:30: info: loop invariant preservation proved
init_arr_index.adb:12:61: info: index check proved
```

Similarly, variants of Init\_Vec\_Zero and Init\_List\_Zero that assign a different value to each element of the collection would be proved by GNATprove.

## **Mapping Loops**

This kind of loops iterates over a collection to map every element of the collection to a new value:

Loop Pattern	Separate Modification of Each Element
Proof Objective	Every element of the collection has an updated value.
Loop Behavior	Loops over the collection and updates every element of the collection.
Loop Invariant	Every element updated so far has its specific value.

In the simplest case, every element is assigned a new value based only on its initial value. For example, in procedure Map\_Arr\_Incr below, every element of array A is incremented by one:

```
with Loop_Types; use Loop_Types;
2
   procedure Map_Arr_Incr (A : in out Arr_T) with
     SPARK_Mode,
     Pre => (for all J in A'Range => A(J) /= Component_T'Last),
5
     Post \Rightarrow (for all J in A'Range \Rightarrow A(J) = A'Old(J) + 1)
6
   is
7
   begin
      for J in A'Range loop
9
10
         A(J) := A(J) + 1;
         pragma Loop_Invariant (for all K in A'First .. J => A(K) = A'Loop_Entry(K) + 1);
11
          -- The following loop invariant is generated automatically by GNATprove:
12
          -- pragma Loop_Invariant (for all K in J + 1 .. A'Last => A(K) = A'Loop_
13
   \hookrightarrow Entry (K));
      end loop;
14
   end Map_Arr_Incr;
```

The loop invariant expresses that all elements up to the current loop index J have been incremented (using *Attribute Loop\_Entry*). With this loop invariant, GNATprove is able to prove the postcondition of Map\_Arr\_Incr, namely that all elements of the array have been incremented:

```
map_arr_incr.adb:6:11: info: postcondition proved
map_arr_incr.adb:6:52: info: overflow check proved
map_arr_incr.adb:10:20: info: overflow check proved
map_arr_incr.adb:11:30: info: loop invariant initialization proved
```

```
map_arr_incr.adb:11:30: info: loop invariant preservation proved
map_arr_incr.adb:11:61: info: index check proved
map_arr_incr.adb:11:79: info: index check proved
map_arr_incr.adb:11:82: info: overflow check proved
```

Note that the commented loop invariant expressing that other elements have not been modified is not needed, as it is an example of *Automatically Generated Loop Invariants*.

Consider now a variant of the same initialization loop over a vector:

```
pragma Unevaluated_Use_Of_Old (Allow);
   with Loop_Types; use Loop_Types; use Loop_Types.Vectors;
2
   use Loop_Types.Vectors.Formal_Model;
5
   procedure Map_Vec_Incr (V : in out Vec_T) with
     SPARK Mode.
6
     Pre => (for all I in 1 .. Last_Index (V) =>
7
                   Element (V, I) /= Component_T'Last),
     Post => Last_Index (V) = Last_Index (V) 'Old
9
     and then (for all I in 1 .. Last_Index (V) =>
10
                     Element (V, I) = Element (Model (V)'Old, I) + 1)
11
12
   begin
13
      for J in 1 .. Last_Index (V) loop
14
         pragma Loop_Invariant (Last_Index (V) = Last_Index (V) 'Loop_Entry);
15
         pragma Loop_Invariant
            (for all I in 1 \dots J - 1 \Rightarrow
              Element (V, I) = Element (Model (V) Loop_Entry, I) + 1);
18
         pragma Loop_Invariant
19
            (for all I in J .. Last_Index (V) =>
20
               Element (V, I) = Element (Model (V) 'Loop_Entry, I));
21
         Replace_Element (V, J, Element (V, J) + 1);
22
      end loop;
   end Map_Vec_Incr;
```

Like before, we need an additionnal loop invariant to state that the length of the vector is not modified by the loop. The other two invariants are direct translations of those used for the loop over arrays: the first one expresses that all elements up to the current loop index J have been incremented, and the second one expresses that other elements have not been modified. Note that, as formal vectors are limited, we need to use the Model function of vectors to express the set of elements contained in the vector before the loop (using attributes Loop\_Entry and Old). With this loop invariant, GNATprove is able to prove the postcondition of Map\_Vec\_Incr, namely that all elements of the vector have been incremented:

```
map_vec_incr.adb:8:16: info: precondition proved
map_vec_incr.adb:8:28: info: range check proved
map_vec_incr.adb:9:11: info: postcondition proved
map_vec_incr.adb:11:18: info: precondition proved
map_vec_incr.adb:11:30: info: range check proved
map_vec_incr.adb:11:35: info: precondition proved
map_vec_incr.adb:11:59: info: precondition proved
map_vec_incr.adb:11:59: info: range check proved
map_vec_incr.adb:11:62: info: overflow check proved
map_vec_incr.adb:15:30: info: loop invariant initialization proved
map_vec_incr.adb:15:30: info: loop invariant preservation proved
map_vec_incr.adb:17:10: info: loop invariant initialization proved
map_vec_incr.adb:18:12: info: precondition proved
map_vec_incr.adb:18:24: info: range check proved
map_vec_incr.adb:18:24: info: range check proved
map_vec_incr.adb:18:29: info: precondition proved
```

```
map_vec_incr.adb:18:60: info: range check proved
map_vec_incr.adb:18:63: info: overflow check proved
map_vec_incr.adb:20:10: info: loop invariant initialization proved
map_vec_incr.adb:20:10: info: loop invariant preservation proved
map_vec_incr.adb:21:12: info: precondition proved
map_vec_incr.adb:21:24: info: range check proved
map_vec_incr.adb:21:29: info: precondition proved
map_vec_incr.adb:21:60: info: range check proved
map_vec_incr.adb:22:07: info: precondition proved
map_vec_incr.adb:22:27: info: range check proved
map_vec_incr.adb:22:30: info: precondition proved
map_vec_incr.adb:22:42: info: range check proved
map_vec_incr.adb:22:42: info: range check proved
map_vec_incr.adb:22:42: info: range check proved
map_vec_incr.adb:22:45: info: overflow check proved
```

Similarly, consider a variant of the same initialization loop over a list:

```
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
   with Ada.Containers; use Ada.Containers; use Loop_Types.Lists.Formal_Model;
2
   procedure Map_List_Incr (L : in out List_T) with
4
     SPARK Mode,
     Pre => (for all E of L => E /= Component_T'Last),
6
     Post => Length (L) = Length (L) 'Old
     and then (for all I in 1 .. Length (L) =>
                     Element (Model (L), I) = Element (Model (L'Old), I) + 1)
9
10
      Cu : Cursor := First (L);
11
   begin
12
      while Has_Element (L, Cu) loop
13
         pragma Loop_Invariant (Length (L) = Length (L) 'Loop_Entry);
         pragma Loop_Invariant
15
            (for all I in 1 .. P.Get (Positions (L), Cu) -1 \Rightarrow
16
               Element (Model (L), I) = Element (Model (L'Loop_Entry), I) + 1);
17
         pragma Loop_Invariant
18
            (for all I in P.Get (Positions (L), Cu) .. Length (L) =>
19
               Element (Model (L), I) = Element (Model (L'Loop_Entry), I));
20
         Replace_Element (L, Cu, Element (L, Cu) + 1);
21
         Next (L, Cu);
22
      end loop;
23
   end Map_List_Incr;
```

Like before, we need to use a cursor to iterate over the list. The loop invariants express that all elements up to the current loop index J have been incremented and that other elements have not been modified. Note that it is necessary to state here that the length of the list is not modified during the loop. It is because the length is used to bound the quantification over the elements of the list both in the invariant and in the postcondition. With this loop invariant, GNATprove is able to prove the postcondition of Map\_List\_Incr, namely that all elements of the list have been incremented:

```
map_list_incr.adb:6:12: info: precondition proved
map_list_incr.adb:7:11: info: postcondition proved
map_list_incr.adb:9:18: info: precondition proved
map_list_incr.adb:9:43: info: precondition proved
map_list_incr.adb:9:70: info: overflow check proved
map_list_incr.adb:14:30: info: loop invariant initialization proved
map_list_incr.adb:14:30: info: loop invariant preservation proved
map_list_incr.adb:16:10: info: loop invariant initialization proved
map_list_incr.adb:16:10: info: loop invariant preservation proved
```

```
map_list_incr.adb:16:29: info: precondition proved
map_list_incr.adb:17:12: info: precondition proved
map_list_incr.adb:17:37: info: precondition proved
map_list_incr.adb:17:71: info: overflow check proved
map_list_incr.adb:19:10: info: loop invariant initialization proved
map_list_incr.adb:19:10: info: loop invariant preservation proved
map_list_incr.adb:19:24: info: precondition proved
map_list_incr.adb:20:12: info: precondition proved
map_list_incr.adb:20:32: info: range check proved
map_list_incr.adb:20:37: info: precondition proved
map_list_incr.adb:20:68: info: range check proved
map_list_incr.adb:21:07: info: precondition proved
map_list_incr.adb:21:31: info: precondition proved
map_list_incr.adb:21:31: info: precondition proved
map_list_incr.adb:21:47: info: overflow check proved
map_list_incr.adb:22:07: info: precondition proved
```

## **Validation Loops**

This kind of loops iterates over a collection to validate that every element of the collection has a valid value. The most common pattern is to exit or return from the loop if an invalid value if encountered:

Loop Pattern	Sequence Validation with Early Exit
Proof Objective	Determine (flag) if there are any invalid elements in a given collection.
Loop Behavior	Loops over the collection and exits/returns if an invalid element is encountered.
Loop Invariant	Every element encountered so far is valid.

Consider a procedure Validate\_Arr\_Zero that checks that all elements of an array A have value zero:

```
with Loop_Types; use Loop_Types;
2
   procedure Validate_Arr_Zero (A : Arr_T; Success : out Boolean) with
4
     SPARK_Mode,
5
     Post => Success = (for all J in A'Range => A(J) = 0)
   is
6
7
   begin
      for J in A'Range loop
         if A(J) /= 0 then
            Success := False;
            return;
11
         end if:
12
         pragma Loop_Invariant (for all K in A'First .. J => A(K) = 0);
13
      end loop;
14
      Success := True;
   end Validate_Arr_Zero;
```

The loop invariant expresses that all elements up to the current loop index J have value zero. With this loop invariant, GNATprove is able to prove the postcondition of Validate\_Arr\_Zero, namely that output parameter Success is True if-and-only-if all elements of the array have value zero:

```
validate_arr_zero.adb:3:41: info: initialization of "Success" proved
validate_arr_zero.adb:5:11: info: postcondition proved
validate_arr_zero.adb:13:30: info: loop invariant initialization proved
validate_arr_zero.adb:13:30: info: loop invariant preservation proved
validate_arr_zero.adb:13:61: info: index check proved
```

Consider now a variant of the same validation loop over a vector:

```
with Loop_Types; use Loop_Types; use Loop_Types. Vectors;
2
   procedure Validate_Vec_Zero (V : Vec_T; Success : out Boolean) with
3
     SPARK_Mode,
     Post => Success = (for all J in First_Index (V) .. Last_Index (V) => Element (V, J)...
   is
6
   begin
      for J in First_Index (V) .. Last_Index (V) loop
8
         if Element (V, J) /= 0 then
9
            Success := False;
10
            return;
11
         end if;
12
         pragma Loop_Invariant (for all K in First_Index (V) .. J => Element (V, K) = 0);
13
      end loop;
14
15
      Success := True;
16
   end Validate_Vec_Zero;
```

Like before, the loop invariant expresses that all elements up to the current loop index J have the value zero. Since variable V is not modified in the loop, no additional loop invariant is needed here for GNATprove to know that its length stays the same (this is different from the case of Init\_Vec\_Zero seen previously). With this loop invariant, GNATprove is able to prove the postcondition of Validate\_Vec\_Zero, namely that output parameter Success is True if-and-only-if all elements of the vector have value zero:

```
validate_vec_zero.adb:3:41: info: initialization of "Success" proved validate_vec_zero.adb:5:11: info: postcondition proved validate_vec_zero.adb:5:72: info: precondition proved validate_vec_zero.adb:5:84: info: range check proved validate_vec_zero.adb:9:10: info: precondition proved validate_vec_zero.adb:9:22: info: range check proved validate_vec_zero.adb:13:30: info: loop invariant initialization proved validate_vec_zero.adb:13:30: info: loop invariant preservation proved validate_vec_zero.adb:13:67: info: precondition proved validate_vec_zero.adb:13:79: info: range check proved
```

Similarly, consider a variant of the same validation loop over a list:

```
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
   with Ada. Containers; use Ada. Containers; use Loop_Types.Lists.Formal_Model;
2
   procedure Validate_List_Zero (L : List_T; Success : out Boolean) with
     SPARK_Mode,
5
     Post \Rightarrow Success = (for all E of L \Rightarrow E = 0)
6
   is
7
      Cu : Cursor := First (L);
   begin
      while Has_Element (L, Cu) loop
10
         pragma Loop_Invariant (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
11
                                     Element (Model (L), I) = 0);
12
          if Element (L, Cu) /= 0 then
13
             Success := False;
14
             return:
15
          end if;
16
          Next (L, Cu);
17
      end loop;
18
19
      Success := True;
20
```

```
end Validate_List_Zero;
```

Like in the case of Init\_List\_Zero seen previously, we need to define a cursor here to iterate over the list. The loop invariant expresses that all elements up to the current cursor Cu have the value zero. With this loop invariant, GNATprove is able to prove the postcondition of Validate\_List\_Zero, namely that output parameter Success is True if-and-only-if all elements of the list have value zero:

```
validate_list_zero.adb:4:43: info: initialization of "Success" proved validate_list_zero.adb:6:11: info: postcondition proved validate_list_zero.adb:6:22: info: precondition proved validate_list_zero.adb:11:30: info: loop invariant initialization proved validate_list_zero.adb:11:30: info: loop invariant preservation proved validate_list_zero.adb:11:49: info: precondition proved validate_list_zero.adb:12:32: info: precondition proved validate_list_zero.adb:13:10: info: precondition proved validate_list_zero.adb:17:07: info: precondition proved
```

The case of sets and maps is similar to the case of lists.

A variant of the previous validation pattern is to continue validating elements even after an invalid value has been encountered, which allows for example logging all invalid values:

Loop	Sequence Validation that Validates Entire Collection
Pattern	
Proof	Determine (flag) if there are any invalid elements in a given collection.
Objec-	
tive	
Loop	Loops over the collection. If an invalid element is encountered, flag this, but keep
Behavior	validating (typically logging every invalidity) for the entire collection.
Loop	If invalidity is not flagged, every element encountered so far is valid.
Invariant	

Consider a variant of Validate\_Arr\_Zero that keeps validating elements of the array after a non-zero element has been encountered:

```
with Loop_Types; use Loop_Types;
2
   procedure Validate_Full_Arr_Zero (A : Arr_T; Success : out Boolean) with
     SPARK Mode,
4
     Post \Rightarrow Success = (for all J in A'Range \Rightarrow A(J) = 0)
   is
   begin
      Success := True;
      for J in A'Range loop
10
         if A(J) /= 0 then
11
12
             Success := False;
             -- perform some logging here instead of returning
13
          end if;
14
         pragma Loop_Invariant (Success = (for all K in A'First .. J => A(K) = 0));
15
      end loop;
16
   end Validate_Full_Arr_Zero;
```

The loop invariant has been modified to state that all elements up to the current loop index J have value zero if-and-only-if the output parameter Success is True. This in turn requires to move the assignment of Success before the loop. With this loop invariant, GNATprove is able to prove the postcondition of Validate\_Full\_Arr\_Zero, which is the same as the postcondition of Validate\_Arr\_Zero, namely that output parameter Success is True if-and-only-if all elements of the array have value zero:

```
validate_full_arr_zero.adb:3:46: info: initialization of "Success" proved
validate_full_arr_zero.adb:5:11: info: postcondition proved
validate_full_arr_zero.adb:15:30: info: loop invariant initialization proved
validate_full_arr_zero.adb:15:30: info: loop invariant preservation proved
validate_full_arr_zero.adb:15:72: info: index check proved
```

Similarly, variants of Validate\_Vec\_Zero and Validate\_List\_Zero that keep validating elements of the collection after a non-zero element has been encountered would be proved by GNATprove.

## **Counting Loops**

This kind of loops iterates over a collection to count the number of elements of the collection that satisfy a given criterion:

Loop	Count Elements Satisfying Criterion
Pattern	
Proof	Count elements that satisfy a given criterion.
Objec-	
tive	
Loop	Loops over the collection. Increments a counter each time the value of an element satisfies
Behav-	the criterion.
ior	
Loop	The value of the counter is either 0 when no element encountered so far satisfies the
Invari-	criterion, or a positive number bounded by the current iteration of the loop otherwise.
ant	

Consider a procedure Count\_Arr\_Zero that counts elements with value zero in array A:

```
with Loop_Types; use Loop_Types;
2
   procedure Count_Arr_Zero (A : Arr_T; Counter : out Natural) with
     SPARK_Mode,
     Post => (Counter in 0 .. A'Length) and then
             ((Counter = 0) = (for all K in A'Range => A(K) /= 0))
6
   is
   begin
      Counter := 0;
10
      for J in A'Range loop
11
         if A(J) = 0 then
12
            Counter := Counter + 1;
13
         end if;
14
         pragma Loop_Invariant (Counter in 0 .. J);
15
         pragma Loop_Invariant ((Counter = 0) = (for all K in A'First .. J => A(K) /=_
   →0));
      end loop;
   end Count_Arr_Zero;
```

The loop invariant expresses that the value of Counter is a natural number bounded by the current loop index J, and that Counter is equal to zero exactly when all elements up to the current loop index have a non-zero value. With this loop invariant, GNATprove is able to prove the postcondition of Count\_Arr\_Zero, namely that output parameter Counter is a natural number bounded by the length of the array A, and that Counter is equal to zero exactly when all elements in A have a non-zero value:

```
count_arr_zero.adb:3:38: info: initialization of "Counter" proved
count_arr_zero.adb:5:11: info: postcondition proved
```

```
count_arr_zero.adb:13:29: info: overflow check proved count_arr_zero.adb:15:30: info: loop invariant initialization proved count_arr_zero.adb:15:30: info: loop invariant preservation proved count_arr_zero.adb:16:30: info: loop invariant initialization proved count_arr_zero.adb:16:30: info: loop invariant preservation proved count_arr_zero.adb:16:78: info: index check proved
```

Consider now a variant of the same counting loop over a vector:

```
with Loop_Types; use Loop_Types; use Loop_Types. Vectors;
2
   procedure Count_Vec_Zero (V : Vec_T; Counter : out Natural) with
3
     SPARK Mode,
4
     Post => (Counter in 0 .. Natural (Length (V))) and then
5
              ((Counter = 0) = (for all K in First_Index (V) .. Last_Index (V) => Element_I
   \rightarrow (V, K) /= 0))
   is
   begin
      Counter := 0;
10
      for J in First_Index (V) .. Last_Index (V) loop
11
         if Element (V, J) = 0 then
12
             Counter := Counter + 1;
13
         end if;
         pragma Loop_Invariant (Counter in 0 .. J);
15
         pragma Loop_Invariant ((Counter = 0) = (for all K in First_Index (V) .. J =>_
16
   \rightarrowElement (V, K) /= 0));
      end loop;
17
   end Count_Vec_Zero;
```

Like before, the loop invariant expresses that the value of Counter is a natural number bounded by the current loop index J, and that Counter is equal to zero exactly when all elements up to the current loop index have a non-zero value. With this loop invariant, GNAT prove is able to prove the postcondition of Count\_Vec\_Zero, namely that output parameter Counter is a natural number bounded by the length of the vector V, and that Counter is equal to zero exactly when all elements in V have a non-zero value:

```
count_vec_zero.adb:3:38: info: initialization of "Counter" proved count_vec_zero.adb:5:11: info: postcondition proved count_vec_zero.adb:6:79: info: precondition proved count_vec_zero.adb:6:91: info: range check proved count_vec_zero.adb:12:10: info: precondition proved count_vec_zero.adb:12:22: info: range check proved count_vec_zero.adb:13:29: info: overflow check proved count_vec_zero.adb:15:30: info: loop invariant initialization proved count_vec_zero.adb:15:30: info: loop invariant preservation proved count_vec_zero.adb:16:30: info: loop invariant initialization proved count_vec_zero.adb:16:30: info: loop invariant preservation proved count_vec_zero.adb:16:84: info: precondition proved count_vec_zero.adb:16:84: info: precondition proved count_vec_zero.adb:16:96: info: range check proved
```

## **Search Loops**

This kind of loops iterates over a collection to search an element of the collection that meets a given search criterion:

Loop Pattern	Search with Early Exit
Proof	Find an element or position that meets a search criterion.
Objective	
Loop	Loops over the collection. Exits when an element that meets the search criterion is
Behavior	found.
Loop Invariant	Every element encountered so far does not meet the search criterion.

Consider a procedure Search\_Arr\_Zero that searches an element with value zero in array A:

```
with Loop_Types; use Loop_Types;
2
   procedure Search_Arr_Zero (A : Arr_T; Pos : out Opt_Index_T; Success : out Boolean)_
    -with
     SPARK_Mode,
     Post => Success = (for some J in A'Range => A(J) = 0) and then
5
              (if Success then A (Pos) = 0)
6
7
   begin
8
      for J in A'Range loop
9
         if A(J) = 0 then
10
            Success := True;
11
            Pos := J;
12
            return;
13
         end if;
14
         pragma Loop_Invariant (for all K in A'First .. J => A(K) /= 0);
15
      end loop;
16
17
      Success := False;
18
      Pos := 0;
19
   end Search_Arr_Zero;
```

The loop invariant expresses that all elements up to the current loop index J have a non-zero value. With this loop invariant, GNATprove is able to prove the postcondition of Search\_Arr\_Zero, namely that output parameter Success is True if-and-only-if there is an element of the array that has value zero, and that Pos is the index of such an element:

```
search_arr_zero.adb:3:39: info: initialization of "Pos" proved search_arr_zero.adb:3:62: info: initialization of "Success" proved search_arr_zero.adb:5:11: info: postcondition proved search_arr_zero.adb:6:31: info: index check proved search_arr_zero.adb:15:30: info: loop invariant initialization proved search_arr_zero.adb:15:30: info: loop invariant preservation proved search_arr_zero.adb:15:61: info: index check proved
```

Consider now a variant of the same search loop over a vector:

```
with Loop_Types; use Loop_Types; use Loop_Types. Vectors;
2
   procedure Search_Vec_Zero (V : Vec_T; Pos : out Opt_Index_T; Success : out Boolean)_
   \hookrightarrowwith
     SPARK_Mode,
     Post => Success = (for some J in First_Index (V) .. Last_Index (V) => Element (V, ...
   \hookrightarrow J) = 0) and then
              (if Success then Element (V, Pos) = 0)
6
   is
   begin
8
9
      for J in First_Index (V) .. Last_Index (V) loop
          if Element (V, J) = 0 then
10
```

```
Success := True;
11
              Pos := J;
12
13
              return;
          end if:
          pragma Loop_Invariant (for all K in First_Index (V) .. J => Element (V, K) /=..
    \hookrightarrow 0);
       end loop;
16
17
       Success := False;
18
       Pos := 0;
19
   end Search_Vec_Zero;
```

Like before, the loop invariant expresses that all elements up to the current loop index J have a non-zero value. With this loop invariant, GNATprove is able to prove the postcondition of Search\_Vec\_Zero, namely that output parameter Success is True if-and-only-if there is an element of the vector that has value zero, and that Pos is the index of such an element:

```
search_vec_zero.adb:3:39: info: initialization of "Pos" proved search_vec_zero.adb:3:62: info: initialization of "Success" proved search_vec_zero.adb:5:11: info: postcondition proved search_vec_zero.adb:5:73: info: precondition proved search_vec_zero.adb:5:85: info: range check proved search_vec_zero.adb:6:28: info: precondition proved search_vec_zero.adb:6:40: info: precondition proved search_vec_zero.adb:10:10: info: precondition proved search_vec_zero.adb:10:22: info: range check proved search_vec_zero.adb:12:17: info: range check proved search_vec_zero.adb:15:30: info: loop invariant initialization proved search_vec_zero.adb:15:30: info: loop invariant preservation proved search_vec_zero.adb:15:67: info: precondition proved search_vec_zero.adb:15:79: info: range check proved
```

Similarly, consider a variant of the same search loop over a list:

```
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
2
   with Ada.Containers; use Ada.Containers; use Loop_Types.Lists.Formal_Model;
   procedure Search_List_Zero (L : List_T; Pos : out Cursor; Success : out Boolean) with
     SPARK Mode,
     Post \Rightarrow Success = (for some E of L \Rightarrow E = 0) and then
6
              (if Success then Element (L, Pos) = 0)
      Cu : Cursor := First (L);
   begin
10
11
      while Has_Element (L, Cu) loop
         pragma Loop_Invariant (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
12
                                     Element (Model (L), I) \neq 0);
13
          if Element (L, Cu) = 0 then
14
             Success := True;
15
             Pos := Cu;
             return;
          end if;
          Next (L, Cu);
19
      end loop;
20
21
22
      Success := False;
23
      Pos := No_Element;
   end Search_List_Zero;
```

The loop invariant expresses that all elements up to the current cursor Cu have a non-zero value. With this loop invariant, GNATprove is able to prove the postcondition of Search\_List\_Zero, namely that output parameter Success is True if-and-only-if there is an element of the list that has value zero, and that Pos is the cursor of such an element:

```
search_list_zero.adb:4:41: info: initialization of "Pos" proved search_list_zero.adb:4:59: info: initialization of "Success" proved search_list_zero.adb:6:11: info: postcondition proved search_list_zero.adb:6:22: info: precondition proved search_list_zero.adb:7:28: info: precondition proved search_list_zero.adb:12:30: info: loop invariant initialization proved search_list_zero.adb:12:30: info: loop invariant preservation proved search_list_zero.adb:12:49: info: precondition proved search_list_zero.adb:13:32: info: precondition proved search_list_zero.adb:14:10: info: precondition proved search_list_zero.adb:19:07: info: precondition proved
```

The case of sets and maps is similar to the case of lists. For more complex examples of search loops, see the *SPARK Tutorial* as well as the section on *How to Write Loop Invariants*.

## **Maximize Loops**

This kind of loops iterates over a collection to search an element of the collection that maximizes a given optimality criterion:

Loop	Search Optimum to Criterion
Pattern	
Proof	Find an element or position that maximizes an optimality criterion.
Objective	
Loop	Loops over the collection. Records maximum value of criterion so far and possibly
Behavior	index that maximizes this criterion.
Loop	Exactly one element encountered so far corresponds to the recorded maximum over
Invariant	other elements encountered so far.

Consider a procedure Search\_Arr\_Max that searches an element maximum value in array A:

```
with Loop_Types; use Loop_Types;
2
   procedure Search_Arr_Max (A : Arr_T; Pos : out Index_T; Max : out Component_T) with
     SPARK_Mode,
     Post => (for all J in A'Range => A(J) <= Max) and then
              (for some J in A'Range => A(J) = Max) and then
6
             A(Pos) = Max
7
   is
8
   begin
Q
      Max := 0;
10
      Pos := A'First;
12
13
      for J in A'Range loop
         if A(J) > Max then
14
            Max := A(J);
15
            Pos := J;
16
         end if;
17
         pragma Loop_Invariant (for all K in A'First .. J => A(K) <= Max);</pre>
18
19
         pragma Loop_Invariant (for some K in A'First .. J => A(K) = Max);
         pragma Loop_Invariant (A(Pos) = Max);
```

```
end loop;
end Search_Arr_Max;
```

The loop invariant expresses that all elements up to the current loop index J have a value less than Max, and that Max is the value of one of these elements. The last loop invariant gives in fact this element, it is A (Pos), but this part of the loop invariant may not be present if the position Pos for the optimum is not recorded. With this loop invariant, GNATprove is able to prove the postcondition of Search\_Arr\_Max, namely that output parameter Max is the maximum of the elements in the array, and that Pos is the index of such an element:

```
search_arr_max.adb:3:38: info: initialization of "Pos" proved search_arr_max.adb:3:57: info: initialization of "Max" proved search_arr_max.adb:5:11: info: postcondition proved search_arr_max.adb:18:30: info: loop invariant initialization proved search_arr_max.adb:18:30: info: loop invariant preservation proved search_arr_max.adb:18:61: info: index check proved search_arr_max.adb:19:30: info: loop invariant initialization proved search_arr_max.adb:19:30: info: loop invariant preservation proved search_arr_max.adb:19:62: info: index check proved search_arr_max.adb:20:30: info: loop invariant initialization proved search_arr_max.adb:20:30: info: loop invariant preservation proved search_arr_max.adb:20:30: info: loop invariant preservation proved
```

Consider now a variant of the same search loop over a vector:

```
with Loop_Types; use Loop_Types; use Loop_Types. Vectors;
2
   procedure Search_Vec_Max (V : Vec_T; Pos : out Index_T; Max : out Component_T) with
3
     SPARK_Mode,
4
     Pre => not Is_Empty (V),
5
     Post => (for all J in First_Index (V) .. Last_Index (V) => Element (V, J) <= Max)_
   →and then
              (for some J in First_Index (V) .. Last_Index (V) => Element (V, J) = Max)_
   \hookrightarrowand then
              Pos in First_Index (V) .. Last_Index (V) and then
              Element (V, Pos) = Max
   is
10
   begin
11
      Max := 0;
12
      Pos := First_Index (V);
13
14
      for J in First_Index (V) .. Last_Index (V) loop
15
          if Element (V, J) > Max then
16
             Max := Element (V, J);
17
             Pos := J;
18
         end if:
         pragma Loop_Invariant (for all K in First_Index (V) .. J => Element (V, K) <=_</pre>
20
         pragma Loop_Invariant (for some K in First_Index (V) .. J => Element (V, K) =
21
   \rightarrowMax);
         pragma Loop_Invariant (Pos in First_Index (V) .. J);
22
         pragma Loop_Invariant (Element (V, Pos) = Max);
23
      end loop;
24
   end Search_Vec_Max;
```

Like before, the loop invariant expresses that all elements up to the current loop index J have a value less than Max, and that Max is the value of one of these elements, most precisely the value of Element (V, Pos) if the position Pos for the optimum is recorded. An additional loop invariant is needed here compared to the case of arrays to state that Pos remains within the bounds of the vector. With this loop invariant, GNATprove is able to prove the postcondition

of Search\_Vec\_Max, namely that output parameter Max is the maximum of the elements in the vector, and that Pos is the index of such an element:

```
search_vec_max.adb:3:38: info: initialization of "Pos" proved
search_vec_max.adb:3:57: info: initialization of "Max" proved
search_vec_max.adb:6:11: info: postcondition proved
search_vec_max.adb:6:62: info: precondition proved
search_vec_max.adb:6:74: info: range check proved
search_vec_max.adb:7:63: info: precondition proved
search_vec_max.adb:7:75: info: range check proved
search_vec_max.adb:9:11: info: precondition proved
search_vec_max.adb:16:10: info: precondition proved
search_vec_max.adb:16:22: info: range check proved
search_vec_max.adb:17:17: info: precondition proved
search_vec_max.adb:17:29: info: range check proved
search_vec_max.adb:18:17: info: range check proved
search_vec_max.adb:20:30: info: loop invariant initialization proved
search_vec_max.adb:20:30: info: loop invariant preservation proved
search_vec_max.adb:20:67: info: precondition proved
search_vec_max.adb:20:79: info: range check proved
search_vec_max.adb:21:30: info: loop invariant initialization proved
search_vec_max.adb:21:30: info: loop invariant preservation proved
search_vec_max.adb:21:68: info: precondition proved
search_vec_max.adb:21:80: info: range check proved
search_vec_max.adb:22:30: info: loop invariant initialization proved
search_vec_max.adb:22:30: info: loop invariant preservation proved
search_vec_max.adb:23:30: info: loop invariant initialization proved
search_vec_max.adb:23:30: info: loop invariant preservation proved
search_vec_max.adb:23:30: info: precondition proved
```

Similarly, consider a variant of the same search loop over a list:

```
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
   with Ada. Containers; use Ada. Containers; use Loop_Types.Lists.Formal_Model;
2
   procedure Search_List_Max (L : List_T; Pos : out Cursor; Max : out Component_T) with
     SPARK_Mode,
     Pre => not Is_Empty (L),
6
     Post => (for all E of L => E <= Max) and then
              (for some E of L => E = Max) and then
             Has_Element (L, Pos) and then
             Element (L, Pos) = Max
10
11
   is
      Cu : Cursor := First (L);
12
   begin
13
      Max := 0;
14
      Pos := Cu;
15
      while Has_Element (L, Cu) loop
17
         pragma Loop_Invariant (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
18
                                    Element (Model (L), I) <= Max);</pre>
19
         pragma Loop_Invariant (Has_Element (L, Pos));
20
         pragma Loop_Invariant (Max = 0 or else Element (L, Pos) = Max);
21
22
         if Element (L, Cu) > Max then
23
            Max := Element (L, Cu);
24
            Pos := Cu;
25
         end if;
26
         Next (L, Cu);
```

```
end loop;
end Search_List_Max;
```

The loop invariant expresses that all elements up to the current cursor Cu have a value less than Max, and that Max is the value of one of these elements, most precisely the value of Element (L, Pos) if the cursor Pos for the optimum is recorded. Like for vectors, an additional loop invariant is needed here compared to the case of arrays to state that cursor Pos is a valid cursor of the list. A minor difference is that a loop invariant now starts with Max = 0 or else .. because the loop invariant is stated at the start of the loop (for convenience with the use of First\_To\_Previous) which requires this modification. With this loop invariant, GNATprove is able to prove the postcondition of Search\_List\_Max, namely that output parameter Max is the maximum of the elements in the list, and that Pos is the cursor of such an element:

```
search_list_max.adb:4:40: info: initialization of "Pos" proved
search_list_max.adb:4:58: info: initialization of "Max" proved
search_list_max.adb:7:11: info: postcondition proved
search_list_max.adb:7:12: info: precondition proved
search_list_max.adb:8:12: info: precondition proved
search_list_max.adb:10:11: info: precondition proved
search_list_max.adb:18:30: info: loop invariant initialization proved
search_list_max.adb:18:30: info: loop invariant preservation proved
search_list_max.adb:18:49: info: precondition proved
search_list_max.adb:19:32: info: precondition proved
search_list_max.adb:20:30: info: loop invariant initialization proved
search_list_max.adb:20:30: info: loop invariant preservation proved
search_list_max.adb:21:30: info: loop invariant initialization proved
search_list_max.adb:21:30: info: loop invariant preservation proved
search_list_max.adb:21:46: info: precondition proved
search_list_max.adb:23:10: info: precondition proved
search_list_max.adb:24:17: info: precondition proved
search_list_max.adb:27:07: info: precondition proved
```

The case of sets and maps is similar to the case of lists. For more complex examples of search loops, see the *SPARK Tutorial* as well as the section on *How to Write Loop Invariants*.

#### **Update Loops**

This kind of loops iterates over a collection to update individual elements based either on their value or on their position. The first pattern we consider is the one that updates elements based on their value:

Loop	Modification of Elements Based on Value
Pattern	
Proof	Elements of the collection are updated based on their value.
Objective	
Loop	Loops over a collection and assigns the elements whose value satisfies a given
Behavior	modification criterion.
Loop	Every element encountered so far has been assigned according to its value.
Invariant	

Consider a procedure Update\_Arr\_Zero that sets to zero all elements in array A that have a value smaller than a given Threshold:

```
6
   begin
7
      for J in A'Range loop
         if A(J) \le Threshold then
Q
            A(J) := 0;
         end if;
         pragma Loop_Invariant (for all K in A'First .. J => A(K) = (if A'Loop_Entry(K))
12
   →<= Threshold then 0 else A'Loop_Entry(K)));</pre>
          -- The following loop invariant is generated automatically by GNATprove:
13
          -- pragma Loop_Invariant (for all K in J + 1 .. A'Last => A(K) = A'Loop_
14
   \rightarrow Entry (K));
      end loop;
   end Update_Arr_Zero;
```

The loop invariant expresses that all elements up to the current loop index J have been zeroed out if initially smaller than Threshold (using Attribute Loop\_Entry). With this loop invariant, GNAT prove is able to prove the postcondition of Update\_Arr\_Zero, namely that all elements initially smaller than Threshold have been zeroed out, and that other elements have not been modified:

```
update_arr_zero.adb:5:11: info: postcondition proved
update_arr_zero.adb:12:30: info: loop invariant initialization proved
update_arr_zero.adb:12:30: info: loop invariant preservation proved
update_arr_zero.adb:12:61: info: index check proved
update_arr_zero.adb:12:83: info: index check proved
update_arr_zero.adb:12:124: info: index check proved
```

Note that the commented loop invariant expressing that other elements have not been modified is not needed, as it is an example of *Automatically Generated Loop Invariants*.

Consider now a variant of the same update loop over a vector:

```
pragma Unevaluated_Use_Of_Old (Allow);
2
   with Loop_Types; use Loop_Types; use Loop_Types.Vectors;
   use Loop_Types.Vectors.Formal_Model;
   procedure Update_Vec_Zero (V : in out Vec_T; Threshold : Component_T) with
5
     SPARK_Mode,
6
     Post => Last_Index (V) = Last_Index (V) 'Old
7
     and (for all I in 1 .. Last_Index (V) =>
                Element (V, I) =
                 (if Element (Model (V) 'Old, I) <= Threshold then 0
10
                  else Element (Model (V)'Old, I)))
11
   is
12
   begin
13
      for J in First_Index (V) .. Last_Index (V) loop
14
         pragma Loop_Invariant (Last_Index (V) = Last_Index (V) 'Loop_Entry);
15
         pragma Loop_Invariant
            (for all I in 1 \dots J - 1 \Rightarrow
17
                 Element (V, I) =
18
                  (if Element (Model (V) 'Loop_Entry, I) <= Threshold then 0
19
                   else Element (Model (V) 'Loop_Entry, I)));
20
         pragma Loop_Invariant
21
            (for all I in J .. Last_Index (V) =>
22
                 Element (V, I) = Element (Model (V) 'Loop_Entry, I));
23
         if Element (V, J) <= Threshold then</pre>
24
             Replace_Element (V, J, 0);
25
         end if;
26
      end loop;
```

```
end Update_Vec_Zero;
```

Like for Map\_Vec\_Incr, we need to use the Model function over arrays to access elements of the vector before the loop as the vector type is limited. The loop invariant expresses that all elements up to the current loop index J have been zeroed out if initially smaller than Threshold, that elements that follow the current loop index have not been modified, and that the length of V is not modified (like in Init\_Vec\_Zero). With this loop invariant, GNATprove is able to prove the postcondition of Update\_Vec\_Zero:

```
update_vec_zero.adb:7:11: info: postcondition proved
update_vec_zero.adb:9:13: info: precondition proved
update_vec_zero.adb:9:25: info: range check proved
update_vec_zero.adb:10:18: info: precondition proved
update_vec_zero.adb:10:42: info: range check proved
update_vec_zero.adb:11:20: info: precondition proved
update_vec_zero.adb:11:44: info: range check proved
update_vec_zero.adb:15:30: info: loop invariant initialization proved
update_vec_zero.adb:15:30: info: loop invariant preservation proved
update_vec_zero.adb:17:10: info: loop invariant initialization proved
update_vec_zero.adb:17:10: info: loop invariant preservation proved
update_vec_zero.adb:17:30: info: overflow check proved
update_vec_zero.adb:18:14: info: precondition proved
update_vec_zero.adb:18:26: info: range check proved
update_vec_zero.adb:19:19: info: precondition proved
update_vec_zero.adb:19:50: info: range check proved
update_vec_zero.adb:20:21: info: precondition proved
update_vec_zero.adb:20:52: info: range check proved
update_vec_zero.adb:22:10: info: loop invariant initialization proved
update_vec_zero.adb:22:10: info: loop invariant preservation proved
update_vec_zero.adb:23:14: info: precondition proved
update_vec_zero.adb:23:26: info: range check proved
update_vec_zero.adb:23:31: info: precondition proved
update_vec_zero.adb:23:62: info: range check proved
update_vec_zero.adb:24:10: info: precondition proved
update_vec_zero.adb:24:22: info: range check proved
update_vec_zero.adb:25:10: info: precondition proved
update_vec_zero.adb:25:30: info: range check proved
```

Similarly, consider a variant of the same update loop over a list:

```
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
   with Ada. Containers; use Ada. Containers; use Loop_Types.Lists.Formal_Model;
2
3
   procedure Update_List_Zero (L : in out List_T; Threshold : Component_T) with
     SPARK_Mode,
5
     Post => Length (L) = Length (L) 'Old
6
     and (for all I in 1 .. Length (L) =>
7
               Element (Model (L), I) =
                 (if Element (Model (L'Old), I) <= Threshold then 0
                 else Element (Model (L'Old), I)))
11
      Cu : Cursor := First (L);
12
   begin
13
      while Has_Element (L, Cu) loop
14
         pragma Loop_Invariant (Length (L) = Length (L) 'Loop_Entry);
15
         pragma Loop_Invariant
16
            (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
17
               Element (Model (L), I) =
18
                 (if Element (Model (L'Loop_Entry), I) <= Threshold then 0
```

```
else Element (Model (L'Loop_Entry), I)));
20
          pragma Loop Invariant
21
            (for all I in P.Get (Positions (L), Cu) .. Length (L) =>
22
                Element (Model (L), I) = Element (Model (L'Loop_Entry), I));
23
          if Element (L, Cu) <= Threshold then</pre>
             Replace_Element (L, Cu, 0);
          end if;
26
         Next (L, Cu);
27
      end loop;
28
   end Update_List_Zero;
```

The loop invariant expresses that all elements up to the current cursor Cu have been zeroed out if initially smaller than Threshold (using function Model to access the element stored at a given position in the list and function Positions to query the position of the current cursor), and that elements that follow the current loop index have not been modified. Note that it is necessary to state here that the length of the list is not modified during the loop. It is because the length is used to bound the quantification over the elements of the list both in the invariant and in the postcondition.

With this loop invariant, GNATprove is able to prove the postcondition of <code>Update\_List\_Zero</code>, namely that all elements initially smaller than <code>Threshold</code> have been zeroed out, and that other elements have not been modified:

```
update_list_zero.adb:6:11: info: postcondition proved
update_list_zero.adb:8:13: info: precondition proved
update_list_zero.adb:9:18: info: precondition proved
update_list_zero.adb:10:20: info: precondition proved
update_list_zero.adb:15:30: info: loop invariant initialization proved
update_list_zero.adb:15:30: info: loop invariant preservation proved
update_list_zero.adb:17:10: info: loop invariant initialization proved
update_list_zero.adb:17:10: info: loop invariant preservation proved
update_list_zero.adb:17:29: info: precondition proved
update_list_zero.adb:18:13: info: precondition proved
update_list_zero.adb:19:18: info: precondition proved
update_list_zero.adb:20:20: info: precondition proved
update_list_zero.adb:22:10: info: loop invariant initialization proved
update_list_zero.adb:22:10: info: loop invariant preservation proved
update_list_zero.adb:22:24: info: precondition proved
update_list_zero.adb:23:13: info: precondition proved
update_list_zero.adb:23:33: info: range check proved
update_list_zero.adb:23:38: info: precondition proved
update_list_zero.adb:23:69: info: range check proved
update_list_zero.adb:24:10: info: precondition proved
update_list_zero.adb:25:10: info: precondition proved
update_list_zero.adb:27:07: info: precondition proved
```

The case of sets and maps is similar to the case of lists.

The second pattern of update loops that we consider now is the one that updates elements based on their position:

Loop	Modification of Elements Based on Position
Pattern	
Proof	Elements of the collection are updated based on their position.
Objective	
Loop	Loops over a collection and assigns the elements whose position satisfies a given
Behavior	modification criterion.
Loop	Every element encountered so far has been assigned according to its position.
Invariant	

Consider a procedure Update\_Range\_Arr\_Zero that sets to zero all elements in array A between indexes First

and Last:

```
with Loop_Types; use Loop_Types;
2
   procedure Update_Range_Arr_Zero (A : in out Arr_T; First, Last : Index_T) with
3
     SPARK_Mode,
4
     Post => A = A'Old'Update (First .. Last => 0)
5
   is
6
   begin
7
      for J in First .. Last loop
         A(J) := 0;
         pragma Loop_Invariant (A = A'Loop_Entry'Update (First .. J => 0));
10
      end loop;
11
   end Update_Range_Arr_Zero;
12
```

The loop invariant expresses that all elements between First and the current loop index J have been zeroed out, and that other elements have not been modified (using a combination of *Attribute Loop\_Entry* and *Attribute Update* to express this concisely). With this loop invariant, GNATprove is able to prove the postcondition of Update\_Range\_Arr\_Zero, namely that all elements between First and Last have been zeroed out, and that other elements have not been modified:

```
update_range_arr_zero.adb:5:11: info: postcondition proved update_range_arr_zero.adb:10:30: info: loop invariant initialization proved update_range_arr_zero.adb:10:30: info: loop invariant preservation proved update_range_arr_zero.adb:10:64: info: range check proved
```

Consider now a variant of the same update loop over a vector:

```
pragma Unevaluated_Use_Of_Old (Allow);
   with Loop_Types; use Loop_Types; use Loop_Types.Vectors;
2
3
   use Loop_Types.Vectors.Formal_Model;
4
   procedure Update_Range_Vec_Zero (V : in out Vec_T; First, Last : Index_T) with
5
     SPARK_Mode,
6
     Pre => Last <= Last_Index (V),</pre>
7
     Post => (for all J in 1 .. Last_Index (V) =>
                   (if J in First .. Last then Element (V, J) = 0
                    else Element (V, J) = Element (Model <math>(V)'Old, J))
10
11
   begin
12
      for J in First .. Last loop
13
         Replace_Element (V, J, 0);
14
         pragma Loop_Invariant (Last_Index (V) = Last_Index (V) 'Loop_Entry);
15
16
         pragma Loop_Invariant
            (for all I in 1 .. Last_Index (V) =>
17
                   (if I in First .. J then Element (V, I) = 0
18
                    else Element (V, I) = Element (Model (V) 'Loop_Entry, I)));
19
      end loop;
20
   end Update_Range_Vec_Zero;
21
```

Like for Map\_Vec\_Incr, we need to use the Model function over arrays to access elements of the vector before the loop as the vector type is limited. The loop invariant expresses that all elements between First and current loop index J have been zeroed, and that other elements have not been modified. With this loop invariant, GNATprove is able to prove the postcondition of Update\_Range\_Vec\_Zero:

```
update_range_vec_zero.adb:8:11: info: postcondition proved update_range_vec_zero.adb:9:44: info: precondition proved update_range_vec_zero.adb:9:56: info: range check proved
```

```
update_range_vec_zero.adb:10:22: info: precondition proved
update_range_vec_zero.adb:10:34: info: range check proved
update_range_vec_zero.adb:10:39: info: precondition proved
update_range_vec_zero.adb:10:63: info: range check proved
update_range_vec_zero.adb:14:07: info: precondition proved
update_range_vec_zero.adb:15:30: info: loop invariant initialization proved
update_range_vec_zero.adb:15:30: info: loop invariant preservation proved
update_range_vec_zero.adb:17:10: info: loop invariant initialization proved
update_range_vec_zero.adb:17:10: info: loop invariant preservation proved
update_range_vec_zero.adb:18:41: info: precondition proved
update_range_vec_zero.adb:18:53: info: range check proved
update_range_vec_zero.adb:19:22: info: precondition proved
update_range_vec_zero.adb:19:34: info: range check proved
update_range_vec_zero.adb:19:39: info: precondition proved
update_range_vec_zero.adb:19:39: info: precondition proved
update_range_vec_zero.adb:19:39: info: precondition proved
update_range_vec_zero.adb:19:39: info: range check proved
```

Similarly, consider a variant of the same update loop over a list:

```
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
   with Ada.Containers; use Ada.Containers; use Loop_Types.Lists.Formal_Model;
2
   procedure Update_Range_List_Zero (L : in out List_T; First, Last : Cursor) with
4
     SPARK_Mode,
     Pre => Has_Element (L, First) and then Has_Element (L, Last)
6
     and then P.Get (Positions (L), First) <= P.Get (Positions (L), Last),</pre>
     Post => Length (L) = Length (L) 'Old
     and Positions (L) = Positions (L) 'Old
9
     and (for all I in 1 .. Length (L) =>
10
                (if I in P.Get (Positions (L), First) .. P.Get (Positions (L), Last) then
11
12
                   Element (Model (L), I) = 0
                 else Element (Model (L), I) = Element (Model (L'Old), I)))
13
14
      Cu : Cursor := First;
15
   begin
16
      loop
17
         pragma Loop_Invariant (Has_Element (L, Cu));
         pragma Loop_Invariant (P.Get (Positions (L), Cu) in P.Get (Positions (L), __
19
    →First) .. P.Get (Positions (L), Last));
         pragma Loop_Invariant (Length (L) = Length (L) 'Loop_Entry);
20
         pragma Loop_Invariant (Positions (L) = Positions (L) 'Loop_Entry);
21
         pragma Loop_Invariant (for all I in 1 .. Length (L) =>
22
                                     (if I in P.Get (Positions (L), First) .. P.Get_
23
   \hookrightarrow (Positions (L), Cu) - 1 then
                                        Element (Model (L), I) = 0
24
                                     else Element (Model (L), I) = Element (Model (L'Loop_
25
   \rightarrowEntry), I)));
         Replace_Element (L, Cu, 0);
26
         exit when Cu = Last;
27
         Next (L, Cu);
      end loop;
   end Update_Range_List_Zero;
```

Compared to the vector example, it requires three additional invariants. As the loop is done via a cursor, the first two loop invariants are necessary to know that the current cursor Cu stays between First and Last in the list. The fourth loop invariant states that the position of cursors in L is not modified during the loop. It is necessary to know that the two cursors First and Last keep designating the same range after the loop. With this loop invariant, GNATprove is able to prove the postcondition of <code>Update\_Range\_List\_Zero</code>, namely that all elements between First and Last have been zeroed out, and that other elements have not been modified:

```
update_range_list_zero.adb:7:13: info: precondition proved
update_range_list_zero.adb:7:45: info: precondition proved
update range list zero.adb:8:11: info: postcondition proved
update_range_list_zero.adb:11:23: info: precondition proved
update_range_list_zero.adb:11:55: info: precondition proved
update_range_list_zero.adb:12:16: info: precondition proved
update_range_list_zero.adb:13:19: info: precondition proved
update_range_list_zero.adb:13:44: info: precondition proved
update_range_list_zero.adb:18:30: info: loop invariant initialization proved
update_range_list_zero.adb:18:30: info: loop invariant preservation proved
update_range_list_zero.adb:19:30: info: loop invariant initialization proved
update_range_list_zero.adb:19:30: info: loop invariant preservation proved
update_range_list_zero.adb:19:31: info: precondition proved
update_range_list_zero.adb:19:60: info: precondition proved
update_range_list_zero.adb:19:92: info: precondition proved
update_range_list_zero.adb:20:30: info: loop invariant initialization proved
update_range_list_zero.adb:20:30: info: loop invariant preservation proved
update_range_list_zero.adb:21:30: info: loop invariant initialization proved
update_range_list_zero.adb:21:30: info: loop invariant preservation proved
update_range_list_zero.adb:22:30: info: loop invariant initialization proved
update_range_list_zero.adb:22:30: info: loop invariant preservation proved
update_range_list_zero.adb:23:42: info: precondition proved
update_range_list_zero.adb:23:74: info: precondition proved
update_range_list_zero.adb:24:36: info: precondition proved
update_range_list_zero.adb:25:38: info: precondition proved
update_range_list_zero.adb:25:63: info: precondition proved
update_range_list_zero.adb:26:07: info: precondition proved
update_range_list_zero.adb:28:07: info: precondition proved
```

# 7.9.3 Manual Proof Examples

The examples in this section contain properties that are difficult to prove automatically and thus require more user interaction to prove completely. The degre of interaction required depends on the difficulty of the proof:

- simple addition of calls to ghost lemmas for arithmetic properties involving multiplication, division and modulo operations, as decribed in *Manual Proof Using SPARK Lemma Library*
- more involved addition of ghost code for universally or existentially quantified properties on data structures and containers, as described in *Manual Proof Using Ghost Code*
- interaction at the level of Verification Condition formulas in the syntax of an interactive prover for arbitrary complex properties, as described in *Manual Proof Using Coq*
- interaction at the level of Verification Condition formulas in the syntax of Why3 for arbitrary complex properties, as described in *Manual Proof Using GPS*

# Manual Proof Using SPARK Lemma Library

If the property to prove is part of the *SPARK Lemma Library*, then manual proof simply consists in calling the appropriate lemma in your code. For example, consider the following assertion to prove, where X1, X2 and Y may be signed or modular positive integers:

```
R1 := X1 / Y;
R2 := X2 / Y;
pragma Assert (R1 <= R2);
```

The property here is the monotonicity of division on positive values. There is a corresponding lemma for both signed and modular integers, for both 32 bits and 64 bits integers:

- for signed 32 bits integers, use SPARK.Integer\_Arithmetic\_Lemmas. Lemma\_Div\_Is\_Monotonic
- for signed 64 bits integers, use SPARK.Long\_Integer\_Arithmetic\_Lemmas. Lemma\_Div\_Is\_Monotonic
- for modular 32 bits integers, use SPARK.Mod32 Arithmetic Lemmas.Lemma Div Is Monotonic
- for modular 64 bits integers, use SPARK.Mod64\_Arithmetic\_Lemmas.Lemma\_Div\_Is\_Monotonic

For example, the lemma for signed integers has the following signature:

```
procedure Lemma_Div_Is_Monotonic
  (Val1 : Int;
   Val2 : Int;
   Denom : Pos)
with
   Global => null,
   Pre => Val1 <= Val2,
   Post => Val1 / Denom <= Val2 / Denom;</pre>
```

Assuming the appropriate library unit is with'ed and used in your code (see *SPARK Lemma Library* for details), using the lemma is simply a call to the ghost procedure Lemma\_Div\_Is\_Monotonic:

```
R1 := X1 / Y;
R2 := X2 / Y;
Lemma_Div_Is_Monotonic (X1, X2, Y);
-- at this program point, the prover knows that R1 <= R2
-- the following assertion is proved automatically:
pragma Assert (R1 <= R2);
```

Note that the lemma may have a precondition, stating in which contexts the lemma holds, which you will need to prove when calling it. For example, a precondition check is generated in the code above to show that X1 <= X2. Similarly, the types of parameters in the lemma may restrict the contexts in which the lemma holds. For example, the type Pos for parameter Denom of Lemma\_Div\_Is\_Monotonic is the type of positive integers. Hence, a range check may be generated in the code above to show that Y is positive.

To apply lemmas to signed or modular integers of different types than the ones used in the instances provided in the library, just convert the expressions passed in arguments, as follows:

```
R1 := X1 / Y;
R2 := X2 / Y;
Lemma_Div_Is_Monotonic (Integer(X1), Integer(X2), Integer(Y));
-- at this program point, the prover knows that R1 <= R2
-- the following assertion is proved automatically:

pragma Assert (R1 <= R2);
```

#### **Manual Proof Using User Lemmas**

If the property to prove is not part of the *SPARK Lemma Library*, then a user can easily add it as a separate lemma in her program. For example, suppose you need to have a proof that a fix list of numbers are prime numbers. This can be expressed easily in a lemma as follows:

```
function Is_Prime (N : Positive) return Boolean is
  (for all J in Positive range 2 .. N - 1 => N mod J /= 0);
```

```
procedure Number_Is_Prime (N : Positive)
with
   Ghost,
   Global => null,
   Pre => N in 15486209 | 15487001 | 15487469,
   Post => Is_Prime (N);
```

Using the lemma is simply a call to the ghost procedure Number\_Is\_Prime:

```
Number_Is_Prime (15486209);
-- at this program point, the prover knows that 15486209 is prime, so
-- the following assertion is proved automatically:
pragma Assert (Is_Prime (15486209));
```

Note that the lemma here has a precondition, which you will need to prove when calling it. For example, the following incorrect call to the lemma will be detected as a precondition check failure:

```
Number_Is_Prime (10); -- check message issued here
```

Then, the lemma procedure can be either implemented as a null procedure, in which case GNATprove will issue a check message about the unproved postcondition, which can be justified (see *Justifying Check Messages*) or proved with Coq (see *Manual Proof Using Coq*):

```
procedure Number_Is_Prime (N : Positive) is null;
```

Or it can be implemented as a normal procedure body with a single assumption:

```
procedure Number_Is_Prime (N : Positive) is
begin
    pragma Assume (Is_Prime (N));
end Number_Is_Prime;
```

Or it can be implemented in some cases as a normal procedure body with ghost code to achieve fully automatic proof, see *Manual Proof Using Ghost Code*.

## **Manual Proof Using Ghost Code**

Guiding automatic solvers by adding intermediate assertions is a commonly used technique. More generally, whole pieces of *Ghost Code* can be added to enhance automated reasoning.

## **Proving Existential Quantification**

Existentially quantified properties are difficult to verify for automatic solvers. Indeed, it requires coming up with a concrete value for which the property holds and solvers are not good at guessing. As an example, consider the following program:

```
pragma Assume (A (A'First) = 0 and then A (A'Last) > 0);

pragma Assert
  (for some I in A'Range =>
        I < A'Last and then A (I) = 0 and then A (I + 1) > 0);
```

Here we assume that the first element of an array A is 0, whereas is last element is positive. In such a case, we are sure that there is an index I in the array such A (I) is 0 but not A (I + 1). Indeed, we know that A starts with a

non-empty sequence of zeros. The last element of this sequence has the expected property. However, automatic solvers are unable to prove such a property automatically because they cannot guess which index they should consider. To help them, we can define a ghost function returning a value for which the property holds, and call it from an assertion:

```
function Find_Pos (A : Nat_Array) return Positive with Ghost,
  Pre => A (A'First) = 0 and then A (A'Last) > 0,
  Post => Find_Pos'Result in A'First .. A'Last - 1 and then
        A (Find_Pos'Result) = 0 and then A (Find_Pos'Result + 1) > 0;

pragma Assume (A (A'First) = 0 and then A (A'Last) > 0);
pragma Assert (Find_Pos (A) in A'Range);
pragma Assert
  (for some I in A'Range =>
        I < A'Last and then A (I) = 0 and then A (I + 1) > 0);
```

Automatic solvers are now able to discharge the proof.

## **Performing Induction**

Another difficult point for automated solvers is proof by induction. Though some automatic solvers do have heuristics allowing them to perform the most simple inductive proofs, they generally are lost when the induction is less straightforward. For example, in the example below, we state that the array A is sorted in two different ways, first by saying that each element is bigger than the one just before, and then by saying that each element is bigger than all the ones before:

```
pragma Assume
  (for all I in A'Range =>
        (if I > A'First then A (I) > A (I - 1)));
pragma Assert
  (for all I in A'Range =>
        (for all J in A'Range => (if I > J then A (I) > A (J)));
```

The second assertion is provable from the first one by induction over the number of elements separating  $\mathbb{I}$  and  $\mathbb{J}$ , but automatic solvers are unable to verify this code. To help them, we can use a ghost loop. In the loop invariant, we say that the property holds for all indexes  $\mathbb{I}$  and  $\mathbb{J}$  separated by less than  $\mathbb{K}$  elements:

GNATprove will verify that the invariant holds in two steps, first it will show that the property holds at the first iteration, and then that, if it holds at a given iteration, then it also holds at the next (see *Loop Invariants*). Both proofs are straightforward using the assumption.

Note that we have introduced a ghost subprogram above to contain the loop. This will allow the compiler to recognize that this loop is ghost, so that it can be entirely removed when assertions are disabled.

If Prove\_Sorted is declared locally to the subprogram that we want to verify, it is not necessary to supply a contract for it, as local subprograms with no contracts are inlined (see *Contextual Analysis of Subprograms Without Contracts*). We can still choose to provide such a contract to turn Prove\_Sorted into a lemma (see *Manual Proof Using User Lemmas*).

## A Concrete Example: a Sort Algorithm

We show how to prove the correctness of a sorting procedure on arrays using ghost code. In particular, we want to show that the sorted array is a permuation of the input array. A common way to define permutations is to use the number of occurrences of elements in the array, defined inductively over the size of its array parameter (but it is not the only one, see *Ghost Variables*):

```
package Sort_Types with SPARK_Mode is
subtype Index is Integer range 1 .. 100;
type Nat_Array is array (Index range <>) of Natural;
end Sort_Types;
```

```
with Sort_Types; use Sort_Types;
2
   package Perm with SPARK_Mode, Ghost is
3
      subtype Nb_Occ is Integer range 0 .. 100;
4
      function Remove_Last (A : Nat_Array) return Nat_Array is
        (A (A'First .. A'Last - 1))
      with Pre => A'Length > 0;
      function Occ_Def (A : Nat_Array; E : Natural) return Nb_Occ is
10
        (if A'Length = 0 then 0
11
         elsif A (A'Last) = E then Occ_Def (Remove_Last (A), E) + 1
12
         else Occ_Def (Remove_Last (A), E))
13
      with
14
        Post => Occ_Def'Result <= A'Length;
15
      pragma Annotate (GNATprove, Terminating, Occ_Def);
16
17
      function Occ (A : Nat_Array; E : Natural) return Nb_Occ is (Occ_Def (A, E))
18
      with
        Post => Occ'Result <= A'Length;
21
      function Is_Perm (A, B : Nat_Array) return Boolean is
22
        (for all E in Natural => Occ (A, E) = Occ (B, E));
23
24
   end Perm:
```

Note that Occ was introduced as a wrapper around the recursive definition of Occ\_Def. This is to work around a current limitation of the tool that only introduces axioms for postconditions of non-recursive functions (to avoid possibly introducing unsound axioms that would not be detected by the tool).

The only property of the function Occ required to prove that swapping two elements of an array is in fact a permutation, is the way Occ is modified when updating a value of the array.

There is no native construction for axioms in SPARK 2014. As a workaround, a ghost subprogram, named "lemma subprogram", can be introduced with the desired property as a postcondition. An instance of the axiom will then be available whenever the subprogram is called. Notice that an explicit call to the lemma subprogram with the proper arguments is required whenever an instance of the axiom is needed, like in manual proofs in an interactive theorem prover. Here is how a lemma subprogram can be defined for the desired property of Occ:

```
(if I /= J then R (J) = A (J)))) with
Pre => I in A'Range;

procedure Occ_Set (A : Nat_Array; I : Index; V, E : Natural; R : Nat_Array)
with
Pre => I in A'Range and then Is_Set (A, I, V, R),
Post =>
  (if V = A (I) then Occ (R, E) = Occ (A, E)
  elsif V = E then Occ (R, E) = Occ (A, E) + 1
  elsif A (I) = E then Occ (R, E) = Occ (A, E) - 1
  else Occ (R, E) = Occ (A, E));

end Perm.Lemma_Subprograms;
```

This "axiom" can then be used to prove an implementation of the selection sort algorithm. Lemma subprograms need to be explicitly called for every natural. To achieve that, a loop is introduced. The inductive proof necessary to demonstrate the universally quantified formula is then achieved thanks to the loop invariant, playing the role of an induction hypothesis:

```
with Perm.Lemma_Subprograms; use Perm.Lemma_Subprograms;
package body Sort
  with SPARK_Mode
is
  procedure Swap (Values : in out Nat_Array;
                   Χ
                        : in
                                   Positive;
                   Υ
                          : in
                                   Positive)
    with
      Pre => (X in Values'Range and then
                  Y in Values'Range and then
                    X /= Y)
      Post => Is_Perm (Values'Old, Values)
    and Values (X) = Values'Old (Y)
    and Values (Y) = Values'Old (X)
    and (for all Z in Values'Range =>
            (if Z \neq X and Z \neq Y then Values (Z) = Values'Old (Z)))
      Temp : Integer;
      -- Ghost variables
      Init : constant Nat_Array (Values'Range) := Values with Ghost;
      Interm : Nat_Array (Values'Range) with Ghost;
      -- Ghost procedure
     procedure Prove_Perm with Ghost,
       Pre => X in Values'Range and then Y in Values'Range and then
       Is_Set (Init, X, Init (Y), Interm)
        and then Is_Set (Interm, Y, Init (X), Values),
       Post => Is_Perm (Init, Values)
      is
      begin
         for E in Natural loop
           Occ_Set (Init, X, Init (Y), E, Interm);
           Occ_Set (Interm, Y, Init (X), E, Values);
           pragma Loop_Invariant
```

```
(for all F in Natural'First .. E =>
              Occ (Values, F) = Occ (Init, F));
      end loop;
   end Prove_Perm;
begin
             := Values (X);
   Values (X) := Values (Y);
   -- Ghost code
   pragma Assert (Is_Set (Init, X, Init (Y), Values));
   Interm := Values;
   Values (Y) := Temp;
   -- Ghost code
   pragma Assert (Is_Set (Interm, Y, Init (X), Values));
   Prove_Perm;
end Swap;
-- Finds the index of the smallest element in the array
function Index_Of_Minimum (Values : in Nat_Array)
                           return Positive
  with
    Pre => Values'Length > 0,
    Post => Index_Of_Minimum'Result in Values'Range and then
    (for all I in Values'Range =>
       Values (Index_Of_Minimum'Result) <= Values (I))</pre>
is
  Min : Positive;
begin
   Min := Values'First;
   for Index in Values'Range loop
      if Values (Index) < Values (Min) then</pre>
         Min := Index;
      end if;
      pragma Loop_Invariant
        (Min in Values'Range and then
           (for all I in Values'First .. Index =>
                Values (Min) <= Values (I)));</pre>
   end loop;
   return Min;
end Index_Of_Minimum;
procedure Selection_Sort (Values : in out Nat_Array) is
   Smallest: Positive; -- Index of the smallest value in the unsorted part
   if Values'Length = 0 then
     return;
   end if;
   for Current in Values'First .. Values'Last - 1 loop
      Smallest := Index_Of_Minimum (Values (Current .. Values'Last));
      if Smallest /= Current then
         Swap (Values => Values,
               X => Current,
               Υ
                      => Smallest);
```

The procedure Selection\_Sort can be verified using GNATprove, with the default prover CVC4, in less than 1s per verification condition.

```
sort.adb:16:16: info: postcondition proved
sort.adb:17:18: info: index check proved
sort.adb:17:35: info: index check proved
sort.adb:18:18: info: index check proved
sort.adb:18:35: info: index check proved
sort.adb:20:48: info: index check proved
sort.adb:20:65: info: index check proved
sort.adb:22:07: info: initialization of "Temp" proved
sort.adb:25:07: info: range check proved
sort.adb:25:53: info: length check proved
sort.adb:26:07: info: initialization of "Interm" proved
sort.adb:26:07: info: range check proved
sort.adb:31:09: info: precondition proved
sort.adb:31:23: info: range check proved
sort.adb:31:32: info: index check proved
sort.adb:32:18: info: precondition proved
sort.adb:32:34: info: range check proved
sort.adb:32:43: info: index check proved
sort.adb:33:17: info: postcondition proved
sort.adb:37:13: info: precondition proved
sort.adb:37:28: info: range check proved
sort.adb:37:37: info: index check proved
sort.adb:38:13: info: precondition proved
sort.adb:38:30: info: range check proved
sort.adb:38:39: info: index check proved
sort.adb:40:16: info: loop invariant initialization proved
sort.adb:40:16: info: loop invariant preservation proved
```

```
sort.adb:46:29: info: index check proved
sort.adb:47:15: info: index check proved
sort.adb:47:29: info: index check proved
sort.adb:50:22: info: assertion proved
sort.adb:50:22: info: precondition proved
sort.adb:50:36: info: range check proved
sort.adb:50:45: info: index check proved
sort.adb:51:14: info: length check proved
sort.adb:51:17: info: length check proved
sort.adb:53:15: info: index check proved
sort.adb:53:21: info: range check proved
sort.adb:56:22: info: assertion proved
sort.adb:56:22: info: precondition proved
sort.adb:56:38: info: range check proved
sort.adb:56:47: info: index check proved
sort.adb:57:07: info: precondition proved
sort.adb:65:16: info: postcondition proved
sort.adb:67:35: info: index check proved
sort.adb:67:55: info: index check proved
sort.adb:69:07: info: initialization of "Min" proved
sort.adb:71:20: info: range check proved
sort.adb:73:38: info: index check proved
sort.adb:74:20: info: range check proved
sort.adb:77:13: info: loop invariant initialization proved
sort.adb:77:13: info: loop invariant preservation proved
sort.adb:79:28: info: index check proved
sort.adb:79:44: info: index check proved
sort.adb:85:07: info: initialization of "Smallest" proved
sort.adb:91:50: info: overflow check proved
sort.adb:92:22: info: precondition proved
sort.adb:92:40: info: range check proved
sort.adb:95:13: info: precondition proved
sort.adb:96:29: info: range check proved
sort.adb:101:13: info: loop invariant initialization proved
sort.adb:101:13: info: loop invariant preservation proved
sort.adb:102:31: info: overflow check proved
sort.adb:103:28: info: index check proved
sort.adb:103:42: info: index check proved
sort.adb:104:33: info: loop invariant initialization proved
sort.adb:104:33: info: loop invariant preservation proved
sort.ads:9:16: info: postcondition proved
sort.ads:11:51: info: overflow check proved
sort.ads:12:22: info: index check proved
sort.ads:12:38: info: index check proved
sort.ads:12:38: info: overflow check proved
```

To complete the verification of our selection sort, the only remaining issue is the correctness of the axiom for Occ. It can be discharged using the definition of Occ. Since this definition is recursive, the proof requires induction, which is not normally in the reach of an automated prover. For GNAT prove to verify it, it must be implemented using recursive calls on itself to assert the induction hypothesis. Note that the proof of the lemma is then conditioned to the termination of the lemma functions, which currently cannot be verified by GNAT prove.

```
package body Perm.Lemma_Subprograms with SPARK_Mode is

procedure Occ_Eq (A, B : Nat_Array; E : Natural) with
Pre => A = B,
Post => Occ (A, E) = Occ (B, E);
```

```
procedure Occ_Eq (A, B : Nat_Array; E : Natural) is
      begin
      if A'Length = 0 then
        return;
      end if;
      if A (A'Last) = E then
        pragma Assert (B (B'Last) = E);
         pragma Assert (B (B'Last) /= E);
      end if;
      Occ_Eq (Remove_Last (A), Remove_Last (B), E);
   end Occ_Eq;
   procedure Occ_Set (A : Nat_Array; I : Index; V, E : Natural; R : Nat_Array)
      B : Nat_Array:= Remove_Last (A);
   begin
      if A'Length = 0 then
        return;
      end if;
      if I = A'Last then
        Occ_Eq (B, Remove_Last (R), E);
      else
         B (I) := V;
         Occ_Eq (Remove_Last (R), B, E);
         Occ_Set (Remove_Last (A), I, V, E, B);
      end if;
   end Occ_Set;
end Perm.Lemma_Subprograms;
```

GNAT prove proves automatically all checks on the final program, with a small timeout of 1s for the default automatic prover CVC4.

```
perm-lemma_subprograms.adb:5:14: info: postcondition proved
perm-lemma_subprograms.adb:13:14: info: index check proved
perm-lemma_subprograms.adb:14:25: info: assertion proved
perm-lemma_subprograms.adb:14:29: info: index check proved
perm-lemma_subprograms.adb:16:25: info: assertion proved
perm-lemma_subprograms.adb:16:29: info: index check proved
perm-lemma_subprograms.adb:19:07: info: precondition proved
perm-lemma_subprograms.adb:19:15: info: precondition proved
perm-lemma_subprograms.adb:19:32: info: precondition proved
perm-lemma_subprograms.adb:25:23: info: precondition proved
perm-lemma_subprograms.adb:32:10: info: precondition proved
perm-lemma_subprograms.adb:32:21: info: precondition proved
perm-lemma_subprograms.adb:34:13: info: index check proved
perm-lemma_subprograms.adb:35:10: info: precondition proved
perm-lemma_subprograms.adb:35:18: info: precondition proved
perm-lemma_subprograms.adb:36:10: info: precondition proved
perm-lemma_subprograms.adb:36:19: info: precondition proved
perm-lemma_subprograms.ads:6:20: info: index check proved
perm-lemma_subprograms.ads:8:39: info: index check proved
perm-lemma_subprograms.ads:8:47: info: index check proved
```

```
perm-lemma_subprograms.ads:13:39: info: precondition proved perm-lemma_subprograms.ads:15:08: info: postcondition proved perm-lemma_subprograms.ads:15:19: info: index check proved perm-lemma_subprograms.ads:17:18: info: index check proved
```

## **Manual Proof Using Coq**

This section presents a simple example of how to prove interactively a check with an interactive prover like Coq when GNATprove fails to prove it automatically (for installation of Coq, see also: *Coq*). Here is a simple SPARK procedure:

```
procedure Nonlinear (X, Y, Z : Positive; R1, R2 : out Natural) with

SPARK_Mode,
Pre => Y > Z,
Post => R1 <= R2

is
begin
R1 := X / Y;
R2 := X / Z;
end Nonlinear;</pre>
```

When only the Alt-Ergo prover is used, GNATprove does not prove automatically the postcondition of the procedure, even when increasing the value of the timeout:

This is expected, as the automatic prover Alt-Ergo has only a simple support for non-linear integer arithmetic. More generally, it is a known difficulty for all automatic provers, although, in the case above, using prover CVC4 is enough to prove automatically the postcondition of procedure Nonlinear. We will use this case to demonstrate the use of a manual prover, as an example of what can be done when automatic provers fail to prove a check. We will use Coq here.

The Coq input file associated to this postcondition can be produced by either selecting  $SPARK \rightarrow Prove\ Check$  and specifying Coq as alternate prover in GPS or by executing on the command-line:

The generated file contains many definitions and axioms that can be used in the proof, in addition to the ones in Coq standard library. The property we want to prove is at the end of the file:

```
/\ (((((o = (ZArith.BinInt.Z.quot x y))
     /\ (in_range (ZArith.BinInt.Z.quot x y)))
     /\ (((mk_int_ref result) = (mk_int_ref r1))
     / (r11 = 0))
     /\ (((o1 = (ZArith.BinInt.Z.quot x z))
     /\ (in_range (ZArith.BinInt.Z.quot x z)))
     /\ ((result1 = r2)
     / (r21 = o1)))
     /\ (((r21 = r22)
     / \ (r11 = r12))
     /\ ((r23 = r21)
     /\ (r13 = r11)))))))))) ->
     (r12 \le r22) %Z.
  intros r1 r2 o o1 result r11 result1 r21 r12 r22 r13 r23
  (h1, (h2, (h3, (h4, (h5, (h6, ((((h7, h8), (h9, h10)), ((h11, h12),
  (h13, h14))), ((h15, h16), (h17, h18))))))).
Qed.
```

From the forall to the first . we can see the expression of what must be proved, also called the goal. The proof starts right after the dot and ends with the <code>Qed</code> keyword. Proofs in Coq are done with the help of different tactics which will change the state of the current goal. The first tactic (automatically added) here is <code>intros</code>, which allows to "extract" variables and hypotheses from the current goal and add them to the current environment. Each parameter to the <code>intros</code> tactic is the name that the extracted element will have in the new environment. The <code>intros</code> tactic here puts all universally quantified variables and all hypotheses in the environment. The goal is reduced to a simple inequality, with all potentially useful information in the environment.

Here is the state of the proof as displayed in a suitable IDE for Coq:

```
1 subgoal
  r1, r2, o, o1, result, r11, result1, r21, r12, r22, r13, r23 : int
  h1 : in_range1 x
  h2: in_range1 y
  h3 : in_range1 z
  h4 : (0 \le 2147483647) %Z \rightarrow in\_range r1
  h5 : (0 \le 2147483647) %Z \rightarrow in_range r2
  h6 : (z < y) %Z
  h7 : o = (x \div y) %Z
  h8 : in_range(x \div y)
  h9 : mk_int__ref result = mk_int__ref r1
  h10 : r11 = o
  h11 : o1 = (x \div z) %Z
  h12 : in_range (x \div z)
  h13 : result1 = r2
  h14 : r21 = o1
  h15 : r21 = r22
  h16 : r11 = r12
  h17 : r23 = r21
  h18 : r13 = r11
                                           _{-}(1/1)
  (r12 \le r22) %Z
```

Some expressions are enclosed in () Z, which means that they are dealing with relative integers. This is necessarily in order to use the operators (e.g. condots) on relative integers instead of using the associated Coq function or to declare a relative integer constant (e.g. condots).

At this state, the hypotheses alone are not enough to prove the goal without proving properties about  $\div$  and < operators. It is necessary to use theorems from the Coq standard library. Coq provides a command SearchAbout to find theorems and definition concerning its argument. For instance, to find the theorems referring to the operator  $\div$ , we use SearchAbout Z.quot., where Z.quot is the underlying function for the  $\div$  operator. Among the theorems displayed, the conclusion (the rightmost term separated by -> operator) of one of them seems to match our current goal:

```
Z.quot_le_compat_l: forall p q r : int, (0 \le p)%Z -> (0 < q \le r)%Z -> (p \div r \le p \div q)%Z
```

The tactic apply allows the use of a theorem or an hypothesis on the current goal. Here we use: apply Z.  $quot_le_compat_l$ . This tactic will try to match the different variables of the theorem with the terms present in the goal. If it succeeds, one subgoal per hypothesis in the theorem will be generated to verify that the terms matched with the theorem variables satisfy the hypotheses on those variables required by the theorem. In this case, p is matched with x, q with z and r with y and the new state is:

As expected, there are two subgoals, one per hypothesis of the theorem. Once the first subgoal is proved, the rest of the script will automatically apply to the second one. Now, if we look back at the SPARK code, X is of type Positive so X is greater than 0 and in\_rangeN (where N is a number) are predicates generated by SPARK to state the range of a value from a ranged subtype interpreted as a relative integer in Coq. Here, the predicate in\_range1

provides the property needed to prove the first subgoal which is that "All elements of subtype positive have their integer interpretation in the range 1 ..  $(2^{31} - 1)$ ". However, the goal does not match exactly the predicate, because one is a comparison with 0, while the other is a comparison with 1. Transitivity on "lesser or equal" relation is needed to prove this goal, of course this is provided in Coq's standard library:

```
Lemma Zle\_trans : forall n m p:Z, (n <= m) Z -> (m <= p) Z -> (n <= p) Z.
```

Since the lemma's conclusion contains only two variables while it uses three, using tactic apply  $Zle\_trans.$  will generate an error stating that Coq was not able to find a term for the variable m. In this case, m needs to be instantiated explicitly, here with the value 1: apply  $Zle\_trans$  with (m:= 1%Z). There are two new subgoals, one to prove that  $0 \le 1$  and the other that  $1 \le x$ :

```
3 subgoals
 r1, r2, result : int
 h1 : in_range1 x
 h2 : in_range1 y
 h3 : in_range1 z
 h4 : (0 \le 2147483647) %Z -> in_range r1
 h5 : (0 \le 2147483647) %Z \rightarrow in_range r2
 h6 : (z < y) %Z
 h8 : in\_range (x ÷ y)
 h9 : mk_int__ref result = mk_int__ref r1
 h12 : in_range (x \div z)
                                       ____(1/3)
  (0 <= 1)%Z
                                  ____(2/3)
  (1 <= x) %Z
  (0 < z \le y) %Z
```

To prove that  $0 \le 1$ , the theorem Lemma  $2le_0_1 : (0 \le 1) \%Z$ . is used. apply  $2le_0_1$  will not generate any new subgoals since it does not contain implications. Coq passes to the next subgoal:

This goal is now adapted to the in\_range1 definition with h1 which does not introduce subgoals, so the subgoal 1 is fully proved, and all that remains is subgoal 2:

```
1 subgoal
    r1, r2, result : int
    h1 : in_range1 x
```

```
h2 : in_range1 y
h3 : in_range1 z
h4 : (0 <= 2147483647)%Z -> in_range r1
h5 : (0 <= 2147483647)%Z -> in_range r2
h6 : (z < y)%Z
h8 : in_range (x ÷ y)
h9 : mk_int__ref result = mk_int__ref r1
h12 : in_range (x ÷ z)

(1/1)
```

Transitivity is needed again, as well as in\_range1. In the previous subgoal, every step was detailed in order to show how the tactic apply worked. Now, let's see that proof doesn't have to be this detailed. The first thing to do is to add the fact that 1 <= z to the current environment: unfold in\_range1 in h3. will add the range of z as an hypthesis in the environment:

At this point, the goal can be solved simply using the omega. tactic. omega is a tactic made to facilitate the verification of properties about relative integers equalities and inequalities. It uses a predefined set of theorems and the hypotheses present in the current environment to try to solve the current goal. omega either solves the goal or, if it fails, it does not generate any subgoals. The benefit of the latter way is that there are less steps than with the previous subgoal for a more complicated goal (there are two inequalities in the second subgoal) and we do not have to find the different theorems we need to solve the goal without omega.

Finally, here is the final version of the proof script for the postcondition:

```
Theorem WP_parameter_def :
 forall (r1:Z) (r2:Z) (o:Z) (o1:Z) (result:Z)
         (r11:Z) (result1:Z) (r21:Z) (r12:Z) (r22:Z)
         (r13:Z) (r23:Z),
    ((in_range1 x)
    /\ ((in_range1 y)
    / \ ((in\_range1 z)
    /\ (((0%Z \le 2147483647%Z)%Z -> (in_range r1))
    /\ (((0%Z \le 2147483647%Z)%Z -> (in_range r2))
    / \setminus ((z < y) %Z
    /\ (((((o = (ZArith.BinInt.Z.quot x y))
    /\ (in_range (ZArith.BinInt.Z.quot x y)))
     /\ (((mk_int_ref result) = (mk_int_ref r1))
     / (r11 = o))
     /\ (((o1 = (ZArith.BinInt.Z.quot x z))
     /\ (in_range (ZArith.BinInt.Z.quot x z)))
     /\ ((result1 = r2)
     /\ (r21 = o1)))
```

```
/\ (((r21 = r22)
     / \ (r11 = r12))
     / \ ((r23 = r21)
     /\ (r13 = r11))))))))) ->
     (r12 \le r22) %Z.
  intros r1 r2 o o1 result r11 result1 r21 r12 r22 r13 r23
  (h1, (h2, (h3, (h4, (h5, (h6, ((((h7, h8), (h9, h10)), ((h11, h12),
  (h13, h14))), ((h15, h16), (h17, h18))))))).
subst o o1 result1 r11 r12 r21 r22 r23 r13.
apply Z.quot_le_compat_1.
  apply Zle\_trans with (m:=1\%Z).
    (* 0 <= 1 *)
    apply Zle_0_1.
    (* 1 \le x *)
    unfold in_range1 in h1.
    apply h1.
  (* 0 < z <= y *)
  unfold in_range1 in h3.
  omega.
Qed.
```

To check and save the proof:

```
gnatprove -P <pri>prj_file>.gpr --limit-line=nonlinear.
adb:4:11:VC_POSTCONDITION --prover=Coq --report=all
```

Now running GNAT prove on the project should confirm that all checks are proved:

```
nonlinear.adb:4:11: info: postcondition proved
nonlinear.adb:7:12: info: range check proved
nonlinear.adb:7:12: info: division check proved
nonlinear.adb:8:12: info: range check proved
nonlinear.adb:8:12: info: division check proved
```

# **Manual Proof Using GPS**

This section presents a simple example of how to prove interactively a check with the manual proof feature. We reuse here the example presented in section *Manual Proof Using Coq*. We launch the Manual Proof on the failed check at:

```
nonlinear.adb:4:11:VC_POSTCONDITION
```

Right click on the corresponding location in the Locations terminal of GPS and select the menu  $SPARK \rightarrow Start$   $Manual\ Proof$ . The manual proof interface immediately starts. Both the Proof Tree and the Verification Condition (VC) appear in separate windows. In particular, the VC ends with the following:

```
axiom H : dynamic_property first last X
axiom H1 : dynamic_property first last Y
axiom H2 : dynamic_property first last Z
axiom H3 : first1 <= last1 -> dynamic_property1 first1 last1 R14
axiom H4 : first1 <= last1 -> dynamic_property1 first1 last1 R23
```

```
axiom H5 : Y > Z
axiom H6 : o1 = div X Y /\ in_rangel (div X Y)
axiom H7 : result = R1
axiom H8 : R13 = o1
axiom H9 : o = div X Z /\ in_rangel (div X Z)
axiom H10 : result1 = R23
axiom H11 : R22 = o
axiom H12 : R22 = R21
axiom H13 : R13 = R12
axiom H14 : R2 = R22
axiom H15 : R11 = R13
goal WP_parameter def : R12 <= R21</pre>
```

The Verification Condition is very similar to the one generated for Coq (as expected: the check is the same). As soon as the menus appear, the user can start using transformations to simplify the goal thus helping automatic provers. We will start the description of a complete proof for this lemma using only altergo. At first, we want to remove the equalities between constants that make the VC very difficult to read. These equalities were generated by the weakest precondition algorithm. They can be safely removed by subst and subst all. In Manual Proof console, type:

```
subst_all
```

The transformation node was added to the Proof Tree and the current node is now changed making your transformation appear and the new Verification Condition to prove has been simplified:

We should also have replaced the value of o1 and o in the goal. These were not replaced because H6 and H7 are conjunctions. We can destruct both hypotheses H6 and H7 in order to make the equalities appear at toplevel:

```
destruct H6
```

#### Then:

```
subst o1
```

After simplifications, the goal is the following:

This is more readable but altergo still does not manage to prove it:

```
altergo
```

answers Unknown as seen in the Proof Tree.

We need to investigate further what we know about div, and what would be useful to prove the goal:

```
search div
```

returns in the Manual Proof console:

```
function div (x:int) (y:int) : int = div1 x y
axiom H1 : in_range1 (div X Y)
axiom H : in_range1 (div X Z)
```

So, div is actually a shortcut for a function named div1. Let's search for this one:

```
search div1
```

Now, we get a lot of axioms about div and mod as expected. In particular, the axiom Div\_mod looks interesting:

```
axiom Div_mod: forall x:int, y:int. not y = 0 \rightarrow x = ((y * div1 x y) + mod1 x y)
```

Perhaps, it is a good idea to instantiate this axiom with X and Y (respectively X and Z) and see what is provable from there:

```
instantiate Div_mod X,Y
```

A new hypothesis appears in the context:

```
axiom Div_mod : not Y = 0 \rightarrow X = ((Y * div1 X Y) + mod1 X Y)
```

After some struggling with those hypotheses, it looks like they won't actually help proving the goal. Let's remove these hypotheses:

```
remove Div_mod
```

Alternatively, we can go back to the node above the current one in the Proof Tree by clicking on it. We can also remove the transformation node corresponding to the use of instantiate by selecting it and writing in Manual Proof console:

```
Remove
```

The actual proof is going to use an additional lemma that we are going to introduce with assert. The Coq proof uses this exact same lemma inside the proof of <code>Z.quot\_le\_compat\_l</code>. We could have expected <code>altergo</code> to have this lemma inside its theories but, currently, it does not:

```
assert (forall q a b:int. 0<b -> 0<a -> b*q <= a -> q <= div1 a b)
```

So, two new nodes appear below the current one (the first to prove the formula we just wrote and the second adding it as an hypothesis). We are going to prove this assert by induction on the unbounded integer q (the base case is 0):

```
induction q from 0
```

Both new goals can be discharged by altergo: this small lemma is proven. Now, we can use it in our proof. We begin by unfolding div to make div1 appear:

```
unfold div
```

Then we can apply our new lemma:

```
apply h
```

We are left with the following three subgoals to prove:

```
goal G : (Z * div1 X Y) <= X
goal G : 0 < X
goal G : 0 < Z</pre>
```

altergo proves the positivity of X and Z easily but it does not find a proof for the first subgoal. We are going to prove this one by transitivity of less or equal using  $Y \star \text{div1} X Y$ . Currently, we don't have a transformation to apply the transitivity directly so we assert it:

```
assert ((Y * div1 X Y <= X && Z) * ((div1 X Y) <= Y * div1 X Y))
```

To make two goals of this conjunction, we are using:

```
split_goal_wp
```

The left part is provable by altergo. On the second part, we are going to apply an axiom CompatOrderMult we found by querying what is known about the multiplication:

search (\*)

We apply it to the current goal:

apply CompatOrderMult

The remaining goals can all be proven by altergo. This closes the proof. A popup should appear asking if the user wants to save and exit. Answer no because we want to make the proof cleaner (you can still save it by writing Save in Manual Proof console). Select a node and type:

clean

All attempted proof that did not succeed are erased and only the successful proofs remain. The proof can now be saved and manual proofs menus closed by clicking on  $SPARK \rightarrow Exit\ Manual\ Proof$  from the menu. The proof is complete and GNAT prove can be called again on the whole project to check that the former failing check is now understood as proved by GNAT prove.

#### List of Useful Transformations and Commands

The transformations all contain a specific documentation through the list-transforms command and help transform\_name command. The most useful transformations/commands are the following:

- apply: apply an hypothesis to the current goal. For example:  $H: x > 0 \rightarrow \text{not } x = 0$  can be applied on the goal G: not x = 0. After the application you will be left to prove a new goal x > 0.
- assert: adds a new lemma you can use for proving the current Verification Condition. For example: assert x = 0 will generate two new subgoals. In the first one you have to prove that x is indeed equal to 0. In the second one, you can use this hypothesis.
- case: takes a formula and perform an analysis by case on its boolean value. You will have to prove your
   Verification Condition once with this formula asserted to true and once asserted to false.
- clean: removes unsuccessful proof attempts below proved goals.
- clear\_but: removes all hypotheses except the one provided by the user as argument. Removing unused context helps the provers. For example, clear\_but H,H2,h will remove everything but hypotheses H H2 and h.
- compute\_in\_goal: performs possible computations in goal.
- destruct: destruct the head constructor of a formula ( /\ , \/ or ->). With H: A /\ B, applying destruct H make two new hypotheses (H: A and H1: B). With H: A \/ B, applying destruct H duplicates the goal which has to be proved with H: A and H: B independently. With H: A -> B, destruct H creates a new subgoal for A and simplify to H: B in the current one.
- eliminate\_epsilon: sometimes the goal appears as epsilon [...]. This transforms epsilons into adapted logic.
- exists: allows the user to provide a term that instantiates a goal starting with an existential.
- help: with no arguments, return basic commands that can be used. If a transformation is given as argument, it displays a small description of the transformation.
- induction: performs an induction on the unbounded integer specified.
- instantiate: instantiates a forall quantification at the head of an hypothesis with a term given by the user (a list of terms can be provided).
- intros: introduces a list of constants/hypotheses. This transformation should not be necessary but it can be used to rename constants/hypotheses.

- left: In a goal, transforms A \/ B into A.
- list-provers: gives a list of the provers available on your machine. You should have at least altergo.
- list-transforms: list transformations.
- pose: defines a new constant equal to a given term.
- print: prints the definition of a name.
- remove: removes a list of hypotheses.
- replace: replace a term by another and create a subgoal asking the user to show that they are equivalent.
- rewrite: rewrites an equality in a goal or hypothesis. For example, with H: x = 0 and goal y = x, rewrite H transforms the goal into y = 0.
- right: In a goal, transforms A \/ B into B.
- search: search all occurrences of a name in the context.
- split\_\*: a set of transformations that split the goals/hypotheses. For example, split\_goal\_wp transforms the goal A /\ B into two new subgoals A and B.
- subst: try to find an equality that could be used for a given constant and replace each occurrence of this constant by the other side of the equality. It then removes said constant.
- subst\_all: do all possible substitutions.
- unfold: unfolds the definition of a function in an hypothesis or a goal.

#### Recommendations

- As for proofs with an external interactive prover, the user should set the attribute Proof\_Dir so that proofs can be saved under version control.
- The Proof\_Dir is recommended to be under a version control system (git or svn for example). The proofs can be tedious to rewrite so it is better not to lose them.
- There is currently no way to adapt stuff that are proven in the current version to potential future ones. The update will have to be done manually but we hope to automate the process in the future,
- This feature is experimental and we currently recommend to keep the proof as short as possible.

#### **Tips**

- If the goal contains epsilons, they can be removed by using eliminate\_epsilon.
- Manual provers can be launched during the edition of the proof like other provers. The user can select a goal node and type coq for example.
- The command line remembers what is typed. Arrow keys can be used to get the lasts queried commands.

# 7.10 Examples in the Toolset Distribution

Further examples of SPARK are distributed with the SPARK toolset. These are contained in the share/examples/spark directory below the directory where the toolset is installed, and can be accessed from the IDE (either GPS or GNATBench) via the  $Help \rightarrow SPARK \rightarrow Examples$  menu item.

These examples range from single subprograms to demo programs with dozens of units. In this section, we describe briefly the code in each example, the properties specified, and the results of GNATprove's analysis.

# 7.10.1 Individual Subprograms

These examples contain usually a single subprogram, and are typically very small (a few dozens slocs).

#### binary\_search and binary\_search\_unconstrained

These programs search for a given value in an ordered array. The postcondition of the main function Binary\_Search expresses that the search is successful if-and-only-if the array contains the value searched, and if so the index returned is one at which the array contains this value. GNATprove proves all checks on these programs. The version with an unconstrained array is the same as the one presented in the section on *How to Write Loop Invariants*, and used in a series of two articles published by Johannes Kanig in Electronic Design to compare dynamic and static verification techniques (see http://blog.adacore.com/testing-static-formal).

#### euclidian division

This program implements the Euclidian division of two integers <code>Dividend</code> and <code>Divisor</code>, returning their quotient and remainder in <code>Quotient</code> and <code>Remainder</code> respectively. The postcondition of procedure <code>Linear\_Div</code> expresses the expected mathematical relation between inputs and outputs. GNAT prove proves all checks on this program.

#### gcd

This program computes the greatest common divisor between two positive numbers. The postcondition of function GCD checks that the number returned is indeed the greatest common divisor of its arguments. Four versions of the function are provided:

- a simple version that searches linearly for the GCD.
- a modification of the simple version with a more mathematical expression of divisibility in the contract of GCD.
- a modification of the simple version that optimizes the search to skip half the candidates for GCD.
- Euclid's algorithm for computing the GCD.

Each successive version makes use of more complex *Ghost Code* to prove that the implementation of GCD satisfies its contract. GNATprove proves all checks on this program, except for some elementary lemmas on modulo operator. This is detailed in the following post on AdaCore blog: https://blog.adacore.com/gnatprove-tips-and-tricks-proving-the-ghost-common-denominator-gcd

# intro

This program computes the price of a basket of items. The postcondition of the main function Price\_Of\_Basket checks that the resulting price is at least the price of the most expensive item. GNATprove proves all checks on this program.

#### linear search

This program searches for a given value in an unordered array. The postcondition of the main function Linear\_Search expresses that if the search is successful then the index returned is one at which the array contains the value searched. GNATprove proves all checks on this program. This program is the same as the one presented in the *SPARK Tutorial*.

# longest\_common\_prefix

This program computes the length of the longest common prefix between two substrings of a common text. The postcondition of the main function LCP expresses this property. GNATprove proves all checks on this program. This program was proposed as a formal verification challenge during VerifyThis Verification Competition in 2012 (see http://fm2012.verifythis.org/).

## pair\_insertion\_sort

This program performs a variant of insertion sort, that inserts in place two elements of an array at each loop iteration. This program was proposed as a formal verification challenge during VerifyThis Verification Competition in 2017 (see <a href="http://www.pm.inf.ethz.ch/verifythis.html">http://www.pm.inf.ethz.ch/verifythis.html</a>). The postcondition of the main function Sort expresses both that the array is sorted on exit, and that it is a permutation of its input value. GNATprove proves all checks on this program. The process to progress through all levels of software assurance with SPARK on this example is detailed in the following post on AdaCore blog: <a href="https://blog.adacore.com/verifythis-challenge-in-spark">https://blog.adacore.com/verifythis-challenge-in-spark</a>

#### search\_linked\_list

This program searches for a given value in an unordered linked list. The postcondition of the main function Search expresses that the search is successful if-and-only-if the list contains the value searched, and if so the cursor returned is one at which the list contains this value. GNATprove proves all checks on these programs.

#### string\_search

This example contains multiple variants of substring search:

- a simple brute force search in Brute\_Force and Brute\_Force\_Slice.
- a more efficient algorithm called quick search in QS.

The postcondition of all variants expresses that the search is successful if-and-only-if the string Haystack contains the substring Needle searched, and if so the index returned is one at which the string contains this substring. GNAT-prove proves all checks on these programs. A detailed account of the development and verification of this example is given in the following post on AdaCore blog: https://blog.adacore.com/applied-formal-logic-searching-in-strings

#### trajectory\_computation

This example contains code from an embedded safety-critical software, which computes the speed of a device submitted to gravitational acceleration and drag from the atmosphere around it. This program was used as challenge example in the article "Automating the Verification of Floating-Point Programs" published at VSTTE 2017 conference.

The Ada files contain multiple variants of the example in increasing order of difficulty, see README file for details. The challenge example used in the article corresponds to files simple\_trajectory.ads and simple\_trajectory.adb. In this version, only the speed is updated, not the distance. Both absence of run-time

errors (including overflows) and safe bounds on the computed speed are proved by using a combination of provers. A dozen intermediate assertions are needed to benefit from this combination, so that different provers can prove different parts of the property.

# 7.10.2 Single Units

These examples contain a single unit, and are usually small (a few hundreds slocs at most).

#### adacore\_u

This folder contains the complete source code of the small examples used in the quiz of the SPARK 2014 course available from the AdaCore University website (at http://university.adacore.com/courses/spark-2014/). They include unannotated units, examples with formally verified data flow, functional, or abstraction contracts, as well as erroneous programs, on which GNATprove detects failing checks.

Opening the example in GPS or GNATbench opens an aggregate project, with separate sub-projects for each lecture.

#### allocators

This program demonstrates how the specification of a SPARK program can be formalized using an abstract model and how the refinement relation between the model an its implementation can be verified using GNATprove. It is described in the article "Abstract Software Specifications and Automatic Proof of Refinement" published at RSSRail 2016 conference (at http://blog.adacore.com/uploads/rssrail.pdf).

The example contains three versions of an allocator package. They are specified in terms of mathematical structures (sequences and sets). The refinement relation between the mathematical model and the implementation is expressed as a ghost function Is\_Valid and enforced through contracts. It can be verified automatically using GNATprove.

- Simple\_Allocator features a naive implementation of the allocator, storing the status (available or allocated) of each resource in a big array. It is specified using a ghost function Model which always returns a valid refinement of the allocator's data. The refinement relation is verified only once, as a postcondition of the Model function. The functional contracts on modifying procedures as well as the refinement relation are straightforward and can be verified easily at level 2 in a few seconds.
- List\_Allocator introduces a free list to access more efficiently the first available resource. Here not every possible state of the allocator data can be refined into a valid model. To work around this problem, the model is stored in a global ghost variable which is updated along with the allocator's data and the refinement relation is expressed as an invariant that must be verified as a postcondition of each modifying procedure. The functional contracts on modifying procedures are straightforward but the refinement relation is now more complicated, as it needs to account for the implementation of the free list. They can be verified at level 4 in less than one minute overall.
- List\_Mod\_Allocator features the same implementation and contracts as List\_Allocator, but its model is returned by a ghost function like in Simple\_Allocator instead of being stored in a global ghost variable. As not every possible state of the allocator can be refined into a valid model, the refinement relation is not expressed as a postcondition of Model, but as an invariant, as in List\_Allocator and must be verified as a postcondition of each modifying procedure. The functional contracts and the refinement relation resemble those of List\_Allocator. However, as we don't construct explicitly the new model after each modification, the proof of the allocator's functional contracts requires induction, which is beyond the reach of automatic solvers. The induction scheme is given here manually in an auto-active style through calls to ghost procedures. The whole program can then be verified automatically at level 4 in less than one minute overall on an 8-cores machine, or in a few minutes on a single core.

See the relevant sections for more details on Ghost Code and Manual Proof Using Ghost Code.

#### cartesian trees

This program is a solution to the second challenge of VerifyThis 2019. For a sequence of distinct numbers S, the Cartesian tree of S is the only binary tree T such that T contains a node per element of S, T has the heap property, and symmetrical traversal of T encounters elements in the order of S. The challenge is split in two parts, first construct all nearest smaller neighbors to the left/right of each element of a sequence using a stack, and then construct the Cartesian tree of the sequence using these neighbors.

Computation of the nearest smaller neighbors is fairly straightforward in SPARK. It still features a relatively involved loop invariant. On the other hand, showing that the tree constructed by the algorithm in the second part is the Cartesian tree of the input sequence is rather involved. It uses ghost code to manually guide automatic solvers (see *Manual Proof Using Ghost Code*).

#### database

This program implements a toy interface to a bank account database, with procedures to deposit and withdraw money, and functions to query the account balance and information. This program was used as running example in the article "Integrating Formal Program Verification with Testing" (at http://www.adacore.com/uploads\_gems/Hi-Lite\_ERTS-2012.pdf). The API is annotated with full functional contracts, as well as test cases expressed with aspect Test\_Case. GNATprove proves all checks on this program.

#### evoting

This program implements a toy e-voting interface, to get candidates and votes from a file, compute the winner of the vote and print it. The API is annotated with functional contracts, some partial and some complete. GNATprove proves all checks on this program, except for initialization of an array initialized piecewise (known limitation of flow analysis) and an array access in a string returned by the standard library function <code>Get\_Line</code> (which would require using a wrapper with contracts).

#### formal\_queue

This program implements a queue of integers using a doubly linked list, with full functional contracts on the API of the queue. GNATprove proves all checks on this program.

### ghc\_sort

This program is a partial solution to the first challenge of VerifyThis 2019. It features a sorting algorithm, which works by splitting the input sequence into monotonic subsequences of maximal length. It then reverses the decreasing subsequences and merges them pairwise until the sequence is reconstructed.

Computation of the sequence of cuts is completely verified. On sorting algorithm, we only check that it returns a sorted sequence of the correct length. We did not attempt to prove that the result of the sort function is a permutation of its input. Indeed, this kind of property is complicated both to formalize and to verify, and generally requires ghost code (see *Manual Proof Using Ghost Code*).

This example does not feature the use of any interactive proof techniques, as proofs attempted were largely in reach of the automated tool. We used support for ownership pointers in SPARK to implement lists of subsequences as a recursive data-type using pointers. It is all proved except for termination of recursive functions used to iterate over the lists.

#### natural

This program implements an interface to manipulate sets of natural numbers, stored in an array. Contracts on the interface subprograms express partial correctness properties, for example that the set contains an element after it has been inserted. GNATprove proves all checks on this program.

#### nuclear\_systems

This program implements a concurrent system to control a nuclear reactor, in which the state of the reactor is queried every few seconds, and the reactor is stopped if either its state is Uncontrolled, or if was not controlled in the previous two seconds (because not queried or because it did not answer). GNATprove proves all checks on this program. This program was presented as an idiomatic way to support selective delays in SPARK in a blog post on "Selective Delays in SPARK and Ravenscar" (see https://two-wrongs.com/selective-delay-in-spark-and-ravenscar. html).

#### n\_queens

This program implements the solution to the N queens problem, to place N queens on an N x N chess board so that no queen can capture another one with a legal move. The API is annotated with full functional contracts. GNATprove proves all checks on this program. This program was proposed as a formal verification challenge during VSTTE Verification Competition in 2010 (see https://sites.google.com/a/vscomp.org/main/).

#### patience

This program implements the game of Patience Solitaire, taking cards one-by-one from a deck of cards and arranging them face up in a sequence of stacks. The invariant maintained when playing is a complex relation between multiple arrays storing the current state of the game. GNATprove proves all checks on this program, when using provers CVC4, Alt-Ergo and Z3. This program was proposed as a formal verification challenge during VSTTE Verification Competition in 2014 (see http://vscomp.org/).

#### prime\_numbers

This program implements two functions Nearest\_Number and Nearest\_Prime\_Number which respectively find the closest coprime number and prime number for a given argument value and a given searching mode among three possibilities: above the value only, below the value only, or both. The spec of both functions is expressed in a Contract\_Cases aspect, and proved automatically with GNATprove. GNATprove also proves automatically the functional contract of Initialize\_Coprime\_List which initializes the list of coprimes for a given argument, using Euclid's method, and returns this list to be used with Nearest\_Number. The list of prime numbers is initialized at package elaboration using the sieve of Erathosthenes, a procedure which is currently not fully proved by GNATprove, due to the use of non-linear integer arithmetic and floating-point square root function.

This program offers a nice display of many SPARK features in a simple setting:

- State Abstraction
- Subprogram Contracts
- Specification Features
- · Loop Invariants
- Ghost Code

The original code was contributed by Guillaume Foliard.

#### red black trees

This example demonstrates *Type Invariants* and *Manual Proof Using Ghost Code* on an implementation of red black trees. It features a minimalist library of trees providing only membership test and insertion. The complexity of this example lies in the invariants that are maintained on the data-structure. Namely, it implements a balanced binary search tree, balancing being enforced by red black coloring.

The implementation is divided in three layers, each concerned with only a part of the global data structure invariant. The first package, named <code>Binary\_Trees</code>, is only concerned with the tree structure, whereas <code>Search\_Trees</code> imposes ordering properties and <code>Red\_Black\_Trees</code> enforces balancing. At each level, the relevant properties are expressed using a <code>Type Invariant</code>. It allows to show each independent invariant at the boundary of its layer, assuming that it holds when working on upper layers.

The example features several particularities which make it complex beyond purely automated reasoning. First, the tree structure is encoded using references in an array, which makes it difficult to reason about disjointness of different branches of a tree. Then, reasoning about reachability in the tree structure requires induction, which is often out of the reach of automatic solvers. Finally, reasoning about value ordering is also a pain point for automatic solvers, as it requires coming up with intermediate values on which to apply transitivity.

To achieve full functional verification of this example, it resorts to manually helping automatic solvers using autoactive techniques. For example, ghost procedures are used to introduce intermediate lemmas, loop invariants are written to achieve inductive proofs, and assertions are introduced to provide new values to be used for transitivity relations.

This program and the verification activities associated to it are described in "Auto-Active Proof of Red-Black Trees in SPARK", presented at NFM 2017 (at https://blog.adacore.com/uploads/Auto-Active-Proof-of-Red-Black-Trees-in-SPARK.pdf).

#### railway\_signaling

This program implements a simple signaling algorithm to avoid collision of trains. The main procedure Move moving a given train along the railroad should preserve the collision-free property One\_Train\_At\_Most\_Per\_Track and the correctness of signaling Safe\_Signaling, namely that:

- tracks that are occupied by a train are signalled in red, and
- tracks that precede an occupied track are signalled in orange.

As the algorithm in Move relies on the correctness of the signaling, the preservation of the collision-free property depends also on the the correctness of the signaling. *Pragma Assume* is used to express an essential property of the railroad on which correctness depends, namely that no track precedes itself. GNATprove proves all checks on this program, when using provers CVC4, Alt-Ergo and Z3.

#### ring\_buffer

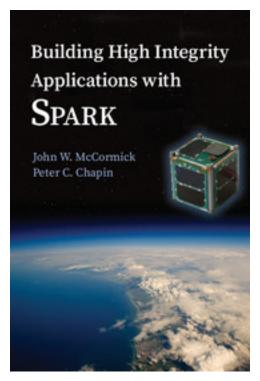
This program implements a ring buffer stored in an array of fixed size, with partial contracts on the API of the ring buffer. GNATprove proves all checks on this program. This program was proposed as a formal verification challenge during VSTTE Verification Competition in 2012 (see https://sites.google.com/site/vstte2012/compet).

#### segway

This program implements a state machine controlling a segway states. The global invariant maintained across states is expressed in an expression function called from preconditions and postconditions. GNATprove proves all checks on this program.

### spark\_book

This collection of examples comes from the book *Building High Integrity Applications with SPARK* written by Prof. John McCormick from University of Northern Iowa and Prof. Peter Chapin from Vermont Technical College, published by Cambridge University Press:



The examples follow the chapters of the book:

- 1. Introduction and overview
- 2. The basic SPARK language
- 3. Programming in the large
- 4. Dependency contracts
- 5. Mathematical background
- 6. Proof
- 7. Interfacing with SPARK
- 8. Software engineering with SPARK
- 9. Advanced techniques

Opening the example in GPS or GNATbench opens a project with all sources. Projects corresponding to individual chapters are available in subdirectories and can be opened manually.

The original source code is available from the publisher's website at http://www.cambridge.org/us/academic/subjects/computer-science/programming-languages-and-applied-logic/building-high-integrity-applications-spark

#### stopwatch

This program implements a stopwatch, and is an example of how concurrent progragms are verified in SPARK. A user can push buttons to start, stop and reset the clock. The clock has a display to show the elapsed time. This example uses protected objects and tasks.

GNAT prove proves all checks on this program, including the safe usage of concurrency.

#### tagged\_stacks

This example features an abstract view of a stack, represented as an abstract tagged type with abstract primitives, as well as two concrete stack implementations deriving from this abstract root. A procedure Test\_Stack defined on any object of the type hierarchy uses dispatching to test any concrete stack implementation.

Note that in this example, LSP checks (see *Object Oriented Programming and Liskov Substitution Principle*) are trivial as no contracts are supplied on overriding subprograms. The differences of behaviors between the two concrete implementations are all accounted for through calls to primitive functions in the classwide contracts.

Also note that we did not provide any loop invariants on the loops of Test\_Stack. Instead we rely on *Automatic Unrolling of Simple For-Loops* to verify the procedure.

GNAT prove proves all checks on this program.

#### tetris

This program implements a simple version of the game of Tetris. An invariant of the game is stated in function Valid\_Configuration, that all procedures of the unit must maintain. This invariant depends on the state of the game which if updated by every procedure. Both the invariant and the state of the game are encoded as *Ghost Code*. The invariant expresses two properties:

- 1. A falling piece never exits the game board, and it does not overlap with pieces that have already fallen.
- 2. After a piece has fallen, the complete lines it may create are removed from the game board.

GNATprove proves all checks on the full version of this program found in tetris\_functional.adb. Intermediate versions of the program show the initial code without any contracts in tetris\_initial.adb, the code with contracts for data dependencies in tetris\_flow.adb and the code with contracts to guard against run-time errors in tetris\_integrity.adb. The complete program, including the BSP to run it on the ATMEL SAM4S board, is available online (see http://blog.adacore.com/tetris-in-spark-on-arm-cortex-m4).

#### tictactoe

This program implements a game of tic-tac-toe. A human player and the computer take turns. Subprograms Player\_Play and Computer\_Play in tictactoe.ads have partial contracts stating that the number of free slots decreases by one after each play.

GNATprove proves all absence of run-time errors on this program, and that the subprogram contracts are correctly implemented. Interestingly, no loop invariants are needed, although the program contains many loops, thanks to the use of *Automatic Unrolling of Simple For-Loops* in GNATprove.

#### traffic light

This program implements two small simulators of traffic lights:

- Unit Road\_Traffic defines safety rules for operating traffic lights over a crossroads. All procedures that change the state of the lights must maintain the safety property.
- Unit Traffic\_Lights defines a concurrent program for operating traffic lights at a pedestian crossing, using two tasks that communicate over a protected object, where the invariant maintained by the protected data is expressed using a subtype predicate.

GNAT prove proves all checks on this program, including the safe usage of concurrency (absence of data races, absence of deadlocks).

## 7.10.3 Multi-Units Demos

These examples contain larger demo programs (of a few hundreds or thousands slocs).

#### autopilot

This program was originally a case study written in SPARK 2005 by John Barnes, presented in section 14.3 of his book "High Integrity Software, The SPARK Approach to Safety and Security" (2003) and section 15.1 of the updated book "SPARK: The Proven Approach to High Integrity Software" (2012). For details on this case study, see one of the above books. The program in the toolset distribution is the SPARK 2014 version of this case study.

The program considers the control system of an autopilot controlling both altitude and heading of an aircraft. The altitude is controlled by manipulating the elevators and the heading is controlled by manipulating the ailerons and rudder.

The values given by instruments are modelled as *External State Abstraction* with asynchronous writers (the sensors) in package Instruments. The states of controllers are modelled as a *State Abstraction* called State in package AP, which is successively refined into finer-grain abstractions in the child packages of AP (for example AP.Altitude and AP.Altitude.Pitch). The actions on the mobile surfaces of the plane are modelled as *External State Abstraction* with asynchronous readers (the actuators) in package Surfaces.

Data and flow dependency contracts are given for all subprograms. GNATprove proves all checks on this program, except for 4 runtime checks related to scaling quantities using a division (a known limitation of automatic provers).

#### bitwalker

This program was originally a case study in C from Siemens rewritten by the Fraunhofer FOKUS research group for applying the Frama-C formal verification tool to it. It was later on rewritten in SPARK and formally proved correct with GNATprove (with 100% of checks automatically proved). This work is described in the article "Specification and Proof of High-Level Functional Properties of Bit-Level Programs" published at NFM 2016 conference (at https://hal.inria.fr/hal-01314876).

This program introduces a function and procedure that read and respectively write a word of bits of a given length from a stream of bytes at a given position. It heavily uses bitwise arithmetic and is fully specified with contracts and automatically proved by GNATprove. In addition, two test procedures call read-then-write and write-then-read and GNATprove is able to prove the expected properties on the interplay between reading and writing.

In this program we use an external axiomatization in order to lift some operators from the underlying Why3 theory of bitvectors to SPARK. In particular the Nth function, at the core of the specification of the program, lets us check if a specific bit in a modular value is set or not. Note that while such a function could be easily implemented in SPARK,

using the one defined in the Why3 theory leads to more automatic proofs because it lets the provers use the associated axioms and lemmas.

#### crazyflie

This program is a translation of the stabilization system of the Crazyflie 2.0, a tiny drone released by Bitcraze AB in 2013 and originally based on an open-source firmware written in C.

This SPARK code interfaces with the other parts of the firmware (ST peripheral libraries, FreeRTOS libraries, Crazyflie sensors and actuators), which remained in C, by using Ada capabilities for multi-language programs.

The goal was to prove absence of runtime errors on the most critical code parts of the drone's firmware. The techniques used to achieve this aim were presented in a post on the AdaCore Blog: http://blog.adacore.com/how-to-prevent-drone-crashes-using-spark

Data dependency contracts are given for most subprograms, specially in the Stabilizer\_Pack package which uses *State Abstraction* to specify this type of contracts.

#### heatingsystem

This program is a standard example of controller, turning on and off the heating depending on the value of the current temperature read by a thermostat and the current mode of operation. Interfaces to the physical world are modelled as *External State Abstraction* for sensors and actuators. Data and flow dependency contracts are given for all subprograms. GNATprove proves all checks on this program.

#### ipstack

This program is an implementation of a TCP/IP stack targeted at bare-board embedded applications in certifiable systems. The API is an event driven architecture (based on LWIP design), with an application interface based on callbacks. The protocols supported are:

- IPv4
- ARP
- UDP
- TCP
- ICMP

This TCP/IP stack can be used either on a PowerPC bare-board system or on a Linux host as a native process. In the latter case, the TAP device is used for communication between the stack and the host system. For more details, see the corresponding README file.

Data dependency contracts are given for most subprograms. These contracts are proved by GNATprove flow analysis, which also proves the absence of reads of uninitialized data.

### openETCS

This program is a case study performed by David Mentré in the context of the openETCS European project aiming at making an open-source, open-proof reference model of ETCS (European Train Control System). ETCS is a radio-based train control system aiming at unifying train signaling and control over all European countries. The results of this case study are described in the article "Rail, Space, Security: Three Case Studies for SPARK 2014".

Package Section\_4\_6 models a subset of the transitions allowed in the overall state automaton that the system should follow. Guards for transitions are expressed by using *Expression Functions*, and the disjointness of these guards is expressed by using *Contract Cases*. GNATprove proves all checks on this part of the program.

Package Step\_Function implements piecewise constant functions used to model for example speed restrictions against distance. Full functional contracts are given for all the services of this package. GNATprove proves all checks on this part of the program, except the more complex postcondition of procedure Restrictive\_Merge.

## sparkskein

This program is an implementation of the Skein cryptographic hash algorithm (see http://www.skein-hash.info/). This implementation is readable, completely portable to a wide-variety of machines of differing word-sizes and endianness. This program was originally written in SPARK 2005 by Rod Chapman as a case study for the applicability of SPARK to cryptographic code. For details on this case study, see the article "SPARKSkein: A Formal and Fast Reference Implementation of Skein" (at http://www.adacore.com/knowledge/technical-papers/sparkskein/). The program in the toolset distribution is the SPARK 2014 version of this case study.

Compared to the original version written for the previous generation of the SPARK toolset, this version requires much less work to obtain complete assurance of the absence of run-time errors. In the following, we call a *precondition element* a conjunct in a precondition, *postcondition element* a conjunct in a postcondition and *loop invariant element* a conjunct in a loop invariant. The number of such elements in a verified program is directly related (usually proportional) to the verification effort, as each such element requires the user to write it, to debug it, and finally to prove it.

- Contrary to GNATprove, the previous toolset did not include *Generation of Dependency Contracts*. This required writing 17 non-trivial global contracts and 24 non-trivial derives contracts. With GNATprove, no data dependency or flow dependency is needed at all. We have kept 17 trivial null data dependency contracts and a single non-trivial data dependency contract for documentation purposes. Similarly, we have kept 11 trivial null flow dependency contracts for documentation purposes.
- SPARK naturally supports nesting of subprograms, which allows a natural top-down decomposition of the main operations into local procedures. This decomposition aids readability and has a negligible impact on performance, assuming the compiler is able to inline the local procedures, but it previously had a very costly impact on formal verification. The previous toolset required the user to write functional contracts on all local subprograms to be able to prove absence of run-time errors in these subprograms. On the contrary, GNATprove performs *Contextual Analysis of Subprograms Without Contracts*, which allows us to save the effort of writing 19 precondition elements and 12 postcondition elements that were needed in the original version.
- The previous toolset required the insertion of lengthy *Loop Invariants*, totalling 43 loop invariant elements (some of them quite complex), while GNATprove currently requires only 1 simple loop invariant stating which components of a record are not modified in the loop. This is partly due to GNATprove now being able to generate loop invariants for unmodified record components (see *Automatically Generated Loop Invariants*).
- The previous toolset generated a logical formula to prove for each path leading to a run-time check or an assertion. This lead to the generation of 367 formulas overall on the original version, almost 5 times more than the 78 checks generated by GNATprove on the new version. This difference is impressive, given that everything was done in the original version to control the explosion of the number of formulas, with the insertion of 24 special annotations in the source code similar to *Pragma Assert\_And\_Cut* in SPARK 2014, while no such work was needed in the new version. Despite this and other differences in efficiency between the two toolsets, the analysis time to ensure complete absence of run-time errors is similar between the two toolsets: 5 min with the previous toolset, half of that with GNATprove.
- Out of the 367 generated formulas, 29 were not proved automatically with the previous toolset: 6 formulas required the insertion of user-defined lemmas in the theorem prover, and 23 formulas required manual proof in a proof assistant. With GNATprove and provers CVC4, Z3 and Alt-Ergo, all checks are proved automatically.

#### spark\_io

This program is an example wrapping of Ada standard input output library in a SPARK compatible library interface. For example, the standard unit Ada.Text\_IO is wrapped in a unit called SPARK.Text\_IO that provides the same services, but uses normal control flow to signal errors instead of exceptions. A type File\_Status decribes either a normal status for a file (Unopened or Success) or an error status (Status\_Error, Mode\_Error, etc.). The standard type for a file Ada.Text\_IO.File\_Type is wrapped into a record type SPARK.Text\_IO File Type together with the status described above.

Wrapper units are also given for most children of the Ada standard input output library Ada.Text\_IO, for example the generic unit SPARK.Text\_IO.Integer\_IO wraps the services of the standard unit Ada.Text\_IO. Integer\_IO. Partial function contracts are expressed on all subprograms. GNATprove proves all checks on the implementation of these wrapper units.

#### text\_io\_get\_line

This program is a simplified extracted version of the standard library function Ada.Text\_IO.Get\_Line, which reads a line of text from an input file. The various versions of Ada.Text\_IO.Get\_Line (procedures and functions) are specified with respect to a simplified model of the file system, with a single file The\_File opened at a location Cur\_Location. The low-level functions providing an efficient implementation (fgets, memcpy, etc.) are also specified with respect to the same model of the file system.

GNATprove proves automatically that the code is free of run-time errors (apart from a few messages that are either intentional or related to the ghost code instrumentation) and that subprogram bodies respect their functional contracts. The story behind this work was presented in a post on the AdaCore Blog: http://blog.adacore.com/formal-verification-of-legacy-code

### thumper

This program is a secure time stamp client/server system that implements RFC-3161 (see https://www.ietf.org/rfc/rfc3161.txt). It allows clients to obtain cryptographic time stamps that can be used to later verify that certain documents existed on or before the time mentioned in the time stamp. Thumper is written in a combination of Ada 2012 and SPARK 2014 and makes use of an external C library. Thumper was developed as a SPARK technology demonstration by Prof. Peter Chapin from Vermont Technical College and his students. It is used as a case study in the book *Building High Integrity Applications with SPARK* written by Prof. John McCormick from University of Northern Iowa and Prof. Peter Chapin, published by Cambridge University Press (see section 8.5).

The program in the toolset distribution is a snapshot of the Thumper project and a supporting project providing ASN.1 support named Hermes, whose up-to-date sources can be obtained separately from GitHub:

- Thumper at https://github.com/pchapin/thumper
- Hermer at https://github.com/pchapin/hermes

The verification objectives pursued in both projects are currently to *Address Data and Control Coupling* with a focus on ensuring secure information flows (especially important for a cryptographic application) and to *Prove Absence of Run-Time Errors* (AoRTE).

#### tokeneer

This program is a highly secure biometric software system that was originally developed by Altran. The system provides protection to secure information held on a network of workstations situated in a physically secure enclave. The Tokeneer project was commissioned by the US National Security Agency (NSA) to demonstrate the feasibility of developing systems to the level of rigor required by the higher assurance levels of the Common Criteria. The

requirements of the system were captured using the Z notation and the implementation was in SPARK 2005. The original development artifacts, including all source code, are publicly available (see http://www.adacore.com/sparkpro/tokeneer).

The program in the toolset distribution is a translation of the original Tokeneer code into SPARK 2014. The core system now consists of approximately 10,000 lines of SPARK 2014 code. There are also approximately 3,700 lines of supporting code written in Ada which mimick the drivers to peripherals connected to the core system.

Data and flow dependency contracts are given for all subprograms. Partial functional contracts are also given for a subset of subprograms. GNATprove currently proves automatically all checks on SPARK code in Tokeneer. The transition from SPARK 2005 to SPARK 2014 was presented in a post on the AdaCore Blog: https://blog.adacore.com/tokeneer-fully-verified-with-spark-2014

Tokeneer can be used as the basis for demonstrating four types of security vulnerabilities that can be detected by GNATprove, when calling GPS with -XSECURITY\_DEMO=True (or changing the value of the scenario variable in GPS). Analyzing the code in that setting detects:

- an information leak in keystore.adb
- a back door in bio.adb
- a buffer overflow in admintoken.adb
- an implementation flaw in alarm.adb

# APPLYING SPARK IN PRACTICE

SPARK tools offer different levels of analysis, which are relevant in different contexts. This section starts with a description of the main *Objectives of Using SPARK*. This list gathers the most commonly found reasons for adopting SPARK in industrial projects, but it is not intended to be an exhaustive list.

Whatever the objective(s) of using SPARK, any project fits in one of four possible *Project Scenarios*:

- the brown field scenario: Maintenance and Evolution of Existing Ada Software
- the green field scenario: New Developments in SPARK
- the migration scenario: Conversion of Existing SPARK Software to SPARK 2014
- the frozen scenario: Analysis of Frozen Ada Software

The end of this section examines each of these scenarios in turn and describes how SPARK can be applied in each case.

# 8.1 Objectives of Using SPARK

# 8.1.1 Safe Coding Standard for Critical Software

SPARK is a subset of Ada meant for formal verification, by excluding features that are difficult or impossible to analyze automatically. This means that SPARK can also be used as a coding standard to restrict the set of features used in critical software. As a safe coding standard checker, SPARK allows both to prevent the introduction of errors by excluding unsafe Ada features, and it facilitates their early detection with GNATprove's flow analysis.

#### **Exclusion of Unsafe Ada Features**

Once the simple task of *Identifying SPARK Code* has been completed, one can use GNATprove in check mode to verify that SPARK restrictions are respected in SPARK code. Here we list some of the most error-prone Ada features that are excluded from SPARK (see *Excluded Ada Features* for the complete list).

- All expressions, including function calls, are free of side-effects. Expressions with side-effects are problematic
  because they hide interactions that occur in the code, in the sense that a computation will not only produce a
  value but also modify some hidden state in the program. In the worst case, they may even introduce interferences
  between subexpressions of a common expression, which results in different executions depending on the order
  of evaluation of subexpressions chosen by the compiler.
- Handling of exceptions is not permitted. Exception handling can create complex and invisible control flows in
  a program, which increases the likelihood of introducing errors during maintenance. What is more, when an
  exception is raised, subprograms that are terminated abnormally leave their variables in a possibly uninitialized
  or inconsistent state, in which data invariants may be broken. This includes values of out parameters, which

additionally are not copied back when passed by copy, thus introducing a dependency on the parameter mode chosen by the compiler.

- The use of access types and allocators is not permitted. Pointers can introduce aliasing, that is, they can allow the same object to be visible through different names at the same program point. This makes it difficult to reason about a program as modifying the object under one of the names will also modify the other names. What is more, access types come with their own load of common mistakes, like double frees and dangling pointers.
- SPARK also prevents dependencies on the elaboration order by ensuring that no package can write into variables
  declared in other packages during its elaboration. The use of controlled types is also forbidden as they lead to
  insertions of implicit calls by the compiler. Finally, goto statements are not permitted as they obfuscate the
  control flow.

# **Early Detection of Errors**

GNATprove's flow analysis will find all the occurrences of the following errors:

- uses of uninitialized variables (see *Data Initialization Policy*)
- aliasing of parameters that can cause interferences, which are often not accounted for by programmers (see *Absence of Interferences*)

It will also warn systematically about the following suspicious behaviors:

- wrong parameter modes (can hurt readability and maintainability or even be the sign of a bug, for example if the programmer forgot to update a parameter, to read the value of an out parameter, or to use the initial value of a parameter)
- unused variables or statements (again, can hurt readability and maintainability or even be the sign of a bug)

# 8.1.2 Prove Absence of Run-Time Errors (AoRTE)

# With Proof Only

GNAT prove can be used to prove the complete absence of possible run-time errors corresponding to:

- all possible explicit raising of exceptions in the program,
- raising exception Constraint\_Error at run time, and
- all possible failures of assertions corresponding to raising exception Assert Error at run time.

AoRTE is important for ensuring safety in all possible operational conditions for safety-critical software (including boundary conditions, or abnormal conditions) or for ensuring availability of a service (absence of DOS attack that can crash the software).

When run-time checks are enabled during execution, Ada programs are not vulnerable to the kind of attacks like buffer overflows that plague programs in C and C++, which allow attackers to gain control over the system. But in the case where run-time checks are disabled (in general for efficiency, but it could be for other reasons), proving their absence with GNATprove also prevents such attacks. This is specially important for ensuring security when some inputs may have been crafted by an attacker.

Few subprogram contracts (*Preconditions* and *Postconditions*) are needed in general to prove AoRTE, far fewer than for proving functional properties. Even fewer subprogram contracts are needed if types are suitably constrained with *Type Contracts*. Typically, 95% to 98% of run-time checks can be proved automatically, and the remaining checks can be either verified with manual provers or justified by manual analysis.

GNATprove supports this type of combination of results in the summary table of *The Analysis Results Summary File*. Multiple columns display the number of checks automatically verified, while the column *Justified* displays the number of checks manually justified. The column *Unproved* should be empty for all checks to be verified.

#### With a Combination of Proof and Test

It is not always possible to achieve 100% proof of AoRTE, for multiple reasons:

- 1. Formal verification is only applicable to the part of the program that is in SPARK. If the program includes parts in Ada that are not in SPARK, for example, then it is not possible to prove AoRTE on those parts.
- 2. Some run-time checks may not be proved automatically due to prover shortcomings (see *Investigating Prover Shortcomings* for details).
- 3. It may not be cost-effective to add the required contracts for proving AoRTE in a less critical part of the code, compared to using testing as a means of verification.

For all these reasons, it is important to be able to combine the results of formal verification and testing on different parts of a codebase. Formal verification works by making some assumptions, and these assumptions should be shown to hold even when formal verification and testing are combined. Certainly, formal verification cannot guarantee the same properties when part of a program is only tested, as when all of a program is proved. The goal then, when combining formal verification and testing, is to reach a level of confidence as good as the level reached by testing alone.

### At the Level of Individual Run-Time Checks

One way to get confidence that unproved run-time checks cannot fail during execution is to exercise them during testing. Test coverage information allows guaranteeing a set of run-time checks have been executed successfully during a test run. This coverage information may be gathered from the execution of a unit testing campaign, an integration testing campaign, or the execution of a dedicated testsuite focussing on exercising the run-time checks (for example on boundary values or random ones).

This strategy is already applied in other static analysis tools, for example in the integration between the CodePeer static analyzer and the VectorCAST testing tool for Ada programs.

# **Between Proof and Integration Testing**

Contracts can also be exercised dynamically during integration testing. In cases where unit testing is not required (either because proof has been applied to all subprograms, or because the verification context allows it), exercising contracts during integration testing can complement proof results, by giving the assurance that the actual compiled program behaves as expected.

This strategy has been applied at Altran on UK military projects submitted to Def Stan 00-56 certification: AoRTE was proved on all the code, and contracts were exercised during integration testing, which allowed to scrap unit testing.

# **Between Proof and Unit Testing**

Contracts on subprograms provide a natural boundary for combining proof and test:

• If proof is used to demonstrate that a subprogram is free of run-time errors and respects its contract, this proof depends on the precondition of the subprogram being respected at the call site. This verification can be achieved by proving the caller too, or by checking dynamically the precondition of the called subprogram during unit testing of the caller.

• If proof is used to demonstrate that a subprogram is free of run-time errors and respects its contract, and this subprogram calls other subprograms, this proof depends on the postconditions of the called subprogram being respected at call sites. This verification can be achieved by proving the callees too, or by checking dynamically the postcondition of the called subprograms during their unit testing.

Thus, it is possible to combine freely subprograms that are proved and subprograms that are unit tested, provided subprogram contracts (*Preconditions*) and *Postconditions*) are exercised during unit testing. This can be achieved by compiling the program with assertions for testing (for example with switch -gnata in GNAT), or by using GNATtest to create the test harness (see section 7.10.12 of GNAT User's Guide on *Testing with Contracts*).

When combining proof and test on individual subprograms, one should make sure that the assumptions made for proof are justified at the boundary between proved subprograms and tested subprograms (see section on *Managing Assumptions*). To help with this verification, special switches are defined in GNAT to add run-time checks that verify dynamically the assumptions made during proof:

- -qnateA adds checks that parameters are not aliased
- -gnateV adds checks that parameters are valid, including parameters of composite types (arrays, records)
- -gnatVa adds checks that objects are valid at more places than -gnateV, but only for scalar objects

This strategy is particularly well suited in the context of the DO-178C certification standard in avionics, which explicitly allows proof or test to be used as verification means on each module.

# 8.1.3 Prove Correct Integration Between Components

### In New Developments

GNATprove can be used to prove correct integration between components, where a component could be a subprogram, a unit or a set of units. Indeed, even if components are verified individually (for example by proof or test or a combination thereof), their combination may still fail because of unforeseen interactions or design problems.

SPARK is ideally equipped to support such analysis, with its detailed *Subprogram Contracts*:

- With *Data Dependencies*, a user can specify exactly the input and output data of a subprogram, which goes a long way towards uncovering unforeseen interactions.
- With functional contracts (*Preconditions* and *Postconditions*), a user can specify precisely properties about the behavior of the subprogram that are relevant for component integration. In general, simple contracts are needed for component integration, which means that they are easy to write and to verify automatically. See section on *Writing Contracts for Program Integrity* for examples of such contracts.

When using data dependencies, GNATprove's flow analysis is sufficient to check correct integration between components. When using functional contracts, GNATprove's proof should also be applied.

# In Replacement of Comments

It is good practice to specify properties of a subprogram that are important for integration in the comments that are attached to the subprogram declaration.

Comments can be advantageously replaced by contracts:

- Comments about the domain of the subprogram can be replaced by *Preconditions*.
- Comments about the effects of the subprogram can be replaced by *Postconditions* and *Data Dependencies*.
- Comments about the result of functions can be replaced by *Postconditions*.
- GNATprove can use the contracts to prove correct integration between components, as in new developments.

Contracts are less ambiguous than comments, and can be accompanied by (or interspersed with) higher level comments that need not be focused on the finer grain details of which variables must have which values, as these are already specified concisely and precisely in the contracts.

# In Replacement of Defensive Coding

In existing Ada code that is migrated to SPARK, defensive coding is typically used to verify the correct integration between components: checks are made at the start of a subprogram that inputs (parameters and global variables) satisfy expected properties, and an exception is raised or the program halted if an unexpected situation is found.

Defensive code can be advantageously replaced by preconditions:

- The dynamic checks performed by defensive code at run time can be performed equally by preconditions, and they can be enabled at a much finer grain thanks to *Pragma Assertion\_Policy*.
- GNATprove can use the preconditions to prove correct integration between components, as in new developments.

# 8.1.4 Prove Functional Correctness

# In New Developments

GNATprove can be used to prove functional correctness of an implementation against its specification. This strongest level of verification can be applied either to specific subprograms, or specific units, or the complete program. For those subprograms whose functional correctness is to be checked, the user should:

- 1. express the specification of the subprogram as a subprogram contract (see *Preconditions* and *Postconditions*);
- 2. use GNAT prove to prove automatically that most checks (including contracts) always hold; and
- 3. address the remaining unproved checks with manual justifications or testing, as already discussed in the section on how to *Prove Absence of Run-Time Errors* (*AoRTE*).

As more complex contracts are required in general, it is expected that achieving that strongest level of verification is also more costly than proving absence of run-time errors. Typically, SPARK features like *Quantified Expressions* and *Expression Functions* are needed to express the specification, and features like *Loop Invariants* are needed to achieve automatic proof. See section on *Writing Contracts for Functional Correctness* for examples of such contracts, and section on *How to Write Loop Invariants* for examples of the required loop invariants.

When the functional specification is expressed as a set of disjoint cases, the SPARK feature of *Contract Cases* can be used to increase readability and to provide an automatic means to verify that cases indeed define a partitioning of the possible operational contexts.

# In Replacement of Unit Testing

In existing Ada code that is migrated to SPARK, unit testing is typically used to verify functional correctness: actual outputs obtained when calling the subprogram are compared to expected outputs for given inputs. A *test case* defines an expected behavior to verify; a *test procedure* implements a *test case* with specific given inputs and expected outputs.

Test cases can be used as a basis for functional contracts, as they define in general a behavior for a set of similar inputs. Thus, a set of test cases can be transformed into *Contract Cases*, where each case corresponds to a test case: the test input constraint becomes the guard of the corresponding case, while the test output constraint becomes the consequence of the corresponding case.

GNATprove can be used to prove this initial functional contract, as in new developments. Then, cases can be progressively generalized (by relaxing the conditions in the guards), or new cases added to the contract, until the full functional behavior of the subprogram is specified and proved.

# 8.1.5 Ensure Correct Behavior of Parameterized Software

In some domains (railway, space), it is common to develop software which depends on parameterization data, which changes from mission to mission. For example, the layout of railroads or the characteristics of the payload for a spacecraft are mission specific, but in general do not require developing completely new software for the mission. Instead, the software may either depend on data definition units which are subject to changes between missions, or the software may load at starting time (possibly during *elaboration* in Ada) the data which defines the characteristics of the mission. Then, the issue is that a verification performed on a specific version of the software (for a given parameterization) is not necessarily valid for all versions of the software. In general, this means that verification has to be performed again for each new version of the software, which can be costly.

SPARK provides a better solution to ensure correct behavior of the software for all possible parameterizations. It requires defining a getter function for every variable or constant in the program that represents an element of parameterization, and calling this getter function instead of reading the variable or constant directly. Because GNATprove performs an analysis based on contracts, all that is known at analysis time about the value returned by a getter function is what is available from its signature and contract. Typically, one may want to use *Scalar Ranges* or *Predicates* to constrain the return subtype of such getter functions, to reflect the operational constraints respected by all parameterizations.

This technique ensures that the results of applying GNATprove are valid not only for the version of the software analyzed, but for any other version that satisfies the same operational constraints. This is valid whatever the objective(s) pursued with the use of SPARK: *Prove Absence of Run-Time Errors* (AoRTE), *Prove Correct Integration Between Components*, *Prove Functional Correctness*, etc.

It may be the case that changing constants into functions makes the code illegal because the constants were used in representation clauses that require static values. In that case, compilation switch <code>-gnatI</code> should be specified when analyzing the modified code with GNATprove, so that representation clauses are ignored. As representation clauses have no effect on GNATprove's analysis, and their validity is checked by GNAT when compiling the original code, the formal verification results are valid for the original code.

For constants of a non-scalar type (for example, constants of record or array type), an alternative way to obtain a similar result as the getter function is to define the constant as a deferred constant, whose initial declaration in the visible part of a package spec does not specify the value of the constant. Then, the private part of the package spec which defines the completion of the deferred constant must be marked SPARK\_Mode => Off, so that clients of the package only see the visible constant declaration without value. In such a case, the analysis of client units with GNAT prove is valid for all possible values of the constant.

# 8.1.6 Safe Optimization of Run-Time Checks

Enabling run-time checks in a program usually increases the running time by around 10%. This may not fit the timing schedule in some highly constrained applications. In some cases where a piece of code is called a large number of times (for example in a loop), enabling run-time checks on that piece of code may increase the running time by far more than 10%. Thus, it may be tempting to remove run-time checking in the complete program (with compilation switch -gnatp) or a selected piece of code (with pragma Suppress), for the purpose of decreasing running time. The problem with that approach is that the program is not protected anymore against programming mistakes (for safety) or attackers (for security).

GNATprove provides a better solution, by allowing users to prove the absence of all run-time errors (or run-time errors of a specific kind, for example overflow checks) in a piece of code, provided the precondition of the enclosing subprogram is respected. Then, all run-time checks (or run-time errors of a specific kind) can be suppressed in that piece of code using pragma Suppress, knowing that they will never fail at run time, provided the precondition of the enclosing subprogram is checked (for example by using *Pragma Assertion\_Policy*). By replacing many checks with one check, we can decrease the running time of the application by doing safe and controlled optimization of run-time checks.

# 8.1.7 Address Data and Control Coupling

As defined in the avionics standard DO-178, data coupling is "The dependence of a software component on data not exclusively under the control of that software component" and control coupling is "The manner or degree by which one software component influences the execution of another software component", where a software component could be a subprogram, a unit or a set of units.

Although analysis of data and control coupling are not performed at the same level of details in non-critical domains, knowledge of data and control coupling is important to assess impact of code changes. In particular, it may be critical for security that some secret data does not leak publicly, which can be rephrased as saying that only the specified data dependencies are allowed. SPARK is ideally equiped to support such analysis, with its detailed *Subprogram Contracts*:

- With *Data Dependencies*, a user can specify exactly the input and output data of a subprogram, which identifies the "data not exclusively under the control of that software component":
  - When taking the subprogram as component, any variable in the data dependencies is in general not exclusively under the control of that software component.
  - When taking the unit (or sets of units) as component, any variable in the data dependencies that is not
    defined in the unit itself (or the set of units) is in general not exclusively under the control of that software
    component.
- With Flow Dependencies, a user can specify the nature of the "dependence of a software component on data not exclusively under the control of that software component", by identifying how that data may influence specific outputs of a subprogram.
- With *Flow Dependencies*, a user can also specify how "one software component influences the execution of another software component", by identifying the shared data potentially written by the subprogram.
- With functional contracts (*Preconditions* and *Postconditions*), a user can specify very precisely the behavior of the subprogram, which defines how it "influences the execution of another software component". These contracts need not be complete, for example they could describe the precedence order rules for calling various subprograms.

When using data and flow dependencies, GNATprove's flow analysis is sufficient to check that the program implements its specifications. When using functional contracts, GNATprove's proof should also be applied.

# 8.1.8 Ensure Portability of Programs

Using SPARK enhances portability of programs by excluding language features that are known to cause portability problems, and by making it possible to obtain guarantees that specific portability problems cannot occur. In particular, analyses of SPARK code can prove the absence of run-time errors in the program, and that specified functional properties always hold.

Still, porting a SPARK program written for a given compiler and target to another compiler and/or target may require changes in the program. As SPARK is a subset of Ada, and because in general only some parts of a complete program are in SPARK, we need to consider first the issue of portability in the context of Ada, and then specialize it in the context of SPARK.

Note that we consider here portability in its strictest sense, whereby a program is portable if its observable behavior is exactly the same across a change of compiler and/or target. In the more common sense of the word, a program is portable if it can be reused without modification on a different target, or when changing compiler. That is consistent with the definition of portability in WikiPedia: "Portability in high-level computer programming is the usability of the same software in different environments". As an example of a difference between both interpretations, many algorithms which use trigonometry are portable in the more common sense, not in the strictest sense.

## **Portability of Ada Programs**

Programs with errors cause additional portability issues not seen in programs without errors, which is why we consider them separately.

## **Portability of Programs Without Errors**

The Ada Reference Manual defines precisely which features of the language depend on choices made by the compiler (see Ada RM 1.1.3 "Conformity of an Implementation with the Standard"):

- Implementation defined behavior The set of possible behaviors is specified in the language, and the particular behavior chosen in a compiler should be documented. An example of implementation defined behavior is the size of predefined integer types (like Integer). All implementation defined behaviors are listed in Ada RM M.2, and GNAT documents its implementation for each of these points in section 7 "Implementation Defined Characteristics" of the GNAT Reference Manual.
- *Unspecified behavior* The set of possible behaviors is specified in the language, but the particular behavior chosen in a compiler need not be documented. An example of unspecified behavior is the order of evaluation of arguments in a subprogram call.

Changes of compiler and/or target may lead to different implementation defined and unspecified behavior, which may or not have a visible effect. For example, changing the order of evaluation of arguments in a subprogram call only has a visible effect if the evaluation of arguments itself has some side-effects.

Section 18.4 "Implementation-dependent characteristics" of the GNAT Reference Manual gives some advice on how to address implementation defined behavior for portability.

A particular issue is that the Ada Reference Manual gives much implementation freedom to the compiler in the implementation of operations of fixed-point and floating-point types:

- The small of a fixed-point type is implementation defined (Ada RM 3.5.9(8/2)) unless specified explicitly.
- The base type of a fixed-point type is implementation defined (Ada RM 3.5.9(12-16)), which has an impact on possible overflows.
- The rounded result of an ordinary fixed-point multiplication or division is implementation defined (Ada RM G.2.3(10)).
- For some combinations of types of operands and results for fixed-point multiplication and division, the value of the result belongs to an implementation defined set of values (Ada RM G.2.3(5)).
- The semantics of operations on floating-point types is implementation defined (Ada RM G.2). It may or may not follow the IEEE 754 floating point standard.
- The precision of elementary functions (exponential and trigonometric functions) is implementation defined (Ada RM G.2.4).

Section 18.1 "Writing Portable Fixed-Point Declarations" of the GNAT Reference Manual gives some advice on how to reduce implementation defined behavior for fixed-point types. Use of IEEE 754 floating-point arithmetic can be enforced in GNAT by using the compilation switches "-msse2 -mfpmath=sse", as documented in section 8.3.1.6 "Floating Point Operations" of the GNAT User's Guide.

Note that a number of restrictions can be used to prevent some features leading to implementation defined or unspecified behavior:

- Restriction No\_Fixed\_Point forbids the use of fixed-point types.
- Restriction No\_Floating\_Point forbids the use of floating-point types.
- $\bullet$  Restriction No\_Implementation\_Aspect\_Specifications forbids the use of implementation defined aspects.

- Restriction No\_Implementation\_Attributes forbids the use of implementation defined attributes.
- Restriction No\_Implementation\_Pragmas forbids the use of implementation defined pragmas.

**Note:** SPARK defines a few constructs (aspects, pragmas and attributes) that are not defined in Ada. While GNAT supports these constructs, care should be exercised to use these constructs with other compilers, or older versions of GNAT. This issue is detailed in section *Portability Issues*.

## **Portability of Programs With Errors**

In addition to the portability issues discussed so far, programs with errors cause specific portability issues related to whether errors are detected and how they are reported. The Ada Reference Manual distinguishes between four types of errors (see Ada RM 1.1.5 "Classification of Errors"):

- *Compile-time errors* These errors make a program illegal, and should be detected by any Ada compiler. They do not cause any portability issue, as they must be fixed before compilation.
- Run-time errors These errors are signaled by raising an exception at run time. They might be a cause of portability problems, as a change of compiler and/or target may lead to new run-time errors. For example, a new compiler may cause the program to use more stack space, leading to an exception Storage\_Error, and a new target may change the size of standard integer types, leading to an exception Constraint\_Error.
- Bounded errors These errors need not be detected either at compiler time or at run time, but their effects should be bounded. For example, reading an uninitialized value may result in any value of the type to be used, or to Program\_Error being raised. Like for run-time errors, they might be a cause of portability problems, as a change of compiler and/or target may lead to new bounded errors.
- *Erroneous execution* For the remaining errors, a program exhibits erroneous execution, which means that the error need not be detected, and its effects are not bounded by the language rules. These errors might be a cause of portability problems.

Portability issues may arise in a number of cases related to errors:

- The original program has an error that is not detected (a run-time error, bounded error or erroneous execution). Changing the compiler and/or target causes the error to be detected (an exception is raised) or to trigger a different behavior. Typically, reads of uninitialized data or illegal accesses to memory that are not detected in the original program may result in errors when changing the compiler and/or the target.
- The original program has no error, but changing the compiler and/or target causes an error to appear, which may or not be detected. Typically, uses of low-level constructs like Unchecked\_Conversion which depend on the exact representation of values in bits may lead to errors when changing the compiler and/or the target. Some run-time errors like overflow errors or storage errors are also particularly sensitive to compiler and target changes.

To avoid portability issues, errors should be avoided by using suitable analyses and reviews in the context of the original and the new compiler and/or target. Whenever possible, these analyses and reviews should be automated by tools to guarantee that all possible errors of a given kind have been reported.

### Benefits of Using SPARK for Portability

The *Language Restrictions* in SPARK favor portability by excluding problematic language features (see *Excluded Ada Features*):

• By excluding side-effects in expressions, SPARK programs cannot suffer from effects occurring in different orders depending on the order of evaluation of expressions chosen by the compiler.

- By excluding aliasing, the behavior of SPARK programs does not depend on the parameter passing mechanism (by copy or by reference) or the order of assignment to out and in-out parameters passed by copy after the call, which are both chosen by the compiler.
- By excluding controlled types, SPARK programs cannot suffer from the presence and ordering of effects taking place as part of the initialization, assignment and finalization of controlled objects, which depend on choices made by the compiler.

As permitted by the SPARK language rules (see section 1.4.1 "Further Details on Formal Verification" of the SPARK Reference Manual), GNATprove rejects with an error programs which may implicitly raise a Program\_Error in parts of code that are in SPARK. For example, all static execution paths in a SPARK function should end with a return statement, a raise statement, or a pragma Assert (False). GNATprove's analysis can be further used to ensure that dynamic executions can only end in a return.

GNATprove reduces portability issues related to the use of fixed-point and floating-point values:

- GNATprove supports a subset of fixed-point types and operations that ensures that the result of an operation always belongs to the *perfect result set* as defined in Ada RM G.2.3. Note that the perfect result set still contains in general two values (the two model fixed-point values above and below the perfect mathematical result), which means that two compilers may give two different results for multiplication and division. Users should thus avoid multiplication and division of fixed-point values for maximal portability. See *Tool Limitations*.
- GNATprove assumes IEEE 754 standard semantics for basic operations of floating-point types (addition, subtraction, multiplication, division). With GNAT, this is achieved by using compilation switches "-msse2 mfpmath=sse". Users should still avoid elementary functions (exponential and trigonometric functions) for maximal portability. See Semantics of Floating Point Operations.

Additionally, GNATprove can detect all occurrences of specific portability issues in SPARK code (that is, parts of the program for which SPARK\_Mode=On is specified, see section on *Identifying SPARK Code*) when run in specific modes (see *Effect of Mode on Output* for a description of the different modes):

- In all modes (including mode check), when switch --pedantic is set, GNATprove issues a warning for every arithmetic operation which could be re-ordered by the compiler, thus leading to a possible overflow with one compiler and not another. For example, arithmetic operation A + B + C can be interpreted as (A + B) + C by one compiler, and A + (B + C) (after re-ordering) by another compiler. Note that GNAT always uses the former version without re-ordering. See *Parenthesized Arithmetic Operations*.
- In modes flow, prove and all, GNATprove issues high check messages on possible parameter aliasing, when such an aliasing may lead to interferences. This includes all cases where the choice of parameter passing mechanism in a compiler (by copy or by reference) might influence the behavior of the subprogram. See *Absence of Interferences*.
- In modes flow, prove and all, GNATprove issues check messages on possible reads of uninitialized data. These messages should be reviewed with respect to the stricter *Data Initialization Policy* in SPARK rather than in Ada. Hence, it is possible when the program does not conform to the stricter SPARK rules to manually validate them, see section *Justifying Check Messages*.
- In modes prove and all, GNATprove issues check messages on all possible run-time errors corresponding to raising exception Constraint\_Error at run time, all possible failures of assertions corresponding to raising exception Assert\_Error at run time, and all possible explicit raising of exceptions in the program.

The analysis of GNATprove can take into account characteristics of the target (size and alignment of standard scalar types, endianness) by specifying a *Target Parameterization*.

# How to Use SPARK for Portability

GNATprove's analysis may be used to enhance the portability of programs. Note that the guarantees provided by this analysis only hold for the source program. To ensure that these guarantees extend to the executable object code, one should independently provide assurance that the object code correctly implements the semantics of the source code.

# **Avoiding Non-Portable Features**

As much as possible, uses of non-portable language features should be avoided, or at least isolated in specific parts of the program to facilitate analyses and reviews when changing the compiler and/or the target.

This includes in particular language features that deal with machine addresses, data representations, interfacing with assembler code, and similar issues (for example, language attribute Size). When changing the compiler and/or the target, the program logic should be carefully reviewed for possible dependences on the original compiler behavior and/or original target characteristics. See also the section 18.4.5 "Target-specific aspects" of the GNAT Reference Manual.

In particular, features that bypass the type system of Ada for reinterpreting values (Unchecked\_Conversion) and memory locations (Address clause overlays, in which multiple objects are defined to share the same address, something that can also be achieved by sharing the same Link\_Name or External\_Name) have no impact on SPARK analysis, yet they may lead to portability issues.

By using the following restrictions (or a subset thereof), one can ensure that the corresponding non-portable features are not used in the program:

```
pragma No_Dependence (Ada.Unchecked_Conversion);
pragma No_Dependence (System.Machine_code);
```

Similarly, the program logic should be carefully reviewed for possible dependency on target characteristics (for example, the size of standard integer types). GNATprove's analysis may help here as it can take into account the characteristics of the target. Hence, proofs of functional properties with GNATprove ensure that these properties will always hold on the target.

In the specific case that the target is changing, it might be useful to run GNATprove's analysis on the program in proof mode, even if it cannot prove completely the absence of run-time errors and that the specified functional properties (if any) hold. Indeed, by running GNATprove twice, once with the original target and once with the new target, comparing the results obtained in both cases might point to parts of the code that are impacted by the change of target, which may require more detailed manual reviews.

Apart from non-portable language features and target characteristics, non-portability in SPARK may come from a small list of causes:

- Possible re-ordering of non-parenthesized arithmetic operations. These can be detected by running GNATprove (see *Benefits of Using SPARK for Portability*). Then, either these operations may not be re-ordered by the compiler (for example, GNAT ensures this property), or re-ordering may not lead to an intermediate overflow (for example, if the base type is large enough), or the user may introduce parentheses to prevent re-ordering.
- Possible aliasing between parameters (or parameters and global variables) of a call causing interferences. These can be detected by running GNATprove (see *Benefits of Using SPARK for Portability*). Then, either aliasing is not possible in reality, or aliasing may not cause different behaviors depending on the parameter passing mechanism chosen in the compiler, or the user may change the code to avoid aliasing. When SPARK subprograms are called from non-SPARK code (for example Ada or C code), manual reviews should be performed to ensure that these calls cannot introduce aliasing between parameters, or between parameters and global variables.
- Possible different choices of base type for user-defined integer types (contrary to derived types or subtypes, which inherit their base type from their parent type). GNATprove follows GNAT in choosing as base type the smallest multiple-words-size integer type that contains the type bounds (see *Base Type of User-Defined Integer Types* for more information).
- Issues related to errors. See section Avoiding Errors to Enhance Portability.
- Issues related to the use of fixed-point or floating-point operations. See section *Portability of Fixed-Point and Floating-Point Computations* below.

### **Avoiding Errors to Enhance Portability**

Because errors in a program make portability particularly challenging (see *Portability of Programs With Errors*), it is important to ensure that a program is error-free for portability. GNATprove's analysis can help by ensuring that the SPARK parts of a program are free from broad kinds of errors:

- all possible reads of uninitialized data
- all possible explicit raise of exceptions in the program
- all possible run-time errors except raising exception Storage\_Error, corresponding to raising exception Program Error, Constraint Error or Tasking Error at run time
- all possible failures of assertions corresponding to raising exception Assert\_Error at run time

When parts of the program are not in SPARK (for example, in Ada or C), the results of GNATprove's analysis depend on assumptions on the correct behavior of the non-SPARK code. For example, callers of a SPARK subprogram should only pass initialized input values, and non-SPARK subprograms called from SPARK code should respect their postcondition. See section *Managing Assumptions* for the complete list of assumptions.

In particular, when changing the target characteristics, GNATprove's analysis can be used to show that no possible overflow can occur as a result of changing the size of standard integer types.

GNATprove's analysis does not detect possible run-time errors corresponding to raising exception Storage\_Error at run time, which should be independently assessed. Because access types and dynamic allocation are forbidden in SPARK, the only possible cause for raising exception Storage\_Error in a SPARK program is overflowing the stack.

# Portability of Fixed-Point and Floating-Point Computations

Portability issues related to the use of fixed-point or floating-point operations can be avoided altogether by ensuring that the program does not use fixed-point or floating-point values, using:

```
pragma Restrictions (No_Fixed_Point);
pragma Restrictions (No_Floating_Point);
```

When fixed-point values are used, the value of the small and size in bits for the type should be specified explicitly, as documented in section 18.1 "Writing Portable Fixed-Point Declarations" of the GNAT Reference Manual:

```
My_Small : constant := 2.0**(-15);
My_First : constant := -1.0;
My_Last : constant := +1.0 - My_Small;

type F2 is delta My_Small range My_First .. My_Last;
for F2'Small use my_Small;
for F2'Size use 16;
```

The program should also avoid multiplication and division of fixed-point values to ensure that the result of arithmetic operations is exactly defined.

When floating-point values are used, use of IEEE 754 standard semantics for basic operations of floating-point types (addition, subtraction, multiplication, division) should be enforced. With GNAT, this is achieved by using compilation switches "-msse2 -mfpmath=sse".

The program should also avoid elementary functions (exponential and trigonometric functions), which can be ensured with a restriction:

```
pragma No_Dependence (Ada.Numerics);
```

If elementary functions are used, subject to reviews for ensuring portability, GNATprove's proof results may depend on the fact that elementary functions can be modeled as mathematical functions of their inputs that always return the same result when taking the same values in arguments. GNAT compiler was modified to ensure this property (see <a href="https://blog.adacore.com/how-our-compiler-learnt-from-our-analyzers">https://blog.adacore.com/how-our-compiler-learnt-from-our-analyzers</a>), which may not hold for other Ada compilers.

## 8.2 Project Scenarios

The workflow for using SPARK depends not only on the chosen *Objectives of Using SPARK*, but also on the context in which SPARK is used: Is it for a new development? Or an evolution of an existing codebase? Is the existing codebase in Ada or in a version of SPARK prior to SPARK 2014? We examine all these project scenarios in this section.

### 8.2.1 Maintenance and Evolution of Existing Ada Software

Although SPARK is a large subset of Ada, it contains a number of *Language Restrictions* which prevent in general direct application of GNATprove to an existing Ada codebase without any modifications. The suggested workflow is to:

- 1. Identify violations of SPARK restrictions.
- 2. For each violation, either rewrite the code in SPARK or mark it SPARK\_Mode => Off (see section on *Identifying SPARK Code*).
- 3. Perform the required analyses to achieve the desired objectives (see section on *Formal Verification with GNAT-prove*), a process which likely involved writing contracts (see in particular section on *How to Write Subprogram Contracts*).
- 4. Make sure that the assumptions made for formal verification are justified at the boundary between SPARK and full Ada code (see section on *Managing Assumptions*).

#### Identifying Violations of SPARK Restrictions

A simple way to identify violations of SPARK restrictions is by *Setting the Default SPARK\_Mode* to SPARK\_Mode => On, and then running GNATprove either in check mode (to report basic violations) or in flow mode (to report violations whose detection requires flow analysis).

If only a subset of the project files should be analyzed, one should create a project file for *Specifying Files To Analyze* or *Excluding Files From Analysis*.

Finally, one may prefer to work her way through the project one unit at a time by *Using SPARK\_Mode in Code*, and running GNATprove on the current unit only.

#### **Rewriting the Code in SPARK**

Depending on the violation, it may be more or less easy to rewrite the code in SPARK:

- Access types should in general be rewritten as private types of a package whose public part is marked SPARK\_Mode => Off. Thus, the body of that package cannot be analyzed by GNATprove, but clients of the package can be analyzed.
- Functions with side-effects should be rewritten as procedures, by adding an additional out parameter for the result of the function.

- Aliasing should be either explicitly signed off by *Justifying Check Messages* or removed by introducing a copy of the object to pass as argument to the call.
- Goto statements should be rewritten into regular control and looping structures when possible.
- Controlled types cannot be rewritten easily.
- Top-level exception handlers can be moved to a wrapper subprogram, which calls the subprogram without handlers and handles the exceptions which may be raised. The callee subprogram (and any callers) can thus be analyzed by GNATprove, while the body of the wrapper subprogram is marked SPARK\_Mode => Off. The same result can be obtained for exception handlers not at top-level by first refactoring the corresponding block into a subprogram.

#### Using SPARK Mode to Select or Exclude Code

Depending on the number and location of remaining violations, SPARK\_Mode can be used in different ways:

- If most of the codebase is in SPARK, Setting the Default SPARK\_Mode to SPARK\_Mode => On is best. Violations should be isolated in parts of the code marked SPARK\_Mode => Off by either Excluding Selected Unit Bodies or Excluding Selected Parts of a Unit.
- Otherwise, SPARK\_Mode => On should be applied selectively for *Verifying Selected Subprograms* or *Verifying Selected Units*. Violations are allowed outside the parts of the code marked SPARK\_Mode => On.
- Even when most of the code is in SPARK, it may be more cost effective to apply SPARK\_Mode => On selectively rather than by default. This is the case in particular when some units have non-SPARK declarations in the public part of their package spec (for example access type definitions). Rewriting the code of these units to isolate the non-SPARK declarations in a part that can be marked SPARK\_Mode => Off may be more costly than specifying no SPARK\_Mode for these units, which allows SPARK code elsewhere in the program to refer to the SPARK entities in these units.

When analyzing a unit for the first time, it may help to gradually mark the code SPARK\_Mode => On:

- 1. Start with the unit spec marked SPARK\_Mode => On and the unit body marked SPARK\_Mode => Off. First run GNATprove in flow mode, then in proof mode, until all errors are resolved (some unproved checks may remain, as errors and checks are different Categories of Messages).
- 2. Continue with the both the unit spec and body marked SPARK\_Mode => On. First run GNATprove in flow mode, then in proof mode, until all errors are resolved.
- 3. Now that GNATprove can analyze the unit without any errors, continue with whatever analysis is required to achieve the desired objectives.

### 8.2.2 New Developments in SPARK

In this scenario, a significant part of a software (possibly a module, possibly the whole software) is developed in SPARK. Typically, SPARK is used for the most critical parts of the software, with less critical parts programmed in Ada, C or Java (for example the graphical interface). A typical development process for this scenario might be:

- 1. Produce the high level (architectural) design in terms of package specifications. Determine which packages will be in SPARK, to be marked SPARK\_Mode => On.
- 2. Alternatively, if the majority of packages are to be SPARK, *Setting the Default SPARK\_Mode* to SPARK\_Mode => On is best. Those few units that are not SPARK should be marked SPARK\_Mode => Off.
- 3. Add *Package Contracts* to SPARK packages and, depending on the desired objectives, add relevant *Subprogram Contracts* to the subprograms declared in these packages. The package contracts should identify the key elements of *State Abstraction* which might also be referred to in *Data Dependencies* and *Flow Dependencies*.

- 4. Begin implementing the package bodies. One typical method of doing this is to use a process of top-down decomposition, starting with a top-level subprogram specification and implementing the body by breaking it down into further (nested) subprograms which are themselves specified but not yet implemented, and to iterate until a level is reached where it is appropriate to start writing executable code. However the exact process is not mandated and will depend on other factors such as the design methodology being employed. Provided unimplemented subprograms are stubbed (that is, they are given dummy bodies), GNATprove can be used at any point to analyze the program.
- 5. As each subprogram is implemented, GNATprove can be used (in mode flow or proof depending on the objectives) to verify it (against its contract, and/or to show absence of run-time errors).

### 8.2.3 Conversion of Existing SPARK Software to SPARK 2014

If an existing piece of software has been developed in a previous version of SPARK and is still undergoing active development/maintenance then it may be advantageous to upgrade to using SPARK 2014 in order to make use of the larger language subset and the new tools and environment. This requires more efforts than previous upgrades between versions of SPARK (SPARK 83, SPARK 95 and SPARK 2005) because the new version SPARK 2014 of SPARK is incompatible with those previous versions of the language. While the programming language itself in those previous versions of SPARK is a strict subset of SPARK 2014, the contracts and assertions in previous versions of SPARK are expressed as stylized comments that are ignored by GNATprove. Instead, those contracts and assertions should be expressed as executable Ada constructs, as presented in the *Overview of SPARK Language*.

The SPARK Language Reference Manual has an appendix containing a SPARK 2005 to SPARK 2014 Mapping Specification which can be used to guide the conversion process. Various options can be considered for the conversion process:

- 1. Only convert annotations into contracts and assertions, with minimal changes to the executable code Note that some changes to the code may be required when converting annotations, for example adding with-clauses in a unit to give visibility over entities used in contracts in this unit but defined in another units (which was performed in previous versions of SPARK with inherit annotations). This conversion should be relatively straightforward by following the mapping of features between the two languages.
  - The SPARK tools should be used to analyze the work in progress throughout the conversion process (which implies that a bottom-up approach may work best) and any errors corrected as they are found. This may also be an occasion to dramatically simplify annotations, as GNATprove requires far fewer of them. See the description of the conversion of SPARKSkein program in the section about *Examples in the Toolset Distribution*, for which a majority of the annotations are not needed anymore.

Once the conversion is complete, development and maintenance can continue in SPARK.

- 2. In addition to converting annotations, benefit from the larger language and more powerful tools to simplify code and contracts SPARK 2014 is far less constraining than previous versions of SPARK in terms of dependencies between units (which can form a graph instead of a tree), control structures (for example arbitrary return statements and exit statements are allowed), data structures (for example scalar types with dynamic bounds are allowed), expressions (for example local variables can be initialized with non-static expressions at declaration). In addition, useful new language constructs are available:
  - Contract Cases can be used to replace complex postconditions with implications.
  - *Predicates* can be used to state invariant properties of subtypes, so that they need not be repeated in preconditions, postconditions, loop invariants, etc.
  - Expression Functions can be used to replace simple query functions and their postcondition.
  - Ghost Code can be used to mark code only used for verification.
  - Loop Variants can be used to prove the termination of loops.

Changing the code to use these new features may favor readability and maintenance. These changes can be performed either while converting annotations, or as a second stage after all annotations have been converted (the case discussed above). Like in the previous case, the SPARK tools should be used to analyze the work in progress throughout the conversion process (which implies that a bottom-up approach may work best) and any errors corrected as they are found. Once the conversion is complete, development and maintenance can continue in SPARK.

3. Gradually convert annotations and code - It is possible to keep annotations in comments for the previous versions of SPARK while gradually adding contracts and assertions in SPARK 2014. The latest version of the SPARK 2005 toolset facilitates this gradual migration by ignoring SPARK pragmas. Thus, new contracts (for example *Preconditions* and *Postconditions*) should be expressed as pragmas rather than aspects in that case.

Typically, annotations and code would be converted when it needs to be changed. The granularity of how much code needs to be converted when a module is touched should be considered, and is likely to be at the level of the whole package.

The latest version of the SPARK 2005 toolset can be used to continue analyzing the parts of the program that do not use the new features of SPARK 2014, including units which have the two versions of contracts in parallel. GNATprove can be used to analyze parts of the program that have contracts in SPARK 2014 syntax, including units which have the two versions of contracts in parallel.

Note that some users may wish to take advantage of the new SPARK contracts and tools whilst retaining the more restrictive nature of SPARK 2005. (Many of the restrictions from SPARK 2005 have been lifted in SPARK because improvements in the tools mean that sound analysis can be performed without them, but some projects may need to operate in a more constrained environment.) This can be achieved using pragma Restrictions (SPARK\_05). For further details of this restriction please see the GNAT Reference Manual.

### 8.2.4 Analysis of Frozen Ada Software

In some very specific cases, users may be interested in the results of GNATprove's analysis on an unmodified code. This may be the case for example if the only objective is to *Ensure Portability of Programs* for existing Ada programs that cannot be modified (due to some certification or legal constraints).

In such a case, the suggested workflow is very similar to the one described for *Maintenance and Evolution of Existing Ada Software*, except the code cannot be rewritten when a violation of SPARK restrictions is encountered, and instead that part of the code should be marked SPARK\_Mode => Off. To minimize the parts of the code that need to be marked SPARK\_Mode => Off, it is in general preferable to apply SPARK\_Mode => On selectively rather than by default, so that units that have non-SPARK declarations in the public part of their package spec (for example access type definitions) need not be marked SPARK\_Mode => Off. See *Using SPARK\_Mode to Select or Exclude Code* for details.

### COMMAND LINE INVOCATION

#### GNAT prove is executed with the following command line:

```
Usage: gnatprove -Pproj [switches] [-cargs switches]
proj is a GNAT project file
-cargs switches are passed to gcc
All main units in proj are analyzed by default. Switches to change this:
-u [files]
                      Analyze only the given files
   [files]
                      Analyze given files and all dependencies
-11
                      Analyze all files (including unused) of all projects
gnatprove basic switches:
-aP=p
                      Add path p to project path
                      Output assumptions information
     --assumptions
     --codepeer=c
                      Enable or disable CodePeer analysis (c=on,off*)
                      Remove GNATprove intermediate files, and exit
     --clean
                      Include CWE ids in message output
     --cwe
 -f
                      Force recompilation/analysis of all units
 -h, --help
                      Display this usage information
    --info
                      Output info messages about the analysis
-j N
                      Use N parallel processes (default: 1; N=0 will use
                      all cores of the machine)
                      Do not stop analysis at the first error
     --level=n
                      Set the level of proof (0 = faster to 4 = more powerful)
    --list-categories Output a list of all message categories and exit
                      Minimal reanalysis
     --mode=m
                       Set the mode of GNATprove (m=check, check_all, flow,
                       prove, all*, stone, bronze, silver, gold)
     --no-subprojects Do not analyze subprojects, only the root project
     --output-msg-only Do not run any provers, output current flow and proof
                      results
 -q, --quiet
                      Be quiet/terse
     --replay
                      Replay proofs, do not attempt new proofs
                      Set the report mode of GNATprove (r=fail*, all,
    --report=r
                      provers, statistics)
    --subdirs=p
                      Create all artifacts in this subdir
-v, --verbose
                      Output extra verbose information
    --version
                      Output version of the tool and exit
    --warnings=w
                      Set the warning mode of GNATprove
                       (w=off, continue*, error)
 * Main mode values
   . check
                         - Fast partial check for SPARK violations
   . check_all, stone
                       - Full check for SPARK violations
```

```
. flow, bronze
                        - Prove correct initialization and data flow
  . prove
                        - Prove absence of run-time errors and contracts
  . all, silver, gold - Activates all modes (default)
* Report mode values
                 - Report failures to prove checks (default)
  . fail
  . all
                 - Report all results of proving checks
                - Same as all, plus prover usage information
  . provers
  . statistics — Same as provers, plus timing and steps information
* Warning mode values
  . off
                 - Do not issue warnings
  . continue
                 - Issue warnings and continue (default)
                  - Treat warnings as errors
  . error
gnatprove advanced switches:
--checks-as-errors Treat unproved check messages as errors
-d, --debug
               Debug mode
--debug-save-vcs Do not delete intermediate files for provers
--flow-debug Extra debugging for flow analysis (requires graphviz)
--limit-line=f:l Limit analysis to given file and line
--limit-line=f:l:c:k Limit analysis to given file, line, column and kind of
                     check
--limit-region=f:1:1 Limit analysis to given file and range of lines
                    Limit analysis to subprogram defined by file and line
--limit-subp=s
--memcached-server=host:portnumber
                     Specify a memcached instance that will be used for
                     caching of proof results.
--memlimit=nnn
                     Set the prover memory limit in MB. Use value 0 for
                     no limit (default when no level set)
                     Do not generate guards for axioms defining contracts of
--no-axiom-guard
                     functions
--no-counterexample Do not generate a counterexample for unproved formulas
--no-global-generation
                     Do not generate Global and Initializes contracts from
                     code, instead assume "null". Note that this option also
                     implies --no-inlining.
                     Do not inline calls to local subprograms for proof
--no-inlining
--no-loop-unrolling Do not unroll loops with static bounds and no
                     (in) variant for proof
                     Add a header with extra information in the generated
--output-header
                     output file
                     Use a strict interpretation of the Ada standard
--pedantic
                    Issue warnings by proof
--proof-warnings
                     Set the proof modes for generation of formulas
--proof=g[:1]
                     (g=per_check*, per_path, progressive) (l=lazy*, all)
--prover=s[,s]*
                     Use given provers (s=altergo, cvc4*, z3, ...)
                     Specify the Ada runtime name/location
--RTS=dir
--steps=nnn
                     Set the maximum number of proof steps (prover-specific)
                     Use value 0 for no steps limit.
                     Set the prover timeout in seconds. Use value 0 for
--timeout=nnn
                     no timeout (default when no level set)
--why3-conf=f
                     Specify a configuration file for why3
* Proof mode values for generation
  . per_check - Generate one formula per check (default when no level set)
  . per_path
                  - Generate one formula per path for each check
  . progressive - Start with one formula per check, then split into
```

```
paths when needed
* Proof mode values for laziness
             - Stop at first unproved formula for each check
 . lazy
                  (most suited for fully automatic proof) (default)
 . all
                 - Attempt to prove all formulas
                  (most suited for combination of automatic and manual proof)
* Prover name values
 (Default prover is cvc4.)
 (Provers marked with [steps] support the --steps switch.)
 . altergo - [steps] Use Alt-Ergo
                - [steps] Use CVC4
 . cvc4
                - [steps] Use Z3
 . z3
```

- Any other prover configured in your .why3.conf file

. . . .

**APPENDIX** 

В

### **ALTERNATIVE PROVERS**

### **B.1 Installed with SPARK Pro**

The provers Alt-Ergo, CVC4 and Z3 are installed with the SPARK tool. By default, GNATprove uses prover CVC4 only. Switch <code>--level</code> changes the default to use one or more provers depending on the chosen level (see *Running GNATprove from the Command Line*). Switch <code>--prover</code> allows to use another prover, or a list of provers. Prover names <code>altergo</code>, <code>cvc4</code> and <code>z3</code> are used to refer to the versions of provers Alt-Ergo, CVC4 and Z3 that are installed with the SPARK toolset. The string <code>alt-ergo</code> can also be used to refer to Alt-Ergo. More information on Alt-Ergo, CVC4 and Z3 can be found on their respective websites:

- Alt-Ergo: https://alt-ergo.ocamlpro.com
- CVC4: http://cvc4.cs.stanford.edu/web/
- Z3: https://github.com/Z3Prover/z3

## **B.2 Installed with SPARK Discovery**

In this case, only prover Alt-Ergo is installed with the SPARK tool. Hence, by default GNATprove only uses prover Alt-Ergo. In particular, switch --level has no impact on the use of different provers.

## **B.3 Installed with SPARK Community**

The provers Alt-Ergo, CVC4 and Z3 are installed with the SPARK tool.

### **B.4 Other Automatic or Manual Provers**

### **B.4.1 Updating the Why3 Configuration File**

GNATprove can call other provers, as long as they are supported by the Why3 platform (see complete list on Why3 webpage). To use another prover, it must be listed in your Why3 configuration file.

To create or update automatically a Why3 configuration file, call the command spark2014-install>/
libexec/spark/bin/why3config --detect-provers. It searches your PATH for any supported provers
and adds them to the default configuration file .why3.conf in your HOME, or a configuration file given in argument
with switch -C <file>. This file consists of a few general settings and a section for each prover which is supported.

GNATprove reads the default configuration file .why3.conf in your HOME, or the configuration file given in argument with switch --why3-conf=<file>. Any prover name configured in this configuration file can be used as an argument to switch --prover.

Note that using this mechanism, you cannot replace the definitions provided with the SPARK tools for the provers altergo, cvc4 and z3.

If more than one prover is specified, the provers are tried in order on each VC, until one of them succeeds or all fail. Interactive provers cannot be combined with other provers, so must appear on their own.

### **B.4.2 Sharing Libraries of Theorems**

When GNATprove is used with a manual prover, the user can provide libraries of theorems to use during the proof process.

To do so, the user will need to set a proof directory (see *Project Attributes* for more details on this directory). The user needs to create a folder with the same name as the chosen manual prover (the casing of the name is the same as the one passed to the switch --prover) and put the library sources inside this folder.

Finally, some additional fields need to be added to the prover configuration in the Why3 configuration file (a basic example of prover configuration can be found in the section on *Coq*):

- configure\_build: this field allows you to specify a command to configure the compilation of the library of theorems. This command will be called each time a source file is added to the library.
- build\_commands: this field allows you to specify a set of command which will be called sequentially to build your library. These commands will be called each time GNATprove runs the corresponding manual prover. (In order to define multiple commands for this field, just set the field multiple times with different values, each time the field is set it adds a new element to the set of build commands).

Inside these commands, pattern %f refers to the name of the library file considered, and %o to the name of the main gnatprove repository generated by GNATprove. This allows referring to the path of the compiled library of theorems inside these commands with %o/user/cprover\_name>.

## B.5 Coq

gnatprove has support for the Coq interactive prover, even though Coq is not part of the SPARK distribution. If you want to use Coq with SPARK, you need to install it yourself on your system and put it in your PATH environment variable. Then, you can simply provide --prover=coq to gnatprove. Note that the only supported version currently is Coq 8.5.

### PROJECT ATTRIBUTES

GNATprove reads the package Prove in the given project file. This package is allowed to contain the following attributes:

- Proof\_Switches, which defines additional command line switches that are used for the invokation of GNAT-prove. This attribute can be used in two different settings:
  - to define switches that should apply to all files in the project. As an example, the following package in the project file sets the default report mode of GNATprove to all:

```
package Prove is
   for Proof_Switches ("Ada") use ("--report=all");
end Prove;
```

- to define switches that should apply only to one file. The following example sets timeout for provers run by GNATprove to 10 seconds for file.adb:

```
package Prove is
   for Proof_Switches ("file.adb") use ("--timeout=10");
end Prove;
```

Switches given on the command line have priority over switches given in the project file, and file-specific switches have priority over switches that apply to all files. A special case is the --level switch: the values for --timeout etc implied by the --level switch are always overridden by more specific switches, regardless of where they appear. For example, the timeout for the analysis of file.adb is set to 10 seconds below, despite the --level=0 switch (which implies a lower timeout) specified for this file:

```
package Prove is
   for Proof_Switches ("Ada") use ("--timeout=10");
   for Proof_Switches ("file.adb") use ("--level=0");
end Prove;
```

The following switches cannot be used inside project files: -P, -aP, --subdirs, --clean, --list-categories, --version.

Only the following switches are allowed for file-specific switches: --steps, --timeout, --memlimit, --proof, --prover, --level, --no-counterexample, --no-inlining, --no-loop-unrolling.

- Switches. This deprecated attribute is the same as Proof Switches ("Ada").
- Proof\_Dir, which defines the directory where are stored the files concerning the state of the proof of a project. This directory contains a sub-directory sessions with one directory per source package analyzed for proof. Each of these package directories contains a Why3 session file. If a manual prover is used to prove some VCs, then a sub-directory called by the name of the prover is created next to sessions, with the same organization

of sub-directories. Each of these package directories contains manual proof files. Common proof files to be used across various proofs can be stored at the toplevel of the prover-specific directory.

**APPENDIX** 

D

### **IMPLEMENTATION DEFINED PRAGMAS**

### D.1 Pragma SPARK\_Mode

SPARK\_Mode is a three-valued aspect. At least until we get to the next paragraph, a SPARK\_Mode of On, Off, or Auto is associated with each Ada construct. Roughly, the meaning of the three values is the following:

- a value of On means that the construct is required to be in SPARK, and the construct will be analyzed by GNATprove.
- a value of Off means that the construct will not be analyzed by GNATprove, and does not need to obey the SPARK restrictions. The construct also cannot be referenced from other parts that are required to be in SPARK.
- a value of Auto means that the construct will not be analyzed, and GNATprove will infer whether this construct can be used in other SPARK parts or not.

We now explain in more detail how the SPARK\_Mode pragma works.

Some Ada constructs are said to have more than one "section". For example, a declaration which requires a completion will have (at least) two sections: the initial declaration and the completion. The SPARK\_Modes of the different sections of one entity may differ. In other words, SPARK\_Mode is not an aspect of an entity but rather of a section of an entity.

For example, if a subprogram declaration has a SPARK\_Mode of On while its body has a SPARK\_Mode of Off, then an error would be generated if the subprogram took a parameter of an access type but not if the subprogram declared a local variable of an access type (recall that access types are not in SPARK).

A package is defined to have 4 sections: its visible part, its private part, its body declarations, and its body statements. A protected or task unit has 3 sections: its visible part, its private part, and its body. Other declarations which require a completion have two sections, as noted above; all other entities and constructs have only one section.

If the SPARK\_Mode of a section of an entity is Off, then the SPARK\_Mode of a later section of that entity shall not be On. [For example, a subprogram can have a SPARK declaration and a non-SPARK body, but not vice versa.]

If the SPARK\_Mode of a section of an entity is Auto, then the SPARK\_Mode of a later section of that entity shall not be On or Off.

The SPARK\_Mode aspect can be specified either via a pragma or via an aspect\_specification. In some contexts, only a pragma can be used because of syntactic limitations. In those contexts where an aspect\_specification can be used, it has the same effect as a corresponding pragma.

The form of a pragma SPARK Mode is as follows:

pragma SPARK\_Mode [ (On | Off) ]

The form for the aspect\_definition of a SPARK\_Mode aspect\_specification is as follows:

```
[ On | Off ]
```

#### For example:

```
package P
  with SPARK_Mode => On
is
```

The pragma can be used as a configuration pragma. The effect of such a configuration pragma is described below in the rules for determining the SPARK\_Mode aspect value for an arbitrary section of an arbitrary Ada entity or construct.

Pragma SPARK\_Mode shall be used as a local pragma in only the following contexts and has the described semantics:

Pragma placement	Affected	Alternative
	construct	aspect form
Start of the visible declarations (preceded only by other pragmas) of a package	Visible part	As part of the
declaration	of the	pack-
	package	age_specification
Start of the visible declarations (preceded only by other pragmas) of a task or	Visible part	As part of the
protected unit	of the unit	declaration
Start of the private declarations of a package, a protected unit, or a task unit (only	Private part	None
other pragmas can appear between the private keyword and the SPARK_Mode		
pragma)		
Immediately at the start of the declarations of a package body (preceded only by	Body dec-	As part of the
other pragmas)	larations of	pack-
	the package	age_body
Start of the elaboration statements of a package body (only other pragmas can	Body	None
appear between the begin keyword and the SPARK_Mode pragma)	statements	
	of the	
	package	
Start of the declarations of a protected or task body (preceded only by other	Body	As part of the
pragmas)		protected or
		task body
After a subprogram declaration (with only other pragmas intervening). [This does	Subpro-	As part of the
not include the case of a subprogram whose initial declaration is via a	gram's	subpro-
subprogram_body_stub. Such a subprogram has only one section because a	specifica-	gram_declaration
subunit is not a completion.]	tion	
Start of the declarations of a subprogram body (preceded only by other pragmas)	Subpro-	As part of the
	gram's	subpro-
	body	gram_body

A default argument of On is assumed for any SPARK\_Mode pragma or aspect\_specification for which no argument is explicitly specified.

A SPARK\_Mode of Auto cannot be explicitly specified; the cases in which a SPARK\_Mode of Auto is implicitly specified are described below. Roughly speaking, Auto indicates that it is left up to the formal verification tools to determine whether or not a given construct is in SPARK.

A SPARK\_Mode pragma or aspect specification shall only apply to a (section of a) package, generic package, subprogram, or generic subprogram.

A SPARK\_Mode of On shall only apply to a (section of a) library-level entity, except for the case of SPARK\_Mode specifications occurring within generic instances. A SPARK\_Mode of On applying to a non-library-level entity within a generic instance has no effect.

The SPARK\_Mode aspect value of an arbitrary section of an arbitrary Ada entity or construct is then defined to be the following value (except if this yields a result of Auto for a non-package; see below):

- If SPARK\_Mode has been specified for the given section of the given entity or construct, then the specified value;
- else for the private part of a public child unit whose parent unit's private part has a SPARK\_Mode of Off, the SPARK\_Mode is Off;
- else for the private part of a package or a protected or task unit, the SPARK\_Mode of the visible part;
- else for a package body's statements, the SPARK\_Mode of the package body's declarations;
- else for the first section (in the case of a package, the visible part) of a public child unit, the SPARK\_Mode of the visible part of the parent unit;
- else for the first section (in the case of a package, the visible part) of a private child unit, the SPARK\_Mode of the private part of the parent unit;
- else for any of the visible part or body declarations of a library unit package or either section of a library unit subprogram, if there is an applicable SPARK\_Mode configuration pragma then the value specified by the pragma; if no such configuration pragma applies, then an implicit specification of Auto is assumed;
- else the SPARK\_Mode of the enclosing section of the nearest enclosing package or subprogram;
- Corner cases: the SPARK\_Mode of the visible declarations of the limited view of a package is always Auto; the SPARK\_Mode of any section of a generic library unit is On. [Recall that any generic unit is in SPARK.]

If the above computation yields a result of Auto for any construct other than one of the four sections of a package, then a result of On or Off is determined instead based on the legality (with respect to the rules of SPARK) of the construct. The construct's SPARK\_Mode is On if and only if the construct is in SPARK. [A SPARK\_Mode of Auto is therefore only possible for (sections of) a package.]

In code where SPARK\_Mode is On (also called "SPARK code"), the rules of SPARK are enforced. In particular, such code shall not reference non-SPARK entities, although such code may reference a SPARK declaration with one or more non-SPARK subsequent sections (e.g., a package whose visible part has a SPARK\_Mode of On but whose private part has a SPARK\_Mode of Off; a package whose visible part has a SPARK\_Mode of Auto may also be referenced).

Code where SPARK\_Mode is Off shall not enclose code where Spark\_Mode is On. However, if an instance of a generic unit is enclosed by code where SPARK\_Mode is Off and if any SPARK\_Mode specifications occur within the generic unit, then the corresponding SPARK\_Mode specifications occurring within the instance have no semantic effect. [In particular, such an ignored SPARK\_Mode specification could not violate the preceding "Off shall not enclose On" rule because the SPARK\_Mode of the entire instance is Off. Similarly, such an ignored SPARK\_Mode specification could not violate the preceding rule that a SPARK\_Mode specification shall only apply to a (section of a) library-level entity.]

For purposes of the "Off shall not enclose On" rule just described, the initial section of a child unit is considered to occur immediately within either the visible part (for a public child unit) or the private part (for a private child unit) of the parent unit. In addition, the private part of a public child package is considered to occur immediately within the private part of the parent unit. [This follows Ada's visibility rules for child units. This means, for example, that if a parent unit's private part has a SPARK\_Mode of Off, then the private part of a public child package shall not have a SPARK\_Node of On. Note also that a SPARK\_Mode configuration pragma which applies only to the specification (not the body) of a child unit is always ineffective; this is a consequence of the rules given above for determining the SPARK\_Mode of the first section of a child unit.]

The rules for a protected unit follow from the rules given for other constructs after notionally rewriting the protected unit as a package.

A protected unit declaration such as

```
protected type Prot
  with SPARK_Mode => On
is
```

```
procedure Op1 (X : in out Integer);
procedure Op2;
procedure Non_SPARK_Profile (Ptr : access Integer)
    with SPARK_Mode => Off;
private
    Aaa, Bbb : Integer := 0;
end Prot;
```

can be thought of, for purposes of SPARK\_Mode rules, as being a lot like

```
package Pkg
  with SPARK_Mode => On
is
  type Prot is limited private;
  procedure Op1 (Obj : in out Prot; X : in out Integer);
  procedure Op2 (Obj : in out Prot);
  procedure Non_SPARK_Profile (Obj : in out Prot; Ptr : access Integer)
    with SPARK_Mode => Off;
private
  type Prot is
  limited record
    Aaa, Bbb : Integer := 0;
  end record;
end Pkg;
```

which is legal. The point is that a protected type which is in SPARK can have protected operation whose declaration is not in SPARK.

SPARK\_Mode is an implementation-defined Ada aspect; it is not (strictly speaking) part of the SPARK language. It is used to notionally transform programs which would otherwise not be in SPARK so that they can be viewed (at least in part) as SPARK programs.

Note that if you would like to mark all your code in SPARK\_Mode, the simplest solution is to specify in your project file:

```
package Builder is
   for Global_Configuration_Pragmas use "spark.adc";
end Builder;
```

and provide a file spark.adc which contains:

```
pragma SPARK_Mode;
```

**APPENDIX** 

E

### EXTERNAL AXIOMATIZATIONS

### E.1 What is it?

It is a feature of the SPARK toolset that allows to manually supply a WhyMl translation for the public specification of a library level package that is in SPARK. This feature is still experimental.

## E.2 Why is it useful?

- For features that cannot easily be described using contracts, like transitivity, counting, or summation
- To link functions to the logic world, like trigonometry functions

### E.3 How does it work?

• To say that a library package has an external axiomatization, we annotate it using:

```
pragma Annotate (GNATprove, External_Axiomatization);
```

- These packages should have SPARK\_Mode On on their public specification and SPARK\_Mode Off on their private part.
- The WhyMl translation for the package should be stored in a subdirectory named \_theories of the proof directory specified for the project.

### E.4 What should the translation look like?

- For each publicly visible entity E in the package P, it should provide the same elements (types as well as logic and program functions) as the automatic translation, all grouped in one single module named P\_e. For example, the module for a function F should provide both a logic function declaration named f\_logic and a program function declaration named f.
- For most types, a model module in defined in ada\_\_model.mlw that can be cloned to get most of the required declarations.
- The manual translation may use any type, constant and function that is visible from the Ada package declaration.
- A good way to start an axiomatization file on a package is to launch the toolset on it and copy paste the modules
  created for each entity of the package. A WhyMl file created by the tool on a package P contains a module for
  every declaration visible from it, only declarations from P itself should be copied. The generated file usually

contains two modules for each entity, one named P\_e and one named P\_e\_axiom. Both should be put together in P\_e for the manual translation. The toolset will replace statically known expressions with their value. Beware that they might be architecture dependent.

### E.5 Example

For example, let us consider the following package, stored in a file sum.ads, providing a summation function for slices of arrays of integers:

```
package Sums with SPARK_Mode is
      pragma Annotate (GNATprove, External_Axiomatization);
2
      subtype Extended_Index is Integer range 0 .. 2 ** 16;
4
      subtype Index is Integer range 1 .. Extended_Index'Last;
6
7
      subtype Vector_Element is
        Integer range Integer'First / Index'Last .. Integer'Last / Index'Last;
8
      type Vector is array (Index range <>) of Vector_Element;
10
11
      type Slice_Bounds is
12
         record
13
            Lo : Index;
14
            Hi : Extended_Index;
15
         end record;
16
17
      function Sum (X : Vector; Bounds : Slice_Bounds) return Integer with
18
        Pre => (Bounds.Lo > Bounds.Hi) or else
19
        (X'First <= Bounds.Lo and Bounds.Hi <= X'Last);
20
21
   end Sums;
```

We can provide the following Why3 translation for it, that we should store in a file named sum.mlw:

```
module Sums__extended_index
use import "_gnatprove_standard".Main
           "_gnatprove_standard".Integer
use import "int".Int
type extended_index
function first : int = 0
function last : int = 65536
predicate in_range (x : int) = first <= x / x <= last
(* Clone of the model module for discrete types with static bounds \star)
clone export "ada__model".Static_Discrete with
type t = extended_index,
function first = first,
function last = last,
predicate in_range = in_range
(* Type for mutable variables of type extended_index *)
type extended_index__ref = { mutable extended_index__content : extended_index }
```

```
val extended index havoc (x : extended index ref) : unit
  writes { x }
 (* All values of type extended_index are in range *)
predicate dynamic_invariant (expr : int) bool bool =
  dynamic_property first last expr
(* We know nothing for default initialization of variables of type
   extended_index *)
predicate default_initial_assumption int bool = true
end
module Sums__extended_index__rep
use import Sums__extended_index
use import "_gnatprove_standard".Main
(* Projection functions from extended_index to int *)
clone export "ada__model".Rep_Proj_Int with
  type t = extended_index,
  predicate in_range = in_range
end
module Sums__index
use import "_gnatprove_standard".Main
use "_gnatprove_standard".Integer
use import "int". Int
type index
function first : int = 1
function last : int = 65536
predicate in_range (x : int) = first <= x /\ x <= last</pre>
 (* Clone of the model module for discrete types with static bounds *)
clone export "ada__model".Static_Discrete with
type t = index,
function first = first,
 function last = last,
predicate in_range = in_range
(* Type for mutable variables of type index *)
type index__ref = { mutable index__content : index }
val index__havoc (x : index__ref) : unit
  writes { x }
(* All values of type index are in range *)
predicate dynamic_invariant (expr : int) bool bool =
  dynamic_property first last expr
(* We know nothing for default initialization of variables of type index *)
predicate default_initial_assumption int bool = true
end
module Sums__index__rep
use import Sums__index
```

```
use import "_gnatprove_standard".Main
 (* Projection functions from index to int *)
clone export "ada__model".Rep_Proj_Int with
  type t = index,
  predicate in_range = in_range
end
module Sums__vector_element
use import "_qnatprove_standard".Main
            \verb"\_gnatprove\_standard".Int\_Division
use import Standard__integer
use import "int". Int
type vector_element
function first : int = Int_Division.div Standard__integer.first 65536
function last : int = Int_Division.div Standard__integer.last 65536
predicate in_range (x : int) = first <= x /\ x <= last</pre>
 (* Clone of the model module for discrete types with static bounds *)
clone export "ada__model".Static_Discrete with
type t = vector_element,
 function first = first,
 function last = last,
predicate in_range = in_range
(* Type for mutable variables of type vector_element *)
type vector_element__ref = { mutable vector_element__content : vector_element }
val vector_element__havoc (x : vector_element__ref) : unit
  writes { x }
end
module Sums__vector_element__rep
use import Sums__vector_element
use import "_gnatprove_standard".Main
(* Projection functions from vector_element to int *)
clone export "ada__model".Rep_Proj_Int with
  type t = vector_element,
  predicate in_range = in_range
end
(* Module for any array type ranging over signed integer types and
  containing vector_element *)
module Array__Int__Sums__vector_element
use import "_gnatprove_standard".Main
use import "int".Int
use
            Sums__vector_element
           Sums__vector_element__rep
function one : int = 1
type component_type = Sums__vector_element.vector_element
```

```
(* Clone of the model module for logical arrays containing vector_element
    and indexed by mathematical integers *)
 clone export "_gnatprove_standard".Array__1 with
type I1.t = int,
predicate I1.le = Int.(<=),</pre>
predicate I1.lt = Int.(<),</pre>
predicate I1.gt = Int.(>),
function I1.add = Int.(+),
function I1.sub = Int.(-),
 function I1.one = one,
type component_type = component_type
 (* Primitive equality between arrays *)
 function bool_eq (a:map) (af:int) (al:int) (b:map) (bf:int) (bl:int) : bool =
   (if af <= al
        then al - af = bl - bf
        else bf > bl) / \setminus
         (forall idx : int. af <= idx <= al ->
             (get a idx) = (get b (bf - af + idx)))
 (* Clone of the model module for comparison of arrays *)
clone export "ada__model".Array_Int_Rep_Comparison_Axiom with
type component_type = component_type,
function to_rep = Sums__vector_element__rep.to_rep,
type map = map,
type Index.t = int,
predicate Index.le = Int.(<=),</pre>
predicate Index.lt = Int.(<),</pre>
predicate Index.gt = Int.(>),
 function Index.add = Int.(+),
function Index.sub = Int.(-),
function Index.one = one,
function get = get,
function bool_eq = bool_eq
end
module Sums__vector
use import "int". Int
use import "_gnatprove_standard".Main
            "_gnatprove_standard".Integer
use
use import Standard__integer
use import Sums__index
use import Sums__vector_element
use
            Array__Int__Sums__vector_element
use
            Standard__integer__rep
            Sums__vector_element__rep
use
predicate index_dynamic_property (first : int) (last : int) (x : int) =
      first <= x / \ x <= last
 (* Clone of the model module for unconstrained arrays *)
 type component_type
  Sums__vector_element.vector_element
 function id (x : int) : int = x
 (* Clone of the model module for unconstrained arrays *)
```

```
clone export "ada__model". Unconstr_Array with
type map = Array__Int__Sums__vector_element.map,
 function array_bool_eq = Array__Int__Sums__vector_element.bool_eq,
type index_base_type = Standard__integer.integer,
type index_rep_type = int,
function to_rep = Standard__integer__rep.to_rep,
function rep_to_int = id,
predicate in_range_base = Standard__integer.in_range,
predicate index_dynamic_property = index_dynamic_property,
predicate index_rep_le = Int.(<=)</pre>
type vector = __t
 (* Type for mutable variables of type vector *)
type vector__ref = { mutable vector__content : vector }
val vector__havoc (x : vector__ref) : unit
  writes { x }
 (* Helper function *)
function _get "inline" (v : vector) (i : int) : int =
            Sums__vector_element__rep.to_rep (Array__Int__Sums__vector_element.get,,
(* If vectors are not empty, their bounds are between Index.first and
   Index.last *)
predicate dynamic_invariant (expr : vector) bool (skip_bounds : bool) bool =
  (if skip_bounds then true
  else dynamic_property Sums__index.first Sums__index.last
         (first expr) (last expr))
end
module Sums__slice_bounds
use import "int". Int
use import "_gnatprove_standard".Main
           "_gnatprove_standard".Integer
use import Sums__index
           Sums__index__rep
use
use import Sums__extended_index
           Sums__extended_index__rep
(* Fields for record type *)
type __split_fields =
 { rec__sums__slice_bounds__lo : index; rec__sums__slice_bounds__hi : extended_index_
←}
type __split_fields__ref = { mutable __split_fields__content : __split_fields }
val __split_fields__havoc (x : __split_fields__ref) : unit
  writes { x }
(* Record type *)
type slice_bounds =
 { __split_fields : __split_fields }
 (* Type for mutable variables of type slice_bounds *)
 type slice_bounds__ref = { mutable slice_bounds__content : slice_bounds }
val slice_bounds__havoc (x : slice_bounds__ref) : unit
  writes { x }
```

```
(* Helper function *)
function _rec__lo "inline" (b : slice_bounds) : int =
             Sums__index__rep.to_rep (rec__sums__slice_bounds__lo (__split_fields_
\hookrightarrow (b)))
(* Helper function *)
function _rec__hi "inline" (b : slice_bounds) : int =
             Sums_extended_index_rep.to_rep (rec_sums_slice_bounds_hi (_split_
\hookrightarrow fields (b)))
 (* Condition to be allowed to access Lo *)
predicate sums__slice_bounds__lo__pred (a : slice_bounds) =
 true
val rec__sums__slice_bounds__lo_
  (a : slice_bounds) :Sums__index.index
 requires { sums__slice_bounds__lo__pred a }
 ensures { result = a.__split_fields.rec__sums__slice_bounds__lo }
 (* Condition to be allowed to access Hi *)
predicate sums__slice_bounds__hi__pred (a : slice_bounds) =
 true
val rec__sums__slice_bounds__hi_
  (a : slice_bounds) :Sums__extended_index.extended_index
 requires { sums__slice_bounds__hi__pred a }
 ensures { result = a.__split_fields.rec__sums__slice_bounds__hi }
 (* Equality function over slice_bounds *)
 function bool_eq (a : slice_bounds) (b : slice_bounds) : bool =
 _rec__lo a = _rec__lo b /\ _rec__hi a = _rec__hi b
function dummy : slice_bounds
 (* No particular property applies to all values of types slice_bounds *)
predicate dynamic_invariant slice_bounds bool bool = true
 (* We know nothing for default initialization of variables of slice_bounds *)
predicate default_initial_assumption slice_bounds bool = true
end
module Sums__sum
use import "int".Int
use import "_gnatprove_standard".Main
            "_gnatprove_standard".Integer
            "_gnatprove_standard".Array__1
use
use import Sums__slice_bounds
use import Sums__index
           Sums__index__rep
use
use import Standard__integer
use import Sums__extended_index
           Sums__extended_index__rep
use import Sums__vector
(* Logic complete function for sum *)
 function sum__logic
```

```
(x : vector) (bounds : slice_bounds) :int
(* Helper function *)
function _sum "inline" (x : vector) (bounds : slice_bounds) :int =
            sum__logic x bounds
(* Axiom for defining the sum function *)
axiom sum_def:
   forall v : vector, b : slice_bounds
     [sum_logic v b].
     Standard__integer.in_range (sum__logic v b) /\
     (* Case of the empty slice *)
     (_rec__lo b > _rec__hi b -> _sum v b = 0) /\
     (* Case of a non-empty slice *)
     (first v <= _rec__lo b <= _rec__hi b <= last v ->
         (* If the slice only contains one element *)
        (_rec__lo b = _rec__hi b -> _sum v b = _get v (_rec__lo b)) /\
        (* Link to smaller slices of the same vector *)
        (forall b1 : slice_bounds [sum__logic v b1].
             (* Ending at the same index *)
             ((_rec__hi b1 = _rec__hi b /\ _rec__lo b < _rec__lo b1 <= _rec__hi b) ->
             let b2 = {__split_fields =
                              {rec__sums__slice_bounds__lo = rec__sums__slice_bounds__
→_lo (__split_fields b);
                         rec__sums__slice_bounds__hi = Sums__extended_index__rep.of_
\rightarrowrep ((_rec__lo b1) - 1)}} in
                _sum v b = _sum v b1 + _sum v b2) / 
             (* Sartind at the same index *)
             ((_rec__lo b1 = _rec__lo b /\ _rec__lo b <= _rec__hi b1 < _rec__hi b) ->
             let b2 = {__split_fields =
                              {rec_sums_slice_bounds_lo = Sums_index_rep.of_rep_
\rightarrow ((_rec_hi b1) + 1);
                         rec__sums__slice_bounds__hi = rec__sums__slice_bounds__hi (_
→_split_fields b) }} in
                _sum v b = _sum v b1 + _sum v b2)))
(* Program partial function with a precondition for sum *)
val sum (x : vector) (bounds : slice_bounds) :int
 requires { _rec__lo bounds > _rec__hi bounds \/
            first x \le _rec_lo bounds / _rec_hi bounds <= last x }
 ensures { result = sum_logic x bounds }
```

**APPENDIX** 

F

### **USES OF PRAGMA ANNOTATE GNATPROVE**

This appendix lists all the uses of pragma Annotate for GNAT prove. Pragma Annotate can also be used to control other AdaCore tools. The uses of this pragma are explained in the User's guide of each tool.

The main usage of pragmas Annotate for GNAT prove is for justifying check messages using *Direct Justification with Pragma Annotate*. Specific versions of this pragma can also be used to influence the generation of proof obligations. Some of these uses can be seen in *SPARK Libraries* for example. These forms of pragma Annotate should be used with care as they can introduce additional assumptions which are not verified by the GNAT prove tool.

## F.1 Using Pragma Annotate to Justify Check Messages

You can use annotations of the form

to justify an unproved check message that cannot be proved by other means. See the section *Direct Justification with Pragma Annotate* for more details about this use of pragma Annotate.

# F.2 Using pragma Annotate to force Proof of Termination

SPARK doesn't usually prove termination of subprograms. You can instruct it do so using annotations of this form:

```
pragma Annotate (GNATprove, Terminating, Subp_Or_Package_Entity);
```

See the section Subprogram Termination about details of this use of pragma Annotate.

## F.3 Customize Quantification over Types with the Iterable Aspect

In SPARK, it is possible to allow quantification over any container type using the Iterable aspect. This aspect provides the primitives of a container type that will be used to iterate over its content. For example, if we write:

where

```
function First (S : Set) return Cursor;
function Has_Element (S : Set; C : Cursor) return Boolean;
function Next (S : Set; C : Cursor) return Cursor;
```

then quantification over containers can be done using the type Cursor. For example, we could state:

```
(for all C in S => P (Element (S, C)))
```

to say that S only contains elements for which a property P holds. For execution, this expression is translated as a loop using the provided First, Has\_Element, and Next primitives. For proof, it is translated as a logic quantification over every element of type Cursor. To restrict the property to cursors that are actually valid in the container, the provided function Has\_Element is used. For example, the property stated above becomes:

```
(for all C : Cursor => (if Has_Element (S, C) then P (Element (S, C)))
```

Like for the standard Ada iteration mechanism, it is possible to allow quantification directly over the elements of the container by providing in addition an Element primitive to the Iterable aspect. For example, if we write:

where

```
function Element (S : Set; C : Cursor) return Element_Type;
```

then quantification over containers can be done directly on its elements. For example, we could rewrite the above property into:

```
(for all E of S \Rightarrow P (E))
```

For execution, quantification over elements of a container is translated as a loop over its cursors. In the same way, for proof, quantification over elements of a container is no more than syntactic sugar for quantification over its cursors. For example, the above property is translated using quantification over cursors:

```
(for all C : Cursor => (if Has_Element (S, C) then P (Element (S, C)))
```

Depending on the application, this translation may be too low-level and introduce an unnecessary burden on the automatic provers. As an example, let us consider a package for functional sets:

Sets contain elements of type Element\_Type. The most basic operation on sets is membership test, here provided by the Mem subprogram. Every other operation, such as intersection here, is then specified in terms of members. Iteration primitives First, Next, Has\_Element, and Element, that take elements of a private type Cursor as an argument, are only provided for the sake of quantification.

Following the scheme described previously, the postcondition of Intersection is translated for proof as:

Using the postcondition of Mem, this can be refined further into:

Though perfectly valid, this translation may produce complicated proofs, especially when verifying complex properties over sets. The GNATprove annotation <code>Iterable\_For\_Proof</code> can be used to change the way <code>for ...</code> of quantification is translated. More precisely, it allows to provide GNATprove with a *Contains* function, that will be used for quantification. For example, on our sets, we could write:

```
function Mem (S : Set; E : Element_Type) return Boolean;
pragma Annotate (GNATprove, Iterable_For_Proof, "Contains", Mem);
```

With this annotation, the postcondition of Intersection is translated in a simpler way, using logic quantification directly over elements:

Note that care should be taken to provide an appropriate function contains, which returns true if and only if the element  $\mathbb{E}$  is present in  $\mathbb{S}$ . This assumption will not be verified by GNATprove.

The annotation Iterable\_For\_Proof can also be used in another case. Operations over complex data structures are sometimes specified using operations over a simpler model type. In this case, it may be more appropriate to translate for ... of quantification as quantification over the model's cursors. As an example, let us consider a package of linked lists that is specified using a sequence that allows accessing the element stored at each position:

```
package Lists with SPARK_Mode is
type Sequence is private with
  Ghost,
  Iterable => (...,
               Element
                           => Get);
function Length (M : Sequence) return Natural with Ghost;
function Get (M : Sequence; P : Positive) return Element_Type with
  Ghost.
  Pre => P <= Length (M);
type Cursor is private;
type List is private with
  Iterable => (...,
                Element.
                           => Element);
function Position (L : List; C : Cursor) return Positive with Ghost;
function Model (L : List) return Sequence with
  Post => (for all I in 1 .. Length (Model'Result) =>
                (for some C in L => Position (L, C) = I));
function Element (L : List; C : Cursor) return Element_Type with
  Pre => Has_Element (L, C),
  Post => Element'Result = Get (Model (L), Position (L, C));
function Has_Element (L : List; C : Cursor) return Boolean with
  Post => Has_Element'Result = (Position (L, C) in 1 .. Length (Model (L)));
procedure Append (L : in out List; E : Element_Type) with
  Post \Rightarrow length (Model (L)) = Length (Model (L))'Old + 1
  and Get (Model (L), Length (Model (L))) = E
  and (for all I in 1 .. Length (Model (L)) 'Old =>
         Get (Model (L), I) = Get (Model (L'Old), I));
function Init (N : Natural; E : Element_Type) return List with
  Post => length (Model (Init'Result)) = N
    and (for all F of Init'Result => F = E);
```

Elements of lists can only be accessed through cursors. To specify easily the effects of position-based operations such as Append, we introduce a ghost type Sequence, that is used to represent logically the content of the linked list in specifications. The sequence associated to a list can be constructed using the Model function. Following the usual translation scheme for quantified expressions, the last line of the postcondition of Init is translated for proof as:

```
(for all C : Cursor =>
   (if Has_Element (Init'Result, C) then Element (Init'Result, C) = E));
```

Using the definition of Element and Has Element, it can then be refined further into:

```
(for all C : Cursor =>
   (if Position (Init'Result, C) in 1 .. Length (Model (Init'Result))
   then Get (Model (Init'Result), Position (Init'Result, C)) = E));
```

To be able to link this property with other properties specified directly on models, like the postcondition of Append, it needs to be lifted to iterate over positions instead of cursors. This can be done using the postcondition of Model that states that there is a valid cursor in L for each position of its model. This lifting requires a lot of quantifier reasoning from the prover, thus making proofs more difficult.

The GNATprove Iterable\_For\_Proof annotation can be used to provide GNATprove with a *Model* function, that will be to translate quantification on complex containers toward quantification on their model. For example, on our lists, we could write:

```
function Model (L : List) return Sequence;
pragma Annotate (GNATprove, Iterable_For_Proof, "Model", Entity => Model);
```

With this annotation, the postcondition of Init is translated directly as a quantification on the elements of the result's model:

Like with the previous annotation, care should be taken to define the model function such that it always return a model containing exactly the same elements as  $\mathbb{L}$ .

# **F.4 Inlining Functions for Proof**

Contracts for functions are generally translated by GNATprove has axioms on otherwise undefined functions. As an example, consider the following function:

```
function Increment (X : Integer) return Integer with
  Post => Increment'Result >= X;
```

It will be translated by GNATprove as follows:

```
function Increment (X : Integer) return Integer;
axiom : (for all X : Integer. Increment (X) >= X);
```

For internal reasons due to ordering issues, expression functions are also defined using axioms. For example:

```
function Is_Positive (X : Integer) return Boolean is (X > 0);
```

will be translated exactly as if its definition was given through a postcondition, namely:

```
function Is_Positive (X : Integer) return Boolean;
axiom : (for all X : Integer. Is_Positive (X) = (X > 0));
```

This encoding may sometimes cause difficulties to the underlying solvers, especially for quantifier instantiation heuristics. This can cause strange behaviors, where an assertion is proven when some calls to expression functions are manually inlined but not without this inlining.

If such a case occurs, it is sometimes possible to instruct the tool to inline the definition of expression functions using pragma Annotate Inline\_For\_Proof. When such a pragma is provided for an expression function, a direct definition will be used for the function instead of an axiom:

```
function Is_Positive (X : Integer) return Boolean is (X > 0);
pragma Annotate (GNATprove, Inline_For_Proof, Is_Positive);
```

The same pragma will also allow to inline a regular function, if its postcondition is simply an equality between its result and an expression:

```
function Is_Positive (X : Integer) return Boolean with
  Post => Is_Positive'Result = (X > 0);
pragma Annotate (GNATprove, Inline_For_Proof, Is_Positive);
```

In this case, GNATprove will introduce a check when verifying the body of  $Is\_Positive$  to make sure that the inline annotation is correct, namely, that  $Is\_Positive$  (X) and X > 0 always yield the same result. This check may not be redundant with the verification of the postcondition of  $Is\_Positive$  if the = symbol on booleans has been overridden.

Note that, since the translation through axioms is necessary for ordering issues, this annotation can sometimes lead to a crash in GNATprove. It is the case for example when the definition of the function uses quantification over a container using the Iterable aspect.

### **GNATPROVE LIMITATIONS**

### **G.1 Tool Limitations**

- 1. The Global contracts generated automatically by GNATprove for subprograms without an explicit one do not take into account indirect calls (through access-to-subprogram and dynamic binding) and indirect reads/writes to global variables (through access variables).
- 2. A subset of all Ada conversions between array types is supported:
  - element types must be exactly the same
  - matching index types must either be both modular with a base type of the same size, or both non modular
- 3. A subset of all Ada fixed-point types and fixed-point operations is supported:
  - · multiplication and division between different fixed-point types and floating-point types are rejected
  - multiplication and division between different fixed-point types are rejected if their smalls are not *compatible* as defined in Ada RM G.2.3(21).
  - conversions from fixed-point types to floating-point types are rejected

These restrictions ensure that the result of fixed-point operations always belongs to the *perfect result set* as defined in Ada RM G.2.3.

- 4. Multidimensional array types are supported up to 4 dimensions.
- 5. Loop\_Invariant and Loop\_Variant pragmas must appear before any non-scalar object declaration.
- 6. Inheriting the same subprogram from multiple interfaces is not supported.
- 7. Formal object parameters of generics of an unconstrained record type with per-object constrained fields are badly supported by the tool and may result in crashes in some cases.
- 8. Quantified expressions with an iterator over a multi dimensional array (for example for all Elem of Arr where Arr is a multi dimensional array) are not supported.
- 9. Constrained subtypes of class-wide types and 'Class attributes of constrained record types are not supported.
- 10. Abstract states cannot be marked Part\_Of a single concurrent object (see SPARK RM 9(3)). An error is raised instead in such cases.
- 11. Classwide Global and Depends contracts as defined in SPARK RM 6.1.6 are not supported.
- 12. Task attributes Identity and Storage Size are not supported.
- 13. Type\_Invariant and Invariant aspects are not supported:
  - · on private types declared in nested packages or child packages
  - · on protected types

- · on tagged types
- on components of tagged types if the tagged type is visible from inside the scope of the invariant bearing type.
- 14. Calls to protected subprograms and protected entries whose prefix denotes a formal subprogram parameter are not supported. Similarly, suspension on suspension objects given as formal subprogram parameters is not supported.

## **G.2 Legality Rules**

- 1. SPARK Reference Manual rule 4.3(1), concerning use of the box symbol "<>" in aggregates, is not currently checked.
- 2. The rule concerned with asserting that all child packages which have state denoted as being Part\_Of a more visible state abstraction are given as constituents in the refinement of the more visible state is not checked (SPARK Reference Manual rule 7.2.6(6)).
- 3. The case of a state abstraction whose Part\_Of aspect denotes a task or protected unit is not currently supported.
- 4. The case of a Refined\_Post specification for a (protected) entry is not currently supported.
- 5. The use of Ada.Synchronous\_Barriers.Synchronous\_Barrier type is not currently allowed in SPARK.
- 6. Entry families are not currently allowed in SPARK.

## **G.3 Flow Analysis Limitations**

- 1. Flow dependencies caused by record assignments is not captured with perfect accuracy. This means that the value of one field might incorrectly be considered to participate in the derivation of another field that it does not really participate in.
- 2. Initialization of multi-dimensional arrays with nested FOR loops can be only detected if the array bounds are given by static expressions.

### **G.4 Proof Limitations**

- 1. Postconditions of recursive functions called in contracts and assertion pragmas are not available, possibly leading to unproved checks. The current workaround is to use a non-recursive wrapper around those functions. Using the switch --info reveals where the information about postcondition may be lost.
- 2. Attribute 'Valid is currently assumed to always return True.
- 3. Values read from an external source are assumed to be valid values. Currently there is no model of invalidity or undefinedness. The onus is on the user to ensure that all values read from an external source are valid. The use of an invalid value invalidates any proofs associated with the value.
- 4. The following attributes are not yet supported in proof: Adjacent, Aft, Bit\_Order, Body\_Version, Copy\_Sign, Definite, Denorm, First\_Valid, Fore, Last\_Valid, Machine, all Machine\_\* attributes, Model, all Model\_\* attributes, Partition\_Id, Remainder, Round, Safe\_First, Safe\_Last, Scale, Scaling, Small, Unbiased\_Rounding, Version, Wide\_Image, Wide\_Value, Wide\_Width, Wide\_Wide\_Image, Wide\_Wide\_Wide\_Width, Width.

The attributes First\_Bit, Last\_Bit and Position are supported but if there is no record representation clause then we assume that their value is nonnegative.

- 5. The 'Update attribute on multidimensional unconstrained arrays is not yet fully supported in proof. Checks might be missing so currently an error is emitted for any use of the 'Update attribute on multidimensional unconstrained arrays.
- 6. GNATprove does not follow the value of tags for tagged objects. As a consequence, tag checks are currently unprovable in most cases.
- 7. Constants declared in loops before the loop invariant are handled as variables by the tool. This means in particular that any information about their values needed after the loop invariant must be stated explicitly in the loop invariant.
- 8. Preconditions on arithmetic and conversion operators (including Time\_Of) in Ada.Execution\_Time and Ada.Real\_Time packages described in SPARK Reference Manual 9.19 are not yet implemented.
- 9. Preconditions on arithmetic and conversion operators (including Time\_Of) in Ada.Calendar package are not yet implemented.

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### **PORTABILITY ISSUES**

## H.1 Compiling with a non-SPARK Aware Compiler

To execute a SPARK program, it is expected that users will compile the program (as an Ada program) using an Ada compiler. The SPARK language definition defines a number of implementation-defined (with respect to the Ada language definition) aspects, attributes, pragmas, and conventions. Ideally a SPARK program will be compiled using an Ada compiler that supports all of these constructs. Portability problems may arise if this is not the case.

This section is a discussion of the strategies available for coping with this situation.

Probably the most important rule is that pragmas should be used instead of aspect\_specification syntax wherever this option is available. For example, use pragma Abstract\_State rather than specifying the Abstract\_State aspect of a package using aspect\_specification syntax. Ada specifies that unrecognized pragmas shall be ignored, as opposed to being rejected. This is not the case for (syntactic) aspect specifications (this terminology is a bit confusing because a pragma can be used to specify an aspect; such a pragma is semantically, but not syntactically, an aspect specification). Furthermore, aspect specification syntax was introduced in Ada 2012 and will be rejected if the program is compiled as, for example, an Ada 95 program.

Many SPARK-defined constructs have no dynamic semantics (e.g., the Global, Depends, and Abstract\_State aspects), so the run-time behavior of a program is unaffected if they are ignored by a compiler. Thus, there is no problem if these constructs are expressed as pragmas which are then ignored by the Ada compiler.

Of those constructs which do have dynamic semantics, most are run-time assertions. These include Loop\_Variant, Loop\_Invariant, Assert\_And\_Cut, Contract\_Cases, Initial\_Condition, and Refined\_Postcondition. Because SPARK requires that the success of these assertions must be statically proven (and that the evaluation of the asserted condition can have no side effects), the run-time behavior of a program is unaffected if they are ignored by a compiler.

The situation with pragma Assume is slightly different because the success of the given condition is not statically proven. If ignoring an Assume pragma at run time is deemed to be unacceptable, then it can be replaced with an Assert pragma (at the cost of introducing a source code difference between the SPARK program that is analyzed statically and the Ada program that is executed). An ignored Assume pragma is the only case where the use of a SPARK-specific construct can lead to a portability problem which is not detected at compile time. In all other cases, either the Ada compiler will reject (as opposed to ignore) an unrecognized construct or the construct can safely be ignored.

An Ada compiler which does not support convention Ghost will reject any use of this convention. Two safe transformations are available for dealing with this situation - either replace uses of convention Ghost with convention Ada or delete the entities declared with a convention of Ghost. Just as was mentioned above in the case of modifying an Assume pragma, either choice introduces an analyzed/executed source code difference.

There are two SPARK attributes which cannot be used if they are not supported by the Ada compiler in question: the Update and Loop\_Entry attributes.

SPARK includes a rule that a package which declares a state abstraction requires a body. In the case of a library unit package (or generic package) which requires a body only because of this rule, an Ada compiler that knows nothing

about state abstractions would reject the body of the package because of the rule (introduced in Ada 95) that a library unit package (or generic package) body is never optional; if it is not required then it is forbidden. In the unlikely event that this scenario arises in practice, the solution is to force the library unit package to require a body for some other reason, typically by adding an Elaborate\_Body pragma.

If a SPARK program is to be compiled and executed as an Ada 95 program (or any other pre-2012 version of Ada), then of course any construct introduced in a later version of Ada must be avoided (unless it is expressed as a safely-ignored pragma). This seems worth mentioning because Ada 2012 constructs such as quantified expressions and conditional expressions are often heavily used in SPARK programs.

## **H.2 Implementation-specific Decisions**

To make analysis as precise as possible and avoid producing too many false alarms, GNATprove makes some assumptions about the behavior of constructs which are listed in the reference manual of Ada as implementation specific. Note that GNATprove always adopts the same choices as the GNAT compiler, so these assumptions should be adequate when compiling with GNAT. However, when another compiler is used, it may be better to avoid these implementation specific constructs (see *Benefits of Using SPARK for Portability* for more details on how this can be achieved).

### **H.2.1 Parenthesized Arithmetic Operations**

In Ada, non-parenthesized arithmetic operations could be re-ordered by the compiler, which may result in a failing computation (due to overflow checking) becoming a successful one, and vice-versa. By default, GNAT prove evaluates all expressions left-to-right, like GNAT. When the switch --pedantic is used, a warning is emitted for every operation that could be re-ordered:

- any operand of a binary adding operation (+,-) that is itself a binary adding operation;
- any operand of a binary multiplying operation (\*,/,mod,rem) that is itself a binary multiplying operation.

### **H.2.2** Base Type of User-Defined Integer Types

GNATprove follows GNAT in choosing as base type the smallest multiple-words-size integer type that contains the type bounds. For example, a user-defined type ranging from 1 to 100 will be given a base type ranging from -128 to 127 by both GNAT and GNATprove. The choice of base types influences in which cases intermediate overflows may be raised during computation. The choice made in GNATprove is the strictest one among existing compilers, as far as we know, which ensures that GNATprove's analysis detects a superset of the overflows that may occur at run time.

### H.2.3 Size of 'Image and 'Img attributes

To avoid spurious range checks on string operations involving occurrences of the 'Img, 'Image, 'Wide\_Image, and 'Wide\_Mide\_Image attributes, GNATprove makes an assumption about the maximal length of the returned string. If the attribute applies to an integer type, the bounds are the maximal size of the result of the attribute as specified in the language depending of the type's base type. Otherwise, GNATprove assumes that the length of such a string cannot exceed 255 (the maximal number of characters in a line) times 8 (the maximal size of a Wide\_Wide\_Character).

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### SEMANTICS OF FLOATING POINT OPERATIONS

SPARK assumes that floating point operations are carried out in single precision (binary32) or double precision (binary64) as defined in the IEEE-754 standard for floating point arithmetic. You should make sure that this is the case on your platform. For example, on x86 platforms, by default some intermediate computations may be carried out in extended precision, leading to unexpected results. With GNAT, you can specify the use of SSE arithmetic by using the compilation switches "-msse2 -mfpmath=sse" which cause all arithmetic to be done using the SSE instruction set which only provides 32-bit and 64-bit IEEE types, and does not provide extended precision. SSE arithmetic is also more efficient. Note that the ABI allows free mixing of units using the two types of floating-point, so it is not necessary to force all units in a program to use SSE arithmetic.

SPARK considers the floating point values which represent positive, negative infinity or NaN as invalid. Proof obligations are generated that such values cannot occur.

SPARK considers rounding on floating point arithmetic operations to follow Round-Nearest-Even (RNE) mode, where a real result is rounded to the nearest floating point value, and ties are resolved to the floating-point with a zero in the last place. This mode of rounding should be forced if needed on the hardware to be able to rely on the results of GNATprove regarding floating point arithmetic.

# SPARK ARCHITECTURE, QUALITY ASSURANCE AND MATURITY

## J.1 Development Process and Quality Assurance

The SPARK development process and quality assurance are following the Adacore Quality Procedures in place for all development at AdaCore. This includes:

- The use of a report tracking system;
- Mechanisms for detecting and fixing defects;
- The usage of repositories and configuration management, the use of continuous integration technology, the stringent requirements on check-ins of source changes;
- The process for implementing new functionality;
- The process for maintaining user documentation;
- Ensuring quality of sources and technical documentation;
- Preparation of releases

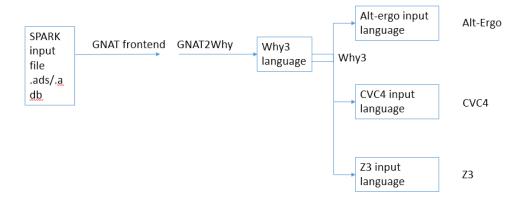
As an extension to Chapter 2, section "AdaCore internal testsuite", SPARK contains its own testsuites:

- The SPARK main testsuite: This testsuite contains 1700 tests. These tests are specifically targeted at the SPARK software and cover typical use cases, often represented by code sent to us by customers, as well as specific features of the SPARK software.
- The ACATS testsuite in SPARK mode: A selection of the ACATS testsuite mentioned in the AdaCore Quality Procedures for the compiler is also used to test the SPARK tools.

These tests are run on various occasions (see also Chapter 2 of the Adacore Quality Procedures): \* During nightly testing, once with assertions enabled, once without (the actual SPARK product); \* After every check-in, during continuous integration; \* To test a patch before check-in using the Mailserver technology.

### J.2 Structure of the SPARK Software

At a high level, SPARK reads source files in the Ada programming language, with some annotations specific to SPARK, processes them, and in the end issues a report about errors found and proved or unproved properties. Looking more closely at how this is achieved, one can see this high-level structure of SPARK:



The development of the GNAT front-end and GNAT2Why components entirely follows the procedures outlined in AdaCore Quality Procedures and the previous section. The other components, however, are mostly developed by third parties. Their development process and the relationship to AdaCore and Altran will be outlined below.

For the nightly testing of SPARK, the GNAT and GNAT2Why components are updated every night according to the changes made during the day by AdaCore and Altran developers. The other tools, however, contain also check-ins by other persons. We update these tools in a controlled way, and after careful testing of the consequences. In other words, a check-in made e.g. to Z3 at some specific date, will not be part of the SPARK package of the same day, instead it will be integrated into SPARK after some time and after thorough testing in the SPARK environment.

#### J.2.1 GNAT front-end

SPARK shares its front-end (parsing and semantic analysis) with the GNAT compiler technology, which is very mature and has been used in countless projects for the last 20 years. The GNAT front-end is developed by AdaCore and follows the AdaCore quality procedures.

### J.2.2 GNAT2Why

This part of SPARK serves two purposes:

- Implement Flow Analysis, the part of the SPARK analysis which detects uninitialized variables, and computes and checks the use of global variables and parameters.
- Translate the Ada source code to the Why language, for further processing by the Why3 tools. GNAT2Why is developed by AdaCore and Altran and follows the AdaCore quality procedures.

### J.2.3 Why3

This part of SPARK takes the information in the Why language produced by GNAT2Why, translates it further into a format suitable for SMT solvers such as Z3 and CVC4, and runs these tools. The results are reported back to gnat2why.

History: Started around the year 2000 by Jean-Christophe Filliâtre as "Why" (see Jean-Christophe Filliâtre. Why: a multi-language multi-prover verification tool. Research Report 1366, LRI, Université Paris Sud, March 2003), it has undergone a number of redevelopments until its current version Why3 (since 2010).

Track record: Apart from SPARK, it is used by Frama-C, Atelier B, and other program verification tools.

Relationship with AdaCore/Altran: The Inria team around Why3 has strong ties with AdaCore and Altran. A number of research projects have been and are being carried out in collaboration with this team. This includes the Hi-Lite

project, which led to the current version of SPARK based on Why3, and the still ongoing project SOPRANO and joint laboratory ProofInUse. In addition, while Why3 is mainly developed at Inria, AdaCore and Altran have made important contributions to the technology, such as the so-called fast-WP, a more efficient implementation of the main algorithm of Why3, and the why3server, a more scalable method of running external tools such as SMT solvers.

• Main developers: Inria research institute

• Main website: http://why3.lri.fr

• Version Management: Git

• License: Open Source, LGPL 2.1

• Public mailing-list: why3-club@lists.gforge.inria.fr

• Bug tracking: https://gforge.inria.fr/tracker/?group\_id=2990

### J.2.4 Alt-Ergo

History: Started around the year 2005 at Inria by Sylvain Conchon and Evelyne Contejean as "Ergo" (see CC(X): Efficiently combining equality and solvable theories without canonizers. Sylvain Conchon, Évelyne Contejean, and Johannes Kanig. SMT Workshop, 2007). Starting from 2013, developed and distributed mainly by OCamlPro. Since then, OCamlPro issues every year a private release and a public release (lagging one year behind the private release). SPARK uses the public release of Alt-Ergo.

Track record: Apart from SPARK, it is used by Frama-C and Atelier B. In particular, used by Airbus for the qualification DO-178C of an aircraft [10].

Relationship with AdaCore/Altran: AdaCore and OCamlPro collaborate in the SOPRANO. AdaCore has contributed some minor changes to Alt-Ergo, including a deterministic resource limiting switch.

• Main developers: OCamlPro

• Main website: https://alt-ergo.ocamlpro.com/

• Version Management: Git

• License: CeCill-C (GPL compatible)

• Public mailing-list: alt-ergo-users@lists.gforge.inria.fr

• Bug tracking: https://github.com/OCamlPro/alt-ergo/issues

#### J.2.5 Z3

History: Started around the year 2007 at Microsoft Research by Leonardo de Moura and Nikolaj Bjørner (see Leonardo de Moura and Nikolaj Bjørner. Efficient E-Matching for SMT solvers. In Automated Deduction - CADE-21, 21st International Conference on Automated Deduction, Bremen, Germany, July 17-20, 2007, Proceedings, volume 4603 of Lecture Notes in Computer Science, pages 183-198. Springer, 2007). Released to open source under a very permissive license in 2015.

Track record: Apart from SPARK, used by Dafny and PEX projects inside Microsoft. Has won the SMT competition several times in several categories.

Relationship with AdaCore/Altran: AdaCore and Altran have provided bug reports, feature requests and small fixes to the Z3 team, in particular related to a deterministic resource limiting switch.

• Main developers: Microsoft

• Main website: https://github.com/Z3Prover/z3

• Version Management: Git

• License: MIT License

• Stackoverflow community: http://stackoverflow.com/questions/tagged/z3

• Bug tracking: https://github.com/Z3Prover/z3/issues/

### J.2.6 CVC4

History: CVC4 is the fourth in the Cooperating Validity Checker family of tools, which dates back to 1996, but does not directly incorporate code from any previous version. CVC4 development started in 2012.

Track record: Very good results in various SMT competitions. Used in TNO tool.

Relationship with AdaCore/Altran: AdaCore and Altran have provided bug reports, feature requests and small fixes to the CVC4 team, in particular related to a deterministic resource limiting switch.

• Main developers: New York University

• Main website: http://cvc4.cs.nyu.edu/web/

• Version Management: Git

• License: Modified BSD License

• Mailing List: cvc-users@cs.nyu.edu

• Bug tracking: http://cvc4.cs.nyu.edu/bugs/

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