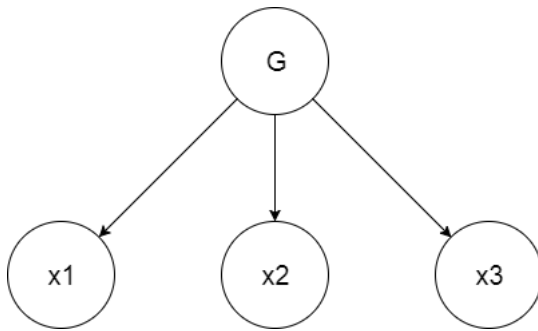


CS 472 HW 7

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14.1) a.)



b.) First apply Bayes Rule to reverse the dependency.

$$P(G|2 \text{ heads}, 1 \text{ tail}) = P(2 \text{ heads}, 1 \text{ tails}|G)P(G)/P(2 \text{ heads}, 1 \text{ tails}) \quad (1)$$

$$P(2 \text{ heads}, 1 \text{ tails}|G) \quad (2)$$

G	P(G)
a	1/3
b	1/3
c	1/3

(a) The CPC
for G

G	X_i	P(G)
a	heads	0.2
b	head	0.6
c	heads	0.8

(b) The CPC for x_i
given G

x_1, x_2 and x_3 are conditionally independent of given G (they are d separated by G). The highest conditionally probability in question can then calculated, where there are 3 choose 2 combinations of the event for a.

$$P(x_1 = tails|G = a)P(x_2 = heads|G = a)P(x_3 = heads|G = a) = 0.032 \quad (3)$$

$$P(2 \text{ heads, } 1 \text{ tails}|G = a) = 3 * 0.032 = 0.096 \quad (4)$$

$$(5)$$

It follows that.

$$P(2 \text{ heads, } 1 \text{ tails}|G = b) = 0.432 \quad (6)$$

$$P(2 \text{ heads, } 1 \text{ tails}|G = c) = 0.384 \quad (7)$$

$$(8)$$

The condition $G = b$ provides the highest conditionally probability.

14.6) a). The network c represent represents the expression. The independence of genes is asserted.

b). a and b both consistent with the claim. However, b may have some unnecessary dependencies based on the description.

c.) a is the best representation for reasons stated above.

d.)

Table 1: CPC for handedness

G_{mother}	G_{father}	$P(G_{child} = l \text{---} -)$	$P(G_{child} = r \text{---} -)$
l	l	1-m	m
l	r	0.5	0.5
r	l	0.5	0.5
r	r	m	1-m

e.)

$$P(G_{child} = l) = \sum_{g_m, g_f} P(G_{child} = l | g_m, g_f) P(g_m, g_f) \quad (9)$$

$$= \sum_{g_m, g_f} P(G_{child} = l | g_m, g_f) P(g_m) P(g_f) \quad (10)$$

$$= (1 - m)q^2 + 0.5q(1 - q) + 0.5(1 - q)q + m(1 - q)^2 \quad (11)$$

$$= q + m - 2mq \quad (12)$$

f.) left-handedness in humans is fairly uncommon ($\approx 10\%$ according to Google). For equilibrium, $P(G_{child} = l) = P(G_{mother} = l) = P(G_{father} = l)$. This implies that $q + m - 2mq = q$, $q = 0.5$. This seems too high for current global statistics.

14.14) a.) ii, and iii are asserted by the network. b.) $P(b, i, \neg m, g, j) = P(b)P(\neg m)P(i|b, \neg m)P(g|b, i, \neg m)P(j|g) = 0.9 * 0.9 * 0.5 * 0.8 * 0.9 = 0.2916$
c.) B, I and M are given as evidence with values of *true*. This gives G a prior of 0.9. The probability of going to jail is:

$$P(J|b, i, m) = \alpha \sum_g P(J, g) \quad (13)$$

$$= \alpha(P(J, g) + P(J, \neg g)) \quad (14)$$

$$= \alpha(\langle P(j, g), P(\neg j, g) \rangle + \langle P(j, \neg g), P(\neg j, \neg g) \rangle) \quad (15)$$

$$= \langle 0.81, 0.19 \rangle \quad (16)$$

$$= \alpha(\langle 0.81, 0.09 \rangle + \langle 0, 0, 1 \rangle) = \langle 0.81, 0.19 \rangle \quad (17)$$

The probability of jail is 0.81.

Markov Blanket for variable M in the network includes M's parents, children and its childrens' other parents: I, G, B