

Problem Set 4

1 Radiative Forcing with CO₂

Carbon dioxide is one of the major gases driving the anthropogenic greenhouse effect (the dominant greenhouse gas is H₂O, but it is not anthropogenic). One of the most impactful transition in CO₂ for our climate is the 15 μm line, which corresponds to the bending oscillation of the linear CO₂ molecule. The main line (there are rotational/vibrational branches that we'll discuss in a later class) has an Einstein A of about $A \sim 10 \text{ s}^{-1}$.

1.1

Assume the gas temperature of the CO₂ is about the same as the Earth's blackbody (255 K), and plot the line profile of this transition with both Doppler and intrinsic components. Use a logarithmic y axis.

1.2

Model the Earth's outgoing emission as a 255 K blackbody. Plot this spectrum, and overlay on it the spectrum including absorption from the 15 μm line of CO₂. At line center, the optical depth of this transition in our atmosphere is about $\tau \sim 3$, so set the number density of CO₂ accordingly.

1.3

Calculate the flux of emission absorbed by CO₂ over the frequency interval where this transition is optically thick ($\tau > 1$). Compare this to the amount of energy absorbed by CO₂ over the entire blackbody spectrum. What fraction of the total energy absorbed is in the optically thick regime?

1.4

Assume that, for all the flux absorbed by CO₂, half of it is radiated upward (i.e. it escapes the atmosphere) and half of it is radiated downward. The flux radiated downward is effectively subtracted from the total flux radiated off by the Earth's blackbody. To radiate off the same amount of flux as it did without CO₂, by how many degrees must the blackbody of the Earth increase? This is called radiative forcing, and you have now roughly calculated the contribution of the 15 μm line of CO₂ to the greenhouse effect!