

# Look up runtimes

- Sorts:

- sort in  $O(n + k)$  time (Feld)(Counting sort)
- sort in  $O(n)$  (List)  
sort alphabetical (bucketsort lexicographical sort)

- Graphen:

- reversen Graph (j,i to i,j)
- Komplement des Graph (Adjazenzmatrix 1 to 0, 0 to 1)
- 2014.5
- Baum-, Rückwärts-, Vorwärts-, oder Querkante

## 1 Sorts

### 1.1 Heapsort

#### 1.1.1 Aufbauphase

```
1 for i=[ $\frac{n}{2}$ ]downto 1
   Sink(i,n)
3
```

#### 1.1.2 Heapify

```

Sink(i,r){
2   x = A[i];
   j = 2*i;
4   while (j ≤ r){
       if (j+1 ≤ r){
6         if (A[j+1]>A[j]){
             j = j+1;
8         }
       }
10      if (x ≥ A[j]){
          break;
12      }
       A[i] = A[j];
14      i = j;
       j = 2*i;
16   }
   A[i] = x;
18 }
```

### 1.1.3 Selektionsphase

```

r = n
2 while (r > 1){
    A[1] <=> A[r];
4    r = r-1;
    Heapify(1,r)
6 }
```

## 1.2 Quicksort

```

Quicksort(l,r){
2   if (L>=r)
       return;
4   x = A[l]      pivot
   i = l+1
6   j = r
   repeat
8       while i<=r && A[i]<x
           i++
10      while j>=l+1 && A[j]>=x
           j--
12      if i<j
           A[i]<=>A[j]
14  until i>j
  A[l]<=>A[j]
16  Quicksort(l,j-1)
  Quicksort(j+1,r)
18 }
```

## 2 Bäume

### 2.1 Aufbau

```

BaueBaum(A,l,r){
2   if (l>r)
       return 0;
4   m =  $\lfloor \frac{l+r}{2} \rfloor$ ;
   p = new bintree_node();
6   p.key = A[m];
   p.left = BaueBaum(l,m-1);
8   p.right = BaueBaum(m+1,r);
   return p;
10 }
```

## 2.2 Lookup

```
Lookup(x)
2   if (p = null)
      return null;
4   while (p ist kein Blatt)
      if x
6
```

## 2.3 Insert

```
1 Insert(Node root, int key, int value){
   if (root = null)
3     root = new Node(key, value);
   else if (key < root.key)
5     root.left = insert(root.left, key, value);
   else // key >= root.key
7     root.right = insert(root.right, key, value);
   return root;
9 }
```

## 2.4 Delete

```
1 Delete(x){
   v = lookup(x);
3   (Sei p vater von v)
   Fall 1: (v ist Blatt){
5     if (v = p.left)
       p.left = null;
7     else
       p.right = null;
9   }
   Fall 2: (v hat ein Kind w){
11    if (v = p.left)
       p.left = w;
13    else
       p.right = w;
15  }
   Fall 3: (v hat 2 Kinder)
17    u = v.left;
    while (u.right != null)
19      u = u.right;
    v.key = u.key;
21 }
```

## 2.5 Print

```

1 Print(node n){
    if node.left != null
3     print(node.left)
    schreibe(node.key)
5     if node.right != null
        print(node.right)
7 }

```

## 2.6 Max/Min Key

```

1 Max(){
    u = rootNode
3     while u.right != null
        u = u.right
5     return u;
    }

9 Min(){
    u = rootNode
11    while u.left != null
        u = u.left
13    return u;
    }
15

```

## 2.7 Rotate

### 2.7.1 Single

```

1 RotateRight(node u){
2     w = u.parent
    v = u.right
4     b = v.left
    v.parent = w
6     if w = null
        v = root
8     else if u = w.left
        w.left = v
10    else
        w.right = v
12    u.parent = v
    v.left = u
14    u.right = b
    if b!=null
16        b.parent = u
    }
18

```

### 2.7.2 Double

```
1 DoubleRR(node u){
    v = u.left
3    rotateLeft(v)
    rotateRight(u)
5 }

7 DoubleRL(node u){
    v = u.right
9    rotateRight(v)
    rotateLeft(u)
11 }
```

## 2.8 Depth-First Search

```
1 DFS(G, v){
    v als beschriften
3    for all adjacent nodes w to v do
        if node is not labeled discovered
5        DFS(G,w)
7 }
```

## 2.9 Breadth-First Search

```
BFS(G,v){
2    Q:= queue initialized with root
    while Q.notEmpty()
4        current = Q.dequeue()
        if current = goal
6        return current
    for each node n that is adjacent to current
8        if n is not discovered
            label n as discovered
10           n.parent = current
            Q.enqueue(n)
12 }
```

## 3 Graphen

## 4 Definitionen

### 4.1 Topologische Sortierung

Eine Abbildung  $ord : V \rightarrow \{1, \dots, n\}$

Es gilt zudem:

- $ord$  ist injektiv
- $\forall (v, w) \in E : ord(v) < ord(w)$