

BIA652C_HW9_AaronYu

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```
In [3]: import numpy as np
import pandas as pd
import sklearn
import matplotlib.pyplot as plt
from sklearn import decomposition
%matplotlib inline
```

```
In [2]: import warnings
warnings.filterwarnings('ignore')
```

0.1 Homework: PCA 1

- Suppose you have a 10-dimensional dataset with 100 sample points. Denote it as 100x10 matrix X . Further assume that X is normalized (sum of each column = 0)
- Suppose the $X^T X$ has eigenvectors $v_1, v_2, v_3, \dots, v_{10}$. Each eigenvector is of dimension 10.
- It has eigenvalues 10, 2, 1, 0.5, 0.3, 0.1, 0.05, 0.03, 0.02, 0.01
- PCA projects the 100x10 data matrix into 100x1 matrix. If we want to get a PCA of the data that explains 90% of the variance, what is the smallest l ?
- How to get the 100x1 PCA matrix from X and the eigenvectors?

```
In [4]: eigenv = np.array([10, 2, 1, 0.5, 0.3, 0.1, 0.05, 0.03, 0.02, 0.01])
```

```
In [9]: var_explained = np.add.accumulate(eigenv) / eigenv.sum()
```

- PCA projects the 100x10 data matrix into 100x1 matrix. If we want to get a PCA of the data that explains 90% of the variance, what is the smallest l ?

```
In [15]: l = [idx for idx, item in enumerate(var_explained) if item > 0.9][0] + 1
```

```
In [17]: print('The smallest l is %d' % l)
```

The smallest l is 3

- How to get the 100x1 PCA matrix from X and the eigenvectors?

```
In [45]: print('We first construct a projection matrix P using the largest l eigenvectors')
```

We first construct a projection matrix P using the largest l eigenvectors, the 100x10

0.2 Homework: PCA 2

- Take around 100 sample digits from the mnist dataset which contains images from hand written digits
- Now apply PCA to reduce the data to 2D
- How much variance can the 2D PCA explain?
- Visualize the 2D data as a scatter plot, and annotate the dots using the digit label.

```
In [18]: from sklearn import datasets
         digits = datasets.load_digits()
         n = digits.target.shape[0]
         import random
         random.seed(123)
         indices = np.array(list(set([random.randint(0, n) for i in range(100)])))
         labels = digits.target[indices]
         data = digits.data[indices]
```

```
In [23]: pca = decomposition.PCA(n_components=2)
```

```
In [27]: pca.fit(data)
```

```
Out[27]: PCA(copy=True, iterated_power='auto', n_components=2, random_state=None,
          svd_solver='auto', tol=0.0, whiten=False)
```

```
In [28]: data_2d = pca.transform(data)
```

```
In [34]: print('%.4f variance can the 2D PCA explain' % pca.explained_variance_ratio)
```

0.2969 variance can the 2D PCA explain

```
In [46]: fig = plt.figure(figsize = (15,9))
         plt.scatter(data_2d[:,0],data_2d[:,1])
         for label, x, y in zip(labels, data_2d[:,0],data_2d[:,1]):
             plt.annotate(label, xy = (x, y), xytext = (-20, 20),
                           textcoords = 'offset points', ha = 'right', va = 'bottom',
                           bbox = dict(boxstyle = 'round,pad=0.5', fc = '#eeeeff', alpha = 0.5),
                           arrowprops = dict(arrowstyle = '->', connectionstyle = 'a
```

