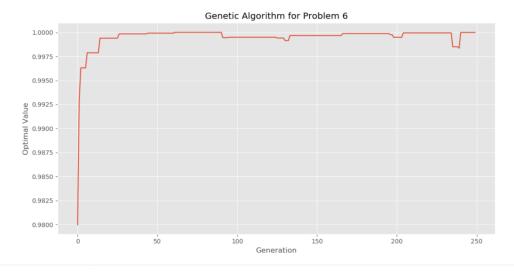
**Problem 6**Maximize  $f(x, y) = \sin^2(5\pi(x^{3/4} - 0.1)) - (y - 1)^4 2 \le x \le 4; -1 \le y \le 2; x+y \le 5$ Maximum=1 at (x,y)=(3.575,1)

Category	Item	Content	
Parameters setting	Population Size	100	
	Crossover Rate	90%	
	Mutation Rate	10%	
	Generation	250 I think 250 is suitable for this problem. (compare to 1000 times, which only improve optimal value 10 <sup>-7</sup> )	
Composition of Chromosomes with precision being 10 <sup>-3</sup>			
Decision Variable X		11 bits	
Decision Variable Y		12 bits	
Total for a chromosome length		23 bits	
Mechanisms			
Selection Mechanism		Roulette Wheel	
Crossover Mechanism		One-point Crossover	
Mutation Mechanism		Bit-by-bit base	
Constraint handling			
Subject to	2≤x≤4; -1≤y≤2	Pre-censoring	
	x+y≤5	Penalty, which add a	
		negative number	
		Check Constraint post-	
		crossover & post-	
		mutation	

The Final Optimization Results		
	0.9999996913865616	
Optimal Value	(For 1000 generation case: 0.9999997922565107)	
Optimal for Decision Variable X	3.6912554958475816	
Optimal for Decision Variable Y	1.221978021978022	

# The evolution history



## Program Code:

## Parameters setting and Pre-censoring of 2 Decision Variable domain

```
Problem 6
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"""

import numpy as np
from matplotlib import pyplot as plt
import pandas as pd
import random

population = 100 # set the number of chromosomes in each population
chs_length, x_length, y_length = 23, 11, 12 # by precision 10^-3; chromosomes total length for 23, and x is 11, y is 12
CR, MR = 0.9, 0.1 # Crossover Rate set 90%; Mutation Rate set 10%
generation = 250 # set the number of generations
pi = m.pi # set \pi , objective function will use it

XBound = [2, 4] # pre-censoring for 2< x < 4
YBound = [-1, 2] # pre-censoring for -1< y < 2
```

#### **Objective Function**

Also Check Constraint post-crossover & post- mutation.

# Create a population of Initialization.

## Set get fitness function and 2 transfer way make Binary to Decimal for X, Y.

#### Roullete Wheel Selection

Set 2 indexes for 2 parents.

The indexes choose one from population size, which depends on their proportion of total fitness.

## **Do Crossover**

Set 2 temporary list to assist exchange.

```
# Roulette Wheel Selection

def selection(pop, fitness):
    # print("p", len(fitness))
    index01 = np.random.choice(a=100, size=1, replace=False, p=fitness / sum(fitness))
    # select a random number as index no.1, which chosen 1 from 100 by their fitness proportion
    parent01 = pop(index01) # determine which chromosome as the parent no.1
    index02 = np.random.choice(a=100, size=1, replace=False, p=fitness / sum(fitness))
    # select a random number as index no.2, which chosen 1 from 100 by their fitness proportion
    parent02 = pop(index02) # determine which chromosome as the parent no.2
    return parent01, parent02, index01, index02

# crossover

def crossover(parent01, parent02):
    if np.random.rand() < CR: # Determine whether DO the crossover or Not
        crossover_location = m.ceil(
            random.random() * (chs_length - 1)) # Determine the crossover location in chromosome
        temp_ch01, temp_ch02 = list(range(1, chs_length)), list(range(1, chs_length))
    # Create 2 temporary lists to assist the crossover process
    temp_ch01[crossover_location:] = parent02[0][crossover_location:]
    # Make the exchange chromosome section in parent no.2 transfer save in temporary no.1
    temp_ch02[crossover_location:] = parent02[0][crossover_location:]
    # Make the exchange chromosome section in parent no.1 transfer save in parent no.1
    parent02[0][crossover_location:] = temp_ch02[crossover_location:]
    # Make the exchange chromosome section in temporary no.1 transfer save in parent no.1
    parent02[0][crossover_location:] = temp_ch02[crossover_location:]
    # Ake the exchange chromosome section in temporary no.2 transfer save in parent no.1
    parent02[0][crossover_location:] = temp_ch02[crossover_location:]
    # Ake the exchange chromosome section in temporary no.2 transfer save in parent no.2
    return [parent01, parent02]
```

#### **Do Mutation**

Check do mutate or not to do it using bit-by-bit.

```
# mutate

def mutate(offspring): # bit-by-bit
list_mut = [] # Create a list to save the after-process offsprings

for i in range(2): # for two parent in processing

for point in range(chs_length): # mutate bit-by-bit mechanism

if np.random.rand() < MR: # Determine each bit will do mutate or not

offspring[i][0][point] = 1 if offspring[i][0][point] == 0 else 0 # make 0 to 1; or 1 to 0

list_mut.append(offspring[i]) # add after-process and no mutated to list

return list_mut
```

### **Executive**

Realization the initialization.

For each chromosome, divide into x & y parts, then transfer into real value.

Do 50 times for selection, crossover and mutation to make offspring achieve 100.

Do the 1000 generations, and show the optimal value for each generations.

```
# the processing flow
popch = initial()
target = [] # record the Max value of each generation

For j in range(generation):
    result = [] # the chromosome values of generation
    fitness = [] # the fitness value from each chromosome
    # print("check_first t", len(fitness))
    for k in range(100):
        x_ = popch[k][:11] # pick up the x part in chromosome
        y_ = popch[k][:11] # pick up the y part in chromosome
        if transfer_x(x_) + transfer_y(y_) > 5: # if x + y > 5, give the penalty
            obj_values = obj_function(transfer_x(x_), transfer_y(y_)) - 100
        else:
            obj_values = obj_function(transfer_x(x_), transfer_y(y_)) # compute their objective value
        result.append(obj_values) # add the objective value into the result list
        fitness.append(get_fitness(result[k])) # make the result get fitness

for i in range(int(population / 2)): # make the offsprings achieve 100

parent01, parent02, index01, index02 = selection(popch, fitness) # select 2 parents
        offspring_list = crossover(parent01, parent02) # the crossover stage
        list_mut = mutate(offspring_list) # the mutation stage
        popch[index01] = list_mut[0] # offspring replace their parent
        popch[index02] = list_mut[1] # offspring replace their parent
        target.append(np.max(result)) # add max value of result to the target list

Print('target(Max Value):', np.max(target)) # print the max value of each generation
```

### **Print the evolution history**

#### Optimal value and their decision variables value.

```
print("Max Value: ", np.max(target)) # print the final optimal value
print("optimal x:", transfer_x(x_)) # print the optimal value of decision variable x
print("optimal y:", transfer_y(y_)) # print the optimal value of decision variable y
target = pd.DataFrame(target)
plt.style.use('ggplot')
plt.plot(range(generation), pd.DataFrame.rolling(target, window=30, min_periods=1).max())
plt.xlabel("Generation")
plt.ylabel("Optimal Value")
plt.title("Generic Algorithm for Problem 6")
plt.figure()
plt.show()
```