Math3_Statistics_LinearAlgebra.pdf

Page 1 – Statistics (I)

- 1. Define mean
- 2. Find mean of [6, 8, 10, 12, 14]
- 3. Median of [3, 8, 11, 13, 18]
- 4. Variance formula
- 5. Standard deviation of [4, 8, 12, 16, 20]
- 6. Outlier definition
- 7. Interquartile range of [2,4,6,8,10,12]
- 8. What is a box plot?
- 9. Probability: roll two dice, both sixes
- 10. What is a frequency table?

Page 2 - Statistics (II)

- 1. Mode of [4, 6, 6, 8, 10, 10, 10]
- 2. What is correlation?
- 3. Scatter plot explanation
- 4. What is a z-score?
- 5. Permutations: 4 letters in "STOP"
- 6. Combinations: choose 2 from 7
- 7. Event A: P(A)=0.4, B: P(B)=0.5, $P(A\cap B)=0.2$. $P(A\cup B)=?$

- 8. Probability: pick red from 3 red, 5 blue balls
- 9. Histogram vs. bar chart
- 10. Probability: flip 2 coins, both heads

Page 3 – Statistics (III)

- 1. Quartiles in [1,2,3,4,5,6,7,8,9]
- 2. Find the mode in [7, 8, 9, 8, 8, 10, 9]
- 3. Variance of [2,2,4,6,6,6,7]
- 4. Probability: get a king from a deck
- 5. What is the mean absolute deviation?
- 6. Frequency polygon explanation
- 7. What is a stem-and-leaf plot?
- 8. Probability: 5 marbles, 2 green. Probability of green?
- 9. Median in [10, 20, 30, 40, 50, 60, 70]
- 10. What is a uniform distribution?

Page 4 – Statistics (IV)

- 1. Range of [1,4,7,12,15]
- 2. Probability: Drawing an ace from 52 cards
- 3. What is normal distribution?
- 4. Probability: toss 3 coins, 2 heads
- 5. What is sample space?
- 6. Expected value definition

- 7. Binomial probability formula
- 8. Cumulative frequency explanation
- 9. Probability: Roll die, even number
- 10. What is a random sample?

Page 5 - Linear Algebra (I)

- 1. Define a matrix
- 2. Multiply: [[1,0],[2,1]] × [[2,2],[1,3]]
- 3. Find the determinant: [[5,7],[2,4]]
- 4. What is a vector?
- 5. Add vectors: [2,3] + [1,4]
- 6. Scalar multiplication of matrix
- 7. If v = [1,2], w = [3,1], dot product?
- 8. What is a square matrix?
- 9. Identity matrix explanation
- 10. Find eigenvalues of [[3,0],[0,2]]

Page 6 - Linear Algebra (II)

- 1. Find the inverse of [[2,1],[1,1]]
- 2. What is a diagonal matrix?
- 3. What is matrix transpose?
- 4. Trace of [[3,2],[4,1]]
- 5. What is a basis?

- 6. Null space definition
- 7. Symmetric matrix explanation
- 8. Solve Ax = b for x: A = [[1,3],[2,4]], b = [5,10]
- 9. Orthogonality definition
- 10. What is a row-reduced echelon form?

Page 7 - Calculus (I)

- 1. Evaluate the derivative of $y = 3e^x$
- 2. Integrate ∫2x dx
- 3. Differentiate $f(x) = x^2 + 5x$
- 4. $\lim(x\to 0) (1-\cos(x))/x^2$
- 5. Find the critical points of $f(x) = x^3 2x$
- 6. Integrate $\int 1/(1 + x^2) dx$
- 7. Area under y = 4x, x=1 to x=5
- 8. Second derivative of $y = x^4$
- 9. What is the limit as $x \rightarrow \infty$ of 1/x?
- 10. Find the inflection points of $f(x) = x^4 8x^2 + 7$

Page 8 – Calculus (II)

- 1. Differentiate $y = \sin(2x)$
- 2. Integrate ∫x cos(x) dx
- 3. What is a Riemann sum?
- 4. $\lim(x\to 1)(x^2-1)/(x-1)$

- 5. Maximum of $f(x) = -x^2 + 2x + 3$
- 6. Find dy/dx for $y = ln(x^2)$
- 7. Taylor expansion of ln(1+x) at x = 0
- 8. What is the Mean Value Theorem?
- 9. Integrate ∫e^x dx
- 10. Chain rule: d/dx [cos(x²)]

Page 9 - Calculus (III)

- 1. Differentiate $y = 3x^2 + 2x + 5$
- 2. Find area between y = x and $y = x^2$, x = 0 to x = 1
- 3. What is an antiderivative?
- 4. Integrate $\int (x^2 + 2x + 1) dx$
- 5. $\lim_{x\to\infty} (x^2 + 2x)/(x^2 + 4x)$
- 6. Find the slope of tangent to $y = x^2$ at x = -1
- 7. What is a local maximum?
- 8. Second derivative of y = cos(x)
- 9. Find inflection point of $y = x^3 3x$
- 10. Integrate ∫sin(x) dx

Page 10 - Word Problems

- 1. Rectangle area 30, width 5. Find length.
- 2. 9 pencils cost \$2. How much for 15?
- 3. Ball thrown upward at 8 m/s, height after 1s?

- 4. If $f(x) = x^2 + 3$, what is f(4)?
- 5. Two numbers add to 50, one is 20. Other?
- 6. 5 tickets, \$12 for adults, \$8 for kids. Total \$44. How many adults?
- 7. Solve: x + 2y = 14, 3x y = 7
- 8. Circle area 50.24. What is the radius? $(\pi=3.14)$
- 9. If x/4 = 5, x = ?
- 10. A car travels at 70 mph for 2.5 hours. How far?