



Birla Institute of Technology & Science, Pilani

Hyderabad Campus

SECOND SEMESTER 2019 - 2020

Course Handout Part II

06-01-2020

In addition to Part - I (General Handout for all courses appended to the timetable) this portion gives further specific details regarding the course.

Course No. : MATH F241
Course Title : Mathematical Methods
Instructor-in-charge : Santanu Koley
Instructors : Santanu Koley, Jagan Mohan Jonnalagadda

Scope and Objective of the Course:

This course introduces different mathematical methods and their applications to many real life problems of science, engineering and technology.

Text Books:

T1: F. B. Hildebrand, Methods of Applied Mathematics, Dover Publications, Second Edition, 1992.

T2: Sudhakar Nair, Advanced Topics in Applied Mathematics: For Engineering and the Physical Sciences, Cambridge University Press, 2011.

Reference Books:

R1: G. B. Arfken and H. J. Weber, Mathematical Methods for Physicist, Academic Press 2002.

R2: Anadi S. Gupta, Calculus of Variations with Applications, Prentice - Hall of India Pvt. Limited, 2004.

R3: Lokenath Debnath and D. Bhatta, Integral Transform and their Applications, Taylor & Francis, 2002.

R4: Ivar Stakgold, Michael J. Holst, Green's Functions and Boundary Value Problems, Wiley, 3rd Edition, 2011.

R5: R P. Kanwal, Linear Integral Equations, Birkhauser Boston, 1996.

Lecture Plan:

| Lecture No. | Learning Objectives | Topics to be covered | Chapter in the Text Book |
|-------------|--|---|--------------------------|
| 1 - 2 | To deal with the formulation and theory of linear integral equations | Integral Equations: Introduction and relation between integral and differential equations. | T1 (3.1 - 3.2) |
| 3 - 5 | To introduce and interpret Green's function | Green's operator and Green's function, adjoint operator, Sturm - Liouville operator. | T1 (3.3) |
| 6 - 12 | To study different analytical procedures available for the exact solution of certain | Classification of integral equations, Fredholm equations, Hilbert - Schmidt theory, Iterative methods for solving equations of the second kind, the Neumann series and Fredholm theory. | T1 (3.6 - 3.11) |



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| | linear integral equations | | |
| 13 - 16 | To describe various numerical methods for obtaining approximate solutions of certain linear integral equations | Approximation of Fredholm equations by set of algebraic equations, approximate methods by undetermined coefficients, method of collocation, method of weighing function, method of least squares. | T1 (3.15 - 3.19) |
| 17 - 18 | To introduce a powerful technique for solving linear and partial differential equations arising in engineering and physics when the domain is infinite or semi-infinite | Dirac - Delta function and its properties. Fourier series, Riemann - Lebesgue lemma, localization lemma, Fourier integral theorem, Fourier cosine and sine transforms. | T2 Chapter I (Articles 1 - 10), T2 (3.1 - 3.4) |
| 19 - 21 | To discuss important properties of Fourier transforms | Properties of Fourier transforms, properties of trigonometric transforms, transforms of elementary functions. | T2 (3.5 - 3.7) |
| 22 - 26 | To illustrate some examples of solutions of differential and integral equations obtained using the Fourier transform | Convolution integral, mixed trigonometric transform, Applications of Fourier transforms, discrete Fourier transform. | T2 (3.8 - 3.9, 3.11, 3.18) |
| 27 - 31 | To introduce the variational notation and derive the Euler equations relevant to a large class of problems | Calculus of Variations: Maxima and minima, The simplest case, illustrative examples, natural boundary conditions, transition conditions, the variational notation, general case of two independent variables. | T1 (2.1 - 2.6) |
| 32 - 33 | To determine one or more functions by a variational procedure in which variations are governed by one or more auxiliary conditions. | Constraints and Lagrange's multipliers. | T1 (2.7) |
| 34-35 | To solve variational problems in which the boundary of the region of integration is not completely specified but is to be determined together with the | Variable end points. | T1 (2.8) |



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| | unknown function or functions. | | |
| 36 - 38 | To illustrate one of the important class of variational problems | Sturm - Liouville problems, Hamilton's principle, Lagrange's equations. | T1 (2.9 – 2.11) |
| 39 - 41 | To obtain approximate solutions of problems expressed in variational form | The Rayleigh - Ritz method. | T1 (2.19) |

Evaluation Scheme:

| S. No. | Evaluation Component | Duration | Weightage (%) | Date & Time | Nature of Component |
|--------|----------------------|----------|---------------|--------------------------------|---------------------|
| 1 | *Quizzes (5) | | 28 | Will be announced in the class | Closed book |
| 2 | Mid Sem Exam | 1.5 Hour | 30 | 4/3 1.30 -3.00 PM | Open book |
| 3 | Comprehensive Exam. | 3 Hours | 42 | 08/05 FN | Closed book |

***Best 4 out of 5 will be taken**

Make-up Policy: Make-up for Mid-Sem Exam will be given only for very genuine cases and prior permission has to be obtained from Instructor In-charge. No make-up for quizzes.

Chamber consultation hour: To be announced by the respective Instructor.

Notices: The notices concerning this course will be displayed in CMS only.

Academic Honesty and Integrity Policy: Academic honesty and integrity are to be maintained by all the students throughout the semester and no type of academic dishonesty is acceptable.

INSTRUCTOR-IN-CHARGE

